

- Introduction to Neural Networks
 - Feed-Forward Neural
 - Feed-Forward Neural
 Networks
 - Hyper-parameters
- Optimization
- Regularization

Machine learning, big data and artificial intelligence – Block 4

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- Feed-Forward Neural
- Feed-Forward Neural Networks
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- Took too much time (roughly 26h) how to solve this? Hints? remove subtasks?
- More teaching on code
- The bugs...
- Minor comments:
 - xgboost video
 - bigger diff between RF and bagging
 - more focus on the assignment on the lecture



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Grading of assignment 1

- Why is SGD important?
- Differece between unsupervised and supervised learning.
 Task or experience?



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Masters thesis proposals

- 1. Evaluation of probabilistic programming frameworks
- 2. Predicting introductions in Swedish parliamentary protocols using BERT
- 3. Topic model inference: (Stochastic) variational inference and Gibbs sampling
- 4. Will Svenska akademins ordlista (SAOL) improve Swedish word embeddings?
- 5. Fine-tune a language model (BERT) on EDGAR-CORPUS
- 6. OCR-error detection using image and text classification



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This week's lecture

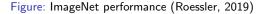
Feed-Forward Neural Networks

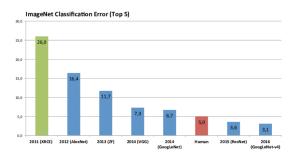


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The Hype: Computer Vision







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The Hype: Speech Recognition

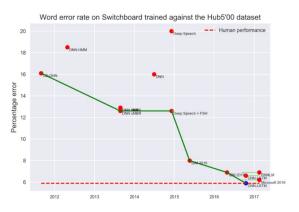


Figure: Speech recognition performance (source:

https://eff.org/ai/metrics)



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The Hype: Natural Language Processing

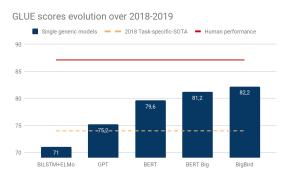


Figure: General Language Understanding (source: https://www.programmersought.com/article/4251948498/)

Work is very much ongoing:

https://gluebenchmark.com/leaderboard



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The Hype

• Although - Neural Networks is not a silver bullet



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The Hype

- Although Neural Networks is not a silver bullet
- Remember the Bayes error



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The Hype

- Although Neural Networks is not a silver bullet
- Remember the Bayes error
- Some times a linear regression (or Random Forest) is enough



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The Feed-Forward Network

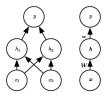


Figure 6.2: An example of a feedforward network, drawn in two different styles. Specifically, this is the feedforward network we use to solve the XOR example. It has a single hidden layer containing two units. (Left)In this style, we draw every unit as a node in the graph. This style is very explicit and unambiguous but for networks larger than this example it can consume too much space. (Right)In this style, we draw a node in the graph for each entire vector representing a layer's activations. This style is much more compact.

Figure: A simple feed-forward network (Goodfellow et al, 2017)

Important concepts:

Layers, neurons, input, output, weights, bias, architecture



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- Different networks for different purposes
 - Convolutional Neural Networks: Computer Vision



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Different Architectures for Different Purposes

- Different networks for different purposes
 - Convolutional Neural Networks: Computer Vision
 - Recurrent Neural Networks: Speech Audio (?)



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Different Architectures for Different Purposes

- Different networks for different purposes
 - Convolutional Neural Networks: Computer Vision
 - Recurrent Neural Networks: Speech Audio (?)
 - Transformers/Attention: Textual data
- The Neural Network Zoo: https: //www.asimovinstitute.org/neural-network-zoo/



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Areas of Use: All fields

- Supervised learning
- Unsupervised learning
- Reinforcement learning



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Why and when neural nets?

- Learning feature representations
- Needs a lot of data to learn complex representations
- Good for sensor data (high-dimensional)



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Why and when neural nets?

- Learning feature representations
- Needs a lot of data to learn complex representations
- Good for sensor data (high-dimensional)
- When should we not use neural networks?



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Learning Representations

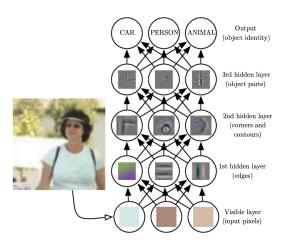


Figure: Learning representations can be crucial (Goodfellow et al, 2017, Fig. 1.2)



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The Feed-Forward Network

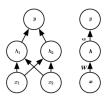


Figure 6.2: An example of a feedforward network, drawn in two different styles. Specifically, this is the feedforward network we use to solve the XOR example. It has a single hidden layer containing two units. (Left/lln this style, we draw every unit as a node in the graph. This style is very explicit and unambiguous but for networks larger than this example it can consume too much space. (Right/lln this style, we draw a node in the graph for each entire vector representing a layer's activations. This style is much more compact.

