732A94 Advanced R Programming Computer lab 6

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Chapter 1

Writing fast R code

In this lab we will will create a package to study the effects of algorithms with different computional complexity and how to speedup R code.

Master students should implement one of the exercises marked with (*).

1.1 The knapsack package

Start out by creating a new package on github, see lab 3 for details on how to setup a package.

The package will contain three different functions for solving what is called the knapsack problem. The knapsack problem is a discrete optimization problem where we have a knapsack that can take a limited weight W and we want to fill this knapsack with a number of items i=1,...,n, each with a weight w_i and a value v_i . The goal is to find the knapsack with the largest value of the elements added to the knapsack. This problem is NP-hard, meaning that it is "at least as hard as the hardest problem in NP" (https://en.wikipedia.org/wiki/NP-hardness). NP is a (fundamental) class of problems for which there are (currently) no polynomial time algorithms to solve them. It is an open (Millennium Prize) problem, whether it is or is not possible to solve these problems in polynomial time.

For a more detailed background of the knapsack problem see **this page** https://en.wikipedia.org/wiki/Knapsack_problem.

The data we will use is generated in the following way. To create larger datasets, just set ${\tt n}$ to a larger number.

```
set.seed(42)
n <- 2000
knapsack_objects <-
data.frame(
w=sample(1:4000, size = n, replace = TRUE),
v=runif(n = n, 0, 10000)
)</pre>
```

1.1.1 The package vignette

The package vignette will be your lab report together with the functions in you package. The vignette should contain the answers to all the questions put below. This vignette should be included with the package and be viewed with browseVignettes(''lab_report_knapsack'').

1.1.2 Brute force search

The only solution that is guaranteed to give a correct answer in all situations for the knapsack problem is using brute-force search, i.e. going through all possible alternatives and return the maximum value found. This approach is of complexity $O(2^n)$ since all possible combinations 2^n needs to be evaluated.

Implement a function you call knapsack_brute_force(x, W) that takes a data.frame cx with two variables v and w and returns the maximum knapsack value and which elements (rows in the data.frame). The variable W is the knapsack size.

The function should check that the inputs are correct (i.e. a $\mathtt{data.frame}$ with two variables \mathtt{v} and \mathtt{w}) with only positive values.

The easiest way to enumerate all different combinations is using a binary representation of the numbers 1 to 2^n and include all elements of that is equal to 1 in the binary representation. A function that can do this for you in R is intToBits(). Below is how the function should work (observe that only the first couple of objects are studied).

```
brute_force_knapsack(x = knapsack_objects[1:8,], W = 3500)
$value
[1] 16770
$elements
[1] 5 8
brute_force_knapsack(x = knapsack_objects[1:12,], W = 3500)
$value
[1] 16770
$elements
[1] 5 8
brute_force_knapsack(x = knapsack_objects[1:8,], W = 2000)
$value
[1] 15428
$elements
[1] 3 8
brute_force_knapsack(x = knapsack_objects[1:12,], W = 2000)
$value
[1] 15428
$elements
[1] 3 8
```

Question How much time does it takes to run the algorithm for n = 16 objects?

1.1.3 Dynamic programming

We will now take another approach to the problem. If the weights are actually discrete values (as in our example) we can use this to create an algorithm that can solve the knapsack problem exact by iterating over all possible values of \mathbf{w} .

The pseudocode for this algorithm can be found **here**

https://en.wikipedia.org/wiki/Knapsack_problem#0.2F1_knapsack_problem. Implement this function as knapsack_dynamic(x, W). This function should return the same results as the brute force algorithm, but unlike the brute force it should scale much better since the algorithm will run in O(Wn).

Question How much time does it takes to run the algorithm for n = 500 objects?

