Dissertation

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10/1/2021

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1 Introduction

1.1 The real estate market and the importance of predictive and descriptive models

1.2 The purpose of the paper

1.3 Structure of the paper

~~ TODO ~~

2 Literature

~~ TODO ~~

3 Exploratory Data Analysis

Before we start searching for the best regression model through formal data analysis and model fitting, it is important to explore our data through numerical and graphical summaries. This will allow for a better understanding of the patterns in and the structure of our data and it will enable us to make educated decisions during model fitting. For this purpose, we start by exploring each variable individually and, then, we focus on the relationships between the variables with emphasis on the ones related to the sale price, which is the variable of interest.

3.1 Exploring variables individually

Table 1: Summary statistics for the categorical variables in the initial data set.

| Variable | # missing | Unique lvls | Counts |
|----------|-----------|-------------|--|
| bath | 0 | 5 | 1: 46, 2: 222, 3: 198, 4: 33, 63: 1 |
| parking | 0 | 4 | Covered: 105, No Parking: 73, Not Provided: 126, Open: 196 |

Table 2: Summary statistics for the numerical variables in the initial data set.

| Variable | # missing | Mean | SD | Min | 25% | Median | 75% | Max |
|-----------------------|-----------|------------|----------------|--------|-----------|----------|-----------|----------|
| elevation | 0 | 30.274 | 5.198555e+00 | 9 | 27.00 | 30.0 | 34.00 | 47 |
| $dist_am1$ | 0 | 8258.486 | 2.590404e+03 | 604 | 6439.75 | 8219.0 | 10011.25 | 20662 |
| $dist_am2$ | 0 | 11036.594 | 2.592219e+03 | 4402 | 9229.25 | 11015.0 | 12848.50 | 20945 |
| $dist_am3$ | 0 | 13092.760 | 2.629431e+03 | 4922 | 11215.75 | 13188.0 | 14775.75 | 23294 |
| sqft | 0 | 1816.096 | 5.721306e + 02 | 932 | 1588.50 | 1770.5 | 2003.00 | 12730 |
| precip | 0 | 793.160 | 2.724887e + 02 | -110 | 610.00 | 790.0 | 980.00 | 1530 |
| price | 0 | 510508.840 | 5.556979e + 05 | 124333 | 380271.00 | 481042.0 | 593750.25 | 12500000 |

As a first step, we are interested in the summary statistics of the individual numerical and categorical variables in our data. The tables 1 and 2 contain useful statistics about the variables, prior to making any

alterations to the original data set. We note that there are no missing values for any of our variables in the data.

Regarding the categorical variables, we observe that there are five and four unique levels for the categorical variables "bath" and "parking", respectively. Table 1 shows that most of the sale entries refer to houses with two baths or an "open" type parking. However, the most important observation to note here is a single entry with 63 bathrooms, which is exceedingly higher than all the rest observations in our data that are limited to just 4 bathrooms at maximum. Such an observation is likely to be an outlier and the exploratory analysis to follow further underpins this assumption.

Table 2 shows statistics about the numerical variables. It becomes apparent that the numerical variables are measured in different numerical scales with differences in the magnitude of their values. In terms of magnitude and standard deviation in ascending order:

- "elevation" presents the smallest values that do not exceed the value of 47 and the smallest standard deviation.
- "precip" and "sqft" come second and third, respectively, with the latter having almost double the standard deviation of the former.
- The three variables representing the distance from three chosen amenities (i.e. dist_am1, dist_am2 and dist_am3) exhibit almost the same standard deviation. However, it seems that the 75th percentile of "dist_am1" is, relatively, almost equal to the 25th percentile of "dist_am2", while the 75th percentile of "dist_am2" is roughly the same as the 25th percentile of "dist_am3". This could indicate that, on average, the distance of houses in the data set from "Amenity 1" could be significantly smaller than that from "Amenity 2" and equally for the distances of houses from the "Amenity 2" and "Amenity 3".
- The numerical scale and the standard deviation of "price" are the largest among all numerical variables. Also, it is interesting to point out that there exists a high outlier in "price", even relative to its large magnitude, as it is 21.5755574 times the standard deviation greater than the mean value. The boxplot in figure 1 further illustrates the extreme outlier in "price".



Figure 1: Boxplot of sale price.

Table 3 focuses on the aforementioned extreme outlier in "price". The table reveals that the outlier (that is, the 348^{th} observation) contains extreme values in other variables as well. Specifically, that same observation is the one related to the 63 bathrooms, which we have already noted as a possible extreme value, and through further exploration we can show that its value of 12730 square feet is also extremely high. Those findings suggest that observation 348 could have probably come from a different population compared to the rest of the observations in the data. In any case, we lack enough data between this extreme observation and the

rest ones, to the point that any model fitting with this outlier included would result in speculating after some range of values and would probably lead to a heavily influenced model. Therefore, we conclude that we have enough evidence to support our decision on removing observation 348 before we move on any further.

Table 3: The extreme observation in the variable 'price'.

| | elevation | dist_am1 | dist_am2 | dist_am3 | bath | sqft | parking | precip | price |
|-----|-----------|----------|----------|----------|------|-------|---------|--------|----------|
| 348 | 31 | 20662 | 20945 | 23294 | 63 | 12730 | Covered | 1130 | 12500000 |

Table 4: Summary statistics for the numerical variables after removing the extreme outlier.

| Variable | # missing | Mean | SD | Min | 25% | Median | 75% | Max |
|-----------------------|-----------|--------------|--------------|--------|----------|--------|----------|--------|
| elevation | 0 | 30.27255 | 5.20367 | 9 | 27.0 | 30 | 34.0 | 47 |
| $dist_am1$ | 0 | 8233.62926 | 2532.61067 | 604 | 6434.5 | 8210 | 9984.5 | 16233 |
| $dist_am2$ | 0 | 11016.73747 | 2556.47368 | 4402 | 9219.5 | 11006 | 12842.0 | 18281 |
| $dist_am3$ | 0 | 13072.31663 | 2591.98862 | 4922 | 11215.5 | 13179 | 14771.0 | 20263 |
| sqft | 0 | 1794.22445 | 297.20037 | 932 | 1588.0 | 1770 | 2002.5 | 2667 |
| precip | 0 | 792.48497 | 272.34339 | -110 | 610.0 | 790 | 980.0 | 1530 |
| price | 0 | 486481.80361 | 142096.23500 | 124333 | 380125.0 | 480167 | 593167.0 | 857667 |

After removing the outlier, our conclusions about the variables "elevation", "dist_am1", "dist_am2", "dist_am3" and "precip" are similar to the ones we derived earlier. However, we observe a significant drop in the maximum value of "sqft" along with a significant decrease in its standard deviation, which has now become relatively close to that of "precip". Also, the maximum value and the standard deviation of "price" incurred a large drop.

The boxplots in figure 2 present graphically the already discussed differences in the magnitude and the variation between the numerical variables, by gradually removing variables from plot to plot. Interestingly, the boxplots suggest that the sample distributions of all numerical variables are fairly symmetrical as we observe the median to lie almost at the middle of the IQR box and roughly equal tails at the top and the bottom. This observation is backed by the computed numerical statistics, where the median is reported to be quite close to the mean value for every numerical variable. A closer view using histograms in figure 3 reveals that the sample distribution of all numerical variables in the data resembles that of a sample coming from a Normal Distribution.

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4 Model Fitting: Selecting the best possible regression model

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5 Conclusions

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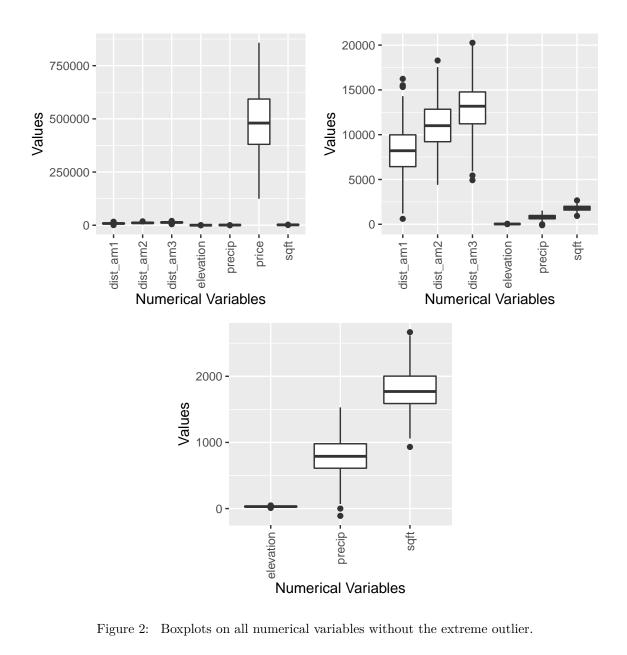


Figure 2: Boxplots on all numerical variables without the extreme outlier.

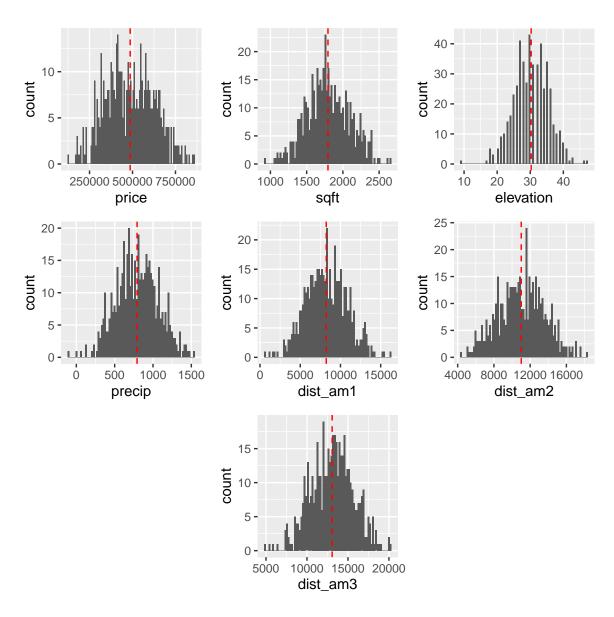


Figure 3: Histograms on all numerical variables without the extreme outlier. The red dashed line represents the mean value of the variable's values.

6 Further Work

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7 References