Report COVID19 Model

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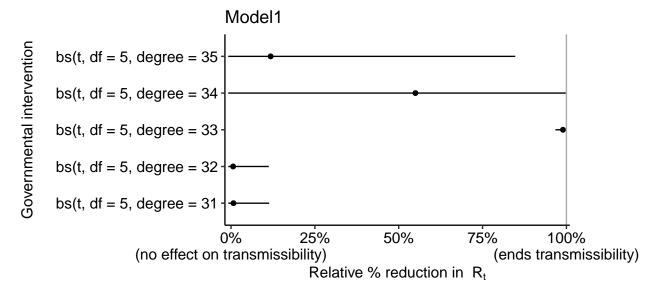
Summary / Take Away

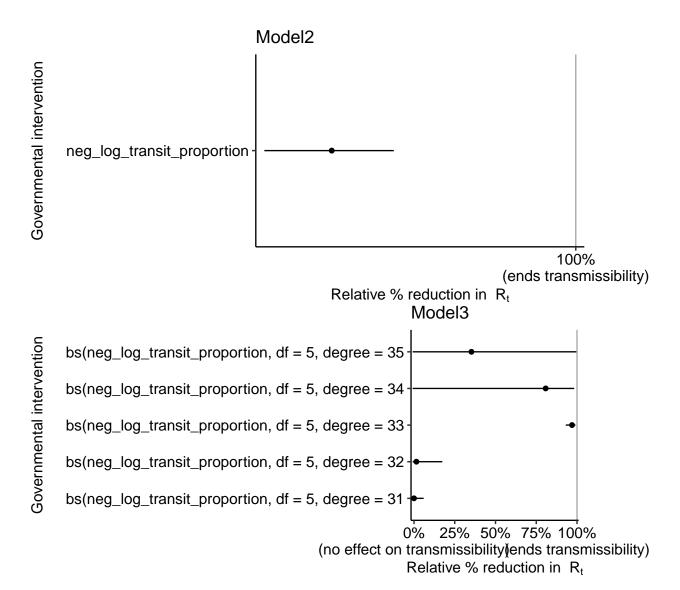
- It is possible to include b-splines in the model.
- It does not seem to give a lot of gains with using b-splines compare to linear effects.
- Using splines for t is working well to capture the underlying change in Rt, although, this should be needed to be different for different countries.

Model descriptions

- Model 1: Splines on t, the time point
- Model 2: Linear neg_log_transit_proportion
- Model 3: Splines on neg_log_transit_proportion

