

# Massive Algorithms

Data Structures and Algorithm Interview Questions from the internet. Help programmers to get hired by dream companies like Google or Facebook.

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Dynamic Programming - Subset Sum Problem

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LeetCode 445 - Add Two Numbers II

LeetCode 448 - Find All Numbers Disappeared in an Array

First pair non matching leaves

HackerRank: Equal

## Labels

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## LeetCode 287 - Perfect Squares

Perfect Squares [LeetCode] | Training dragons the hard way - Programming Every Day!

Given a positive integer  $n$ , find the least number of perfect square numbers (for example,  $1, 4, 9, 16, \dots$ ) which sum to  $n$ .

For example, given  $n = 12$ , return  $3$  because  $12 = 4 + 4 + 4$ ; given  $n = 13$ , return  $2$  because  $13 = 4 + 9$ .

<http://www.zrzahid.com/least-number-of-perfect-squares-that-sums-to-n/>

maximum perfect square less than  $n$  will be  $\sqrt{n}$ . So, we can check for each numbers in  $j=1$  to  $\sqrt{n}$  whether we can break  $n$  into two parts such that one part is a perfect square  $j*j$  and the remaining part  $n-j*j$  can be broken into perfect squares in similar manner. Clearly it has a recurrence relation  $ps(n)=j*j+ps(n-j*j)$ , for all possible  $1 \leq j \leq \sqrt{n}$ . We need to find such  $j$  that minimizes number of perfect squares generated.

```
Let, PSN(i) is minimum number of perfect squares that sum to i
PSN(i) = min{1+PSN(i-j*j)}, for all j, 1≤j≤√n
```

O(nlogn) DP solution

<https://discuss.leetcode.com/topic/26400/an-easy-understanding-dp-solution-in-java/>

```
public static int perfectSquareDP(int n){
    if(n <= 0){
        return 0;
    }

    int[] dp = new int[n+1];
    Arrays.fill(dp, Integer.MAX_VALUE);
    dp[0] = 0;
    dp[1] = 1;

    //to compute least perfect for n we compute top down for each
    //possible value sum from 2 to n
    for(int i = 2; i<=n; i++){
        //for a particular value i we can break it as sum of a perfect square j*j and
        //all perfect squares from solution of the remainder (i-j*j)
        for(int j = 1; j*j<=i; j++){
            dp[i] = Math.min(dp[i], 1+dp[i-j*j]);
        }
    }

    return dp[n];
}
```

Google™ Custom Search



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▼ 2015 (1762)

► December (135)

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资格赛 题目二 长方形 -  
CYJB - 博客园

[CTCI] 最小调整有序 -  
Eason Liu - 博客园

LeetCode 287 - Find the  
Duplicate Number -  
Google ...

Rearrange a given linked  
list in-place. - Geeksfor...

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Airbnb电面面经 - ---☆心随  
风飞 - 博客频道 -  
CSDN.NET

Snapchat Interview

Phone number to Letters  
Dropbox

Json Encoding

LeetCode 286 - Walls and  
Gates

LIKE CODING: MJ [40]  
Count squares

每日一贴:  
[http://www.mitbbs.com/mit  
bbs\\_article\\_t.php?b...](http://www.mitbbs.com/mitbbs_article_t.php?b...)

Check if two given strings  
are isomorphic to each ...

Print all non-increasing  
sequences of sum equal  
to...

Suffix Array

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Fastest Solution – Lagrange’s four-square theorem

```
private static boolean is_square(int n){
    int sqrt_n = (int) (Math.sqrt(n));
    return (sqrt_n*sqrt_n == n);
}

// Based on Lagrange's Four Square theorem, there
// are only 4 possible results: 1, 2, 3, 4.
public static int perfectSquaresLagrange(int n)
{
    // If n is a perfect square, return 1.
    if(is_square(n))
    {
        return 1;
    }

    // The result is 4 if n can be written in the
    // form of 4^k*(8*m + 7).
    while ((n & 3) == 0) // n%4 == 0
    {
        n >>= 2;
    }
    if ((n & 7) == 7) // n%8 == 7
    {
        return 4;
    }

    // Check whether 2 is the result.
    int sqrt_n = (int) (Math.sqrt(n));
    for(int i = 1; i <= sqrt_n; i++)
    {
        if (is_square(n - i*i))
        {
            return 2;
        }
    }

    return 3;
}
```

