Linear Regression on Boston Housing Dataset

This data was originally a part of UCI Machine Learning Repository and has been removed now. This data also ships with the scikit-learn library. There are 506 samples and 13 feature variables in this data-set. The objective is to predict the value of prices of the house using the given features.

The description of all the features is given below:

CRIM: Per capita crime rate by town

ZN: Proportion of residential land zoned for lots over 25,000 sq. ft

INDUS: Proportion of non-retail business acres per town

CHAS: Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)

NOX: Nitric oxide concentration (parts per 10 million)

RM: Average number of rooms per dwelling

AGE: Proportion of owner-occupied units built prior to 1940

DIS: Weighted distances to five Boston employment centers

RAD: Index of accessibility to radial highways

TAX: Full-value property tax rate per \$10,000

B: $1000(Bk - 0.63)^2$, where Bk is the proportion of [people of African American descent] by town

LSTAT: Percentage of lower status of the population

MEDV: Median value of owner-occupied homes in \$1000s

Import the required Libraries

```
import numpy as np
import matplotlib.pyplot as plt

import pandas as pd
import seaborn as sns

//matplotlib inline
```

Load the Boston Housing DataSet from scikit-learn

```
In [2]: from sklearn.datasets import load_boston
boston_dataset = load_boston()
```

```
# boston_dataset is a dictionary
# let's check what it contains
boston_dataset.keys()
```

C:\Users\gptkgf\anaconda3\lib\site-packages\sklearn\utils\deprecation.py:87: Futur eWarning: Function load_boston is deprecated; `load_boston` is deprecated in 1.0 a nd will be removed in 1.2.

The Boston housing prices dataset has an ethical problem. You can refer to the documentation of this function for further details.

The scikit-learn maintainers therefore strongly discourage the use of this dataset unless the purpose of the code is to study and educate about ethical issues in data science and machine learning.

In this special case, you can fetch the dataset from the original source::

```
import numpy as np

data_url = "http://lib.stat.cmu.edu/datasets/boston"
raw_df = pd.read_csv(data_url, sep="\s+", skiprows=22, header=None)
data = np.hstack([raw_df.values[::2, :], raw_df.values[1::2, :2]])
target = raw_df.values[1::2, 2]
```

Alternative datasets include the California housing dataset (i.e. :func:`~sklearn.datasets.fetch_california_housing`) and the Ames housing dataset. You can load the datasets as follows::

from sklearn.datasets import fetch_california_housing
housing = fetch_california_housing()

for the California housing dataset and::

```
from sklearn.datasets import fetch_openml
housing = fetch_openml(name="house_prices", as_frame=True)
```

for the Ames housing dataset.
warnings.warn(msg, category=FutureWarning)

Out[2]: dict_keys(['data', 'target', 'feature_names', 'DESCR', 'filename', 'data_module'])

Load the data into pandas dataframe

import pandas as pd

In [3]: boston = pd.DataFrame(boston_dataset.data, columns=boston_dataset.feature_names)
boston.head()

Out[3]:		CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LSTAT
	0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.98
	1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.14
	2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.03
	3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.94
	4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.33

In [4]: boston.info()

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 506 entries, 0 to 505
Data columns (total 13 columns):
    Column
            Non-Null Count Dtype
    -----
---
            -----
0
    CRIM
            506 non-null
                           float64
1
    ΖN
            506 non-null float64
2
    INDUS
            506 non-null float64
            506 non-null float64
3
    CHAS
    NOX
            506 non-null float64
4
5
    RM
            506 non-null float64
    AGE
            506 non-null float64
6
            506 non-null float64
7
    DIS
            506 non-null float64
8
    RAD
9
    TAX
            506 non-null float64
10 PTRATIO 506 non-null float64
11 B
            506 non-null
                           float64
12 LSTAT
            506 non-null
                           float64
dtypes: float64(13)
memory usage: 51.5 KB
```

The target values is missing from the data. Create a new column of target values and add it to dataframe

:	<pre>boston['PRICE'] = boston_dataset.target</pre>													
	boston													
		CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	В	LSTA
	0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	15.3	396.90	4.9
	1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	17.8	396.90	9.1
	2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	17.8	392.83	4.0
	3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	18.7	394.63	2.9
	4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	18.7	396.90	5.3
	•••													
	501	0.06263	0.0	11.93	0.0	0.573	6.593	69.1	2.4786	1.0	273.0	21.0	391.99	9.6
	502	0.04527	0.0	11.93	0.0	0.573	6.120	76.7	2.2875	1.0	273.0	21.0	396.90	9.0
	503	0.06076	0.0	11.93	0.0	0.573	6.976	91.0	2.1675	1.0	273.0	21.0	396.90	5.6
	504	0.10959	0.0	11.93	0.0	0.573	6.794	89.3	2.3889	1.0	273.0	21.0	393.45	6.4
	505	0.04741	0.0	11.93	0.0	0.573	6.030	8.08	2.5050	1.0	273.0	21.0	396.90	7.8
5	506 r	ows × 14	colui	mns										

Data preprocessing