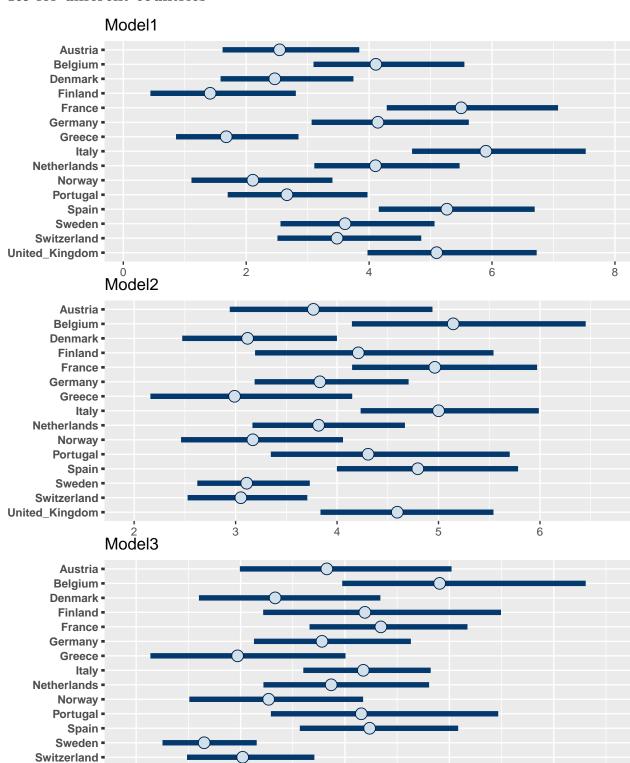
Covariate effects



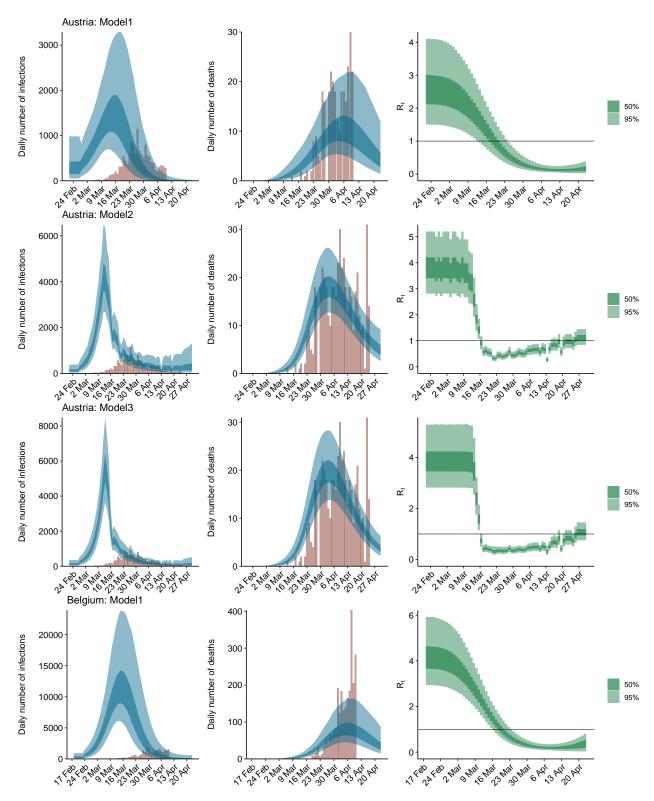