X 动态规划 (Dynamic Programming) - 时间复杂度都是O(n3/2)

<http://bookshadow.com/weblog/2015/09/09/leetcode-perfect-squares/>

时间复杂度：O(n \* sqrt n)

初始化将dp数组置为无穷大；令dp[y \* y] = 1，其中：y \* y <= n

状态转移方程：

```
dp[x + y * y] = min(dp[x + y * y], dp[x] + 1)
```

其中：x + y \* y <= n

```
public int numSquares(int n) {
    int dp[] = new int[n + 1];
    Arrays.fill(dp, Integer.MAX_VALUE);
    for (int i = 1; i * i <= n; i++) {
```

Given a Boolean Matrix, find k such that all eleme...

Sort the input character array | CareerCup

Find minimum window length which accommodate all g...

Algo#1: Inorder Predecessor in Binary Tree

Inorder predecessor and successor for a given key ...

Inorder Successor in Binary Tree | Algorithms

Leetcode - Inorder Successor in Binary Search Tree...

Googol String - GCM 2016 Round A - Problem A

Most Divisors | Algorithm Notes

Count even length binary sequences with same sum o...

History Query on Stack | Algorithm Notes

Max XOR sub sequence | Algorithm Notes

Conway's Game of Life | Algorithm Notes

Generate an Alphabetic Sequence

Print a pattern without using any loop - GeeksforG...

Given a string, print all possible palindromic par...

Minimum difference between two elements in array |...

Longest Repeating Subsequence - GeeksforGeeks

Algorithm Approaches

LIKE CODING: MJ [39] Valid Parentheses

LeetCode - Move Zeroes

LeetCode 282 - Expression Add Operators

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Array O(N) (29)

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Microsoft 100 - July (28)

```
        dp[i * i] = 1;
    }
    for (int i = 1; i <= n; i++) {
        for (int j = 1; i + j * j <= n; j++) {
            dp[i + j * j] = Math.min(dp[i] + 1, dp[i + j * j]);
        }
    }
    return dp[n];
}
```

```
int numSquares(int n) {
    static vector<int> dp {0};
    int m = dp.size();
    dp.resize(max(m, n+1), INT_MAX);
    for (int i=1, i2; (i2 = i*i)<=n; ++i)
        for (int j=max(m, i2); j<=n; ++j)
            if (dp[j] > dp[j-i2] + 1) dp[j] = dp[j-i2] + 1;
    return dp[n];
}
```

<http://buttercola.blogspot.com/2015/09/leetcode-perfect-squares.html>

```
public int numSquares(int n) {
    if (n <= 0) {
        return 0;
    }

    int[] dp = new int[n + 1];

    for (int i = 1; i <= n; i++) {
        dp[i] = Integer.MAX_VALUE; // \\
        for (int j = 1; j * j <= i; j++) {
            dp[i] = Math.min(dp[i], dp[i - j * j] + 1);
        }
    }

    return dp[n];
}
```

<https://asanchina.wordpress.com/2015/09/11/perfect-squares/>

```
public int numSquares(int n) {
    if(n==1 || n==2 || n==3) return n;

    //dp[i] store the result of "i"
```

MJ [37] Cross River

Find maximum value of Sum( i\*arr[i]) with only rot...

Given an array of pairs, find all symmetric pairs ...

Cracking the coding interview--Q4.7

Root to leaf path sum equal to a given number - Ge...

[笔试] 设计一个新型的计算器 | 指尖的舞者

Maximum weight transformation of a given string - ...

Bitmasking and Dynamic Programming | Set 1 (Count ...

Find the largest subarray with 0 sum - GeeksforGee...

Check if a given number is sparse or not - Geeksfo...

Facebook Hacker Cup 2014 Quals: Square Detector | ...

Corporate Gifting - Facebook Hacker Cup 2015 Round...

Facebook Hacker Cup 2015 Round 1 --- Winning at Sp...

Hackercup 2015: Autocomplete - Coding in A Smart W...

Facebook Hacker Cup 2015 Round 1 Homework

Facebook Hacker Cup: "Studious Student" Solution i...

Facebook Hacker Cup 2012: Billboards Solution | Pr...

Word Break Related

[LeetCode] Word Break II

Leetcode 139 - Word Break (Java)

[google面试题] 判断是橘子还是香蕉 - JobHunting版 - 未名存档

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- Shortest Path (16)

```
int[] dp = new int[n+1];

dp[0] = 0; dp[1] = 1; dp[2] = 2; dp[3] = 3;
for(int i = 4; i < n+1; ++i)
{
    //now divide i to two parts: i = left + right
    int right = 1;
    dp[i] = i;
    while(i >= right*right)
    {
        dp[i] = dp[i]>dp[i-right*right]+1?dp[i-right*right]+1:dp[i];
        ++right;
    }
}
return dp[n];
}
```

<https://github.com/shawnfan/LeetCode/blob/master/Java/Perfect%20Squares.java>

```
public int numSquares(int n) {
    if (n <= 0) {
        return 0;
    }
    int[] dp = new int[n + 1];
    dp[0] = 0;

    for (int i = 1; i <= n; i++) {
        int maxSqrNum = (int)Math.floor(Math.sqrt(i));
        int min = Integer.MAX_VALUE;
        for (int j = 1; j <= maxSqrNum; j++) {
            min = Math.min(min, dp[i - j * j] + 1);
        }
        dp[i] = min;
    }
    return dp[n];
}
```

- Googol: English To 'Pig Latin'
- 【新提醒】Uber Intern Onsite四轮附求职感想【一亩三分地论坛面经版】 - Power...
- Find all possible outcomes of a given expression -...
- LeetCode Q209 Minimum Size Subarray Sum | Lei Jian...
- LeetCode 214 - Shortest Palindrome
- [leetcode]Invert Binary Tree
- LeetCode - Product of Array Except Self (Java)
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- Weighted Reservoir Sampling
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- Check String Order - Google Intreview
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- Detect cycle in an array
- find the minimal difference between two sorted arr...
- 4\*4 matrix, walk from top left to right bottom, an...
- Print Common Nodes in Two Binary Search Trees - Ge...
- google面经 - 未名空间(mitbbs.com)
- Leetcode: Google interview questions #3
- Algorithm Game - Fishing -

String Search (16)

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(12)

尺取法 (12)

AOJ (11)

Binary Search -

<http://shibaili.blogspot.com/2015/09/day-125-279-perfect-squares.html>

```
int numSquares(int n) {  
    vector<int> dp(n + 1, INT_MAX);  
    dp[0] = 0;  
  
    for (int i = 0; i <= n; i++) {  
        for (int j = 1; j * j + i <= n; j++) {  
            dp[i + j * j] = min(dp[i + j * j], dp[i] + 1);  
        }  
    }  
    return dp[n];  
}
```

Recursive Version: O(n \* sqrt(n)) dp递归, 同样复杂度, 但过不了oj

```
int helper(unordered_map<int,int> &dic,int n) {  
    if (n < 4) return n;  
    if (dic.find(n) != dic.end()) return dic[n];  
  
    int minLen = INT_MAX;  
    int i = (int)sqrt(n);  
    for (; i > 0; i--) {  
        minLen = min(minLen, helper(dic, n - i * i) + 1);  
    }  
    dic[n] = minLen;  
    return minLen;  
}  
  
int numSquares(int n) {  
    unordered_map<int,int> dic;  
    return helper(dic,n);  
}
```

由于该题有许多大型的测试样例, 因此对于速度比较慢的编程语言, 在测试样例之间共享计算结果, 可以节省时间开销。

参考链接: <https://leetcode.com/discuss/56993/static-dp-c-12-ms-python-172-ms-ruby-384-ms>

```
class Solution(object):  
    _dp = [0]  
    def numSquares(self, n):  
        dp = self._dp
```

Google Interview

Popular Number

Leetcode: Google interview  
questions #1

这道G的题怎么做? - 未名  
空间(mitbbs.com)

Most Frequent Nodes in  
BST - Google Interview

Leetcode: Extra: 主要是  
game theory

Zig-zag matrix - Rosetta  
Code

Find maximum of minimum  
for every window size in  
a...

