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Machine learning – Block 1(a)

Måns Magnusson
Department of Statistics, Uppsala University

Autumn 2025

- What is AI and ML?
- Course information
- Introduction to Supervised Learning
 - Example: Logistic regression
- Optimization in Machine Learning



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This block

- What is AI and ML?
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- What is AI and Machine Learning?
- Course Information and Practicalities
- Introduction to Supervised Learning
- (Stochastic) Gradient Descent
- Regularization



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Section 1

What is AI and ML?



What exactly is machine learning and artificial intelligence?

The word "AI" is often used quite loosely:

To briefly explain how Linear Regression helped us reverse engineer the BSR equation, let's break it down. Linear Regression is an AI equation that finds the proper coefficients for an equation by sorting through massive amounts of data. The equation looks something like $BSR = X(a) + Y(b) + Z(c) \dots$ and so and so forth.

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What is Artificial Intelligence?

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What is Artificial General Intelligence?

Artificial general intelligence (AGI) is the hypothetical intelligence of a machine that has the capacity to understand or learn any intellectual task that a human being can. – Wikipedia

Also called:

1. Strong AI
2. General AI
3. Full AI



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Artificial super intelligence (ASI) is "any intellect that greatly exceeds the cognitive performance of humans in virtually all domains of interest" – Nick Bostrom



A Definition of AGI (Hendrycks et al., 2025)

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- **AGI**: a model that matches or exceeds the **cognitive versatility and proficiency** of a well-educated adult.
- **Cattell–Horn–Carroll (CHC)** theory of human cognition.
- Evaluates ten broad cognitive domains:
 - Knowledge, Reading & Writing, Math, Reasoning
 - Working/Long-term Memory, Visual, Auditory, Speed
- Current models total score: **GPT-4: 27%, GPT-5: 57%**.



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A Definition of AGI (Hendrycks et al., 2025)

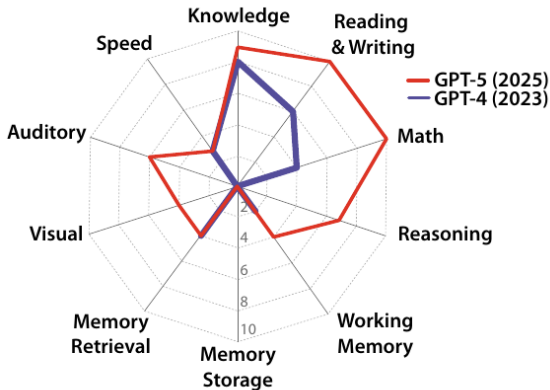


Figure 1:

Cognitive abilities of GPT-4 vs GPT-5.



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Machine Learning is the field of study that gives the computer the ability to learn without being explicitly programmed. – Arthur Samuel (1959)

A computer program is said to learn from experience E with respect to some class of tasks T and performance measure P , if its performance at tasks in T , as measured by P , improves with experience E . – Tom Mitchell (1998)



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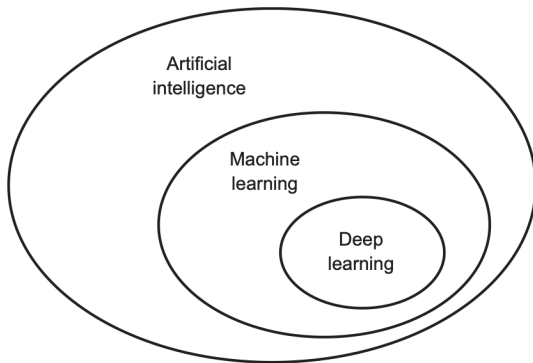
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Learning from data. – Hastie, Tibshirani, Friedman (2009)



What is Machine Learning?

Figure: ML, AI and DL (Chollet, 2018, Figure 1.1)



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Figure: A new paradigm? (Chollet, 2018, Figure 1.2)

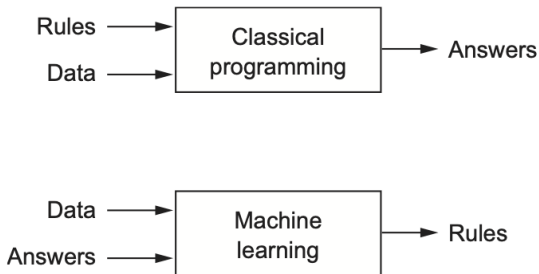




Figure: Regression vs. Pure Predictions (Efron, 2020, Table 5)

Table 5. A comparison checklist of differences between traditional regression methods and pure prediction algorithms.

