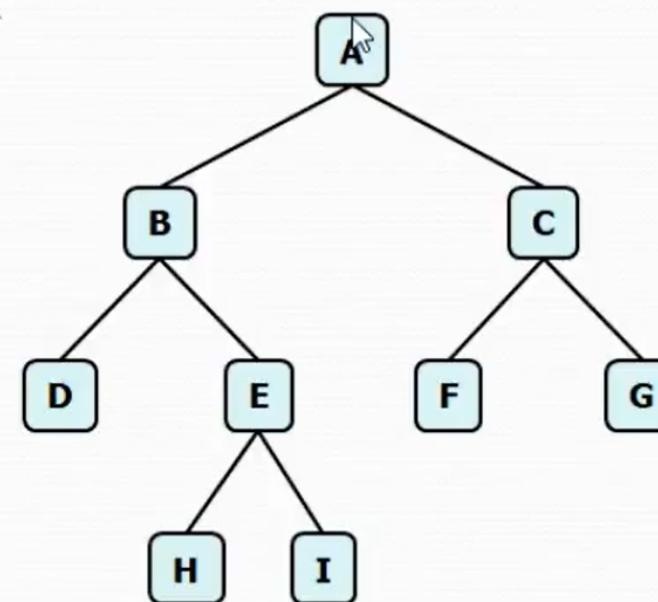


InOrder Traversal: Example

Output: D B H E I A F C G



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PostOrder Traversal

- Visit the left sub-tree in PostOrder
- Visit right sub-tree in PostOrder
- Visit root node

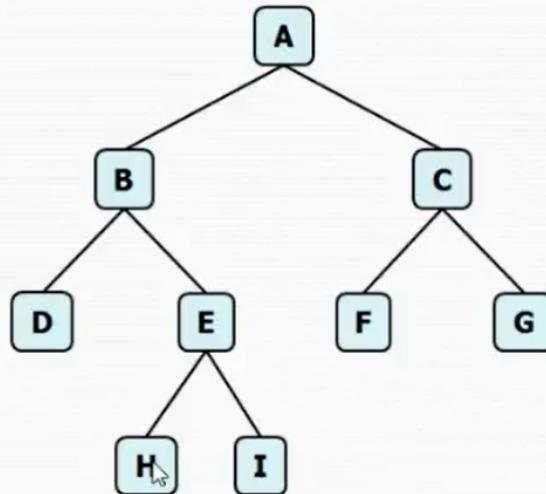
```
PostOrderTraversal(Tree) {  
    if (isEmpty(Tree)) return;  
    else {  
        PostOrderTraversal(tree->left);  
        PostOrderTraversal(tree->right);  
        print (tree->data);  
    }  
}
```

A

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PostOrder Traversal: Example

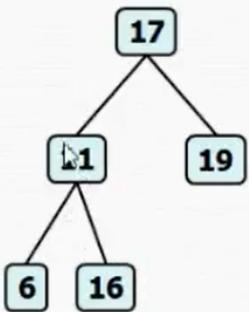
Output: D H I E B F G C A



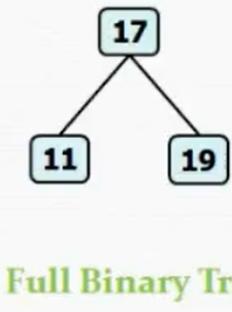
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Full Binary Tree

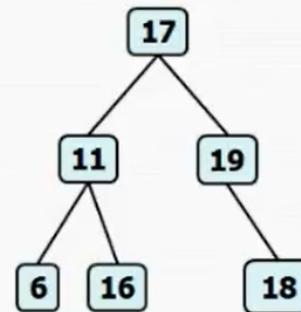
- Either a node has 2 children or no child in a binary tree



Full Binary Tree



Full Binary Tree



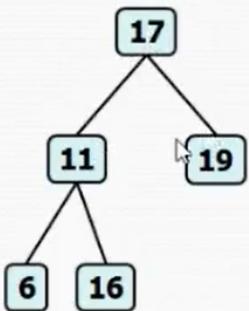
Not Full Binary Tree



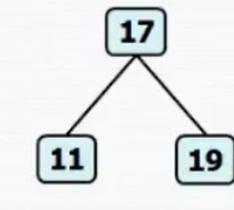
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Perfect Binary Tree

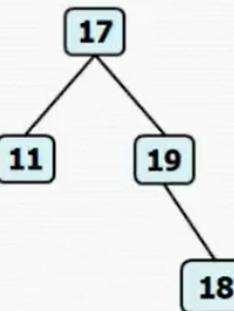
- All internal nodes has two children and all leaves are at same level/depth



full; not perfect



Full; perfect



Not full; not perfect



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Perfect Binary Tree

- Level i has 2^{i-1} nodes
- If leaves are level at h
 - Number of leaves is 2^{h-1}
 - Number of internal node = $1+2+2^2+2^3+\dots+2^{h-2} = 2^{h-1}-1$
= number of leaves - 1
 - Total number of nodes = $2^{h-1} + 2^{h-1} - 1 = 2^h - 1$