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LeetCode 287 - Perfect  
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Double Square Problem  
Analysis | LeetCode +  
Facebo...

flatten json to a list of map

Uber Interview

Find the largest rectangle  
of 1's with swapping of...

Binary Search Tree  
Complete Implementation  
in JAVA...

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- Tutorialhorizon (10)
- X Sum (10)

```
while len(dp) <= n:
    dp += min(dp[-i*i] for i in range(1, int(len(dp)**0.5+1))) + 1,
    return dp[n]
```

<https://leetcode.com/discuss/58056/summary-of-different-solutions-bfs-static-and-mathematics>

A Static DP solution in Java: 15ms.

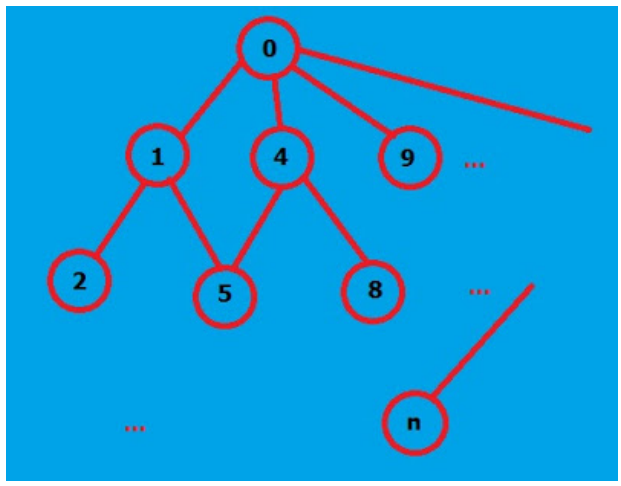
```
static List<Integer> result = new ArrayList<>();
public int numSquares(int n) {
    if (result.size() == 0) {
        result.add(0);
    }
    while (result.size() <= n) {
        int m = result.size();
        int tempMin = Integer.MAX_VALUE;
        for (int j = 1; j * j <= m; j++) {
            tempMin = Math.min(tempMin, result.get(m - j * j) + 1);
        }
        result.add(tempMin);
    }
    return result.get(n);
}
```

II. Breadth First Search

Summary of 4 different solutions (BFS, DP, static DP and mathematics)

<http://traceformula.blogspot.com/2015/09/perfect-squares-leetcode.html>

In general, the time complexity of BFS is  $O(|V| + |E|)$  where  $|V|$  is the number of vertices in the graph and  $|E|$  is the number of edges in the graph. As in the constructed graph,  $|V| = n$  and  $|E| \leq n^2$ . The time complexity of the BFS here is  $O(n^2)$ .



Picture 1: Graph of numbers

In this problem, we define a graph where each number from 0 to  $n$  is a node. Two numbers  $p < q$  is connected if  $(q-p)$  is a perfect square.

So we can simply do a Breadth First Search from the node 0.

```
01. class Solution(object):
02.     _dp = [0]
03.     def numSquares(self, n):
```

```

04. | """
05. | :type n: int
06. | :rtype: int
07. | """
08. |
09. | q1 = [0]
10. | q2 = []
11. | level = 0
12. | visited = [False] * (n+1)
13. | while True:
14. |     level += 1
15. |     for v in q1:
16. |         i = 0
17. |         while True:
18. |             i += 1
19. |             t = v + i * i
20. |             if t == n: return level
21. |             if t > n: break
22. |             if visited[t]: continue
23. |             q2.append(t)
24. |             visited[t] = True
25. |         q1 = q2
26. |         q2 = []
27. |
28. | return 0

```

<http://nb4799.neu.edu/wordpress/?p=1010>

Don't forget to use a set `visited` to record which nodes have been visited. A node can be reached through multiple ways but BFS always makes sure whenever it is reached with the least steps, it is flagged as visited.

