

Time Complexity of functions

(Here n is size of input array)

Functions in Class maxHeap:

- `find_parent`: $O(1)$
 - takes constant time
- `find_lchild`: $O(1)$
 - takes constant time
- `find_rchild`: $O(1)$
 - takes constant time
- `sift_up`: $O(\log n)$
 - as this function recursively calls itself hence time complexity is $O(h)$ or $O(\log n)$
- `sift_down`: $O(\log n)$
 - as this function recursively calls itself hence time complexity is $O(h)$ or $O(\log n)$
- `is_valid_index`: $O(1)$
 - takes constant time
- `get_max`: $O(1)$
 - as it just returns element of array(i.e. In constant time)
- `delete_max`: $O(\log n)$
 - As it is sum of constant time and time taken by `sift_down` function(i.e. $O(\log n) + k \cdot O(1) = O(\log n)$)
- `insert`: $O(\log n)$
 - as it calls `sift_up` function ($O(\log n) + k \cdot O(1) = O(\log n)$)

HeapSort Function:

Time complexity is: $O(n \log n)$

(as for loop run n times and each time it calls delete function)

Input and Output:

The Random Array is:

```
{ 871, 20989, 843, 1828, 10112, 10533, 2228, 22144, 6631,  
12991, 17088, 14354, 2376, 24210, 11938, 3732, 32392, 16065,  
20359, 25552, }
```

The Output Array is:

```
{ 843, 871, 1828, 2228, 2376, 3732, 6631, 10112, 10533, 11938,  
12991, 14354, 16065, 17088, 20359, 20989, 22144, 24210, 25552,  
32392, }
```

Output obtained is a sorted array.