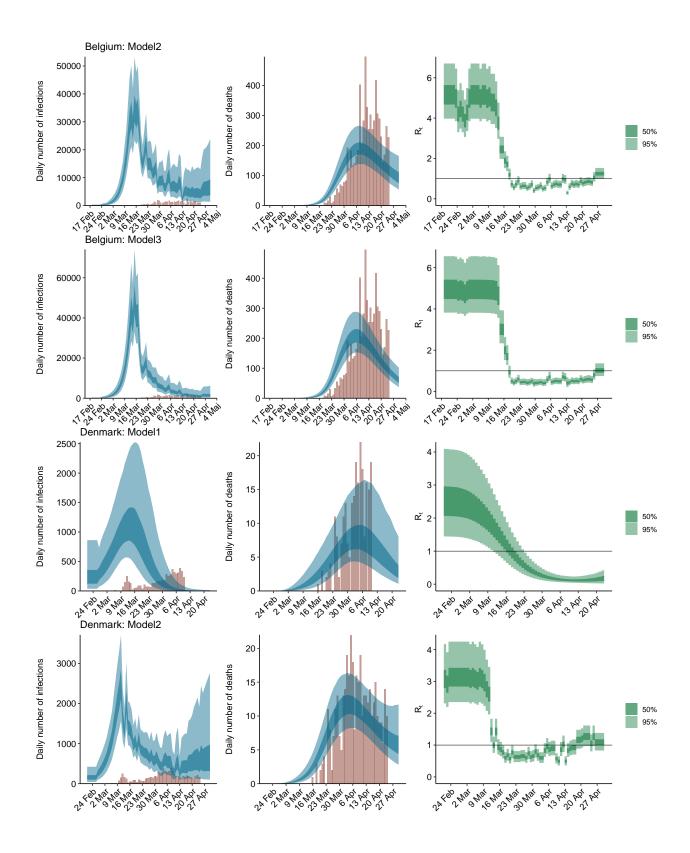
R0 for different countries

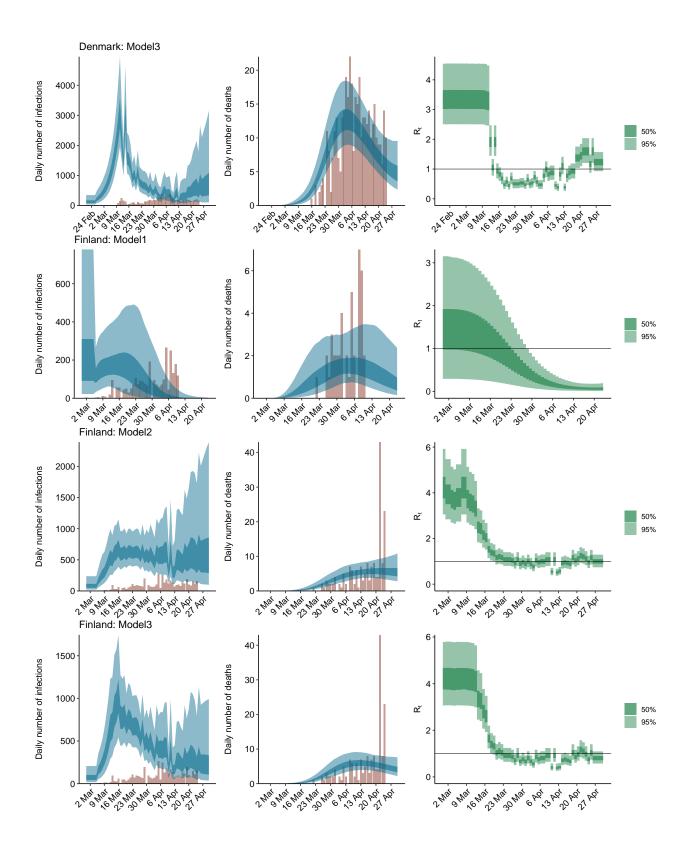
United_Kingdom -

