Recluse: A Privacy-Preserved Single Sign-On System Achieving Unlinkable Users' Traces

I. Introduction

To maintain each user's profile and provide individual services, each service provider needs to identify each user, which requires the users to be authenticated at multiple online services repeatedly. Single Sign-On (SSO) systems enable users to access multiple services (called relying parties, RP) with the single authentication performed at the Identity Provider (IdP). With SSO system deployed, a user only needs to maintain the credential of the IdP, who offers user's attributes (i.e., identity proof) for each RP to accomplish the user's identification. SSO system also brings the convenience to RPs, as the risks in the users' authentication are shifted to the IdP, for example, RPs don't need to consider the leakage of users' credentials. Therefore, SSO systems are widely deployed and integrated. The survey on the top 100 websites from SimilarWeb [1] demonstrates that only 25 websites (excluding the ones not for browser accessing) do not integrate the SSO service.

In addition to the convenience for both the users and RPs, current SSO systems introduce the new privacy leakage risk for the users. Instead of maintaining the user's information (including identifier) independently in those systems not integrating the SSO service, the IdP maintains the user's attributes and identity proof in SSO systems, which allows the IdP or the colluded RPs to infer the access trace of a specified user. In details, the privacy leakage risks include:

- Identity linkage, the colluded RPs may link a user if the user's identifiers (generated by the IdP) in these RPs are the same or derivable, and use the attributes maintained in each RP to profile a user.
- Access tracing, the IdP knows which RP a specified user has accessed, as the construction and transmission of the identity proof make the IdP obtain the identifier and URL of the RP accessed by the users.

The privacy leakage is even worse in the widely deployed SSO systems (e.g., Google Identity and Facebook Login). Google and Facebook seem to become the real Mr. Know It All, as they know who you are, where you live, what you have interest in and so on, as long as you use the provided (SSO) service. Firstly, the IdP (e.g., Google and Facebook) maintains various attributes (including address, age, gender, education level and employment details) of the huge number of users, while the protection still needs to be improved, for example, 50 million people's profiles were leaked by Facebook and utilized by Cambridge Analytica to build the portrait of voters for personalised political advertisements [2] in 2016. Secondly, the IdP attempts to collect more information about the users. In addition to the access trace, Google offer $20 gift card for installing the Screenwise Meter [3] to collect the user's behaviours in each RP.

To prevent the colluded RPs from performing the identity linkage, the user's identifier in one RP should never be the same with or derivable from the ones of other RPs. The widely adopted SSO standards (e.g., OIDC and SAML) have specified the requirements for the IdP to generate the user's identifiers in RPs, i.e., a Pairwise Pseudonymous Identifier (PPID) in OIDC [4] and Pairwise Subject Identifier in SAML [5], while the requirement is satisfied in different ways for the implementations of SSO systems. For example, in MITREid Connect, an open-source OIDC implementation, PPID is a random sequence, which is generated by the `Java.Util.UUID` provided by Java, and bound with the RP.

To prevent IdP from tracing the RPs accessed by the user, two SSO systems (BrowserID [6] and SPRESSO [7]) are proposed to hide the user's accessed RPs from IdP in the construction and transmission of identity proof. In BrowserID, the identity proof is signed with the private key generated by user, and transmitted to the RP through the user directly, while the corresponding public key is bound with users' email by IdP who needs not obtain the information of accessed RP. In SPRESSO, RP uses the encrypted RP domain and a nonce as the identifier, so that the real identity of RP is never exposed to IdP, while the identity proof is transmitted to the RP through a trusted entity (named FWD) who doesn't know the user's identity.

However, there is no existing SSO system which prevents both the access tracing and identity linkage. The implementations of OIDC and SAML prevent the identity linkage, but allow the IdP to obtain the identifiers of accessed RPs, while BrowserID and SPRESSO are designed to avoid the IdP to obtain the access tracing, but the colluded RPs may still link the user as the unique email address is used as the identifier in all RPs.

Widely deployed SSO systems (e.g. OIDC) are unable to hide RPs' identity from IdP for security considerations. Firstly, the identity proof should only be sent to the correct RP, which prevents the adversary from performing the impersonation attack with the leaked identity proof. Secondly, the

identity proof should be bound with a specific RP and user, which ensures the identity proof is only valid in the certain RP, and avoids the misuse of identity proof, for example, the adversary fails to use the identity proof for a corrupted RP to access another RP on behalf of the victim user. However, although BrowserID and SPRESSO achieve the goal of hiding RP from IdP, distinct user identifiers are not available in these systems. As distinct user identifier has to be bound with specific RP, to decide which user identifier is to be used for specific authentication, IdP has to know which RP the request is from. Therefore, in order to provide the same identity to the RP in the multiple logins of a user, both BrowserID and SPRESSO use the email address as the identity, which makes the user linkage (from multiple RPs) possible.

In this paper, we propose the first scheme which deals with all the privacy issues introduced by SSO comprehensively. Recluse enables the RP to hide its identity from IdP for users authentication, as well as IdP is able to provide distinct user identifiers for each RP. To achieve the above goals, we proposed the scheme for RP and user identifier generating, which allows that, 1) RP has the ability to offer the changing RP identifiers to IdP in each authentication, from which the real RP identity is not possible to be derived without the trapdoor; 2) IdP is able to generate unique user identifier (`user_idp_id`) bound with specific RP identifier, from which the user identifier in RP(`user_rp_id`)is to be derived with the trapdoor. However, multiple RPs are unable to link the user by `user_rp_id` or `user_idp_id`.

Moreover, Recluse is implemented based on OIDC with the support of Dynamic Registration [8]. For OIDC system the Reluse only requires: (1) a new set of public parameters and web interfaces are provided additionally; (2) the new RP identifier and PPID generating algorithm is supported. Compared with BrowserID and SPRESSO, Recluse does not only deal with the privacy issues comprehensively but also be compatible with traditional OIDC system, which is not achieved by neither BrowserID and SPRESSO. BrowserID requires that the user's identity proof should be generated by user's browser, as well as SPRESSO has to introduce new trustful party into the system.