Why can't we use DFS? Why can't we report steps when we reach `n` by DFS? Because unlike BFS, DFS doesn't make sure you are always using the least step to reach a node.

if you want to find "... 's least number to do something", you can try to think about solving it in BFS way.

```

def numSquares(self, n):
    """
    :type n: int
    :rtype: int

    """
    # corner case 1
    if n < 0:
        return -1

    # corner case 2
    if n==0:

```

```

        return 1

    q = deque()
    visited = set()

    # val, step
    q.append((0,0))
    visited.add(0)

    while q:
        val, step = q.popleft()

        for i in xrange(1, n+1):
            tmp = val + i**2

            if tmp > n:
                break

            if tmp == n:
                return step+1

            else:
                if tmp not in visited:
                    visited.add(tmp)
                    q.append((tmp, step+1))

    # Should never reach here

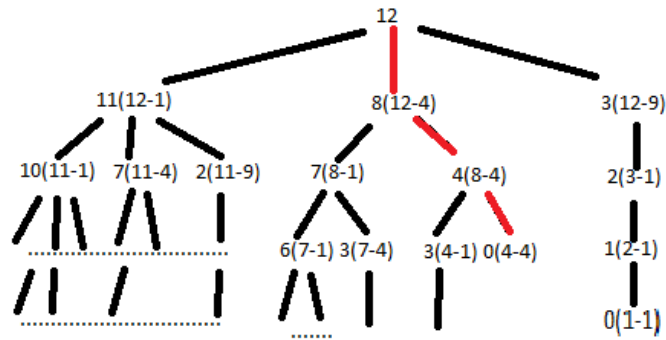
    return -1

```

<https://leetcode.com/discuss/62229/short-python-solution-using-bfs>

The basic idea of this solution is a BSF search for shortest path, take 12 as an example, as shown below, the shortest path is 12-8-4-0:





```
def numSquares(self, n):
```

```
    if n < 2:
```

```
        return n
```

```
    lst = []
```

```
    i = 1
```

```
    while i * i <= n:
```

```
        lst.append(i * i)
```

```
        i += 1
```

```
    cnt = 0
```

```
    toCheck = {n}
```

```
    while toCheck:
```

```
        cnt += 1
```

```
        temp = set()
```

```
        for x in toCheck:
```

```
            for y in lst:
```

```
                if x == y:
```

```
                    return cnt
```

```
                if x < y:
```

```
                    break
```

```
                temp.add(x-y)
```

```
        toCheck = temp
```

```
    return cnt
```

<https://leetcode.com/discuss/58056/summary-of-different-solutions-bfs-static-and-mathematics>

Java BFS implementation: Start from node 0 in queue, and keep pushing in perfect square number + curr value, once we reach number n, we found the solution.

```
public int numSquares(int n) {
    Queue<Integer> q = new LinkedList<>();
    Set<Integer> visited = new HashSet<>();
    q.offer(0);
    visited.add(0);
    int depth = 0;
    while(!q.isEmpty()) {
        int size = q.size();
        depth++;
        while(size-- > 0) {
```

```

    int u = q.poll();
    for(int i = 1; i*i <= n; i++) {
        int v = u+i*i;
        if(v == n) {
            return depth;
        }
        if(v > n) {
            break;
        }
        if(!visited.contains(v)) {
            q.offer(v);
            visited.add(v);
        }
    }
}
return depth;
}

```

<http://nb4799.neu.edu/wordpress/?p=1010>

```
def numSquares(self, n):
```

```
    """
```

```
    :type n: int
```

```
    :rtype: int
```

```
    """
```

```
    # corner case 1
```

```
    if n < 0:
```

```
        return -1
```

```
    # corner case 2
```

```
    if n==0:
```

```
        return 1
```

```
    q = deque()
```

```
    visited = set()
```

```
    # val, step
```

```
    q.append((0,0))
```

```
    visited.add(0)
```

```
    while q:
```

```
        val, step = q.popleft()
```

```
        for i in xrange(1, n+1):
```

```
            tmp = val + i**2
```

```

        if tmp > n:

            break

        if tmp == n:

            return step+1

        else:

            if tmp not in visited:

                visited.add(tmp)

                q.append((tmp, step+1))

# Should never reach here

return -1

