

# Assignment 1. (30 Aug)

Q1.

a)

$S_1$

$S_2$

A

B

(Switch ON)

out

0

0

0

0

1

1

1

0

1

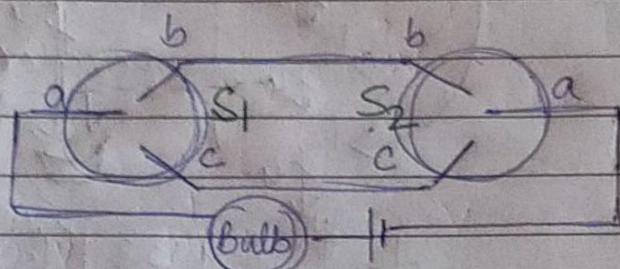
1

1

0

XOR gate.

(b)



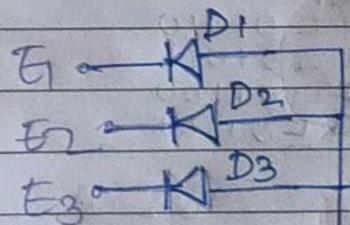
For always lighting of bulb  $\rightarrow$  path unbroken.  
both a connected to b or c.  
ie. Both switch on or off.

$$\Rightarrow S_1 \cdot S_2 + \bar{S}_1 \cdot \bar{S}_2$$

$$\Rightarrow S_1 \oplus S_2 \quad \text{or} \quad S_1 \odot S_2$$

## XNOR Gate

Q2.



diodes are ideal.

$E_1 \quad E_2 \quad E_3 \quad V_0$

all $\rightarrow$ 1	1	1	1	1
diodes OFF	1	1	0	0
	1	0	1	0
	0	1	1	0
	0	0	1	0
	1	0	0	0
	0	1	0	0
	0	0	0	0

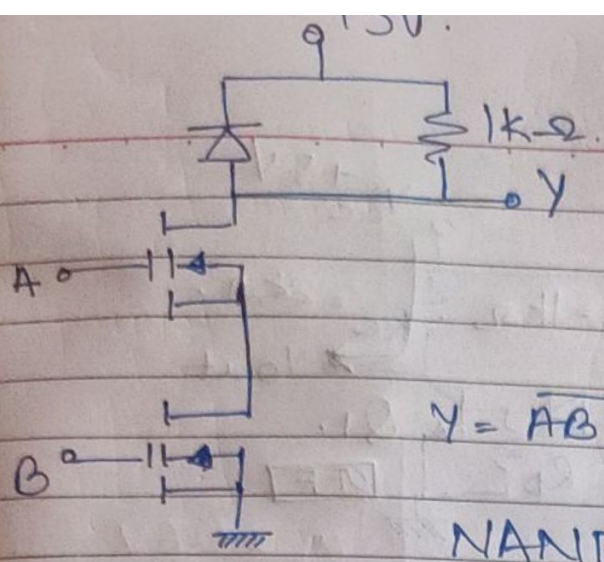
at least any diode short circuited.

diodes ON  $\rightarrow$  0 0 0 0

## AND Gate



(3/a)

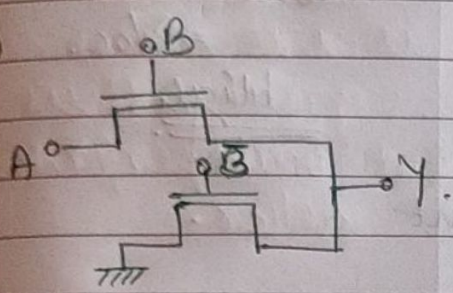


A	B	Y	nmos ON
1	1	0	∴ Y connected to ground.
1	0	1	nmos OFF ∴ Y connected to +5V.
0	1	1	
0	0	1	

$Y = \overline{AB}$

NAND Gate

(b)