```
In [5]: # check for missing values in all the columns
boston.isnull().sum()
```

```
CRIM
                       0
Out[5]:
          ΖN
                       0
          INDUS
                       0
          CHAS
                      0
                      0
          NOX
                       0
          RM
          AGE
                       0
          DIS
                       0
          RAD
                      0
          TAX
                      0
          PTRATIO
                      0
                      0
          LSTAT
                      0
          MEDV
                      0
          dtype: int64
```

Data Visualization

Correlation matrix

```
In [7]: # compute the pair wise correlation for all columns
    correlation_matrix = boston.corr().round(2)

In [8]: # use the heatmap function from seaborn to plot the correlation matrix
    # annot = True to print the values inside the square
    sns.heatmap(data=correlation_matrix, annot=True)
```

Out[8]: <AxesSubplot:>



Observations

From the above coorelation plot we can see that PRICE is strongly correlated to LSTAT,
 RM

• RAD and TAX are stronly correlated, so we don't include this in our features together to avoid multi-colinearity

```
In [7]: plt.figure(figsize=(20, 5))
features = ['LSTAT', 'RM']
target = boston['PRICE']

for i, col in enumerate(features):
    plt.subplot(1, len(features) , i+1)
    x = boston[col]
    y = target
    plt.scatter(x, y, marker='o')
    plt.title(col)
    plt.xlabel(col)
    plt.ylabel('PRICE')

LSTAT

RM

September 2

September 3

September 3

September 4

September 3

September 4

September 4
```

Prepare the data for training

```
In [10]: X = pd.DataFrame(np.c_[boston['LSTAT'], boston['RM']], columns = ['LSTAT','RM'])
Y = boston['PRICE']
```

Split the data into training and testing sets

```
In [11]: from sklearn.model_selection import train_test_split

# splits the training and test data set in 80% : 20%
# assign random_state to any value. This ensures consistency.
X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size = 0.2, random_sprint(X_train.shape)
print(X_test.shape)
print(Y_train.shape)
print(Y_test.shape)

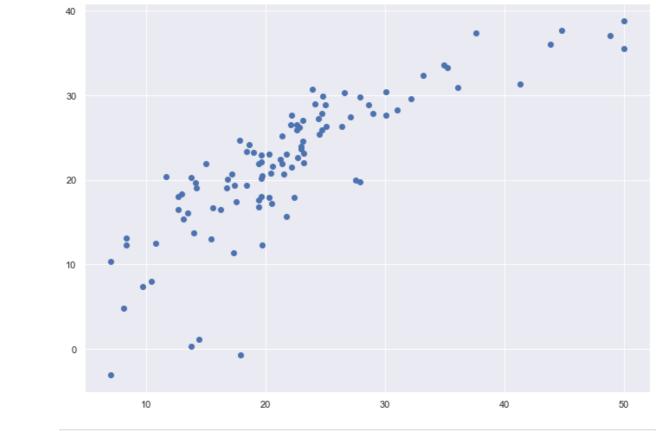
(404, 2)
(102, 2)
(404,)
(102,)
```

Train the model using sklearn LinearRegression

```
In [12]: from sklearn.linear_model import LinearRegression
    from sklearn.metrics import mean_squared_error, r2_score
    lin_model = LinearRegression()
    lin_model.fit(X_train, Y_train)