To deal with the security considerations introduced by hiding RP in OIDC: 1) the identity proof should only be sent to the correct RP; 2) identity proof should not be misused. The following requirements should be fulfilled by Recluse:

- A new algorithm is proposed to negotiate the RP's identifier between the user and RP for each login. Therefore, the RP's identifier in multiple authentications are different, and IdP fails to infer RP's information or link it in different authentications. Moreover, neither RP nor the user may control the generated identifier, which avoids the misuse of the identity proof. The detailed analysis is provided in Section V.
- A browser extension is introduced to transmit the messages (i.e., request and response) related with the authentication, which ensures only the correct RP receives the id token.
- A new generation algorithm of PPID is provided, which makes the PPIDs for one user in one RP indistinguishable from others (e.g., different users in different RPs), while only the RP (and the user) has the trapdoor to derive the unique identifier from different PPIDs for one user in one RP.

We build the prototype system by running the Recluse IdP on the modified MITREid Connect, RP on the SpringMVC frame work and extension on chrome browser. Finally we prove the availability of the Recluse and evaluate the delay introduced by Recluse.

The main contributions of Recluse are as follows:

- We propose a new scheme which deals with all the privacy issues introduced by SSO comprehensively. It has the ability to prevent IdP from tracking users' login trace, as well as multiple RPs are unable to link the users either.
- We developed the prototype of Recluse. The evaluation demonstrates the effectiveness and efficiency of Recluse. We also provide a systematic analysis of Recluse to prove that Recluse introduces no degradation in the security of Recluse.

The rest of this paper is organized as follows. We introduce the background and the threat model in Sections **??** and **??**. Section IV describes the design and details of Recluse. A systematical analysis is presented in Section V. We provide the implementation specifics and evaluation in Section VII, then introduce the related works in Section IX, and draw the conclusion finally.

II. Background

Recluse is an extension of OIDC to prevent the IdP from inferring the user's accessed RP, with the security of SSO systems under consideration. This section provides the necessary background information about OIDC and adopts OIDC as the example to present the security consideration of SSO systems.

A. OpenID Connect

OpenID Connect (current version 1.0) is an extension of OAuth (current version 2.0). The OIDC or OAuth systems contains following entities:

- **User** is the entity to be authenticated in this system who holds the credentials for the IdP. User takes part in the the system through the user agent.
- **User agent** is the software used by the user, such as browser and the application on the mobile device. User agent is required to transmit the authentication request and identity proof between IdP and RP correctly.
- **IdP** is the entity who authenticates the user and provide the identity proof. IdP authenticates the user, verifies the authentication request from RP, generates user's PPID

and issues the identity proof signed with its private key. Besides, IdP provides the notification to user about the range of exposed attributes to RP and guarantees that the identity proof should only be sent to the corresponding RP.

- **RP** is the entity who provides the service and need to identify the user. RP builds the authentication request to IdP with its identifier and endpoint for identity proof. RP identifies a user through the PPID in identity proof.

OAuth is originally designed for authorizing the RP to obtain the user's personal protected resources stored at the resource holder. That is, the RP obtains an access token generated by the resource holder after a clear consent from the user, and uses the access token to obtain the specified resources of the user from the resource holder. However, plenty of RPs adopt OAuth 2.0 in the user authentication, which is not formally defined in the specifications [9], [10], and makes impersonation attack possible [11], [12]. For example, the access token isn't required tp be bound with the RP, the adversary may act as a RP to obtain the access token and use it to impersonate as the victim user in another RP.

OIDC is designed to extend OAuth for user authentication by binding the identity proof for authentication with the information of RP. OIDC provides three protocol flows: authorization code flow, implicit flow and hybrid flow (i.e., a mix-up of the previous two flows). In the authorization code flow, the identity proof is the authorization code sent by the IdP, which is bound with the RP, as only the target RP is able to obtain the user's attributes with this authorization code and the corresponding secret.

The implicit flow of OIDC achieves the binding between the identity proof and the RP, by introducing a new token (i.e., id token). In details, id token includes the user's PPID (i.e., `sub`), the RP's identifier (i.e., `aud`), the valid period and the other requested attributes. The IdP completes the construction of the id token by generating the signature of these elements with its private key, and sends it to the correct RP through the redirect URL registered previously. The RP validates the id token, by verifying the signature with the IdP's public key, checking the correctness of the valid period and the consistency of `aud` with the identifier stored locally. Figure 1 provides the details in the implicit flow of OIDC, where the dashed lines represent the message transmission in the browser while the solid lines denote the network traffic. The detailed processes are as follows:

- Step 1: User attempts to login at one RP.
- Step 2: The RP redirects the user to the corresponding IdP with a newly constructed request of id token. The request contains RP's identifier (i.e., `client_id`), the endpoint (i.e., `redirect_uri`) to receive the id token, and the set of requested attributes (i.e., `scope`). Here, the `openid` should be included in `scope` to request the id token.

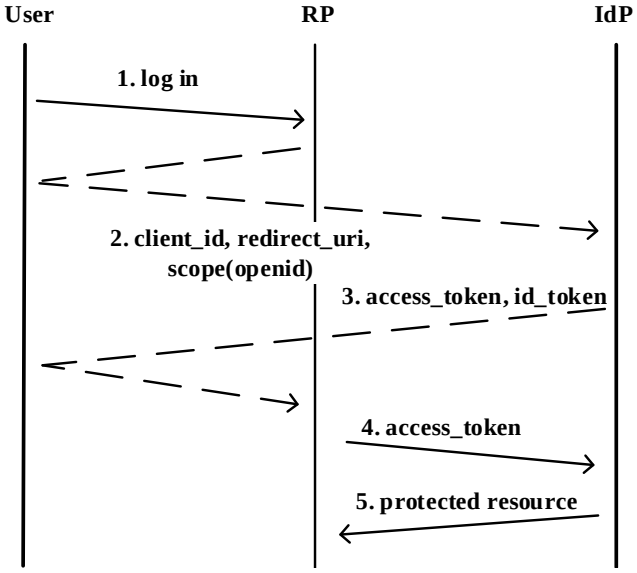

Fig. 1: The implicit protocol flow of OIDC.

- Step 3: The IdP generates the id token and the access token for the user who has been authenticated already, and constructs the response with endpoint (i.e., `redirect_uri`) in request if it is the same with the registered one for the RP. If the user hasn't been authenticated, an extra authentication process is performed.
- Step 4, 5: The RP verifies the id token, identifies the user with `sub` in the id token, and requests the other attributes from IdP with the access token.

