

# MantaPay Protocol Specification

v0.4.0

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## Abstract

MantaPay is an implementation of a *decentralized anonymous payment* scheme based on the MANTADAP protocol outlined in the original [MANTA whitepaper](#).

## Contents

<b>1</b>	<b>Introduction</b>	<b>1</b>
<b>2</b>	<b>Notation</b>	<b>2</b>
<b>3</b>	<b>Concepts</b>	<b>2</b>
3.1	Assets	2
3.2	Addresses	2
3.3	Ledger	3
3.3.1	UTXO Set	3
3.3.2	EncryptedNotes	3
3.3.3	VoidNumber Set	3
<b>4</b>	<b>Abstract Protocol</b>	<b>3</b>
4.1	Abstract Cryptographic Schemes	3
4.2	Addresses and Key Components	6
4.3	Transfer Protocol	7
<b>5</b>	<b>Concrete Protocol</b>	<b>9</b>
5.1	Constants	9
5.2	Concrete Cryptographic Schemes	9
5.2.1	Commitments	9
5.2.2	Hash Functions	9
5.2.3	Encryption	9
5.2.4	Zero-Knowledge Proving Systems	9
5.2.4.1	Groth16	9
5.2.4.2	PLONK	9
<b>6</b>	<b>Differences from MANTADAP</b>	<b>9</b>
6.1	Reusable Addresses	9
6.2	Transfer Circuit Unification	9
<b>7</b>	<b>Acknowledgements</b>	<b>9</b>
<b>8</b>	<b>References</b>	<b>9</b>

## 1 Introduction

**TODO:** add introductory remarks

## 2 Notation

The following notation is used throughout this specification:

- `Type` is the type of types<sup>1</sup>.
- If  $x : T$  then  $x$  is a value and  $T$  is a type, denoted  $T : \text{Type}$ , and we say that  $x$  *has type*  $T$ .
- `Bool` is the type of booleans with values `True` and `False`.
- For any types  $A : \text{Type}$  and  $B : \text{Type}$  we denote the *type of functions* from  $A$  to  $B$  as  $A \rightarrow B : \text{Type}$ .
- For any types  $A : \text{Type}$  and  $B : \text{Type}$  we denote the *product type* over  $A$  and  $B$  as  $A \times B : \text{Type}$  with constructor  $(-, -) : T \rightarrow (S \rightarrow T \times S)$ .
- For any type  $T : \text{Type}$ , we define  $\text{Option}(T) : \text{Type}$  as the inductive type with constructors:

$$\begin{aligned} \text{None} &: \text{Option}(T) \\ \text{Some} &: T \rightarrow \text{Option}(T) \end{aligned}$$

- We denote the *type of finite sets* over a type  $T : \text{Type}$  as  $\text{FinSet}(T) : \text{Type}$ . The membership predicate for a value  $x : T$  in a finite set  $S : \text{FinSet}(T)$  is denoted  $x \in S$ .
- We denote the *type of distributions* over a type  $T : \text{Type}$  as  $\mathfrak{D}(T) : \text{Type}$ . A value  $x$  sampled from  $\mathfrak{D}(T)$  is denoted  $x \sim \mathfrak{D}(T)$  and the fact that the value  $x$  belongs to the range of  $\mathfrak{D}(T)$  is denoted  $x \in \mathfrak{D}(T)$ . So namely,  $y \in \{x \mid x \sim \mathfrak{D}(T)\} \leftrightarrow y \in \mathfrak{D}(T)$ .
- Depending on the context, the notation  $|\cdot|$  denotes either the absolute value of a quantity, the length of a vector, the number of characters in a string, or the cardinality of a set.