A	B	Y
1	1	1
1	0	0
0	1	0
0	0	0

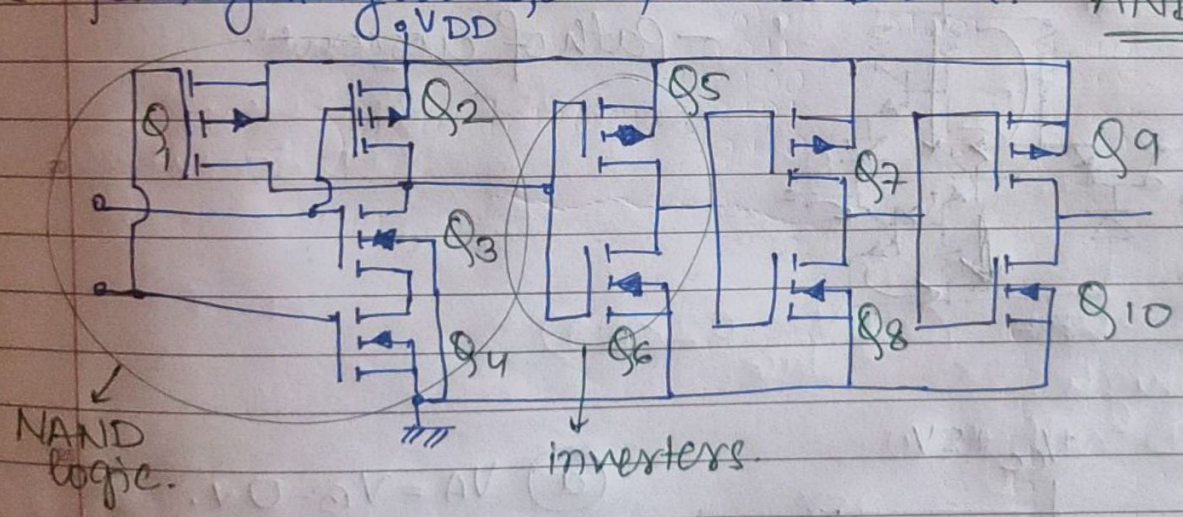
Annotations:   
 - For (1,1): B=1, Y is connected to A.  
 - For (1,0), (0,1), (0,0): Y connected to ground.

AND Gate

$Y = AB$

(c) ~~for high-level synthesis, a specific combination~~

AND Gate



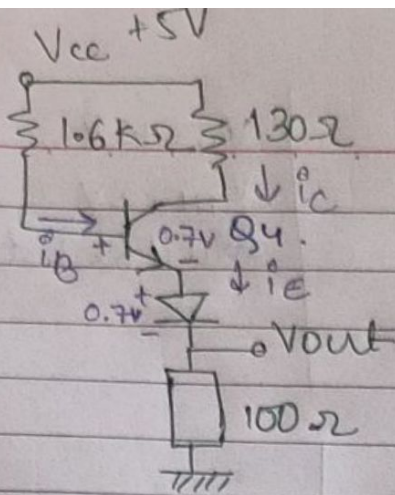
NAND + 3 (inverters) → AND gate.







(a)



Both  $V_A, V_B = 0$ .

$Q_2, Q_3 \rightarrow OFF$ .

KVL:

assuming active region.

$$i_c = \beta i_b$$

$$5 - 1600i_b - 0.7 - 0.7 - 100i_e = 0$$

$$3.6 = 1600i_b + 5100i_b$$

$$3.6 = 6700i_b$$

$$i_b = 0.537 \text{ mA}$$

$$V_{CE} = V_C - V_E$$

$$= (5 - 9 \times 130) - (100i_e + 0.7)$$

$$= -1.93$$

$< V_{CEsat}$   
transistor is in saturation.