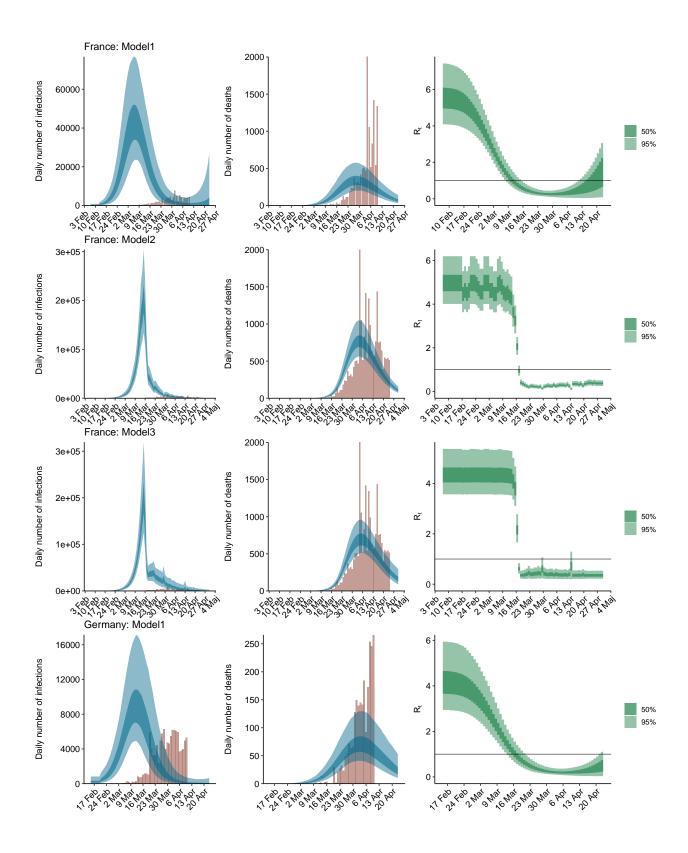


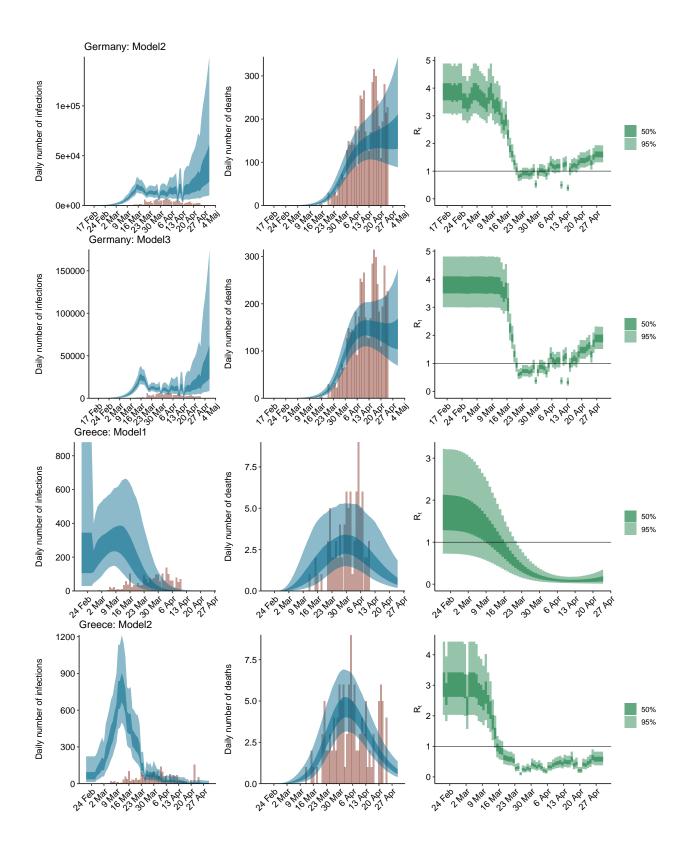
Infections, deaths and Rt by country and model

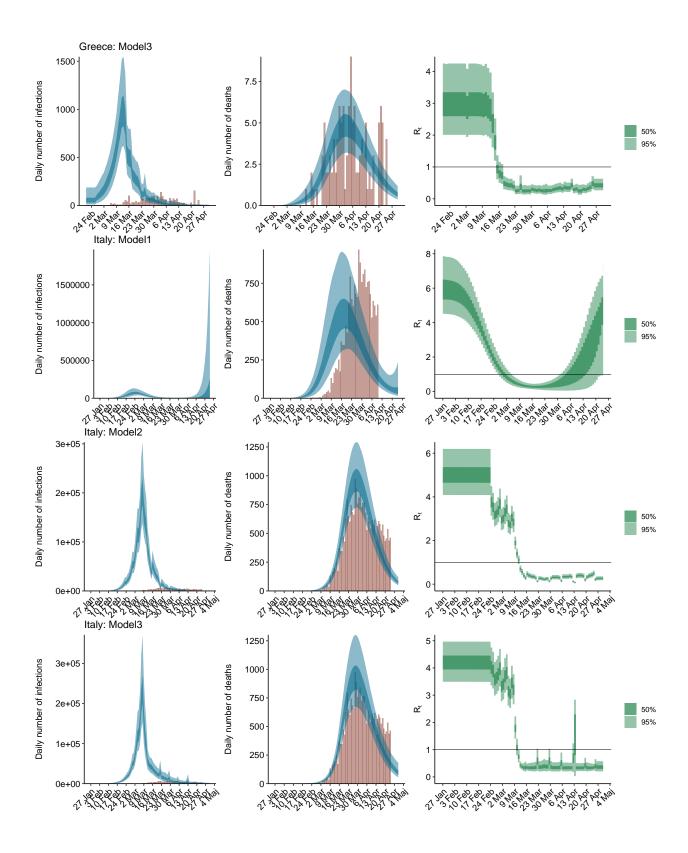


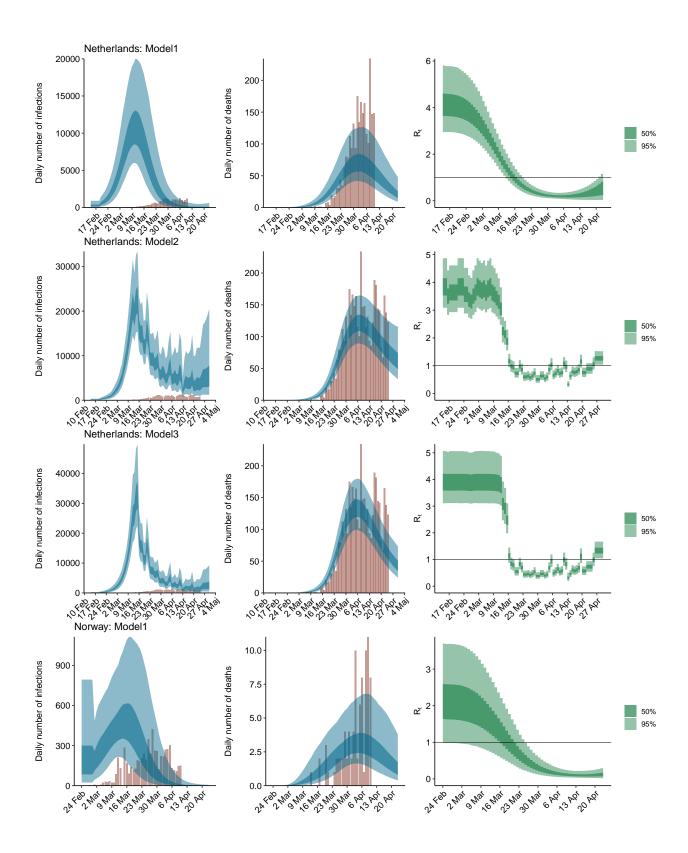


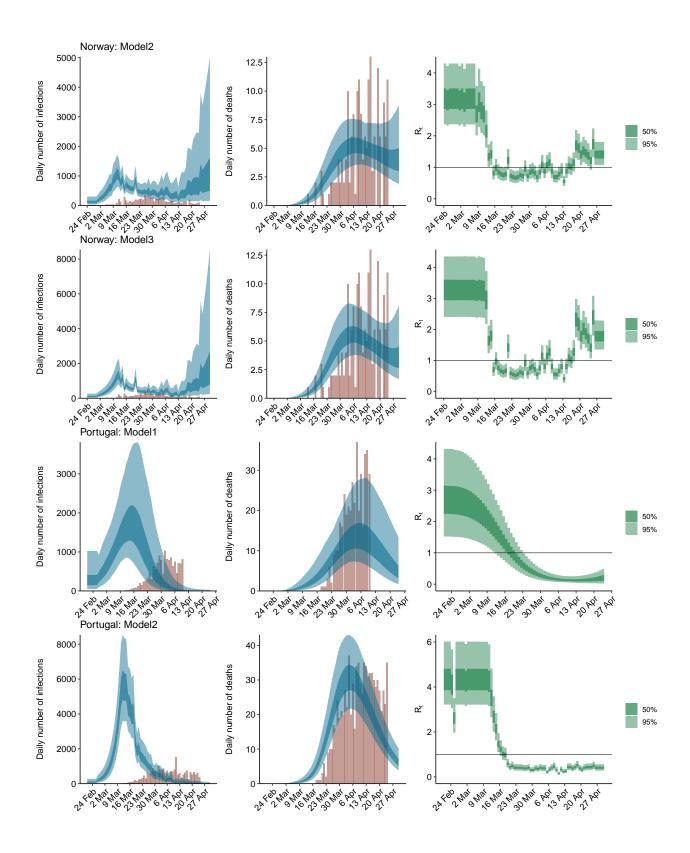


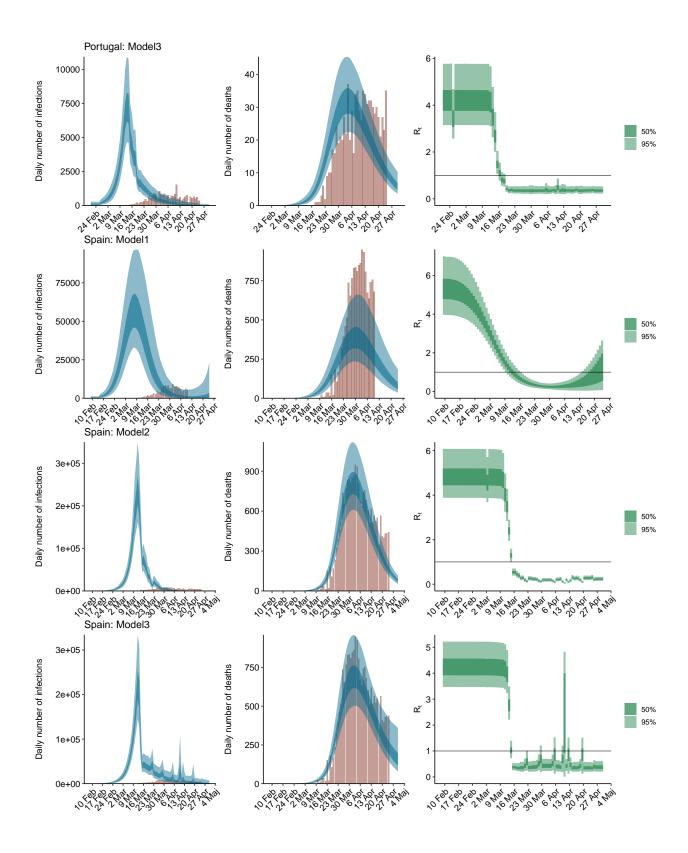


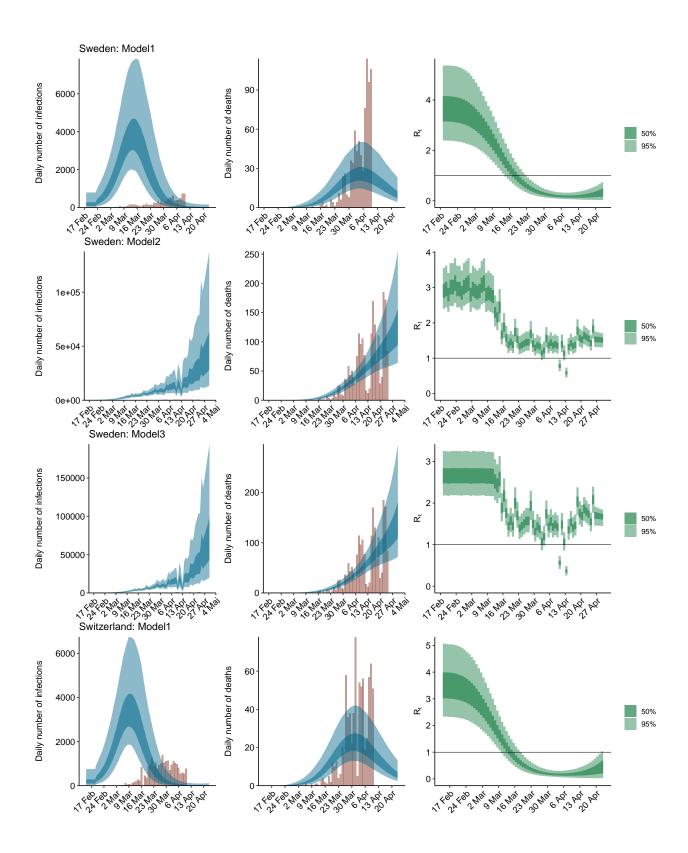


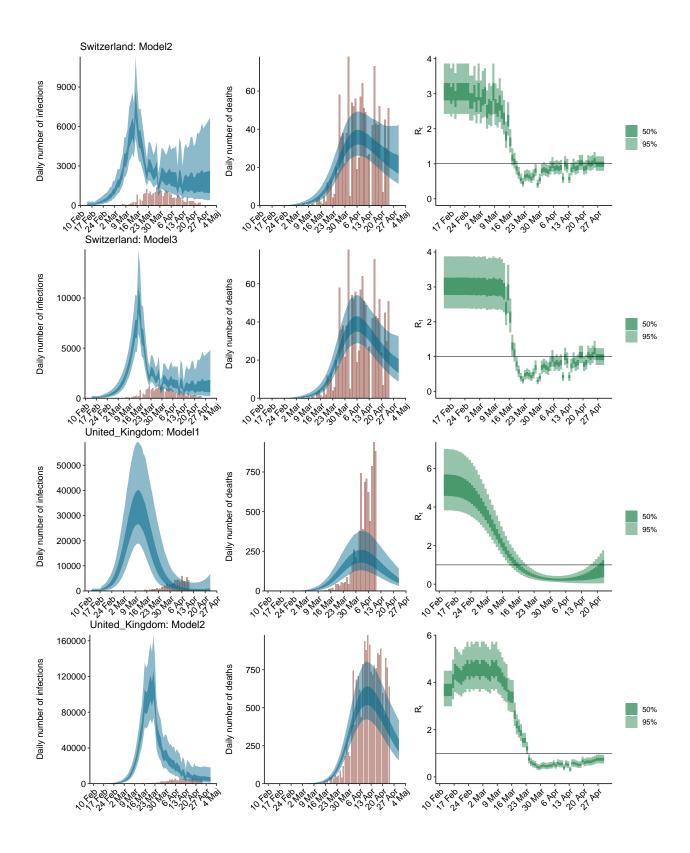


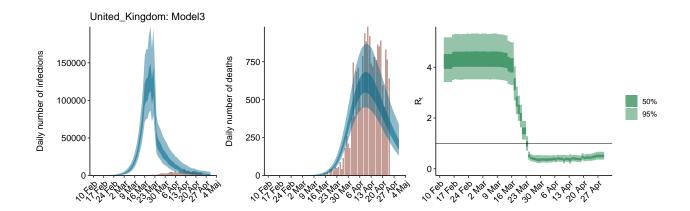












Stan code

```
## S4 class stanmodel 'base_general_speed' coded as follows:
     int <lower=1> M; // number of countries
##
##
     int <lower=1> P; // number of covariates
     int <lower=1> NO; // number of days for which to impute infections
##
     int<lower=1> N[M]; // days of observed data for country m. each entry must be <= N2
##
##
     int<lower=1> N2; // days of observed data + # of days to forecast
##
     int cases[N2,M]; // reported cases
     int deaths[N2, M]; // reported deaths -- the rows with i > N contain -1 and should be ignored
##
##
     matrix[N2, M] f; // h * s
     matrix[N2, P] X[M];
##
##
     int EpidemicStart[M];
##
     real pop[M];
##
     real SI[N2]; // fixed pre-calculated SI using emprical data from Neil
## }
##
## transformed data {
     vector[N2] SI_rev; // SI in reverse order
##
     vector[N2] f_rev[M]; // f in reversed order
##
##
##
     for(i in 1:N2)