	Traditional regressions methods	Pure prediction algorithms
1.	Surface plus noise models (continuous, smooth)	Direct prediction (possibly discrete, jagged)
2.	Scientific truth (long-term)	Empirical prediction accuracy (possibly short-term)
3.	Parametric modeling (causality)	Nonparametric (black box)
4.	Parsimonious modeling (researchers choose covariates)	Anti-parsimony (algorithm chooses predictors)
5.	$\mathbf{x} \ p \times n$: with $p \ll n$ (homogeneous data)	$p \gg n$, both possibly enormous (mixed data)
6.	Theory of optimal inference (mle, Neyman–Pearson)	Training/test paradigm (Common Task Framework)

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Different names for the same things

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- Machine learning has developed in parallel with Statistics
 - Common with different names for the same thing:
 1. Time series classification (ML) vs. Functional data classification (Stats)



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 4. Weights (ML) vs. Parameters (Stats)



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 3. Learning (ML) vs. Estimation (Stats)
 4. Weights (ML) vs. Parameters (Stats)
 5. Features (ML) vs. Covariates (Stats)



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Different flavors of ML

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 - Optimization in Machine Learning
- Supervised learning
 - Unsupervised learning
 - Reinforcement learning



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The Bitter Lesson (Rich Sutton, 2019)

- Over 70 years of AI research show that *methods leveraging computation* outperform those using human knowledge.

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- Researchers often try to build human understanding into systems — this helps short term, but limits long-term progress.



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- *Computation, search, and learning* scale with Moore's law — they keep improving as compute increases.



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- Examples: Chess, Go, speech recognition, vision, language models — all advanced by scaling compute, not by encoding expert knowledge.



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- *Computation, search, and learning* scale with Moore's law — they keep improving as compute increases.
- Examples: Chess, Go, speech recognition, vision, language models — all advanced by scaling compute, not by encoding expert knowledge.
- The bitter truth: **General-purpose, scalable methods** win; human-designed structure eventually holds us back.



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Questions?

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Questions?



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Section 2

Course information



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Course information

The aims of this course are that you should:

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Course information

The aims of this course are that you should:

1. get a good knowledge of a large number of machine learning models,
2. become able to use methods for evaluating and improving predictive models,
3. become able to handle big data,
4. become able to train and use machine learning models in R,
5. become able to train and use neural networks using Keras/TensorFlow.
6. become able to describe and discuss ethical aspects of big data and black box-models,

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Course Outline

Two main parts:

- What is AI and ML?
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- Core Content (8 lecture blocks):
 - Supervised learning (5 blocks)
 - Introduction, statistical learning (1 block)
 - Tree-based methods (1 block)
 - Neural Networks (3 block)
 - Unsupervised learning (2 blocks)
 - Reinforcement learning (1 block)



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- Oral exam (Block 1-5) **New for this year**



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- Mini-project on a supervised project (2-3 students)



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Exact dates and details; see the course page.



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Core Content

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- Each block consist of:
 - Online video material (optional)
 - Reading assignments (approx. 2-4h, 50-90 pages a week)
 - One-two Lecture(s) (optional)
 - An individual computer assignment (approx. 14-16h).
 - Three Zoom computer lab sessions (optional)



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 - An individual computer assignment (approx. 14-16h).
 - Three Zoom computer lab sessions (optional)
- Reading: Mandatory and optional (overlap)
- Recommended workflow for each block
 - Do the reading assignments
 - Watch the videos (optional)
 - Attend the lecture (optional) **to ask questions.**
 - Do the computer assignment
 - Attend the zoom lab session (optional) **to ask questions.**



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Lectures

- What is AI and ML?
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- Present overall theory, concepts and content (overview)



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 - Guest lectures on the course (worthwhile):
 1. Jonas Wallin, Lund University (regularization)



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 5. Väinö Yrjänäinen, UU (word embeddings)



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 5. Väinö Yrjänäinen, UU (word embeddings)
- No lectures after 19th/20th of December



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Examination

- To pass (G): All labs (at 75%), mini-project and **oral exam** needs to be passed

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- To pass with distinction (VG): 7/10 VG points

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- To pass with distinction (VG): 7/10 VG points
- Each assignment has an extra (VG) task worth 1 VG point.
- The mini-project is worth 2 VG-points (if it is passed with distinction).
- Ph.D. students: I suggest you get VG to pass the course. Make the project a potential paper.
- Reassessment of grades (supply form to course admin)
- Failing the course: You will need to redo all assignments, oral exam and mini-project.



