

ACADGILD ASSIGNMENT 9.1

SESSION 9: Statistical Inference

1. If Z is norm (mean = 0, sd = 1)

A) find $P(Z > 2.64)$

B) find $P(|Z| > 1.39)$

Answer:

A) $P(Z > 2.64)$

`pnorm(2.64, lower.tail = FALSE)`

Output from R-console

```
pnorm(2.64, lower.tail = FALSE)
```

```
[1] 0.004145301
```

B) $P(|Z| > 1.39)$

$2 * \text{pnorm}(-1.39)$

Output from R-console

```
2 * pnorm(-1.39)
```

```
[1] 0.1645289
```

2. Suppose p = the proportion of students who are admitted to the graduate school of the University of California at Berkeley, and suppose that a public relation officer boasts that UCB has historically had a 40% acceptance rate for its graduate school. Consider the data stored in the table `UCBAdmissions` from 1973. Assuming these observations constituted a simple random sample, are they consistent with the officer's claim, or do they provide evidence that the acceptance rate was significantly less than 40%? Use an $\hat{I}_{\pm} = 0.01$ significance level.

Answer:

Our null hypothesis in this problem is $H_0 : p = 0.4$ and the alternative hypothesis is $H_1 : p < 0.4$. We reject the null hypothesis if \hat{p} is too small, that is, if $\hat{p} - 0.4 \sqrt{0.4(1 - 0.4)/n} < -z_{\alpha}$, where $\alpha = 0.01$ and $-z_{0.01}$ is

```
qnorm(0.99)
```

```
A <- as.data.frame(UCBAdmissions)
```

```
head(A)
```

```
xtabs(Freq ~ Admit, data = A)
```

```
phat <- 1755/(1755 + 2771)
```

```
(phat - 0.4)/sqrt(0.4 * 0.6/(1755 + 2771))
```

Output from R-console

```
> qnorm(0.99)
[1] 2.326348
> A <- as.data.frame(UCBAdmissions)
> head(A)
  Admit Gender Dept Freq
1 Admitted   Male   A  512
2 Rejected   Male   A  313
3 Admitted Female   A   89
4 Rejected Female   A   19
5 Admitted   Male   B  353
6 Rejected   Male   B  207
> xtabs(Freq ~ Admit, data = A)
Admit
Admitted Rejected
  1755      2771
> phat <- 1755/(1755 + 2771)
> (phat - 0.4)/sqrt(0.4 * 0.6/(1755 + 2771))
[1] -1.680919
>
```

Our test statistic is not less than -2.32 , so it does not fall into the critical region.

Therefore, we fail to reject the null hypothesis that the true proportion of students admitted to graduate school is less than 40% and say that the observed data are consistent with the officer's claim at the $\alpha = 0.01$ significance level

RStudio

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Project: (None)

Environment History Connections

Global Environment

Data

A	24 obs. of 4 variables
RcmdrTestDrive	168 obs. of 9 variables

Values

phat	0.387759611135661
Y	num [1:2(1d)] 131 159

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<input type="checkbox"/> bitops	Bitwise Operations	1.0-6
<input type="checkbox"/> callr	Call R from R	3.1.1

```
1 qnorm(0.99)
2 A <- as.data.frame(UCBAdmissions)
3 head(A)
4 xtabs(Freq ~ Admit, data = A)
5 phat <- 1755/(1755 + 2771)
6 (phat - 0.4)/sqrt(0.4 * 0.6/(1755 + 2771))
7
```

7:1 [Top Level] R Script

Console ~/

```
> head(A)
  Admit Gender Dept Freq
1 Admitted Male A 512
2 Rejected Male A 313
3 Admitted Female A 89
4 Rejected Female A 19
5 Admitted Male B 353
6 Rejected Male B 207
> xtabs(Freq ~ Admit, data = A)
Admit
Admitted Rejected
1755 2771
> phat <- 1755/(1755 + 2771)
> (phat - 0.4)/sqrt(0.4 * 0.6/(1755 + 2771))
[1] -1.680919
>
```

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ENG 3:22 PM 2/4/2019