## 3 Concepts

### 3.1 Assets

The `Asset` is the fundamental currency object in the MantaPay protocol. An asset  $a : \text{Asset}$  is a tuple

$$a = (a.\text{id}, a.\text{value}) : \text{AssetId} \times \text{AssetValue}$$

The MantaPay protocol is a *decentralized anonymous payment* scheme which facilitates the private ownership and private transfer of `Asset` objects. The `AssetId` field encodes the type of currency being used, and the `AssetValue` encodes how many units of that currency are being used, in the standard base unit of that currency.

Whenever an `Asset` is being used in a public setting, we simply refer to it as an `Asset`, but when the `AssetId` and/or `AssetValue` of a particular `Asset` is meant to be hidden from public view, we refer to the `Asset` as either, *secret*, *private*, *hidden*, or *shielded*.

Assets form the basic units of *transactions* which consume Assets on input, transform them, and return Assets on output. To preserve the economic value stored in Assets, the sum of the input `AssetValues` must balance the sum of the output `AssetValues`, and all assets in a single transaction must have the same `AssetId`<sup>2</sup>.

### 3.2 Addresses

In order for participants in the MantaPay protocol to send and receive Assets, they must create secret and public *addresses* according to an *address scheme*. For MantaPay, the address scheme consists of a *spending key* `sk`, a *viewing key* `vk`, and a *receiving key* `rk`. The keys have the following uses/properties:

- Access to a receiving key `rk` represents the ability to send Assets to the owner of the associated `sk`.
- Access to a viewing key `vk` represents the ability to reveal shielded Asset information for Assets belonging to the owner of the associated `sk`.
- Access to a spending key `sk` represents the ability to spend Assets that were received under the associated receiving key `rk`.

<sup>1</sup>By *type of types*, we mean the type of *first-level* types in some family of type universes. Discussion of the type theory necessary to make these notions rigorous is beyond the scope of this paper.

<sup>2</sup>It is beyond the scope of this paper to discuss transactions with inputs and outputs that feature different `AssetIds`, like those that would be featured in a *decentralized anonymous exchange*.

See § 4.2 for more information on how these keys are constructed and used for spending, viewing, and receiving Assets.

### 3.3 Ledger

Ensuring that Assets maintain their economic value is not only dependent on transactions preserving inputs and outputs, but also that Assets are not *double-spent*. The *double-spending problem* can be solved by using a public ledger<sup>3</sup> that keeps track of the flow of Assets from one participant to the other. Unfortunately, using a public ledger alone does not allow participants to remain anonymous, so MantaPay extends the public ledger by adding a special account called the **ShieldedAssetPool**. The **ShieldedAssetPool** is responsible for keeping track of the Assets which have been anonymized by the protocol.

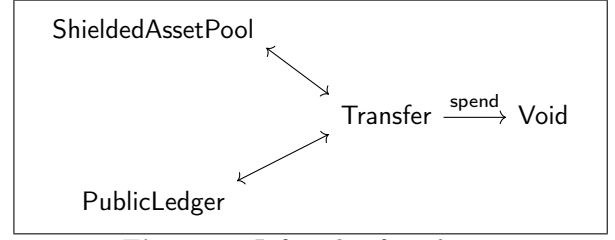


Figure 1: Lifecycle of an Asset.

Assets can be in one of three states, **public** (tracked by the **PublicLedger**), **allocated** (spendable subset of the **ShieldedAssetPool**), or **spent** (voided Assets). By way of the § 4.3 Transfer Protocol, Assets can be sent to and from the **PublicLedger** and the **ShieldedAssetPool**.

The **ShieldedAssetPool** is made up of four parts:

1. **ShieldedAssetPool Balance**: The MantaPay ledger contains a collection of Assets which represent the combined economic value of the **ShieldedAssetPool** and the **PublicLedger**. The **ShieldedAssetPool Balance** is the subset of this total value that has been anonymized by the MantaPay protocol.
2. § 3.3.1 **UTXO Set**: A collection of claims to subsets of the **ShieldedAssetPool**, each owned by participants of the MantaPay protocol.
3. § 3.3.2 **EncryptedNotes**: For each UTXO there is a matching **EncryptedNote** which contains information necessary to spend the Asset, which is committed in the UTXO, but can only be decrypted by the recipient of the Asset, specifically, the correct viewing key *vk*. See § 3.2 for more.
4. § 3.3.3 **VoidNumber Set**: A collection of commitments keeping track of those UTXOs which have participated in exactly one instance of the Transfer Protocol.

