

Brown'sche Bewegung

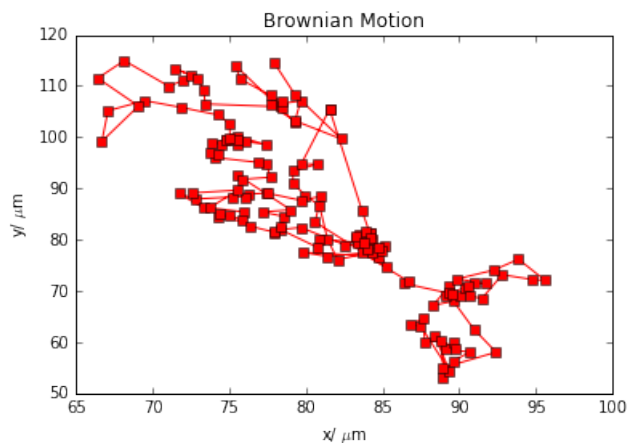
Teil 1: Importieren und Darstellen der Daten

```
In [2]: #Importieren der notwendigen Module
%matplotlib inline
import matplotlib.pyplot as plt
import matplotlib.mlab as mlab
import numpy as np

def comma_to_float(valstr):
    return float(valstr.decode("utf-8").replace(',','.'))
```

```
In [55]: #Einlesen der Daten
t,x,y = np.loadtxt('/Users/Peter/Desktop/Python-Kurs/MessungJSPM.dat', skiprows=1, usecols=(1,2,3),
                  converters= {1:comma_to_float, 2:comma_to_float,
                               3:comma_to_float},unpack=True)
```

```
In [56]: #Wir verschaffen uns einen Überblick über die Bewegung des Teilchens mit Hilfe eines Punkt-Linien-Diagramms
plt.plot(x,y,marker='s', color = 'red', linewidth = 1 )
plt.xlabel('x/'+' $\\mu$'+'m')
plt.ylabel('y/'+' $\\mu$'+'m')
plt.title('Brownian Motion')
plt.savefig('brown1.pdf', format = 'PDF')
```



Teil 2: Berechnung mittleres Verschiebungsquadrat und Fehler

```
In [66]: dt = np.array([])
dx = np.array([])
dy = np.array([])

for i in range(len(t)-1):
    dt = np.append(dt,t[i+1] - t[i])
    dx = np.append(dx,x[i+1]-x[i])
    dy = np.append(dy,y[i+1] - y[i])

r_squared=dx**2+dy**2
r_squared_mean=np.mean(r_squared)
```

```

print("r_squared_mean= ", r_squared_mean)
r_squared_mean_std=np.std(r_squared)/np.sqrt(len(r_squared))
print("r_squared_mean_std= ", r_squared_mean_std)
dt_mean=np.mean(dt)
print("dt_mean= ", dt_mean)

# gefundene Werte, wenn alle Messdaten benutzt werden:
#r_squared_mean= 14.6056025102
#r_squared_mean_std= 3.08628207078
#dt_mean= 1.00053061224

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dt_mean= 1.00053061224

```

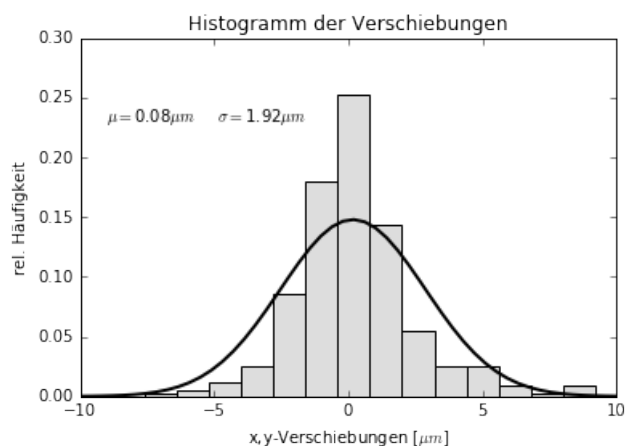
Teil 3: Kontrollverteilung

```

In [85]: plt.hist(all_data, normed=1, bins=np.arange(-10, 10, 1.2),color='#D
DDDDD')

mu=np.mean(all_data)
sigma=np.std(all_data)
gauss = mlab.normpdf(np.linspace(-10,10), mu , sigma)
plt.plot(np.linspace(-10,10), gauss, 'r-', linewidth=2,color='#0000
00')
plt.title('Histogramm der Verschiebungen')
plt.xlabel('x,y-Verschiebungen [$\mu$ m$'])
plt.ylabel('rel. Häufigkeit')
plt.text(-9, 0.23, '$\mu$='+str(round(np.mean(np.append(dx,dy)),2))
+'$\mu$ m $\quad$'+ '$\sigma$='+str(round(np.std(np.append(dx,dy)),2
))+'$\mu$ m$')
plt.savefig('brown_2.1.pdf', format='PDF')