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Computer Assignments

- Main part of the course
Learning by doing
- Machine learning = Statistics + Computer Science
Hence a lot of programming



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- Both implementation of core components and
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- We will mark and return each assignment within 10 working days.



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- Zoom sessions:
 1. First lab each week will include a 15 min introduction
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Figure: Workload last year to pass (G)

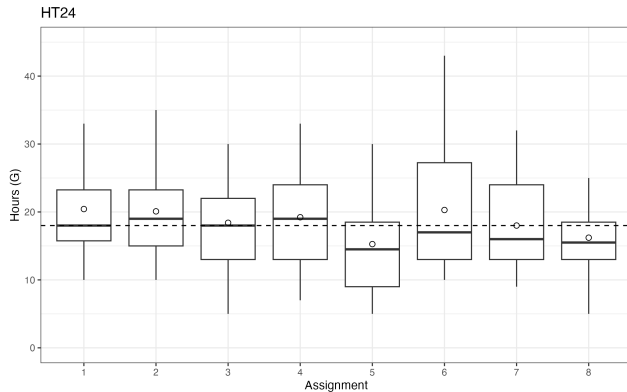
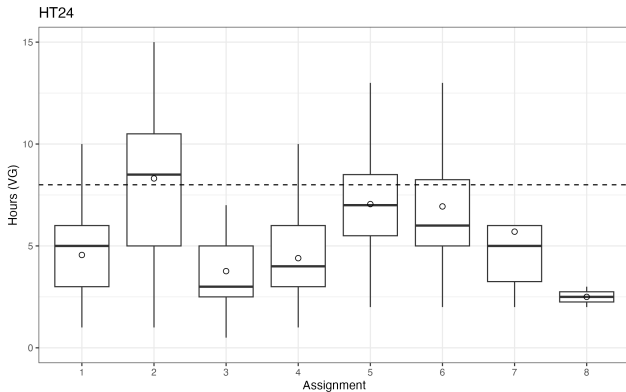




Figure: Workload last year to pass with distinction (VG)





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Oral Exam

- What is AI and ML?
- **Course information**
- Introduction to Supervised Learning
 - Example: Logistic regression
- Optimization in Machine Learning
- New this year. **Purpose:** Additional exam of assignments (ChatGPT proof)



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Oral Exam

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- New this year. **Purpose:** Additional exam of assignments (ChatGPT proof)
- Approx 70 questions based on the assignment 1-5 and the reading assignments.
- **If a question is not covered by the material - reach out!**
- The 9th of November 13.15-16.00 H319
- Random student will answer 1-2 random questions.
- Pass/Fail at the spot.
- Examiner Måns and Hannes.



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Mini-project

- See project instructions on webpage for details.

- What is AI and ML?
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Mini-project

- See project instructions on webpage for details.
- **Supervised problem** of choice on real data.
- 2-3 students.

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- 2-3 students.
- Supply step 1 proposal at the end of block 3.
- Supply step 2 proposal at the end of block 6.
- Project will last two weeks (half time) - but start earlier. Good case to show potential employers.
- Recommended data: Images, text or tabular data (e.g. avoid time series).
- Feel free to build upon the Bayesian project (e.g. compare with Bayesian methods).
- Approximate 40 hours of work *per student*.



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- The project should result in a 4 page report (PDF) using the ICML LaTeX template (see course page).
- Project oral presentation (10-15 minutes)



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- Project oral presentation (10-15 minutes)
- The first author is corresponding author



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- Project oral presentation (10-15 minutes)
- The first author is corresponding author
- Mini-project and master thesis:
 - The mini-project can be used to explore thesis project



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Practicalities

- Course page: Github – please do a PR if something is wrong!

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- Assignments: Studium



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- Assignments: Studium
- Literature
 - Bishop & Bishop (2024) *Deep Learning - Foundations and Concepts*.
 - Hastie, Tibshirani & Friedman (2009). *Elements of Statistical Learning*.
 - Sutton and Barto (2020) *Reinforcement learning: An introduction*
 - Chollet & Allaire (2018) *Deep Learning with R* (optional)
 - Additional articles, tutorials, videos etc. posted on course (github) homepage
 - Mandatory and optional material: Overlap exists!