An Asset is in the **public** state if it belongs to the **PublicLedger**. An Asset is in the **allocated** state if a UTXO for the Asset is a member of the UTXO Set, but its matching **VoidNumber** is **not** in the **VoidNumber Set**. An Asset is in the **spent** state if it was **allocated** in the past, but its matching **VoidNumber** is now in the **VoidNumber Set**.

The operation of the different parts of the **ShieldedAssetPool** is elaborated in the following subsections.

#### 3.3.1 UTXO Set

#### 3.3.2 EncryptedNotes

#### 3.3.3 VoidNumber Set

## 4 Abstract Protocol

### 4.1 Abstract Cryptographic Schemes

**Definition 4.1.1.** A *commitment scheme* COM is defined by the schema:

$$\begin{aligned}
 &\text{Trapdoor} : \text{Type} \\
 &\quad \text{Input} : \text{Type} \\
 &\quad \text{Output} : \text{Type} \\
 &\text{TrapdoorDistribution} : \mathcal{D}(\text{Trapdoor}) \\
 &\quad \text{commit} : \text{Trapdoor} \times \text{Input} \rightarrow \text{Output}
 \end{aligned}$$

with the following properties:

<sup>3</sup>A public (or private) ledger is not enough to solve the *double-spending problem*. A *consensus mechanism* is also required to ensure that all participants agree on the current state of the ledger. The *consensus mechanism* that secures the MantaPay ledger is beyond the scope of this paper.

- **Binding:** It is infeasible to find an  $x, y : \text{Input}$  and  $r, s : \text{Trapdoor}$  such that  $x \neq y$  and  $\text{commit}(r, x) = \text{commit}(s, y)$ .
- **Hiding:** For all  $x, y : \text{Input}$ , the distributions  $\{\text{commit}(r, x) \mid r \sim \text{TrapdoorDistribution}\}$  and  $\{\text{commit}(r, y) \mid r \sim \text{TrapdoorDistribution}\}$  are *computationally indistinguishable*.

**Notation:** For convenience we refer to  $\text{COM.commit}(r, x)$  by  $\text{COM}_r(x)$ .

**Definition 4.1.2.** A *hash function* CRH is defined by the schema:

Input : Type  
Output : Type  
hash : Input  $\rightarrow$  Output

with the following properties:

- **Pre-Image Resistance:** For a given  $y : \text{Output}$ , it is infeasible to find  $x : \text{Input}$  such that  $\text{hash}(x) = y$ .
- **Collision Resistance:** It is infeasible to find an  $x_1, x_2 : \text{Input}$  such that  $x_1 \neq x_2$  and  $\text{hash}(x_1) = \text{hash}(x_2)$ .

**Notation:** For convenience we refer to  $\text{CRH.hash}(x)$  by  $\text{CRH}(x)$ .

**Definition 4.1.3.** A *symmetric-key encryption scheme* SYM is defined by the schema:

Key : Type  
Plaintext : Type  
Ciphertext : Type  
encrypt : Key  $\times$  Plaintext  $\rightarrow$  Ciphertext  
decrypt : Key  $\times$  Ciphertext  $\rightarrow$  Option(Plaintext)

with the following properties:

- **Validity:** For all keys  $k : \text{Key}$  and plaintexts  $p : \text{Plaintext}$ , we have that

$$\text{decrypt}(k, \text{encrypt}(k, p)) = \text{Some}(p)$$

- **TODO:** hiding, one-time encryption security?