Out[12]: LinearRegression()
```

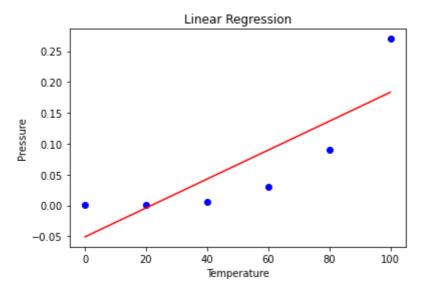
```
In [13]: # model evaluation for training set
         y_train_predict = lin_model.predict(X_train)
         rmse = (np.sqrt(mean_squared_error(Y_train, y_train_predict)))
         r2 = r2_score(Y_train, y_train_predict)
         print("The model performance for training set")
         print("----")
         print('RMSE is {}'.format(rmse))
         print('R2 score is {}'.format(r2))
         print("\n")
         # model evaluation for testing set
         y_test_predict = lin_model.predict(X_test)
         # root mean square error of the model
         rmse = (np.sqrt(mean_squared_error(Y_test, y_test_predict)))
         # r-squared score of the model
         r2 = r2_score(Y_test, y_test_predict)
         print("The model performance for testing set")
         print("-----")
         print('RMSE is {}'.format(rmse))
         print('R2 score is {}'.format(r2))
         The model performance for training set
         RMSE is 5.6371293350711955
         R2 score is 0.6300745149331701
         The model performance for testing set
         RMSE is 5.13740078470291
         R2 score is 0.6628996975186954
In [14]: # plotting the y_test vs y_pred
         # ideally should have been a straight line
         plt.scatter(Y_test, y_test_predict)
         plt.show()
```



 12/15/22, 4:09 PM GradientDescent

```
import numpy as np
In [80]:
          import matplotlib.pyplot as plt
          %matplotlib inline
In [81]:
          def gradient_descent(x,y):
              m = b = 1
              rate = 0.01
              n = len(x)
              plt.scatter(x,y)
              for i in range(100):
                  y_predicted = m * x + b
                  plt.plot(x,y_predicted,color='green')
                  md = -(2/n)*sum(x*(y-y\_predicted))
                  yd = -(2/n)*sum(y-y\_predicted)
                  m = m - rate * md
                  b = b - rate * yd
In [82]: x = np.array([1,2,3,4,5])
          y = np.array([5,7,9,11,13])
In [83]: gradient_descent(x,y)
          14
          12
          10
           8
           6
           4
                   1.5
                         2.0
                               2.5
                                                           5.0
                                    3.0
                                          3.5
                                               4.0
                                                     4.5
```

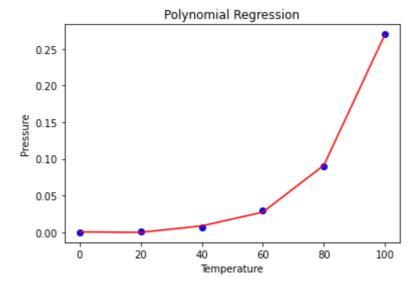
```
# Importing the libraries
 In [1]:
         import numpy as np
         import matplotlib.pyplot as plt
         import pandas as pd
         # Importing the dataset
         datas = pd.read_csv('data.csv')
         datas
 Out[1]:
            sno Temperature Pressure
         0
              1
                          0
                               0.0002
              2
                         20
                               0.0012
         2
              3
                         40
                               0.0060
         3
                         60
                               0.0300
         4
              5
                         80
                               0.0900
                        100
                               0.2700
 In [2]: X = datas.iloc[:, 1:2].values
         y = datas.iloc[:, 2].values
 In [3]: # Fitting Linear Regression to the dataset
         from sklearn.linear_model import LinearRegression
         lin = LinearRegression()
         lin.fit(X, y)
         LinearRegression()
Out[3]:
In [13]:
         # Fitting Polynomial Regression to the dataset
         from sklearn.preprocessing import PolynomialFeatures
         poly = PolynomialFeatures(degree = 4)
         X_poly = poly.fit_transform(X)
         poly.fit(X_poly, y)
         lin2 = LinearRegression()
         lin2.fit(X_poly, y)
         LinearRegression()
Out[13]:
         # Visualising the Linear Regression results
In [14]:
         plt.scatter(X, y, color = 'blue')
         plt.plot(X, lin.predict(X), color = 'red')
         plt.title('Linear Regression')
         plt.xlabel('Temperature')
         plt.ylabel('Pressure')
         plt.show()
```