       SI_rev[i] = SI[N2-i+1];
##
##
     for(m in 1:M){
##
       for(i in 1:N2) {
##
        f_{rev}[m, i] = f[N2-i+1,m];
##
##
     }
##
## }
##
##
## parameters {
##
     real<lower=0> mu[M]; // intercept for Rt
##
     real<lower=0> alpha_hier[P]; // sudo parameter for the hier term for alpha
     real<lower=0> kappa;
##
##
     real<lower=0> y[M];
     real<lower=0> phi;
##
     real<lower=0> tau;
```

```
real <lower=0> ifr_noise[M];
##
## }
##
## transformed parameters {
##
       vector[P] alpha;
       matrix[N2, M] prediction = rep_matrix(0,N2,M);
##
       matrix[N2, M] E_deaths = rep_matrix(0,N2,M);
##
       matrix[N2, M] Rt = rep_matrix(0,N2,M);
##
##
       matrix[N2, M] Rt_adj = Rt;
##
##
##
         matrix[N2,M] cumm_sum = rep_matrix(0,N2,M);
##
         for(i in 1:P){
           alpha[i] = alpha_hier[i] - (log(1.05) / 6.0);
##
##
         }
##
         for (m in 1:M){
           /*
##
##
           for (i in 2:N0){
##
             cumm_sum[i,m] = cumm_sum[i-1,m] + y[m];
##
##
           */
##
           prediction[1:N0,m] = rep_vector(y[m],N0); // learn the number of cases in the first NO days
##
           cumm_sum[2:N0,m] = cumulative_sum(prediction[2:N0,m]);
##
##
           Rt[,m] = mu[m] * exp(-X[m] * alpha);