```

Use BFS to solve this problem. We can think of a tree graph in which nodes are value  $0, 1, \dots, n$ . A link only exists between  $i$  and  $j$  ( $i < j$ ) if  $j = i + \text{square\_num}$ . We start from node 0 and add all nodes reachable from 0 to queue. Then we start to fetch elements from the queue to continue to explore until we reach node  $n$ . Since BFS guarantees that for every round all nodes in the queue have same depth, so whenever we reach node  $n$ , we know the least depth needed to reach  $n$ , i.e., the least number of square number to add to  $n$ .

Don't forget to use a set `visited` to record which nodes have been visited. A node can be reached through multiple ways but BFS always makes sure whenever it is reached with the least steps, it is flagged as visited.

Why can't we use DFS? Why can't we report steps when we reach  $n$  by DFS? Because unlike BFS, DFS doesn't make sure you are always using the least step to reach a node. Imagine DFS may traverse all nodes to reach  $n$  because each node is its previous node plus one (because one is a square number.) When you reach  $n$ , you use  $n$  steps. But it may or may not be the least number required to reach  $n$ .

This teaches us a lesson that if you want to find "...s least number to do something", you can try to think about solving it in BFS way.

In this problem, we define a graph where each number from  $0$  to  $n$  is a node. Two numbers  $p < q$  is connected if  $(q-p)$  is a perfect square.

So we can simply do a Breadth First Search from the node  $0$ .

```

01. | class Solution(object):
02. |     _dp = [0]
03. |     def numSquares(self, n):
04. |         q1 = [0]
05. |         q2 = []
06. |         level = 0
07. |         visited = [False] * (n+1)
08. |         while True:
09. |             level += 1
10. |             for v in q1:
11. |                 i = 0

```

```

12.         while True:
13.             i += 1
14.             t = v + i * i
15.             if t == n: return level
16.             if t > n: break
17.             if visited[t]: continue
18.             q2.append(t)
19.             visited[t] = True
20.         q1 = q2
21.         q2 = []
22.
23.     return 0

```

## X DFS

[http://blog.csdn.net/elton\\_xiao/article/details/49021623](http://blog.csdn.net/elton_xiao/article/details/49021623)

模型同上，进行深度优先搜索。

从n出发，减去一个平方，即得到下一层的一个节点。直到找到节点0为止。

遍历所有路径，记录下最短的路径数。

1. 遍历时，使用变量level，限制递归的深度。以节省时间。

2. 先减去较大的平方，再减去较小的平方。这样，当搜索到节点0时，所用的步数（即深度），不会特别大。从而用此深度，限制后续的搜索深度。

因为我们要找的是最短路径。

反之如果从1个平方开始递减的话，会出现大量的无用搜索。比如每次只减掉1，搜索n，将第一次会达到n层。

<https://leetcode.com/discuss/58056/summary-of-different-solutions-bfs-static-and-mathematics>

```

int numSquares(int n) {
    vector<int> nums(n+1);
    return helper(n, nums, n);
}

```

```

int helper(int n, vector<int>& nums, int level) {
    if (!n)
        return 0;
    if (nums[n])
        return nums[n];
    if (!level)
        return -1;

```

```

    --level;
    const int up = sqrt(n);
    int ans = n;
    int res = n;
    for (int i=up; i>=1 && res; i--) {
        res = helper(n-i*i, nums, min(ans, level));
        if (res >= 0)
            ans = min(ans, res);
    }
    nums[n] = ans + 1;
    return nums[n];
}

```

<https://leetcode.com/discuss/62782/recursive-dfs-solution-in-java-which-i-believe-has-o-run-time>

