AI1103: Assignment 1

Javaji Manoj Bhargav - CS20BTECH11022

Download all python codes from

https://github.com/Manojbhargav1305/AI1103/tree/main/Assignment1/codes

and latex codes from

https://github.com/Manojbhargav1305/AI1103/blob/main/Assignment1/Assignment1.tex

PROBLEM(2.8)

Two groups are competing for the position on the board of directors of a corporation. The probabilities that the first and the second groups will win are 0.6 and 0.4 respectively. Further, if the first group wins, the probability of introducing a new product is 0.7 and the corresponding probability is 0.3 if the second group wins. Find the probability that the new product introduced was by the second group.

SOLUTION

let $M \in \{0, 1\}$ be a random variable such that M = 0 represents product is not introduced by winning group and M = 1 represents product is introduced by the winning group.let $H \in \{0, 1\}$ be another random variable such that H = 0 represents that group A wins,H = 1 represents that group B wins. we know that Bayes theorem:

TABLE 0

variable	description	
M = 0	product not introduced by winning group	
M = 1	product introduced by winning group	
H = 0	group A wins	
H = 1	group B wins	

TABLE 0: 1

	H = 0	H=1
M = 0	0.28	0.18
M = 1	0.42	0.12

$$P = (A|B) = \frac{P(A \cap B)}{P(B)}, if P(B) \neq 0$$
 (0.0.1)

so required probability that new product was introduced by group B be P.

$$P = Pr(M = 0|H = 0) + Pr(M = 1|H = 1) \quad (0.0.2)$$
$$= 0.18 + 0.12 \quad (0.0.3)$$
$$= 0.30 \quad (0.0.4)$$
$$(0.0.5)$$

hence the required probability that the product was introduced by the second group is 0.30