Figure: A simple feed-forward network (Goodfellow et al, 2017, Fig. 6.2)

In mathematical notation:

$$y_i = \mathbf{w}^T g(\mathbf{W}^T \mathbf{x}_i + \mathbf{b}_1) + \mathbf{b}_2$$



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The Feed-Forward Network

$$y_i = \mathbf{w}^T g(\mathbf{W}^T \mathbf{x}_i + \mathbf{b}_1) + \mathbf{b}_2$$

$$W=egin{pmatrix} 1 & 1 \ 1 & 1 \end{pmatrix}$$
 , $w=egin{pmatrix} 1 \ -2 \end{pmatrix}$, $b_1=egin{pmatrix} 1 \ -1 \end{pmatrix}$, $b_2=egin{pmatrix} 0 \end{pmatrix}$

$$g(z) = ReLU(z) = max(0, z), x_i = \begin{pmatrix} 0 \\ 0 \end{pmatrix},$$

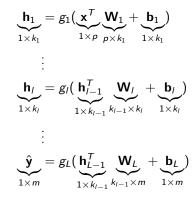
$$y_i = \begin{pmatrix} 1 \\ -2 \end{pmatrix}^T g(\begin{pmatrix} 0 \\ 0 \end{pmatrix} + \begin{pmatrix} 1 \\ -1 \end{pmatrix}) + (0)$$
$$y_i = \begin{pmatrix} 1 \\ -2 \end{pmatrix}^T \begin{pmatrix} 1 \\ 0 \end{pmatrix} + (0) = 1$$



The Feed-Forward Network

A feed-forward network for one observation (x_i) .

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$$\hat{y} = f_L(f_{L-1}(...f_1(x)...))$$



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Activation functions (g_l)

• Sometimes use notation σ as in $\sigma(Wh+b)$



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Activation functions (g_l)

- Sometimes use notation σ as in $\sigma(Wh + b)$
- Historically g(z) has been the sigmoid or or hyperbolic tangent (tanh)

$$g_{\text{sigmoid}}(z) = \frac{e^z}{e^z + 1} = \frac{1}{1 + e^{-z}}$$

$$g_{tanh}(z) = \frac{\sinh z}{\cosh z} = \frac{e^{2z} - 1}{e^{2z} + 1}$$



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Now, usually variants of Rectified linear unit (ReLU)

$$g_{ReLU}(z) = max(0, z)$$

- Easier to estimate with SGD
- Easier for deep models
- Last activation is the output function g_L, usually a softmax (if classification)

$$f(z_i) = \frac{e^{z_i}}{\sum_{i=1}^J e^{z_i}}$$



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Activation functions (g_l)

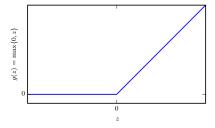


Figure: Rectified Linear Unit (Goodfellow et al, 2017, Fig. 6.3)



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Universal Approximation Theorem

"A feed-forward neural network with a linear output layer and at least one hidden layer with any 'squashing' activation function can approximate any Borel measurable function from one finite-dimensional space to another with any desired non-zero amount of error, provided that the network is given enough hidden units." (Goodfellow et al. 2017, p. 198)

- Also holds for ReLU
- No garantuee we can learn the network
- No garantuee that it will generalize
- No indication of how large the network need to be



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Hyper-parameters in feed-forward networks

- The number of layers
- The number of neurons
- Activation functions
- The type of layers (CNN, MaxPooling, Multi-head attention)



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How to choose parameters

- Trial and error on validation sets
- Art rather than science
- Specialized approaches (Bayesian Optimization)



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How to choose parameters

- Trial and error on validation sets
- Art rather than science
- Specialized approaches (Bayesian Optimization)
- Grid search (combinatorical explosion)
 - Really bad with many parameters with less effects
 - If we have 5 irrelevant parameters we try 3 values for: 125 training per relevant run
 - Instead use...