I'm not certain on my math so please correct me if I'm wrong, but the run-time should be  $O(n^{1/2} * n^{1/4} * n^{1/8} * \dots)$ , repeating as many times as there are layers in the minimum, which regardless of the number of layers approaches  $O(n)$ .

```
public int numSquares(int n) {  
    return dfs(n, 0, n);  
}  
  
public int dfs(int n, int level, int min) {  
    if(n == 0 || level >= min) return level;  
    for(int i = (int) Math.sqrt(n); i > 0; i--) {  
        min = dfs(n - ((int) Math.pow(i, 2)), level+1, min);  
    }  
    return min;  
}
```

### 1. 暴力枚举 brute force **time complexity: exponential**

```
int numSquares(int n) {  
    int digit = sqrt(n);  
    if(digit*digit == n) return 1;  
  
    int minimum = n; //this is the maximum number  
    dfs(n, 0, digit, 0, minimum);  
    return minimum;  
}  
  
void dfs(int n, int curSum, int curDigit, int curNum, int& minimum)  
{  
    if(curSum > n) return;  
    if(curSum == n)  
    {  
        minimum = minimum > curNum ? curNum : minimum;  
        return;  
    }  
    if(curDigit <= 0) return;  
    if(curDigit == 1)  
    {  
        curNum += n - curSum;  
        minimum = minimum > curNum ? curNum : minimum;  
        return;  
    }  
    //either use curDigit or not use  
    if(n - curSum >= curDigit * curDigit)
```

```

        dfs(n, curSum+curDigit*curDigit, curDigit, curNum+1, minimum);
        dfs(n, curSum, curDigit-1, curNum, minimum);
    }

```

<http://blog.csdn.net/u012290414/article/details/48730819>

This doesn't use visited - not efficient.

<http://traceformula.blogspot.com/2015/09/perfect-squares-leetcode-part-2-solve.html>

I want to confirm that all the returned values will always be in range [1,4] inclusively. Why is that? It is because we have **Lagrange's Four Square Theorem**, also known as **Bachet's conjecture**:

**Every natural numbers can be expressed as a sum of four square numbers. (\*)**

As a note, many proofs of the theorem use the **Euler's four square identity**:

$$\begin{aligned}
 (a_1^2 + a_2^2 + a_3^2 + a_4^2)(b_1^2 + b_2^2 + b_3^2 + b_4^2) = \\
 (a_1b_1 + a_2b_2 + a_3b_3 + a_4b_4)^2 + \\
 (a_1b_2 - a_2b_1 + a_3b_4 - a_4b_3)^2 + \\
 (a_1b_3 - a_2b_4 - a_3b_1 + a_4b_2)^2 + \\
 (a_1b_4 + a_2b_3 - a_3b_2 - a_4b_1)^2.
 \end{aligned}$$

Picture 1: Euler's Four Square Identity

<http://www.alpertron.com.ar/4SQUARES.HTM>

From the article, you can find that if a number is in the form  $n = 4^r(8k+7)$  (Where ^ is power), then  $n$  cannot be represented as a sum of less than 4 perfect squares. If  $n$  is not in the above form, then  $n$  can be represented as a sum of 1, 2, or 3 perfect squares.

```

01. | public boolean is_square(int n){
02. |     int temp = (int) Math.sqrt(n);
03. |     return temp * temp == n;
04. | }
05. | public int numSquares(int n) {
06. |     while ((n & 3) == 0) //n % 4 == 0
07. |         n >>= 2;
08. |     if ((n & 7) == 7) return 4; //n% 8 == 7
09. |
10. |     if(is_square(n)) return 1;
11. |     int sqrt_n = (int) Math.sqrt(n);
12. |     for (int i = 1; i<= sqrt_n; i++){
13. |         if (is_square(n-i*i)) return 2;
14. |     }
15. |     return 3;
16. | }

```

<https://discuss.leetcode.com/topic/24255/summary-of-4-different-solutions-bfs-dp-static-dp-and-mathematics/2>

Read full article from [Perfect Squares \[LeetCode\]](#) | [Training dragons the hard way - Programming Every Day!](#)

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