A

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Perfect Binary Tree

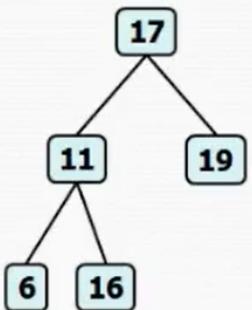
- Level i has 2^{i-1} nodes
- If leaves are level at h
 - Number of leaves is 2^{h-1}
 - Number of internal node = $1+2+2^2+2^3+\dots+2^{h-2} = 2^{h-1} - 1$
= number of leaves - 1
 - Total number of nodes = $2^{h-1} + 2^{h-1} - 1 = 2^h - 1$
- If total number of nodes is n
 - Number of leaves = $(n+1)/2$
 - Height of tree = $\log_2 (\text{number of leaves}) = \log_2((n+1)/2)$

A

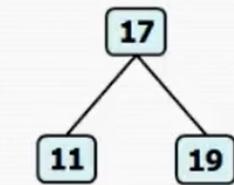
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Complete Binary Tree

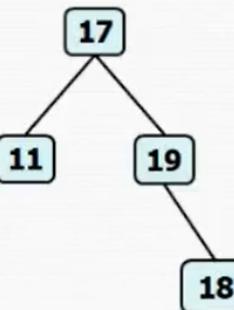
- All levels are completely filled except last. Also, all nodes in last level are as far left as possible



Full;
Not perfect;
Complete



Full;
Perfect;
Complete



Not full;
Not perfect;
Not Complete



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Complete Binary Tree

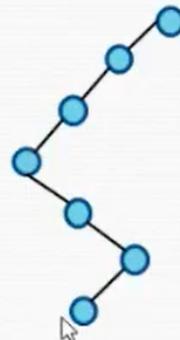
- Perfect tree is a special case of complete tree with last level completely filled.
- In some literature, Perfect binary tree is referred as Complete binary tree. In that case, Complete binary tree is referred Almost Complete binary tree.

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Height of a Binary Tree

- If a binary tree has n nodes and height h , then
 - Level i has at most 2^{i-1} nodes
 - $n \leq 2^{h+1} - 1$
 - Hence, $h \geq \log_2(n+1)/2$ i.e. minimum height of a tree with n nodes is $O(\log_2 n)$
 - Maximum height of a tree with n nodes is $n-1$ which is obtained when every non-leaf node has exactly one child



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Linear Representation of Binary Tree

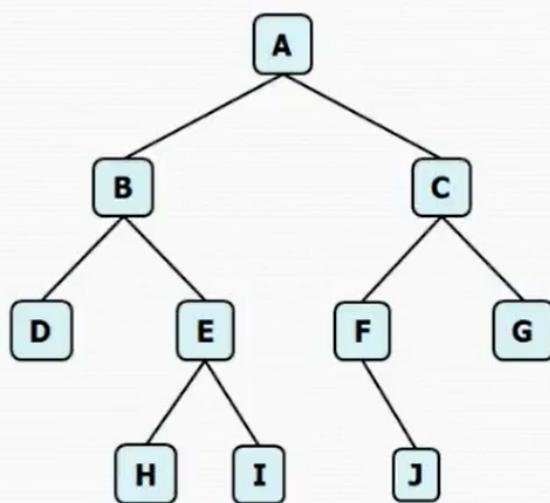
- Binary tree can also be represented using arrays
- Store root node at index **0**
- Store left child of a parent node is at $2*i+1$ where **i** is the index of parent node in array
- Store right child of a parent node is at $2*i+2$ where **i** is the index of parent node in array
- Parent of a node at index **i** can be found at $(i-1)/2$ except for root node

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Example

A	B	C	D	E	F	G		H	I		J
0	1	2	3	4	5	6	7	8	9	10	11



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Linear Representation of Binary Tree

- If a node doesn't have a left or/and right child, indices for left or/and right child are empty
- If index of a child is greater than size of array, child of that node does not exist

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30:54 / 45:37



Searching a Binary Tree

- BFS or DFS
- Worst case time complexity = $O(n)$ where n is the number of nodes in binary tree
- Can we improve searching?

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39:16 / 45:37



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emu-juny-upp (2021-10-29 at 01:49 GMT-7)

Binary Search Tree

- Root is greater than left child and less than right child
- Equal keys can be kept in left or right sub-tree
- Same strategy should be followed for whole tree for repeated keys

All values in the left subtree are less than the value in the root node.

All values in the right subtree are greater than the value in the root node.

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tree

E (Root node)

C

H

A

D

F

I

G

J

(Left subtree)

(Right subtree)