Dynamic Registration. The id token (also, the authorization code) is bound with the RP's identifier. OIDC provides the dynamic registration [8] mechanism to register the RP dynamically. After the first successful registration, RP obtains a registration token from the IdP, and is able to update its information (e.g., the `redirect URI` and the response type) by a dynamic registration process with the registration token. One successful dynamic registration process will make the IdP assign a new unique client id for this RP.

B. Security Consideration

Widely deployed SSO systems, such OIDC, are designed with the following security considerations, and various implementations of IdP and RP are also analyzed with the same security principles under the assumption that IdP is trusted. Here, we list the security considerations:

- **Content Checking:** The contents in the identity proof are generated under a clear consent of the user. The contents include the RP's information and the range of exposed attributes.
- **Confidentiality:** The confidentiality of the identity proof is ensured, that is, only the target RP obtains the identity proof which will never be leaked by the honest RP. The

HTTPS connection is used to protect the identity proof between the IdP and the user, while the trusted user agent (e.g., the browser) ensures the identity proof only sent to the correct URL (of RP) which is confirmed by the user and the IdP.
- **Integrity:** No one except the IdP is able to construct a valid identity proof. Any modification in the identity proof makes the identity proof invalid.
- **Binding:** The identity proof is only valid for the target RP, as it is bound with only the target RP, and the honest RP has the ability to verify the consistency.

III. Challenges and Solutions

As SSO systems introduce the novel way for the RPs to identify the user, the authentication security and users' privacy should be considered.

A. Threat Model

In SSO systems, an adversary tries to break the authentication security in following ways:

- Impersonation Attack: Adversaries log in to the honest RP as the honest user.
- Identity Injection: Honest user logs in to the honest RP under adversaries' identity.

Besides, the adversary also has the interests in users' login traces, the private issue introduced by SSO systems. To undermine a user's privacy, the adversary tries to achieve the following goals:

- Adversary finds out which RP a user has accessed by acting as the honest IdP.
- Adversary links the same user in multiple RPs controlled by adversary.

In SSO systems, IdP has the max authority in this system. Therefore, IdP should be considered honest but curious. Otherwise, an malicious IdP has the ability to log in to any RP as any honest user (impersonation attack) and enforce any honest user to log in honest RP under an adversary's identity (identity injection). Moreover, a user's login trace is never hidden from collusion between IdP and RP. It is considered that any RP could be corrupted and any user may be the adversary. User agent is considered completely honest but under control of the user. Therefore, the user agent is seemed as a part of user. Moreover, as network flows are protected by various ways, such as TLS, the network attacker is not considered. The ability of each entity acted by adversary are shown as follows:

- **Curious IdP** acts as an completely honest IdP.
- **Malicious RP** has the ability to build any response, as well as the authentication request, for user's requestion.
- **Malicious User** is able to intercept and tamper all the data transmitted through itself.

However, Identity Injection only occurs when 1) IdP is dishonest; 2) the transmission between RP and IdP is corrupted by either corrupted user agent or unprotected network flows. Therefore, Identity Injection is not considered.

B. Challenges

To protect users from the privacy issues introduced by SSO systems, the scheme should simultaneously achieve the following goals:

- Hiding RP's identity from IdP.
- Providing distinct user identifier for each RP.

However, it will introduce prominent challenges.

As it has been described in Section I, it is required to expose the identifier of users' accessed RP for security consideration. Hiding RP's identity from IdP breaks the security considerations listed in Section II.

- **Breaking Binding:** To hide RP's identity, IdP is unable to know which RP the identity proof is issued for. Therefore, the identity proof is no longer bound with the specific RP, which results in the misuse of identity proof. An adversary has the ability to achieve an honest user's identity proof by various ways, for example, once the user logs in the corrupted RP controlled by the adversary with his/her identity proof, the adversary is able to access other honest RPs with the honest user's identity by using this identity proof (Impersonation Attack).
- **Breaking Confidentiality:** To hide RP's identity, IdP is unable to know the correct endpoint provided by the RP to receive the identity proof. For example, in OIDC, IdP holds the list of all the endpoints of RP waiting for `id_token`, so IdP is able to guarantee that the identity proof is only to be sent to the endpoint in this list. Without the endpoint representing RP's identity, an RP controlled by the adversary has the ability to build the authentication request by setting another honest RP's identifier (if RP's identifier is used in a way without exposing RP's identity) and the adversary's endpoint. IdP is to send the identity proof issued for the honest RP to the adversary. Therefore, the adversary has the ability to achieve the identity proof valid in honest RPs, which results in Impersonation Attack.
- **Ignoring Content Checking:** To hide RP's identity, IdP is unable to know the RP's unique real name, which represents the RP. Therefore, the notification of target RP's identity to user is no longer provided by IdP. An adversary has the ability to utilize this vulnerability as well as breaking confidentiality to achieve honest user's valid identity proof for other honest RPs (Impersonation Attack). Additionally, as SSO systems require user's clear consent for certain login to specific RP, the phishing attack can be avoided in some situations by RP's name checking. The ignoring of content checking breaks the protection from phishing attack.

Additionally, it introduces another challenge to provide distinct user identifier while hiding RP's identity

- **RP is unable to identify the user:** To hide RP's identity, the single RP's multiple authentication requests should be considered from different RPs by IdP. However, the user identifier provided by IdP is solely bound with an RP to avoid linking the user through RPs' collusion. It means that the single user's multiple identifiers for one RP will never be constant. Therefore, RP is unable to identify the user no longer.

C. Solutions

To deal with the challenges introduced by hiding RP's identity from IdP, the following methods are proposed:

- **Providing the RP identifier which is only valid in corresponding RP without exposing RP's real identity.** The RP identifier should be generated in a way so that for each authentication the identifiers are different. Moreover, the generation should be beyond any entities' control to avoid the misuse of user's identity proof, which happens when different RPs use the same identifier. Therefore, we propose the scheme that the identifier should be generated under the negotiation between the user and RP. However, in this way, the malicious RP and user have the ability to build any negotiation requests and responses they need. Adversaries try to the honest RP use the same identifier with a corrupted one to obtain an honest user's identity proof valid in other honest RPs, which will be analysed detailedly in Section V. Moreover, the curious IdP tries to derive the real identity of RP from the RP identifier. It is also to be analysed in Section V.
- **Providing the distinct user identifier which make RP able to identify the user.** It is required that the user identifier provided by IdP (named `user_id`) should be different in each authentication, but RP is able to derive the specific user identifier for each RP (named `user_rp_id`) which is constant for each RP with the `user_id`. However, the current ways to generate user identifier, such as using random character string as user identifier and binding it with specific RP identifier in database, is not appropriate. Therefore, we proposed a novel `user_id` generating algorithm associated with RP identifier generating which allows only the corresponding RP has the trapdoor to derive the `user_rp_id` from `user_id`. In this way, malicious RPs try to link the user by the `user_id`, which is also to be analysed in Section V.
- **Binding the RP identifier with RP's attributes.** It is required that the identity proof issued for specific RP identifier should be sent to the corresponding endpoint. However, RP identifier is generated temporarily by user and RP unrelated with any RP, so that IdP is unable to decide which endpoint the identity proof should be sent to. Therefore, the enhanced user agent is required to guarantee the identity proof's transmission without introducing new trustful entity into SSO system. It is required that the RP identifier generation should be based on the basic identifier element (named `basic_rp_id`) issued by RP, as well as the `basic_rp_id` should be bound with specific endpoint. Moreover, if IdP publishes the relationship of all the RPs on its website, unless user agent caches all the relationship, the access for specific RP's relationship is to expose the user's accessed RP. Therefore, IdP should offer the certification signed with its private key for each RP, which contains the RP's `basic_rp_id` and endpoint list. User agent should have the ability to verify this certification. Similarly, the responsibility of notifying user with RP's identity should be shifted to user agent. Same as binding the RP identifier with correct endpoint, RP's certification should contains RP's name and user agent should show it to user clearly while authenticating.

D. Challenges and Solutions in OIDC

OIDC is designed for the centralized systems. Therefore, prior coordination is required between RP and IdP so that RP registers its individual attributes (i.e., `redirect_uris`) and gets client attributes (i.e., `client_id`) issued by IdP. While the authentication request is transmitted from RP, IdP verifies the validation of `client_id` and `redirect_uri` because it only provide service to those RPs already registered. Therefore, if an RP builds the authentication request without `client_id` and `redirect_uri`, IdP considers it invalid.

With dynamic registration, an RP has the ability to re-register the new `client_id` and `redirect_uri` with IdP. Therefore, it is needed that before the authentication request is transmitted to IdP, RP should re-register the newly generated `client_id` and completely random `redirect_uri` with IdP. The registration should be conducted by the user to avoid direct interactive between RP and IdP. However, the specification [8] of OIDC dynamic registration requires the registration request should carry a bearer token as well as the new `client_id` is generated by IdP. To avoid IdP finding out RP's identity through dynamic registration, the requirement of registration token should be omitted. It is also needed to enable RP to assign the specific `client_id`. It is observed that although `client_id` is defined to be generated by IdP, some OIDC systems (e.g., MITREid Connect) enable the `client_id` be the input attribute.

IV. Design of Recluse

The overview of login flow is shown in Figure 2, which contains RP identifier negotiation, dynamic registration and token obtaining. The of each phase in login flow is shown as follows:

1. RP identifier Negotiation: For each SSO procedure, user is going to start negotiation with user. RP identifier is a random number which does not represent any RP, generated by rp-id-generating algorithm. However, the

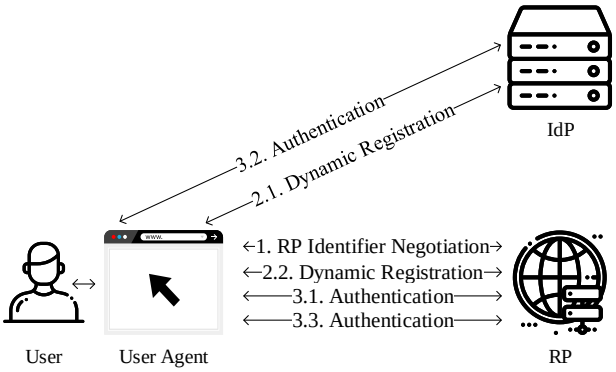

Fig. 2: Overview of System

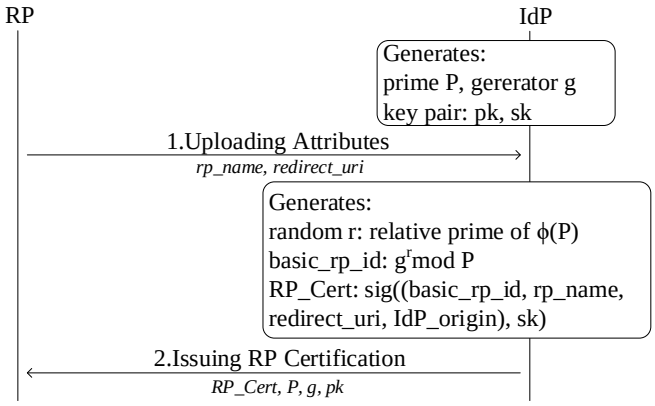

Fig. 3: Prior Registration

identifier is bound with specific authentication which is able to be confirmed by user and RP.

2. Dynamic Registration: To make the RP identifier generated by negotiation is valid in IdP, user is to register this identifier with IdP through the dynamic registration API provided by IdP. IdP is going to check whether the identifier is unique and require RP to restart identifier negotiation if the identifier has be used by another RP.
3. Authentication: After dynamic registration, RP builds the authentication request and redirects it to IdP through user agent. After receiving the request, IdP firstly authenticates user and then issues identity proof for RP, which contains the user id generated through the user-id-generating algorithm. Then IdP redirects the identity to RP through user agent, and RP identify the user through identity proof.

A. Prior Registration

The prior registration between RP and IdP is shown as Figure 3. The registration process is as follows:

1. Uploading Attributes: Firstly, IdP generates its prime P, the primitive root g of P, the key pair `pk` and `sk`. Then RP uploads it attributes, such as its name, endpoint, identity proof (e.g., business license) and so on.
2. Issuing RP Certification: IdP verifies the identity of RP and generates the RP certification including `basic\_rp\_id`, `rp\_name`, `redirect\_uri` and `IdP\_origin`. IdP returns the RP certification, P, the key pair to RP.

The prior registration required for IdP to verify the basic attributes of RP, such as name, endpoints for identity proof, so that Idp is able to provide the RP certification to RP which includes the unique identifier for each RP and its attributes. With the RP certification, user agent has the ability to verify the RP's endpoint for identity proof and notify user with RP's identity. Additionally, the parameters, prime P (used for user id generating) with its generator g, public key of IdP `pk` is provided in registration as well. Same as RP, user need to register with IdP and IdP generates unique user id for each user.