$$V_{CEsat} = 0.3 \text{ V}$$

$$5 - 1600i_b - 0.7 - 0.7 - 100i_e = 0$$

$$3.6 = 1600i_b + 100i_e$$

$$5 - 130i_c - 0.3 - 0.7 - 100i_e = 0$$

$$4 = 130i_c + 100i_e$$

$$V_{out} = 100i_e$$

$$\therefore V_{out} = 3.6 \text{ V}$$

$$V_{BQ_2} = 0.3 \text{ V}$$

$Q_2 \rightarrow OFF$

$$i_{cQ_2} = i_{BQ_1} \approx 0$$

$$3.6 = 100i_e + 1600i_b$$

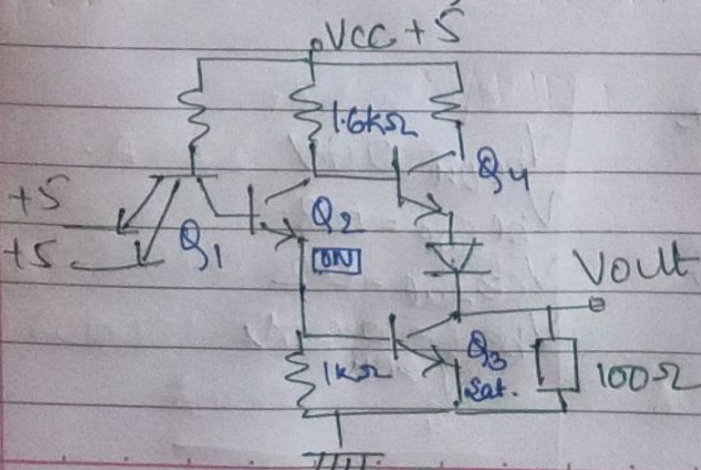
(b)

$$V_A = V_B = 5 \text{ V}$$

$Q_2 ON$

$Q_3 (Sat)$

$$\therefore V_{out} = 0.3 \text{ V}$$





Q7.

$$V_{OL} = 0.9V \quad V_{IL} = 1.2V$$

$$V_{OH} = 4.5V \quad V_{IH} = 3.2V$$

$$N_{ML} = ? \quad \text{transition width} = ?$$

$$N_{MH} = ? \quad \text{logic swing} = ?$$

$$V_{IL} = 1.5V$$

$$V_{IH} = 3V$$

will it be better?

$$N_{ML} = V_{IL} - V_{OL}$$

$$= 1.2 - 0.9 = 0.3V$$

$$N_{MH} = V_{OH} - V_{IH}$$

$$= 4.5 - 3.2 = 1.3V$$

$$\text{transition width} = V_{IH} - V_{IL}$$

$$= 3.2 - 1.2 = 2V$$

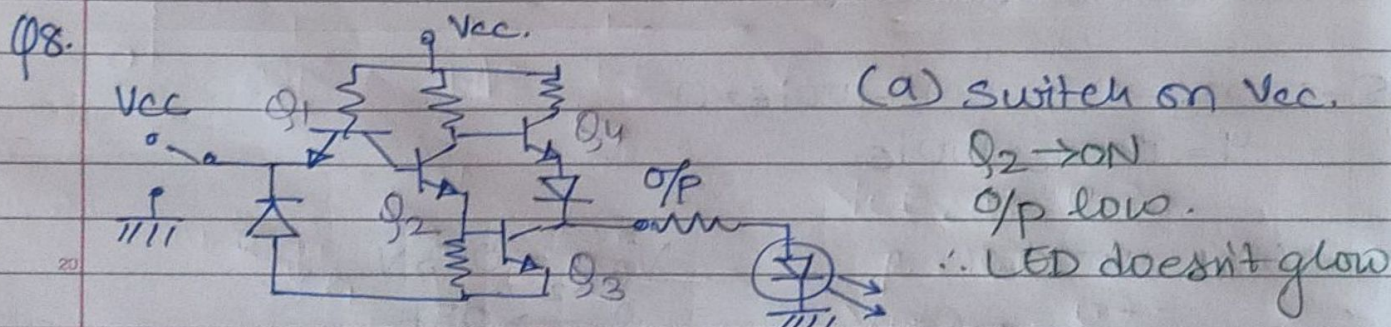
$$\text{logic swing} = V_{OH} - V_{IH}$$

$$= 4.5 - 3.2 = 1.3V$$

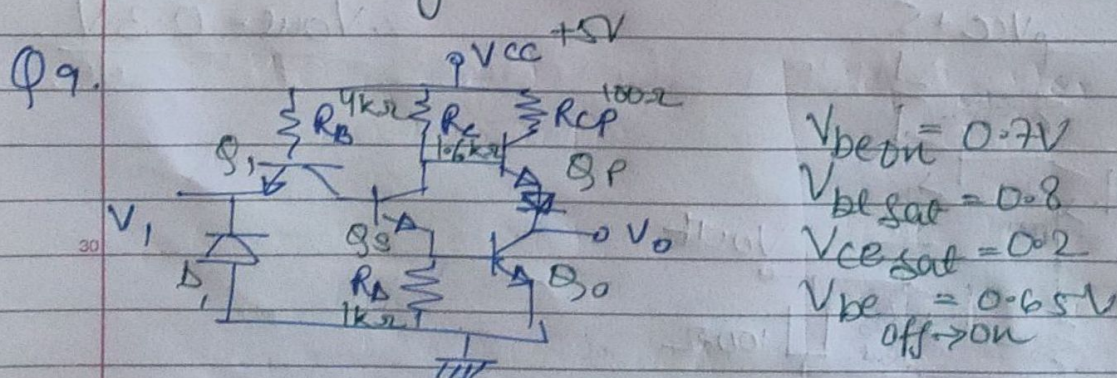
$$N_{ML} = 0.6V$$

$$N_{MH} = 1.5V$$

as noise margins is greater thus it would perform better.



(b) Switch on 0V  
 $Q_2 \rightarrow OFF$  (as  $V_{base} = 0.2 < 0.7$ )  
 O/p high.  
 LED will glow.





by inc.  $V_i$  from  $0 \rightarrow V_{cc}$ .

$$V_i \in [0, 0.45]$$

$Q_1 \rightarrow$  Saturation

$Q_2 \rightarrow$  OFF until  $V_i + 0.2 < 6.5$

$Q_0 \rightarrow$  OFF  $V_i \leq 0.45$

$$I_{Rc} = I_{BP}$$

$$V_o = V_{cc} - 0.7 - 0.7 = 3.6V$$

for high  $I_c$ ,  $Q_p \rightarrow$  saturates.

$$V_o = V_{cc} - 0.8 - 0.8 = 3.4V$$

after  $V_i \in [0.45, 1.15]$

$Q_s \rightarrow$  ON

$Q_1 \rightarrow$  Saturation

$Q_0 \rightarrow$  OFF

$Q_p \rightarrow$  active.

$$A_{Vs} = \frac{-R_c}{R_D} = -1.6 \rightarrow V_i \in [0.45, 1.05]$$

$Q_0 \rightarrow$  OFF until  $V_{RD} \leq 0.65$

$Q_0 \rightarrow$  ON when  $V_i + 0.2 - 0.7 - 0.65 = 0$   
 $V_i = 1.15$

$$V_o = V_{cc} - I_c R_c - 0.8 - 0.8 = 3.4 - 0.65 \times 1.6$$

$$V_o = 2.36V$$

$$\begin{aligned} V_{RD} &= 0.65 \\ I_{ES} &= 0.65 \text{ mA} \\ I_{CS} &\approx I_{ES} \end{aligned}$$

$Q_s, Q_0 \rightarrow$  active

$Q_1 \rightarrow$  Saturation

$Q_2 \rightarrow$  (active  $\Rightarrow$  OFF)

$$r_d \approx 1k\Omega$$

$$\begin{aligned} \Delta V_o &= A_{Vs} \Delta V_{Bs} + A_{Vo} \Delta V_{Bo} \\ A_v &= A_{Vs} + A_{Vo} = -6.8 \end{aligned}$$

$$A_{Vs} = \frac{-R_c}{R_D \parallel r_d} = -3.2$$

$$A_{Vo} = \frac{\Delta V_o}{\Delta V_{Bo}} = \frac{-\beta_F R_c \text{ eff}}{r_d} = \frac{-\beta_F (r_d + r_d + R_c)}{\beta_F} = -3.6$$



$Q_0 \rightarrow$  saturate at  $V_{BE} = 0.8V$

$$V_1 = 0.8 + 0.7 - 0.2$$

$$= 1.3V$$

$$V_0 = 0.2$$

as saturation.

If  $V_{in} \geq 7.3V$ .

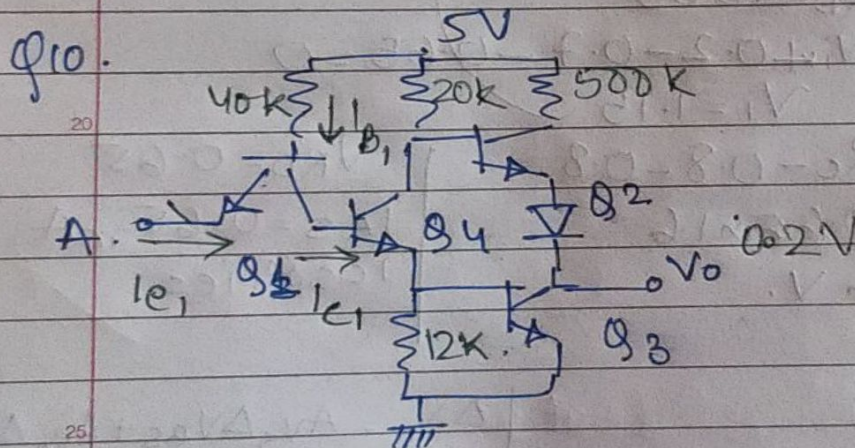
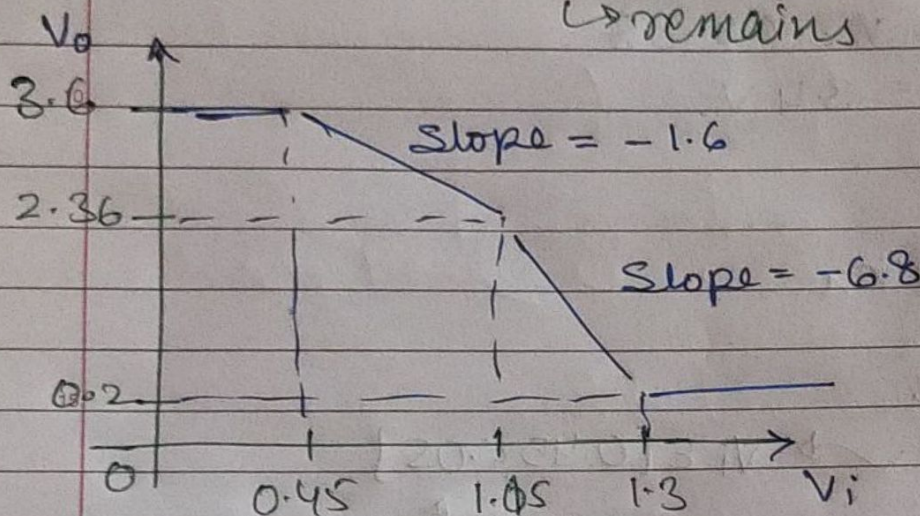
$Q_3, Q_0 \rightarrow$  saturates.

$$V_1 = 0.8 + 0.8 - 0.2$$

$$= 1.4$$

$$V_0 = 0.2 \quad (V_{CE} \text{ saturation})$$

$\hookrightarrow$  remains



$$V_{CE \text{ sat}} = 0.2$$

$$\beta = 100$$

$$V_{BE \text{ sat}} = 0.7$$

$$\alpha = 0.01 \quad (Q_1)$$

inverse active mode

$$5 - 40I_{B1} = 2.1$$

$$I_{B1} = 0.0725 \text{ mA}$$

$$\alpha Q_1 = \frac{I_{e1}}{I_{B1}} = 0.01$$

$$I_{e1} = \frac{1}{100} \times 0.0725 \text{ mA}$$

$$I_{e1} = I_{B1} + I_{e1} = 0.07322 \text{ mA}$$

$$I_{B4} = I_{C1} = 0.07322 \text{ mA}$$

$$I_{C4} = \beta I_{B4} = 100 \times 0.07322$$

$$I_{C4} = 7.322 \text{ mA}$$