1.1.4 Greedy heuristic

A last approach is to use the a heuristic or approximation for the problem. This algorithm will not give an exact result (but it can be shown that it will return at least 50% of the true maximum value), but it will reduce the computational complexity considerably (actually to $O(n \log n)$ due to the sorting part of the algorithm). A short description on how to implement the greedy approach can be found here

https://en.wikipedia.org/wiki/Knapsack_problem#Greedy_approximation_algorithm. Below is an example on how the function should work.

```
greedy_knapsack(x = knapsack_objects[1:800,], W = 3500)
$value
[1] 192647
$elements
[1] 92 574 472 80 110 537 332 117 37 776 577 288 234 255 500 794 55
[18] 290 436 346 282 764 599 303 345 300 243 43 747 35 77 229 719 564
greedy_knapsack(x = knapsack_objects[1:1200,], W = 2000)
$value
[1] 212337
$elements
[1] 92 574 472
                   80 110 840 537 1000 332 117
                                                      37 1197 1152 947
         776 577 288 1147 1131 234 255 1006
[15] 904
                                                833 1176 1092 873
                                                                   828
[29] 1059
          500 1090 794 1033
```

Question How much time does it takes to run the algorithm for n = 1000000 objects?

1.1.5 Implement a test suite for your package

Add the testsuites for the greedy_knapsack() and brute_force_knapsack() that are found here: https://github.com/STIMALiU/AdvRCourse/blob/master/Testsuites/

Based on these test suites, write your own test suite for $knapsack_dynamic(x, W)$ by copying unit test from the other test suites. It is possible that your greedy algorithm will return a better solution, than in the test suites. In such a situation you have to motivate that your algorithm is still a gready one and has O(n) running time. Try to find the reason why a better solution is found.

1.1.6 Profile your code and optimize your code

Now profile and optimize your code to see if you can increase the speed in any way using any of the techniques described in the lectures and here http://adv-r.had.co.nz/Profiling.html. Use the package lineprof to identify bottlenecks, see if you can write this code any faster.

Question What performance gain could you get by trying to improving your code?

1.1.7 (*) Implentation in Rcpp

Another way of improving your code would be to run some parts of the code using Rcpp and writing this part of the code using C++. More details on how to use Rcpp can be found here http://adv-r.had.co.nz/Rcpp.html.

In the function you choose to improve by adding the logical argument fast. The argument should be FALSE by default (so it works with the test suite where we have not specified the argument fast). Implement the fast version of the function using Rcpp.

Question What performance gain could you get by using Rcpp and C++?

1.1.8 (*) Parallelize brute force search

The brute force algorithm is straight forward to parallelize for computers with multiple cores. Implement an argument parallel in brute_force_knapsack() that is FALSE by default (so it works with the test suite where we have not specified the argument parallel). If set to TRUE, the function should parallelize over the detected cores.

Note! Your implementation will be platform dependent and only work with MacOS/Linux or Windows.

Question What performance gain could you get by parallelizing brute force search?

1.1.9 Document your package using roxygen2

Document all your function and package using roxygen2.

1.2 (*) Profile and improve your existing API package

Use the package lineprof to identify the bottlenecks in your code from last week. Try to improve this as much as you can, run your test suite continuously to check that you do not introduce any new bugs.

1.3 Seminar and examination

During the seminar you will bring your own computer and demonstrate your package and what you found difficult in the project.

We will present as many packages as possible during the seminar and you should

- 1. Show that the package can be built using R Studio and that all unit tests is passing.
- 2. Show your vignette/run the examples live.
- 3. Present the speed of your different algorithms.

1.3.1 Examination

Turn in a the address to your github repo with the package using LISAM. To pass the lab you need to:

- 1. Have the R package up on GitHub with a Travis CI pass/fail badge.
- 2. Test suites should be included in the package for greedy_knapsack(), brute_force_knapsack() and knapsack_dynamic(x, W).
- 3. The package should build without warnings (pass) on Travis CI.
- 4. All issues raised by Travis CI should be taken care or justified why they are not a problem or cannot be corrected. Be careful with namespace issues, these you HAVE to take care of.