B. Rp-id-generating and User-id-generating algorithm

The rp-id-generating and user-id-generating algorithm are created based on Discrete Logarithm problem [13]. IdP carefully chooses a big prime P and its primitive root `g` as generator for system. When the RP registers with IdP, IdP provides a unique primitive root as the RP's root identifier (called `basic_rp_id`).

The generation of `rp_id` and `user_id` is shown as Figure 4, as well as the trapdoor for RP to derive `user_rp_id` is as shown.

For each login process, the user and RP negotiate the temporary RP identifier bound with specific authentication. While starting a login procedure, there is Diffie-Hellman key Exchange [14] between RP and user, through which the random r is generated. However, to make sure that there is r^{-1}, that $r \cdot r^{-1} = 1 mod \phi(P)$, r should be the relative prime of $\phi(P)$, so that if r is even r should be added by one. Although there is little possibility that r is the multiple of p or q, it is not considered in the illustration. However, the re-negotiation is required in the practical system if r is the multiple of p or q. The RP identifier is generated as:

$$rp\_id = basic\_rp\_id^r mod P \tag{1}$$

such that rp_id is another primitive element module p. And r^{-1} is generated through Extended Euclidean algorithm.

IdP labels each user at IdP with the unique identifier called $baisc\_user\_id$. To generate the specific user identifier for each rp_id, the algorithm is

$$user\_id = rp\_id^{basic\_user\_id} mod P \tag{2}$$

so

$$user\_id = basic\_rp\_id^{r \cdot basic\_user\_id} mod P \tag{3}$$

[1] P is generated as $P = q \cdot 2 + 1$, while q is prime as well.

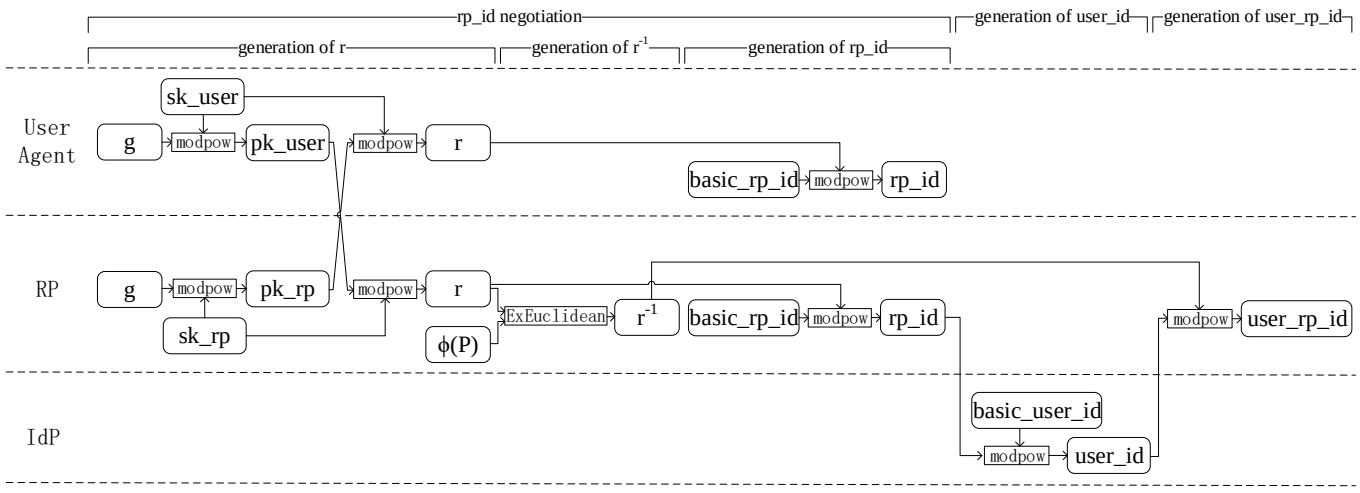

Fig. 4: Generation of rp_id and user_id

While receiving $user\_id$ from IdP, RP can derive the constant user identifier from if

$$user\_rp\_id = user\_id^{r^{-1}} modP \tag{4}$$

so

$$user\_rp\_id = basic\_rp\_id^{(1 mod \phi(P)) \cdot basic\_user\_id} modP \tag{5}$$

so

$$user\_rp\_id = basic\_rp\_id^{basic\_user\_id} modP \tag{6}$$

For single user in a RP, $user\_rp\_id$ is unchanged. However, $user_rp_id$s are distinct in each RP because $basic_rp_id$s are different in each RP.

C. Login Flow

The login flow is shown as Figure 5.

1) RP Identifier Negotiation: RP identifier negotiation starts form step 1 to step 4. The user accesses the service provided by RP in his/her browser. To log in this RP, user needs to click the login button offered by Recluse. Firstly, the user agent sends the `Start Negotiation` request to RP, so that RP generates the random sk_rp and $pk\_rp = g^{sk\_rp} modP$ as the private key and public key for DH Key exchanging. Secondly, RP builds the `Negotiation Response` with newly generated pk_rp as well as the `RP_Cert` issued by IdP. User agent similarly generates random sk_user and pk_user, and $r = pk\_rp^{sk\_user} modP$. However, to make sure that r is the relative prime of $\phi(P)$, it is required that r should be odd and the greatest common divisor of r and $\phi(P)$ is 1. Then user agent continues the `Negotiation` sending pk_user and r to RP. RP generates the local r in the same way as user agent and compares the local r and user agent generated r. If rs are equal, RP generates $rp\_id = basic\_rp\_id^r modP$, as well as r^{-1} through Extend Euclidean algorithm, which meets $r \cdot r^{-1} = 1 mod \phi(P)$. Finally RP transmits the rp_id to user agent.

2) Dynamic Registration: Dynamic registration is from step 5 to step 7. While user agent receives teh rp_id from RP, it is required the rp_id from RP should be equal with it generated by user agent. Then user agent generates the `fake\_uri` which contains the random string and keeps it for further identity proof transmission. User agent sends the `Dynamic Registration` request to IdP with newly generated rp_id and `fake_uri` and redirects the `Dynamic Registration Response` to RP.