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- If you have complaint - reach out to me in assignment evaluations!



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Course improvements since last year

- What is AI and ML?
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- Oral exam (I hope it works!)
 - New lecture (maybe) on diffusion models



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Questions?

Questions?



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Section 3

Introduction to Supervised Learning



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Supervised learning

Figure: Relationship between apartment size and price ([source](#))



Problem: We want to predict the price of a new apartment.



- General problem: We have *training* data

$$\mathbf{d} = \{(y_i, \mathbf{x}_i), i = 1, \dots, n\}.$$

- \mathbf{x}_i = features/input/predictors/features/independent variables
- y_i = labels/output/dependent variable
- We want to *learn* a function $\hat{y} = f(x_{new})$ with as good performance as possible.

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- y_i = labels/output/dependent variable
- We want to *learn* a function $\hat{y} = f(x_{new})$ with as good performance as possible.
- Regression problems: $y_i \in \mathbb{R}$
- Classification problems: $y_i \in a, b, c, \dots$ where a, b, c, \dots are discrete classes.



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Example of supervised problems

Any examples of applications?

- What is AI and ML?
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Example of supervised problems

Any examples of applications?

- Is this e-mail message spam or not?

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Example of supervised problems

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- Is this e-mail message spam or not?
- Image recognition/classification



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Example of supervised problems

Any examples of applications?

- Is this e-mail message spam or not?
- Image recognition/classification
- Image object traction (position in a video)

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Example of supervised problems

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- Is this e-mail message spam or not?
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Example of supervised problems

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- Is this e-mail message spam or not?
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- Does this customer have stable finances or not?

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Example of supervised problems

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- Face recognition
- Is this tumour malign or not?



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Logistic regression and classification

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When the y_i in a regression problem is binary (or more generally, categorical), it becomes a **classification problem**.



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When the y_i in a regression problem is binary (or more generally, categorical), it becomes a **classification problem**.

The question that the model tries to answer is: does this observation belong to class 0 or class 1?



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When the y_i in a regression problem is binary (or more generally, categorical), it becomes a **classification problem**.

The question that the model tries to answer is: does this observation belong to class 0 or class 1?

Logistic regression is a workhorse for classification problems.



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Logistic regression

When analysing binary data y_1, \dots, y_N , we usually assume that the Y_i follow binomial (or Bernoulli) distributions.

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Logistic regression

When analysing binary data y_1, \dots, y_N , we usually assume that the Y_i follow binomial (or Bernoulli) distributions.

Assume that Y_1, \dots, Y_N are independent with $Y_i \sim \text{Bernoulli}(\pi_i)$.



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Assume that Y_1, \dots, Y_N are independent with $Y_i \sim \text{Bernoulli}(\pi_i)$.

$Y_i \in 0, 1$ with success probability π_i and $\mu_i = E(Y_i) = \pi_i$.



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When analysing binary data y_1, \dots, y_N , we usually assume that the Y_i follow binomial (or Bernoulli) distributions.

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$Y_i \in 0, 1$ with success probability π_i and $\mu_i = E(Y_i) = \pi_i$.

- The natural parameter of the binomial distribution is

$$g(\pi_i) = \log \left(\frac{\pi_i}{1 - \pi_i} \right),$$

called the **logit** or **log odds**.



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$$g(\pi_i) = \log \left(\frac{\pi_i}{1 - \pi_i} \right),$$

called the **logit** or **log odds**.

- A GLM using this link function is called **logistic regression**, but other link functions are also often used in practice. Many times we use likelihood functions



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Logistic regression

There are two equivalent formulas for **logistic regression**:

$$\log \left(\frac{\pi_i}{1 - \pi_i} \right) = \beta_0 + \beta_1 x_{i1} + \beta_2 x_{i2} + \cdots + \beta_p x_{ip}, \quad i = 1, \dots, N$$

and

$$\pi_i = \frac{\exp \left(\beta_0 + \sum_{j=1}^p \beta_j x_{ij} \right)}{1 + \exp \left(\beta_0 + \sum_{j=1}^p \beta_j x_{ij} \right)}.$$