**Definition 4.1.4.** A *key-agreement scheme* KA is defined by the schema:

PublicKey : Type  
SecretKey : Type  
SharedSecret : Type  
derive : SecretKey  $\rightarrow$  PublicKey  
agree : SecretKey  $\times$  PublicKey  $\rightarrow$  SharedSecret

with the following properties:

- **Agreement:** For all  $\text{sk}_1, \text{sk}_2 : \text{SecretKey}$ ,  $\text{agree}(\text{sk}_1, \text{derive}(\text{sk}_2)) = \text{agree}(\text{sk}_2, \text{derive}(\text{sk}_1))$
- **TODO:** security properties

**Definition 4.1.5.** A *key-derivation function* KDF defined over a symmetric-key encryption scheme SYM and a key-agreement scheme KA is a function of type:

$$\text{KDF} : \text{KA.SharedSecret} \rightarrow \text{SYM.Key}$$

**Definition 4.1.6.** An *integrated encryption scheme* IES is a hybrid encryption scheme made of up a symmetric-key encryption scheme SYM, a key-agreement scheme KA, and a KDF to convert from KA.SharedSecret to SYM.Key. We can define the following encryption/decryption algorithms:

- **Encryption:** Given a secret key  $\text{sk} : \text{KA.SecretKey}$ , a public key  $\text{pk} : \text{KA.PublicKey}$ , and plaintext  $p : \text{SYM.Plaintext}$ , we produce the pair

$$m := (\text{KA.derive}(\text{sk}), \text{SYM.encrypt}(\text{KDF}(\text{KA.agree}(\text{sk}, \text{pk})), p)) : \text{KA.PublicKey} \times \text{SYM.Ciphertext}$$

- **Decryption:** Given a secret key  $sk : \text{KA.SecretKey}$ , and an encrypted message, as above,  $m := (pk, c) : \text{KA.PublicKey} \times \text{SYM.Ciphertext}$ , we can decrypt  $m$ , producing the plaintext,

$$p := \text{SYM.decrypt}(\text{KDF}(\text{KA.agree}(sk, pk)), c) : \text{Option}(\text{SYM.Plaintext})$$

which should decrypt successfully if the  $\text{KA.PublicKey}$  that  $m$  was encrypted with is the derived key of  $sk : \text{KA.SecretKey}$ .

**Notation:** We denote the above *encrypted message* type as  $\text{Message} := \text{KA.PublicKey} \times \text{SYM.Ciphertext}$ , and the above two algorithms by

$$\begin{aligned} \text{encrypt} &: \text{KA.SecretKey} \times \text{KA.PublicKey} \times \text{SYM.Plaintext} \rightarrow \text{Message} \\ \text{decrypt} &: \text{KA.SecretKey} \times \text{SYM.Ciphertext} \rightarrow \text{Option}(\text{SYM.Plaintext}) \end{aligned}$$

**TODO:** security properties, combine with SYM and KA properties, like the fact that some of these keys should be ephemeral, etc.

**TODO:** add explicit message authentication

**Definition 4.1.7.** A *key-diversification scheme* KDIV over a key-agreement scheme KA is defined by the schema:

$$\begin{aligned} \text{public} &: \text{KA.SecretKey} \times \text{KA.PublicKey} \times \text{KA.PublicKey} \rightarrow \text{KA.PublicKey} \\ \text{secret} &: \text{KA.PublicKey} \times \text{KA.SecretKey} \times \text{KA.SecretKey} \rightarrow \text{KA.SecretKey} \end{aligned}$$

**Notation:** We refer to the first argument to a KDIV function as the *diversifier* and we write it as a subscript

$$\text{public}_d(x, y) := \text{public}(d, x, y) \text{ and } \text{secret}_d(x, y) := \text{secret}(d, x, y)$$

For convenience we also write  $\text{KDIV}_d$  to mean  $\text{KDIV.public}_d$  or  $\text{KDIV.secret}_d$ , when the context is clear.