3) Authentication: Authentication is from step 8 to step 12. After dynamic registration, RP builds the `Authentication Request` including rp_id as well as the `redirect_uri` representing the endpoint, and redirects it to IdP through user agent. User agent tampers the authentication request, compares rp_id with the local one, verifies the validation of the `redirect_uri` and replaces it with the fake one. Then user agent transmits the `Authentication Request` to IdP. After receiving the request, IdP firstly authenticates user and then generates $user\_id = rp\_id^{basic\_user\_id} modP$. The identity proof signed with IdP's private key including the $user\_id$ is redirected to the `fake_uri` through user agent, who intercepts the transmission and transmit it to the endpoint `redirect_uri` in authentication request. Finally, RP derives the constant $user\_rp\_id$ from $user\_id$. If the $user\_rp\_id$ has already been registered, RP send `Authentication Finished` with the message `success` to user agent.

V. Security Analysis

In order to prove the privacy and security properties of Recluse system, we firstly demonstrate that for any adversary in the system, a user's access to an specific RP untraceable from it to another one. Besides, we illustrate the potential attacks discussed in the previous work about SSO security and the security issues introduced by Recluse.

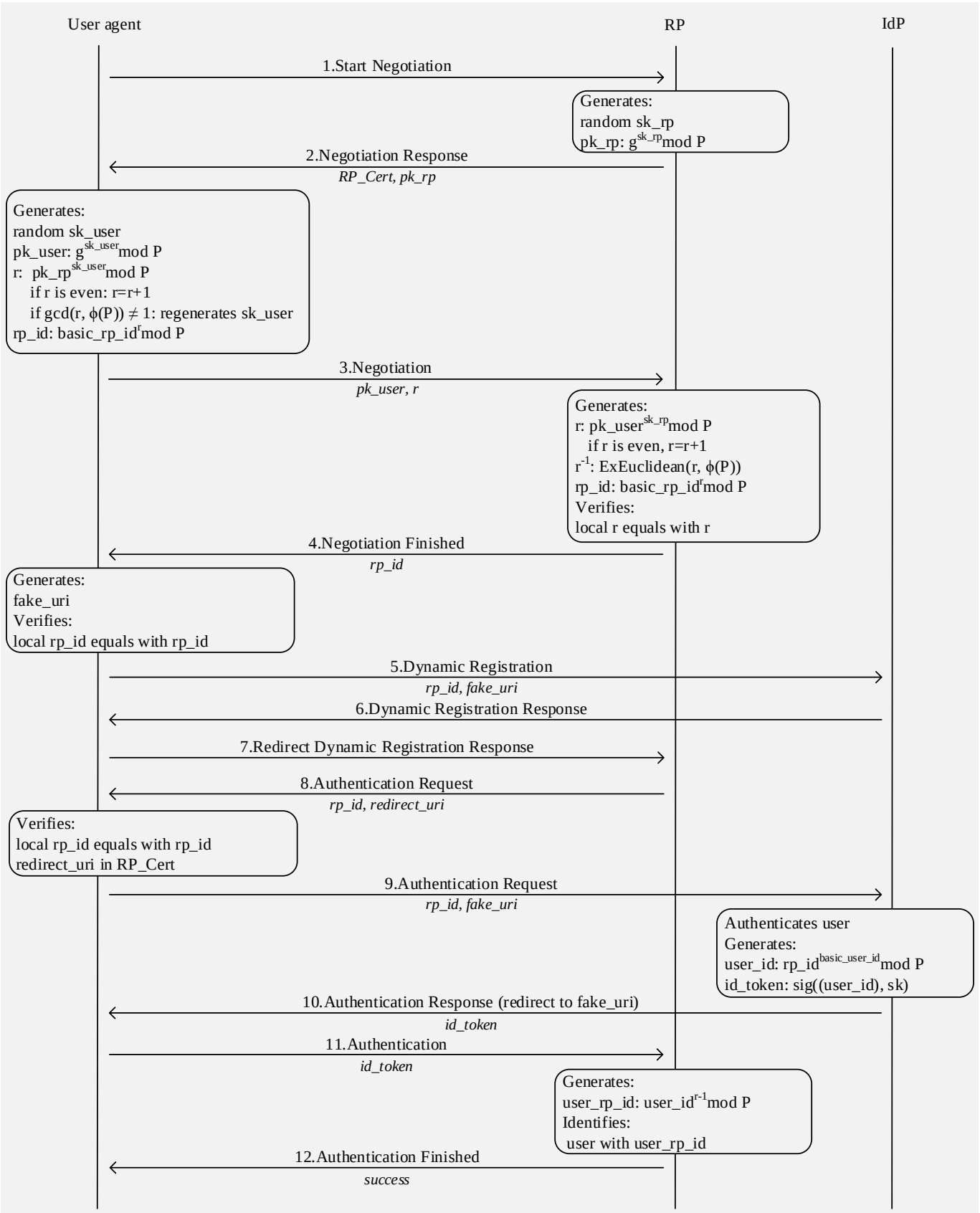

Fig. 5: Login Flow

Firstly, to explicitly illustrate how an adversary works in the SSO system, the `authentication flow` is created to defined the authentication of specific IdP, RP and user. For example, now there are IdP, $User_A$, $User_B$, RP_A and RP_B, who are able to form 4 `authentication flows`, (IdP, $User_A$, RP_A), (IdP, $User_A$, RP_B), (IdP, $User_B$, RP_A) and (IdP, $User_B$, RP_B). An adversary has the ability to act one or more entities in single or multiple `authentication flows`. That is, an adversary is able to act as, i) the single entity in one `authentication flow`, such as the curious IdP; ii) the same entity in multiple `authentication flows`, such as acting as different RPs for the same honest user ; iii) the different entities in multiple `authentication flows`, such as acting as the RP for the honest user and the user for the honest RP at the same time. However, it is considered an adversary should not act as both the IdP and RP in single `authentication flow`.

A. Privacy

We now define the untraceability of SSO system. It is in the SSO system, for an adversary controlling curious IdP, it is impossible to inspect whether two `authentication flows` are to same RP or not, however, for an adversary controlling malicious RPs, it is impossible to inspect whether two `authentication flows` are from same user or not.

