# JHU Statistical Inference Project - Part 1

#### Emanuel Chalela

#### 20/12/2020

#### Instructions

- 1. Show the sample mean and compare it to the theoretical mean of the distribution.
- 2. Show how variable the sample is (via variance) and compare it to the theoretical variance of the distribution.
- 3. Show that the distribution is approximately normal.

#### Loading Libraries

```
library("data.table")
library("ggplot2")
library("tinytex")
```

#### Task

```
# set seed for reproducability
set.seed(1234)
# set lambda to 0.2
lambda <- 0.2
# 40 samples
n <- 40
# 1000 simulations
simulations <- 1000
# simulate
simulate
simulated_exponentials <- replicate(simulations, rexp(n, lambda))
# calculate mean of exponentials
means_exponentials <- apply(simulated_exponentials, 2, mean)</pre>
```

#### Question 1

Show where the distribution is centered at and compare it to the theoretical center of the distribution.

```
analytical_mean <- mean(means_exponentials)
analytical_mean</pre>
```

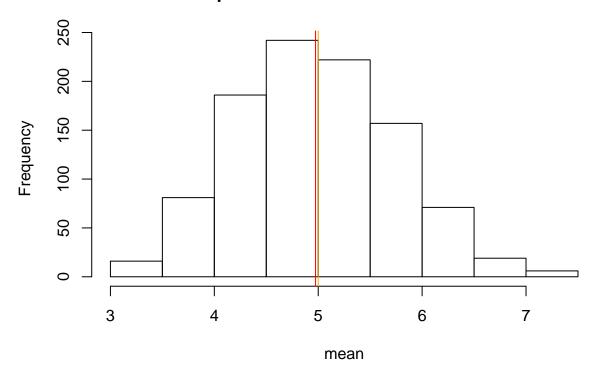
```
## [1] 4.974239
```

```
# analytical mean
theory_mean <- 1/lambda
theory_mean</pre>
```

## [1] 5

```
# visualization
hist(means_exponentials, xlab = "mean", main = "Exponential Function Simulations")
abline(v = analytical_mean, col = "red")
abline(v = theory_mean, col = "orange")
```

### **Exponential Function Simulations**



The analytics mean is 4.993867 the theoretical mean 5. The center of distribution of averages of 40 exponentials is very close to the theoretical center of the distribution.

#### Question 2

Show how variable it is and compare it to the theoretical variance of the distribution..

```
# standard deviation of distribution
standard_deviation_dist <- sd(means_exponentials)
standard_deviation_dist</pre>
```

## [1] 0.7554171

```
# standard deviation from analytical expression
standard_deviation_theory <- (1/lambda)/sqrt(n)
standard_deviation_theory</pre>
```

## [1] 0.7905694

```
# variance of distribution
variance_dist <- standard_deviation_dist^2
variance_dist</pre>
```

## [1] 0.5706551

```
# variance from analytical expression
variance_theory <- ((1/lambda)*(1/sqrt(n)))^2
variance_theory</pre>
```

## [1] 0.625

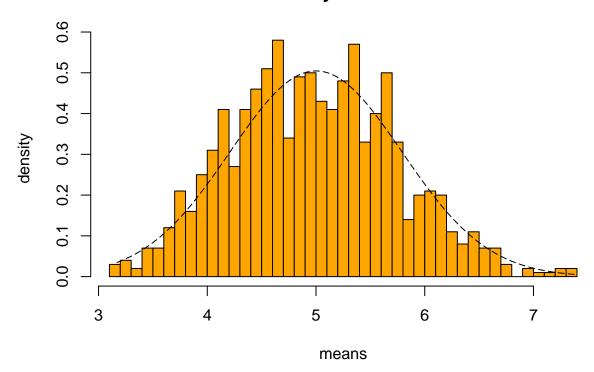
Standard Deviation of the distribution is 0.7931608 with the theoretical SD calculated as 0.7905694. The Theoretical variance is calculated as ((1/??)\*(1/???n))2 = 0.625. The actual variance of the distribution is 0.6291041

#### Question 3

Show that the distribution is approximately normal.

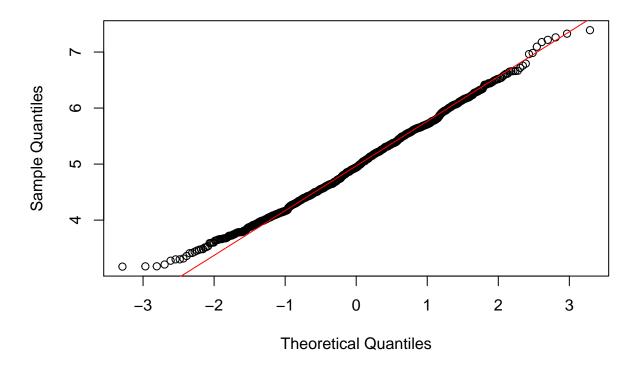
```
xfit <- seq(min(means_exponentials), max(means_exponentials), length=100)
yfit <- dnorm(xfit, mean=1/lambda, sd=(1/lambda/sqrt(n)))
hist(means_exponentials,breaks=n,prob=T,col="orange",xlab = "means",main="Density of means",ylab="densi lines(xfit, yfit, pch=22, col="black", lty=5)</pre>
```

# **Density of means**



# compare the distribution of averages of 40 exponentials to a normal distribution
qqnorm(means\_exponentials)
qqline(means\_exponentials, col = 2)

# Normal Q-Q Plot



Due to Due to the central limit theorem (CLT), the distribution of averages of 40 exponentials is very close to a normal distribution.