Every KDIV also has the following properties:

- **Derivation Invariance:** For any diversifier  $d : \text{KA.SecretKey}$  and pair of secret keys  $(sk_1, sk_2)$  we have

$$\text{KDIV}_d(\text{KA.derive}(sk_1), \text{KA.derive}(sk_2)) = \text{KA.derive}(\text{KDIV}_{\text{KA.derive}(d)}(sk_1, sk_2))$$

- **TODO:** security properties?

**Definition 4.1.8.** A *dynamic cryptographic accumulator* DCA is defined by the schema:

$$\begin{aligned} \text{Item} &: \text{Type} \\ \text{State} &: \text{Type} \\ \text{Checkpoint} &: \text{Type} \\ \text{Proof} &: \text{Type} \\ \text{checkpoint} &: \text{State} \rightarrow \text{Checkpoint} \\ \text{update} &: \text{Item} \times \text{State} \rightarrow \text{State} \\ \text{contains} &: \text{Item} \times \text{State} \rightarrow \text{Option}(\text{Checkpoint} \times \text{Proof}) \\ \text{verify} &: \text{Item} \times \text{Checkpoint} \times \text{Proof} \rightarrow \text{Bool} \end{aligned}$$

**Definition 4.1.9.** A *non-interactive zero-knowledge proving system* ZKPS is defined by the schema:

$$\begin{aligned} \text{Statement} &: \text{Type} \\ \text{ProvingKey} &: \text{Type} \\ \text{VerifyingKey} &: \text{Type} \\ \text{PublicInput} &: \text{Type} \\ \text{SecretInput} &: \text{Type} \\ \text{Proof} &: \text{Type} \\ \text{keys} &: \text{Statement} \rightarrow \mathcal{D}(\text{ProvingKey} \times \text{VerifyingKey}) \\ \text{prove} &: \text{Statement} \times \text{ProvingKey} \times \text{PublicInput} \times \text{SecretInput} \rightarrow \mathcal{D}(\text{Option}(\text{Proof})) \\ \text{verify} &: \text{VerifyingKey} \times \text{PublicInput} \times \text{Proof} \rightarrow \text{Bool} \end{aligned}$$

**Notation:** We use the following notation for a ZKPS:

- We write the Statement and ProvingKey arguments of `prove` in the superscript and subscript respectively,

$$\text{prove}_{\text{pk}}^P(x, w) := \text{prove}(P, \text{pk}, x, w)$$

- We write the VerifyingKey argument of `verify` in the subscript,

$$\text{verify}_{\text{vk}}(x, \pi) := \text{verify}(\text{vk}, x, \pi)$$

- We say that  $(x, w) : \text{PublicInput} \times \text{SecretInput}$  has the property of being a **satisfying** input whenever

$$\text{satisfying}(x, w) := \exists \pi : \text{Proof}, \text{Some}(\pi) \in \text{prove}_{\text{pk}}^P(x, w)$$

Every ZKPS has the following properties for a fixed statement  $P : \text{Statement}$  and keys  $(\text{pk}, \text{vk}) \sim \text{keys}(P)$ :

- **Completeness:** For all  $(x, w) : \text{PublicInput} \times \text{SecretInput}$ , if there exists a proof  $\pi : \text{Proof}$ , such that  $\text{Some}(\pi) \in \text{prove}_{\text{pk}}^P(x, w)$ , then  $\text{verify}_{\text{vk}}(x, \pi) = \text{True}$ .
- **Knowledge Soundness:** For any polynomial-size adversary  $\mathcal{A}$ ,

$$\mathcal{A} : \text{ProvingKey} \times \text{VerifyingKey} \rightarrow \mathcal{D}(\text{PublicInput} \times \text{Proof})$$

there exists a polynomial-size extractor  $\mathcal{E}_{\mathcal{A}}$

$$\mathcal{E}_{\mathcal{A}} : \text{ProvingKey} \times \text{VerifyingKey} \rightarrow \mathcal{D}(\text{SecretInput})$$