##
             Rt_adj[1:N0,m] = Rt[1:N0,m];
##
           for (i in (NO+1):N2) {
##
             /*
##
             real convolution=0;
##
             for(j in 1:(i-1)) {
               convolution += prediction[j, m] * SI[i-j];
##
##
##
             */
##
             real convolution = dot_product(sub_col(prediction, 1, m, i-1), tail(SI_rev, i-1));
##
##
             cumm_sum[i,m] = cumm_sum[i-1,m] + prediction[i-1,m];
##
             Rt_adj[i,m] = ((pop[m]-cumm_sum[i,m]) / pop[m]) * Rt[i,m];
##
             prediction[i, m] = Rt_adj[i,m] * convolution;
##
##
           E_{deaths}[1, m] = 1e-15 * prediction[1,m];
##
##
           for (i in 2:N2){
##
             // for(j in 1:(i-1)){
##
                  E_deaths[i,m] += prediction[j,m] * f[i-j,m] * ifr_noise[m];
##
             // }
##
             E_deaths[i,m] = ifr_noise[m] * dot_product(sub_col(prediction, 1, m, i-1), tail(f_rev[m],
##
##
         }
       }
##
## }
## model {
##
     tau ~ exponential(0.03);
##
     for (m in 1:M){
##
         y[m] ~ exponential(1/tau);
```

```
}
##
##
    phi ~ normal(0,5);
##
     kappa ~ normal(0,0.5);
     mu ~ normal(3.28, kappa); // citation: https://academic.oup.com/jtm/article/27/2/taaa021/5735319