```
In [15]: # Visualising the Polynomial Regression results
plt.scatter(X, y, color = 'blue')

plt.plot(X, lin2.predict(poly.fit_transform(X)), color = 'red')
plt.title('Polynomial Regression')
plt.xlabel('Temperature')
plt.ylabel('Pressure')

plt.show()
```



12/15/22, 4:09 PM regression

```
In [1]: # import packages
    import pandas as pd
    import numpy as np

    from sklearn.preprocessing import StandardScaler
    from sklearn.linear_model import LinearRegression
    from sklearn.metrics import mean_squared_error,r2_score

In [2]: from sklearn.model_selection import train_test_split

In [3]: df = pd.read_csv('Advertising.csv')
    df
```

Out[3]:		TV	radio	newspaper	sales
	0	230.1	37.8	69.2	22.1
	1	44.5	39.3	45.1	10.4
	2	17.2	45.9	69.3	9.3
	3	151.5	41.3	58.5	18.5
	4	180.8	10.8	58.4	12.9
	195	38.2	3.7	13.8	7.6
	196	94.2	4.9	8.1	9.7
	197	177.0	9.3	6.4	12.8
	198	283.6	42.0	66.2	25.5
	199	232.1	8.6	8.7	13.4

200 rows × 4 columns

```
In [4]: # dropping rows which have null values
    df.dropna(inplace=True,axis=0)
    df
```

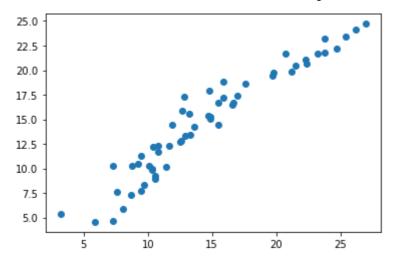
12/15/22, 4:09 PM regression

```
Out[4]:
                  TV radio newspaper sales
             0 230.1
                         37.8
                                     69.2
                                            22.1
                 44.5
                         39.3
                                            10.4
                                     45.1
                 17.2
                        45.9
                                     69.3
                                             9.3
             3 151.5
                                     58.5
                                            18.5
                        41.3
               180.8
                         10.8
                                     58.4
                                            12.9
           195
                 38.2
                          3.7
                                      13.8
                                             7.6
           196 94.2
                          4.9
                                       8.1
                                             9.7
           197 177.0
                          9.3
                                       6.4
                                            12.8
           198 283.6
                         42.0
                                      66.2
                                            25.5
           199 232.1
                          8.6
                                       8.7
                                            13.4
```

189 rows × 4 columns

```
In [5]:
         y = df['sales']
         X = df.drop('sales',axis=1)
In [6]: # splitting the dataframe into train and test sets
         X_train,X_test,y_train,y_test = train_test_split(X,y,test_size=0.3,random_state=10:
         #normalizing the values in each column
In [7]:
         scaler = StandardScaler()
         scaler.fit(X_train)
         X_train = scaler.transform(X_train)
         X_test = scaler.transform(X_test)
In [8]: | lr = LinearRegression()
         model = lr.fit(X_train,y_train)
         y_pred = model.predict(X_test)
In [9]:
         ydf = pd.DataFrame({'y_test':y_test,'y_pred':y_pred})
         rslt_df = ydf.sort_values(by = 'y_test')
In [10]:
         print(mean_squared_error(y_test,y_pred)) #lesser the better
         2.7506859249500466
In [11]:
         print(r2_score(y_test, y_pred)) #high value- better model
         0.9148625826187149
In [12]:
         import matplotlib.pyplot as plt
         plt.scatter(ydf['y_test'],ydf['y_pred'])
         #it should be a straight line to satisfy normality assumption
         <matplotlib.collections.PathCollection at 0x2364e818b20>
Out[12]:
```

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```
In [15]: model.coef_
Out[15]: array([ 3.78101153,  2.58704901, -0.03067692])

In [16]: model.intercept_
Out[16]: 13.9454545454544
```