such that the following probability is negligible:

$$\Pr \left[ \begin{array}{l} \text{satisfying}(x, w) = \text{False} \\ \text{verify}_{\text{vk}}(x, w) = \text{True} \end{array} \middle| \begin{array}{l} (\text{pk}, \text{vk}) \sim \text{keys}(P) \\ (x, \pi) \sim \mathcal{A}(\text{pk}, \text{vk}) \\ w \sim \mathcal{E}_{\mathcal{A}}(\text{pk}, \text{vk}) \end{array} \right]$$

- **Statistical Zero-Knowledge:** There exists a stateful simulator  $\mathcal{S}$ , such that for all stateful distinguishers  $\mathcal{D}$ , the difference between the following two probabilities is negligible:

$$\Pr \left[ \begin{array}{l} \text{satisfying}(x, w) = \text{True} \\ \mathcal{D}(\pi) = \text{True} \end{array} \middle| \begin{array}{l} (\text{pk}, \text{vk}) \sim \text{keys}(P) \\ (x, w) \sim \mathcal{D}(\text{pk}, \text{vk}) \\ \text{Some}(\pi) \sim \text{prove}_{\text{pk}}^P(x, w) \end{array} \right] \text{ and } \Pr \left[ \begin{array}{l} \text{satisfying}(x, w) = \text{True} \\ \mathcal{D}(\pi) = \text{True} \end{array} \middle| \begin{array}{l} (\text{pk}, \text{vk}) \sim \mathcal{S}(P) \\ (x, w) \sim \mathcal{D}(\text{pk}, \text{vk}) \\ \pi \sim \mathcal{S}(x) \end{array} \right]$$

- **Succinctness:** For all  $(x, w) : \text{PublicInput} \times \text{SecretInput}$ , if  $\text{prove}(P, \text{pk}, x, w) = \text{Some}(\pi)$ , then  $|\pi| = \mathcal{O}(1)$ , and  $\text{verify}(\text{vk}, x, \pi)$  runs in time  $\mathcal{O}(|x|)$ .

## 4.2 Addresses and Key Components

Given a choice of IES for the Transfer protocol we have the following definitions:

**Definition 4.2.1.** A **SpendingKey** is the following pair of keys:

$$\begin{aligned} \text{view} &: \text{IES.KA.SecretKey} \\ \text{spend} &: \text{IES.KA.SecretKey} \end{aligned}$$

The first secret key is called the **ViewingKey**.

**Definition 4.2.2.** A **ReceivingKey** is the following pair of keys:

$$\begin{aligned} \text{view} &: \text{IES.KA.PublicKey} \\ \text{spend} &: \text{IES.KA.PublicKey} \end{aligned}$$

which is derived from a spending key  $\text{sk} : \text{SpendingKey}$  by deriving each component:

$$\begin{aligned} \text{rk.view} &:= \text{KA.derive}(\text{sk.view}) \\ \text{rk.spend} &:= \text{KA.derive}(\text{sk.spend}) \end{aligned}$$

### 4.3 Transfer Protocol

**Definition 4.3.1.** A Sender is the following tuple:

$sk : \text{SpendingKey}$   
 $\tilde{d} : \text{IES.KA.PublicKey}$   
 $\text{trapdoor} : \text{IES.KA.PublicKey}$   
 $\text{asset} : \text{Asset}$   
 $cm : \text{UTXO}$   
 $cm_c : \text{UTXOSet.Checkpoint}$   
 $cm_\pi : \text{UTXOSet.Proof}$   
 $vn : \text{VoidNumber}$

A Sender,  $S$ , is constructed from a spending key  $sk : \text{SpendingKey}$  and an encrypted message  $\text{note} : \text{EncryptedNote}$  with the following algorithm:

$S.sk := sk$   
 $\tilde{d}, c := \text{note}$   
 $\text{Some}(\text{asset}) := \text{IES.decrypt}(S.sk.view, c)$   
 $S.asset := \text{asset}$   
 $S.\tilde{d} := \tilde{d}$   
 $S.trapdoor := \text{KA.derive}(\text{KDIV}_{S.\tilde{d}}(S.sk.view, S.sk.spend))$   
 $S.cm := \text{COM}_{S.trapdoor}(S.asset)$   
 $\text{Some}(cm_c, cm_\pi) := \text{UTXOSet.contains}(S.cm, \text{Ledger.utxos}())$   
 $S.cm_c := cm_c$   
 $S.cm_\pi := cm_\pi$   
 $S.vn := \text{COM}_{S.\tilde{d}}(S.sk.view || S.sk.spend)$

**Definition 4.3.2.** A SenderPost is the following tuple extracted from a Sender:

$cm_c : \text{UTXOSet.Checkpoint}$   
 $vn : \text{VoidNumber}$

**Definition 4.3.3.** A Receiver is the following tuple:

$rk : \text{ReceivingKey}$   
 $d : \text{IES.KA.SecretKey}$   
 $\text{trapdoor} : \text{IES.KA.PublicKey}$   
 $\text{asset} : \text{Asset}$   
 $cm : \text{UTXO}$   
 $\text{note} : \text{EncryptedNote}$

A Receiver,  $R$ , is constructed from a receiving key  $rk : \text{ReceivingKey}$ , an asset  $\text{asset} : \text{Asset}$ , and a chosen diversifier  $d : \text{IES.KA.SecretKey}$  with the following algorithm:

$R.rk := rk$   
 $R.d := d$   
 $R.trapdoor := \text{KDIV}_{R.d}(R.rk.view, R.rk.spend)$   
 $R.asset := \text{asset}$   
 $R.cm := \text{COM}_{R.trapdoor}(R.asset)$   
 $R.note := \text{IES.encrypt}(R.d, R.rk.view, \text{asset})$

**Definition 4.3.4.** A ReceiverPost is the following tuple extracted from a Receiver:

cm : UTXO  
note : EncryptedNote

**Definition 4.3.5.** A Source (or a Sink) is an Asset representing a public input (or output) of a Transfer.

**Definition 4.3.6.** A Transfer is the following tuple:

sources : FinSet(Asset)  
senders : FinSet(Sender)  
receivers : FinSet(Receiver)  
sinks : FinSet(Asset)

The *shape* of a Transfer is the following 4-tuple of cardinalities of those sets

$$(|T.sources|, |T.senders|, |T.receivers|, |T.sinks|)$$

In order for a Transfer to be considered *valid*, it must adhere to the following constraints:

- **Same Id:** All the AssetIds in the Transfer must be equal.
- **Balanced:** The sum of input AssetValues must be equal to the sum of output AssetValues.
- **Well-formed Senders:** All of the Senders in the Transfer must be constructed according to the above Sender definition.
- **Well-formed Receivers:** All of the Receivers in the Transfer must be constructed according to the above Receiver definition.

In order to prove that these constraints are satisfied for a given Transfer, we build a zero-knowledge proof which will witness that the Transfer is valid and should be accepted by the ledger. It is not necessary to prove that the encryption of Receiver.note and the decryption of a note from the ledger are valid. Deviation from the protocol in encryption or decryption does not reduce the security of the protocol for honest participants.