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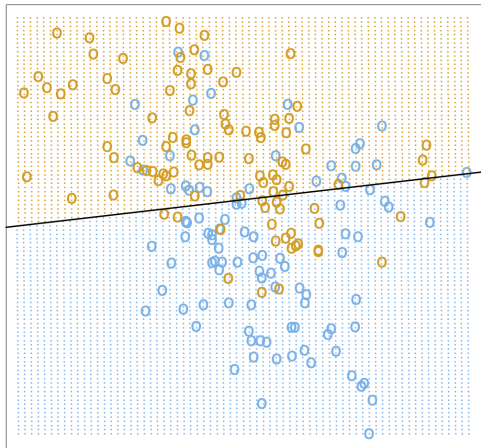
- We *train* a logistic regression model using MLE using the training data.
- Our estimation/training output the MLE $\hat{\theta}$
- We then compute $\hat{p}_i = g^{-1}(\hat{\theta}x_{new})$ for a new observation
- We use a **decision rule** to predict value 0 or 1:

$$\hat{y}_i(\hat{p}_i) = \begin{cases} 1, & \text{if } \hat{p}_i \geq 0.5 \\ 0, & \text{otherwise} \end{cases}$$



Logistic regression: Example

Figure: Decision boundry with two covariates (Hastie et al, 2009, Figure 2.1)



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An example: E-mail classification

E-mail Spam

Predict if a new, unseen,
e-mail is spam or ham.





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Questions?

Questions?



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Section 4

Optimization in Machine Learning



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Training of ML algorithms

1. Training is usually done by minimizing the objective/loss/cost function $L(\theta)$ for $\theta \in \mathbf{R}^P$.
2. Example: Logistic regression, here we can use the **negative** log-likelihood as loss function:

$$L(\theta, \mathbf{y}, \mathbf{X}) = -\log \prod_{i=1}^N p_i^{y_i} (1 - p_i)^{1-y_i},$$

where

$$\log \frac{p_i}{1 - p_i} = \mathbf{x}_i \theta,$$



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where

$$\log \frac{p_i}{1 - p_i} = \mathbf{x}_i \theta,$$

3. In Machine Learning: P and N might be very large...



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Gradient Decent

1. The workhorse of Machine Learning

$$\theta_t = \theta_{t-1} - \eta \nabla L(\theta_{t-1}, \mathbf{X}, \mathbf{y}),$$

where

$$\nabla f(p) = \begin{bmatrix} \frac{\partial f}{\partial x_1}(p) \\ \vdots \\ \frac{\partial f}{\partial x_n}(p) \end{bmatrix}$$

2. $L(\theta)$ needs to be differentiable



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Gradient Descent Analogy

Figure: Gradient Descent Analogy ([source](#))

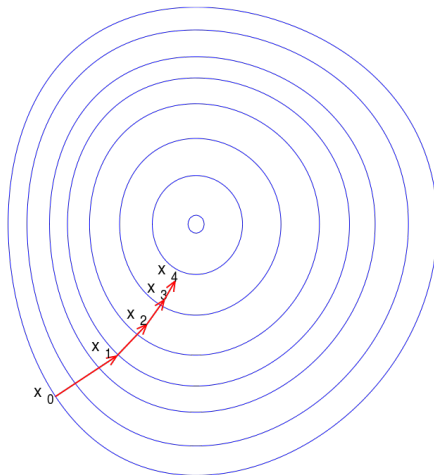




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Gradient Descent (cont.)

Figure: Gradient Descent ([source](#))





Why Gradient Descent?

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- Gradient Descent is a poor algorithm (Newton's method, Iteratively Reweighted Least Squares are 'better')
 - So why is gradient descent relevant?



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- Gradient Descent is a poor algorithm (Newton's method, Iteratively Reweighted Least Squares are 'better')
 - So why is gradient descent relevant?
 - The two benefits with Gradient Descent:
 1. Only uses the gradient—scales to large P
 2. Can scale to large data with Stochastic Gradient Descent—scales to large N



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Stochastic Gradient Descent

- What is AI and ML?
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- Many loss functions (and gradients) are a sum over N observations (e.g. log-likelihoods).



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- Many loss functions (and gradients) are a sum over N observations (e.g. log-likelihoods).
- We can estimate $\nabla L(\theta, X_i, y_i)$ by choosing a random observation (with index i)

$$E(\nabla L(\theta, X_i, y_i)) = \frac{1}{Z} \nabla L(\theta, \mathbf{X}, \mathbf{y}),$$

for some constant Z .