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 - Instead use...
- Random search



Grid search vs. Random Search

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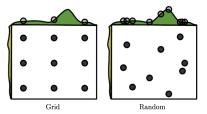


Figure: Grid search and random search (Goodfellow et al, 2017, Fig. 11.2)



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Optimization of Neural Networks

- Difficult problem
- Many local minima (weight space symmetry)
- Platueas and sadel points
 - Gradient is small but not a minimum or maximum
 - Sadel points increases with the number of dimensions (?)
 - · Large areas with small change in cost function



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Optimization of Neural Networks II

- A lot of parameters (W and b)
- Usually a lot of data



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Optimization of Neural Networks II

- A lot of parameters (W and b)
- Usually a lot of data
- Stochastic Gradient Descent, commonly
 - Adam



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Optimization of Neural Networks II

- A lot of parameters (W and b)
- Usually a lot of data
- Stochastic Gradient Descent, commonly
 - Adam
- To compute gradients: backpropagation
 - Chain-rule for derivatives



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Initial values

- We need to have starting values for SGD non-trivial
- Bad initial values might
 - Bad convergence (local optimum)
 - Numerical problems
- We want to break symmetry between layers
- Initialization can be seen as a hyperparameter
- Good practice
 - Initialize values randomly close to zero (uniform or normal)



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Neural Networks in Practice: TensorFlow and Keras

- Tensorflow
 - Framework for large-scale machine learning and Neural Networks
 - Developed by Google
 - Computational graphs
 - Handles:
 - Computing gradients for Neural Networks
 - Enable simple use of graphical processing units (GPU) and Tensor processing Units (TPU)
 - Used in both research and production
- Keras
 - Syntax for 'building' Neural Networks
 - Platform independent (ish)





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Regularization of Neural Networks

• Reduce traing error but improve test/validation error



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Regularization of Neural Networks

- Reduce traing error but improve test/validation error
- Neural Networks are extremely flexible / high model capacity



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Regularization of Neural Networks

- Reduce traing error but improve test/validation error
- Neural Networks are extremely flexible / high model capacity
- Regularization is crucial for good generalizability of NN



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Weight decay / Norm penalty

Let

$$\tilde{J}(W, b) = J(W, b) + \alpha \Omega(W),$$

where J(W, b) is the cost function and $\alpha\Omega(W)$ is the penalty for the weight matrices.

 \bullet α is the strength of the penalty.





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Weight decay / Norm penalty

Let

$$\Omega_1(W) = \sum_i \sum_i |w|_{i,j}$$
,

and

$$\Omega_2(W) = \sum_i \sum_j w_{i,j}^2,$$

be the L_1 and L_2 regularization respectively.

We can then get the cost function

$$\tilde{J}(W,b) = J(W,b) + \sum_{l} \alpha_{l} \Omega_{2}(W_{l}),$$



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Weight decay / Norm penalty

Lets define the cost function as

$$\tilde{J}(w) = J(w) + \alpha \Omega_2(w)$$
$$= J(w) + \alpha w^T w$$

• Then the gradient update becomes

$$\nabla_w \tilde{J}(w) = \nabla_w J(w) + 2\alpha w$$

• To update our weights with gradient descent

$$w \leftarrow w - \epsilon(\nabla_w J(w) + 2\alpha w)$$

$$w \leftarrow (1 - 2\alpha \epsilon)w - \epsilon \nabla_w J(w)$$



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Weight decay / Norm penalty

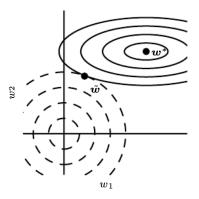


Figure: L₂ regularization (Goodfellow et al, 2017, Fig. 7.1)



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Early Stopping

- Stop optimization early based on validation error
- Rerun to that number of epochs (hyperparameter)
- Can be shown to be quivalent (under strict assumptions) to L_2 regularization

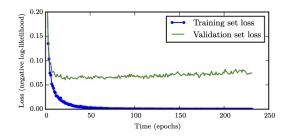


Figure: Early Stopping (Goodfellow et al, 2017, Fig. 7.3)



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Early Stopping

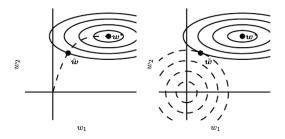


Figure: Early Stopping (Goodfellow et al, 2017, Fig. 7.4)



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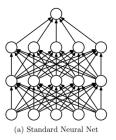
Dropout

- In each iteration:
 - Sample an indicator I_i for each node i
 - Set the value h_i to 0 with probability p
- The dropout probability is typically 0.8 for input nodes and 0.5 for hidden nodes
- Forces the network to
 - not rely on individual nodes
 - spread out the weights over more nodes
- Can be seen as an ensamble method



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Dropout



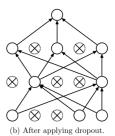


Figure 1: Dropout Neural Net Model. Left: A standard neural net with 2 hidden layers. Right: An example of a thinned net produced by applying dropout to the network on the left. Crossed units have been dropped.

Figure: Dropout (Srivastava et al, 2014)



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Other regularization techniques

- In CNN: Dataset augmentation
- Get more data...