**Definition 4.3.7.** (Transfer Validity Statement) A transfer  $T : \text{Transfer}$  is considered *valid* if and only if

1. All the AssetIds in  $T$  are equal:

$$\left| \left( \bigcup_{a \in T.sources} a.id \right) \cup \left( \bigcup_{S \in T.senders} S.asset.id \right) \cup \left( \bigcup_{R \in T.receivers} R.asset.id \right) \cup \left( \bigcup_{a \in T.sinks} a.id \right) \right| = 1$$

2. The sum of input AssetValues is equal to the sum of output AssetValues:

$$\left( \sum_{a \in T.sources} a.value \right) + \left( \sum_{S \in T.senders} S.asset.value \right) = \left( \sum_{R \in T.receivers} R.asset.value \right) + \left( \sum_{a \in T.sinks} a.value \right)$$

3. For all  $S \in T.senders$ , the Sender  $S$  is well-formed:

$$\begin{aligned} S.trapdoor &= \text{KA.derive}(\text{KDIV}_{S.d}(S.sk.view, S.sk.spend)) \\ S.cm &= \text{COM}_{S.trapdoor}(S.asset) \\ S.vn &= \text{COM}_{S.d}(S.sk.view || S.sk.spend) \\ \text{UTXOSet.verify}(S.cm, S.cm_e, S.cm_\pi) &= \text{True} \end{aligned}$$

4. For all  $(i, R) \in \text{enumerate}(T.receivers)$ , the Receiver  $R$  is well-formed at index  $i$  with respect to FAIR:

$$\begin{aligned} R.d &= \text{CRH}(i || R.rk.view || R.rk.spend || \text{FAIR}) \\ R.trapdoor &= \text{KDIV}_{R.d}(R.rk.view, R.rk.spend) \\ R.cm &= \text{COM}_{R.trapdoor}(R.asset) \end{aligned}$$

where FAIR is the following constant, using the ledger as a randomness oracle:

$$\text{FAIR} := \text{CRH}(\text{UTXOSet.checkpoint}(\text{Ledger.utxos}()) || \text{Concat}_{S \in T.senders}(S.sk.spend))$$



**Notation:** This statement is denoted `ValidTransfer` and is assumed to be expressible as a `Statement` of `ZKPS`.

**Definition 4.3.8.** A `TransferPost` is the following tuple:

$$\begin{aligned} \text{sources} &: \text{FinSet}(\text{Asset}) \\ \text{senders} &: \text{FinSet}(\text{SenderPost}) \\ \text{receivers} &: \text{FinSet}(\text{ReceiverPost}) \\ \text{sinks} &: \text{FinSet}(\text{Asset}) \\ \pi &: \text{ZKPS.Proof} \end{aligned}$$

A `TransferPost`,  $P$ , is constructed by assembling the zero-knowledge proof of `Transfer` validity from a known proving key  $\text{pk} : \text{ZKPS.ProvingKey}$  and a given  $T : \text{Transfer}$ :

$$\begin{aligned} x &:= \text{Transfer.public}(T) \\ w &:= \text{Transfer.secret}(T) \\ \text{Some}(\pi) &:= \text{ZKPS.prove}_{\text{pk}}^{\text{ValidTransfer}}(x, w) \\ P.\text{sources} &:= x.\text{sources} \\ P.\text{senders} &:= x.\text{senders} \\ P.\text{receivers} &:= x.\text{receivers} \\ P.\text{sinks} &:= x.\text{sinks} \\ P.\pi &:= \pi \end{aligned}$$

## 5 Concrete Protocol

### 5.1 Constants

**TODO:** add constants for the protocol

### 5.2 Concrete Cryptographic Schemes

**TODO:** add names of cryptographic scheme implementations

#### 5.2.1 Commitments

#### 5.2.2 Hash Functions

#### 5.2.3 Encryption

#### 5.2.4 Zero-Knowledge Proving Systems

##### 5.2.4.1 Groth16

##### 5.2.4.2 PLONK

## 6 Differences from `MANTADAP`

### 6.1 Reusable Addresses

**TODO:** compare old one-time address protocol to reusable addresses and why reusable is better

### 6.2 Transfer Circuit Unification

**TODO:** compare new single transfer circuit to the many old circuits

## 7 Acknowledgements

**TODO:** add acknowledgements

## 8 References

**TODO:** add references