Assuming there are two `authentication flows` from the same user to the same RP. In Recluse system, for the curious IdP, the only parameter related with RP is rp_id, as other parameters are related or generated by user, such as $fake\_uri$. To break the untraceability, IdP tries to derive the $basic\_rp\_id$ of RP from rp_id or inspect whether the rp_ids are generated by the same $basic\_rp\_id$. However, as rp_id is generated by the formula (1), so

$$basic\_rp\_id = rp\_id^{r^{-1}} modP \tag{7}$$

However, r and r^{-1} is unknown to the IdP, so that IdP is unable to derive the $basic\_rp\_id$ from the rp_id. Moreover, even the IdP suspects that the rp_id is generated by the specific RP, it is impossible for IdP to verify it as the rp_id can be generated based on any primitive root of P. Besides, assuming that the rp_ids in different `authentication flows` are rp_id_1 and rp_id_2 generated by r_1 and r_2. There is

$$rp\_id_1 = rp\_id_2^{r_1/r_2} modp \tag{8}$$

So only the entity who carries the r_1 and r_2 is able to verify whether rp_id_1 and rp_id_2 generated by the same RP.

Inspecting whether the users in two `authentication flows` are the same user relies on the $baisc\_user\_id$ or the relation between $user_id$s or $user_rp_id$s. Assuming the same user log in different RPs where the $user_id$s are $user\_id_1$ and $user\_id_2$, $user_rp_id$s are $user\_rp\_id_1$ and $user\_rp\_id_2$, and $basic_rp_id$s are $basic\_rp\_id_1$ and $basic\_rp\_id_2$. We define that $\alpha = \log_{basic\_rp\_id_2} basic\_rp\_id_1$. There is

$$user\_rp\_id_1 = user\_rp\_id_2^{\alpha} \tag{9}$$

and

$$user\_id_1 = user\_id_2^{\alpha \cdot r_1/r_2} \tag{10}$$

The α is unknown to the malicious, so that the adversary is unable to inspect whether the two `authentication flows` are from the same user. However, the malicious also tries to lead the same user in two `authentication flows` using the same $user\_rp\_id$ or $user\_id$. According to formula (2) and (4), the user should use the same $basic\_rp\_id$ or rp_id in two `authentication flows`. So the $user\_rp\_id$ is impossible to be same as $basic\_rp\_id$ is issued by IdP and verified by user agent. And rp_id is generated through the negotiation between user and RP, so that RP is unable to lead the user to use the same rp_id in different `authentication flows`.

B. Impersonation attack

RP conducts impersonation attack by getting user's id_token which is valid in other RPs. OpenID Connect protocol protect id_token from malicious RP by keep RP owns unique client_id and check RP's redirect_uri during login. Unique client_id makes one RP's id_token invalid in other RPs. And IdP only redirects id_token to it's relevant RP's redirect_uri registered in IdP so that attacker is never able get RP's id_token. There are three conditions for a malicious to try getting a validate id_token. 1) Malicious RP has already finished client_id negotiation with an RP as a user. As client_id is generated by both RP and user, malicious RP is unable to get the id_token with the same client_id. 2)Malicious RP has got a user's id_token, same as condition 1 malicious RP is unable to negotiate the same client_id with another RP. 3) Malicious RP acts as the man in the middle between RP and user. As RP sends its URL in rp_certificate user only sends its id_token to this URL so that attacker can never achieve id_token. As a summary, malicious is unable to conduct impersonation attack.

Malicious user is only able to conduct impersonation attack by tempering id_token. If attacker has already get victim's user_rp_id, attacker is able to calculate $user\_id = user\_rp\_id^r modp$. r is shared by RP and attacker. However id_token is protected by the signature generated by IdP so that it is impossible for attacker to log in RP as victim.

C. Abduction attack

To lead user to login an RP as attacker, attacker needs to make sure that user receive a malicious token from IdP. As https is used to protect parameters transforming between user and IdP, it's impossible to temper user's token during transmission. The other way to conduct the attack is phishing attack on IdP. In traditional SSO protocol such as OAuth 2.0

and OpenID Connect, it is possible for malicious to conduct phishing attack on IdP. As it is shown in 1 step 2, the request from user to IdP is built by RP. If an malicious RP set the IdP'url as its phishing site, an unwary user may input its id and password on the phishing website so that attacker is able to get the full control of user's account. In PriOIDC as RP_Cert contains IdP's url, user agent is going to compare the IdP's url in request and RP_Cert. If they are not matched, the request is deemed invalid.

Phishing attack on RP in SSO system is quite different from it in normal website. In SSO system even an unwary user has visited a phishing RP's website, IdP is going to ask user to make sure RP's identity in 1 step 2. The identity is bound with RP's client id and client id is bound with its redirect uri. If malicious RP constructs the request in 1 step 2 to IdP with its personal client id, user is able to find out the true identity of RP and protect itself from phishing attack. In traditional SSO system if malicious uses a client id of another RP, IdP is going to redirect user to the corresponding redirect uri. In PriOIDC user agent is going to compare redirect uri from RP with the redirect uri in RP_Cert.If uris are not matched, the request is regarded invalid. A phishing RP can never achieve another RP's token and never lead user to log in its website.

D. Discussion

An external attacker is also taken into account in SSO system. External attacker is able to capture and temper all the network flow through user, RP and IdP. External attacker's targets include impersonation attack, abduction attack and privacy undermining attack. If an attacker keeps its eye on a specific user, it is able to find that the user's login on different RPs. So it is easy for an external attacker to draw a user's login trace. Privacy protection is not effective for external attacker. To protect user from privacy leaking a proxy is probably a appropriate scheme. Proxy is able to mix multi-user's request and keep user's login trace invisible to attacker. User's dynamic IP makes proxy impossible to get user's login trace from user's IP External attacker is going to steal user's id_token from network flow to make the attack and it is also going to make the attack by temper user's id_token into attacker's id_token when id_token is transformed on the network. As all the network flows are protected by https, external attacker is unable to conduct the attacks.

VI. Implementation

VII. Evaluation

Time

Storage

A. Settings

B. Result

C. Comparison

VIII. Discussion

IX. Related Works

In 2014, Chen et al. [11] concludes the problems developers may face to in using sso protocol. It describes the requirements for authentication and authorization and different between them. They illustrate what kind of protocol is appropriate to authentication. And in this work the importance of secure base for token transmission is also pointed.

In 2016, Daniel et al. [15] conduct comprehensive formal security Analysis of OAuth 2.0. In this work, they illustrate attacks on OAuth 2.0 and OpenID Connect. Besides they also presents the snalysis of OAuth 2.0 about authorization and authentication properties and so on.