```

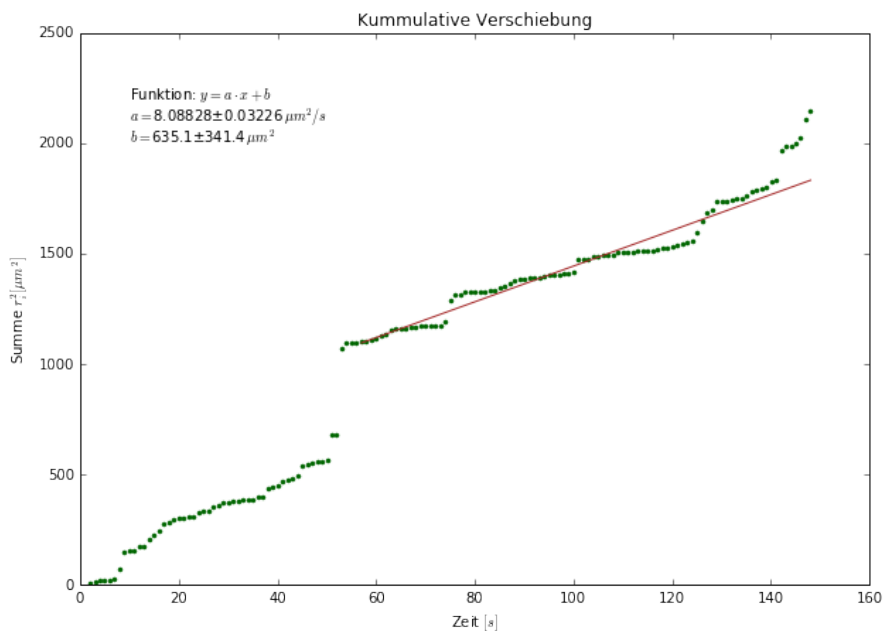


Teil 4: Kumulative Verteilung der Verschiebungsquadrate

```
In [83]: r_kumm=np.cumsum(r_squared)
plt.figure(figsize=(10,7))
plt.plot(t[:-1], r_kumm, marker='.', color='#006600', linewidth=0)
plt.xlabel('Zeit [s]')
plt.ylabel('Summe  $r_i^2$  [ $\mu\text{m}^2$ ]')
plt.title('Kummulative Verschiebung')

from scipy.optimize import curve_fit

def linear(x,a,b):
    return a*x+b
popt, pcov = curve_fit(linear, t[57:-8], r_kumm[57:-7])
plt.text(10,2200,"Funktion:  $y=a \cdot x + b$ ")
plt.text(10,2100,"$a=$" + "{0:.5f}".format(popt[0]) +u"\u00B1"+ "{0:.5f}".format(pcov[0,0]) + "$\, \mu\text{m}^2 / \text{s}$")
plt.text(10,2000,"$b=$" + "{0:.1f}".format(popt[1]) +u"\u00B1"+ "{0:.1f}".format(pcov[1,1]) + "$\, \mu\text{m}^2$")
plt.plot(t[55:-1], linear(t[55:-1],*popt), color="brown")
plt.savefig('brown3.pdf', format='PDF', orientation='landscape', papertype = 'a4')
```



In []: