

Q1. Given a set of training datapoints (dimension: 4), create a **random forest** with 3 trees, where every tree has depth 1 only. For each tree, choose any 2 of the dimensions. Given the test datapoint, what will be output of the random forest?

Training set: $(x_1=1, x_2=2, x_3=1, x_4=4, y=1); (x_1=5, x_2=2, x_3=1, x_4=4, y=2);$
 $(x_1=1, x_2=2, x_3=1, x_4=2, y=3); (x_1=1, x_2=2, x_3=8, x_4=4, y=1);$
 $(x_1=1, x_2=5, x_3=3, x_4=2, y=2); (x_1=5, x_2=2, x_3=3, x_4=4, y=3);$
 $(x_1=9, x_2=2, x_3=8, x_4=4, y=1); (x_1=8, x_2=2, x_3=5, x_4=4, y=2);$
 $(x_1=3, x_2=2, x_3=2, x_4=3, y=3); (x_1=6, x_2=9, x_3=9, x_4=8, y=1);$
 $(x_1=9, x_2=8, x_3=7, x_4=6, y=2); (x_1=1, x_2=9, x_3=5, x_4=5, y=3);$

Test set: $(x_1=7, x_2=1, x_3=9, x_4=3, y=?); (x_1=-4, x_2=9, x_3=1, x_4=3, y=?); (x_1=12, x_2=-3, x_3=-9, x_4=18, y=?)$

Q2. You are given 6 2D data points with binary class labels. Start with a linear classifier $y = \text{sign}(x_1 - x_2)$ where x_1, x_2 are the two dimensions. Run Adaboost algorithm for 2 iterations, and thus obtain 2 more linear classifiers along with their weights. Carry out ensemble classification of these points using the 3 linear classifiers (including initial one).

IDNo	1	2	3	4	5	6
X1	2.3	4.8	2.1	4.5	7.2	1.7
X2	3.8	3.4	5.8	7.3	11.6	6.2
Y	1	1	-1	1	-1	-1

Q3. Given a set of 2D training datapoints with binary labels, find a **linear classifier** for them using **perceptron algorithm**. Start iterations with the X-axis ($x_2=0$) as w .

$(x_1=4, x_2=2, y=1); (x_1=2, x_2=3, y=1); (x_1=3, x_2=6, y=1); (x_1=4, x_2=4, y=1);$

$(x_1=6, x_2=2, y=-1); (x_1=8, x_2=5, y=-1); (x_1=7, x_2=1, y=-1); (x_1=6, x_2=6, y=-1)$

Q4. Consider a dataset with 4 labelled points:

ID	1	2	3	4
X1	2	3	5	6
X2	3	1	3	2
Y	A	A	B	B

Find a linear classifier parallel to the X2-axis, such that the total margin with respect to both of the classes is maximized. What is the total margin of your classifier? Suppose you build an SVM on these 4 points, and it returns $w = (1, 0, b)$. What can be possible values of " α " and ' b ' for the 4 points?

Q5. Consider the following 8 labelled points. Suppose you train a soft-margin SVM on them, and the resulting α -values are given below. What are the max-margin and marginal classifiers? Calculate the slack variables attached with each of the data-points in the above situation.

ID	1	2	3	4	5	6	7	8
X1	-4	-6	1	6	-3	2	-2	2
X2	3	1	2	0	-2	1	-3	-5
Y	B	B	B	B	A	A	A	A
α	0	0	5/8	0	-3/8	5/8	3/8	0