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- This give us the following algorithm:

$$\theta_t = \theta_{t-1} - \eta_t \hat{\nabla} L(\theta_{t-1}, X_i, y_i),$$

where i is random sampled index.

- *Note!*
We need to have an unbiased estimator for $\nabla L(\theta, \mathbf{X}, \mathbf{y})$



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We need to have an unbiased estimator for $\nabla L(\theta, \mathbf{X}, \mathbf{y})$
- What is an iteration?



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- *Note!*
We need to have an unbiased estimator for $\nabla L(\theta, \mathbf{X}, \mathbf{y})$
- What is an iteration?
- Epochs vs. Iterations



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Stochastic Gradient Descent

- What is AI and ML?
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- Learning rate η_t is important
- Will it converge to an optimum?



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Stochastic Gradient Descent

- Learning rate η_t is important
- Will it converge to an optimum?
- We need to reduce η_t over time

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Stochastic Gradient Descent

- Learning rate η_t is important
- Will it converge to an optimum?
- We need to reduce η_t over time
- Robbins–Monro (1951) conditions:
 1. $\eta_t \geq 0 \quad \forall t \geq 0$
 2. $\sum_t^\infty \eta_t = \infty$
 3. $\sum_t^\infty \eta_t^2 < \infty$



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A simple solution is:

$$\eta_t = \frac{1}{t}, \quad (t \geq 1)$$



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Mini-batch gradient descent

- What is AI and ML?
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- Can we estimate the gradient in a better way?



- What is AI and ML?
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 - Example: Logistic regression
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- Can we estimate the gradient in a better way?
- We take a mini-batch of size B :

$$\theta_t = \theta_{t-1} - \eta_t \nabla L(\theta, \mathbf{X}_{(S)_i}, y_{(S)_i}),$$

where $(S)_i$ is a set of random sample (without replacement) indices and $|(S)_i| = B$.



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- B is usually set to optimize hardware



SGD with momentum

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SGD with momentum

- SGD can be slow to converge due to 'jumping' behaviour
- Can improve behaviour using momentum – the rolling mean of gradients
- Additional hyperparameter α to control the momentum

$$m_t = \alpha m_{t-1} + \eta_t \hat{\nabla} L(\theta_{t-1}, X_i, y_i),$$

$$\theta_t = \theta_{t-1} - m_t,$$

Figure: SGD with momentum



(a) SGD without momentum



(b) SGD with momentum



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SGD with momentum, Intuition

Figure: SGD with momentum, Intuition (CC)





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SGD with momentum

Example of SGD with momentum [here](#).



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Adaptive Moment Estimation (Adam)

- Adapt η_t to individual parameters

$$m_t = \beta_1 m_{t-1} + (1 - \beta_1) \hat{\nabla} L(\theta_{t-1}, X_i, y_i)$$

$$v_t = \beta_2 v_{t-1} + (1 - \beta_2) \hat{\nabla} L(\theta_{t-1}, X_i, y_i)^2$$

- Bias correction
(due to initialization at 0)

$$\hat{m}_t = \frac{m_t}{1 - \beta_1^t}$$

$$\hat{v}_t = \frac{v_t}{1 - \beta_2^t}$$

- Update

$$\theta_t = \theta_{t-1} - \frac{\eta}{\sqrt{\hat{v}_t} + \epsilon} \hat{m}_t,$$

- Common values: $\beta_1 = 0.9$, $\beta_2 = 0.999$, and $\epsilon = 10^{-8}$



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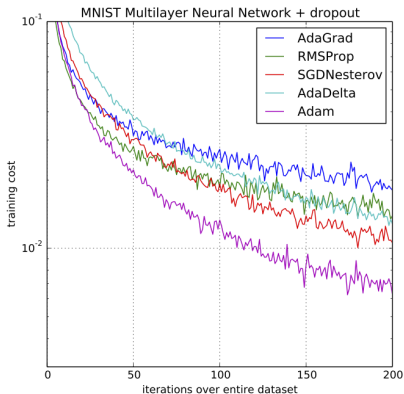
- Common values: $\beta_1 = 0.9$, $\beta_2 = 0.999$, and $\epsilon = 10^{-8}$
- RMSprop is another (similar) alternative



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Adam

Figure: The Adam Optimizer (Kingma and Ba, 2014)



For convergence proofs, see:
Defossez et al (2020) "A Simple Convergence Proof of Adam and Adagrad"