##
##
     alpha_hier ~ gamma(.1667,1);
     ifr_noise ~ normal(1,0.1);
##
##
     for(m in 1:M){
##
       deaths[EpidemicStart[m]:N[m], m] ~ neg_binomial_2(E_deaths[EpidemicStart[m]:N[m], m], phi);
##
## }
##
##
   generated quantities {
       matrix[N2, M] prediction0 = rep_matrix(0,N2,M);
##
##
       matrix[N2, M] E_deaths0 = rep_matrix(0,N2,M);
##
##
##
         matrix[N2,M] cumm_sum0 = rep_matrix(0,N2,M);
         for (m in 1:M){
##
            for (i in 2:N0){
##
             cumm_sum0[i,m] = cumm_sum0[i-1,m] + y[m];
##
##
##
           prediction0[1:N0,m] = rep_vector(y[m],N0);
           for (i in (NO+1):N2) {
##
##
             real convolution0 = 0;
##
             for(j in 1:(i-1)) {
##
               convolution0 += prediction0[j, m] * SI[i-j];
##
             }
             cumm_sum0[i,m] = cumm_sum0[i-1,m] + prediction0[i-1,m];
##
             prediction0[i, m] = ((pop[m]-cumm_sum0[i,m]) / pop[m]) * mu[m] * convolution0;
##
##
##
##
           E_{deaths0[1, m]} = uniform_rng(1e-16, 1e-15);
##
           for (i in 2:N2){
##
             for(j in 1:(i-1)){
               E_deaths0[i,m] += prediction0[j,m] * f[i-j,m] * ifr_noise[m];
##
##
##
           }
##
         }
##
       }
## }
##
```