Besides of OAuth 2.0 and OpenID Connect 1.0, Juraj et al. [16] find XSW vulnerabilities which allows attackers insert malicious elements in 11 SAML frameworks. It allows adversaries to compromise the integrity of SAML and causes different types of attack in each frameworks.

Other security analysis [17] [18] [12] [19] [20] on SSO system concludes the rules SSO protocol must obey with different manners.

In 2010, Han et al. [21] proposed a dynamic SSO system with digital signature to guarantee unforgeability. To protect user's privacy, it uses broadcast encryption to make sure only the designated service providers is able to check the validity of user's credential. User uses zero-knowledge proofs to show it is the owner of the valid credential. But in this system verifier is unable to find out the relevance of same user's different requests so that it cannot provide customization service to a user. So this system is not appropriate for current web applications.

In 2013, Wang et al. proposed anonymous single sign-on schemes transformed from group signatures. In an ASSO scheme, a user gets credential from a trusted third party (same as IdP) once. Then user is able to authenticate itself to different service providers (same as RP) by generating a user proof via using the same credential. SPs can confirm the validity of each user but should not be able to trace the users identity.

Anonymous SSO schemes prevents the IdP from obtaining the user's identity for RPs who do not require the user's identity nor PII, and just need to check whether the user is authorized or not. These anonymous schemes, such as the anonymous scheme proposed by Han et al. [22], allow user to obtain a token from IdP by proving that he/she is someone who has registered in the Central Authority based on Zero-Knowledge Proof. RP is only able to check the validation of the token but unable to identify the user. In 2018, Han et al. [22] proposed a novel SSO system which uses zero knowledge to keep user anonymous in the system. A user is

able to obtain a ticket for a verifier (RP) from a ticket issuer (IdP) anonymously without informing ticket issuer anything about its identity. Ticket issuer is unable to find out whether two ticket is required by same user or not. The ticket is only validate in the designated verifier. Verifier cannot collude with other verifiers to link a user's service requests. Same as the last work, system verifier is unable to find out the relevance of same user's different requests so that it cannot provide customization service to a user. So this system is not appropriate for current web applications.

BrowserID [23] [24] is a user privacy respecting SSO system proposed by Molliza. BrowserID allows user to generates asymmetric key pair and upload its public to IdP. IdP put user's email and public key together and generates its signature as user certificate (UC). User signs origin of the RP with its private key as identity assertion (IA). A pair containing a UC and a matching IA is called a certificate assertion pair (CAP) and RP authenticates a user by its CAP. But UC contains user's email so that RPs are able to link a user's logins in different RPs.

SPRESSO [7] allows RP to encrypt its identity and a random number with symmetric algorithm as a tag to present itself in each login. And token containing user's email and tag signed by IdP is also encrypted by a symmetric key provided by RP. During parameters transmission a third party credible website is required to forward important data. As token contains user's email, RPs are able to link a user's logins in different RPs.

All the SSO system protocols above are quite different from current popular SSO protocol. So it is difficult for IdPs and RPs to remould their system into new protocols.

X. CONCLUSION

REFERENCES

[1] "Top websites," https://pro.similarweb.com/#/industry/topsites/All/999/1m?webSource=Total, Accessed July 20, 2019.

[2] Carole Cadwalladr and Emma Graham-Harrison, "Revealed: 50 million facebook profiles harvested for cambridge analytica in major data breach," https://www.theguardian.com/news/2018/mar/17/cambridge-analytica-facebook-influence-us-election, Accessed July 20, 2019.

[3] SYDNEY LI and JASON KELLEY, "Revealed: 50 million facebook profiles harvested for cambridge analytica in major data breach," https://www.eff.org/deeplinks/2019/02/google-screenwise-unwise-trade-all-your-privacy-cash, Accessed July 20, 2019.

[4] J. Bradley N. Sakimura, NRI, "Openid connect core 1.0 incorporating errata set 1," https://openid.net/specs/openid-connect-core-1_0.html#CodeFlowSteps.

[5] Thomas Hardjono and Scott Cantor, "Saml v2.0 subject identifier attributes profile version 1.0," *OASIS standard*, 2019.

[6] Mozilla Developer Network (MDN), "Persona," https://developer.mozilla.org/en-US/docs/Archive/Mozilla/Persona.

[7] Daniel Fett, Ralf Küsters, and Guido Schmitz, "SPRESSO: A secure, privacy-respecting single sign-on system for the web," in *Proceedings of the 22nd ACM SIGSAC Conference on Computer and Communications Security, Denver, CO, USA, October 12-16, 2015*, 2015, pp. 1358–1369.

[8] J. Bradley N. Sakimura, NRI, "Openid connect dynamic client registration 1.0 incorporating errata set 1," https://openid.net/specs/openid-connect-registration-1_0.html.

[9] Dick Hardt, "The oauth 2.0 authorization framework," *RFC*, vol. 6749, pp. 1–76, 2012.

[10] Michael B. Jones and Dick Hardt, "The oauth 2.0 authorization framework: Bearer token usage," *RFC*, vol. 6750, pp. 1–18, 2012.

[11] Eric Y. Chen, Yutong Pei, Shuo Chen, Yuan Tian, Robert Kotcher, and Patrick Tague, "Oauth demystified for mobile application developers," in *Proceedings of the 2014 ACM SIGSAC Conference on Computer and Communications Security, Scottsdale, AZ, USA, November 3-7, 2014*, 2014, pp. 892–903.

[12] Hui Wang, Yuanyuan Zhang, Juanru Li, and Dawu Gu, "The achilles heel of oauth: a multi-platform study of oauth-based authentication," in *Proceedings of the 32nd Annual Conference on Computer Security Applications, ACSAC 2016, Los Angeles, CA, USA, December 5-9, 2016*, 2016, pp. 167–176.

[13] Peter Shiu, "Cryptography: Theory and practice (3rd edn), by douglas r. stinson. pp. 593. 2006. (hbk) 39.99. isbn 1 58488 508 4 (chapman and hall / crc).," *The Mathematical Gazette*, vol. 91, no. 520, pp. 189, 2007.

[14] Whitfield Diffie and Martin E. Hellman, "New directions in cryptography," *IEEE Trans. Information Theory*, vol. 22, no. 6, pp. 644–654, 1976.

[15] Daniel Fett, Ralf Küsters, and Guido Schmitz, "A comprehensive formal security analysis of oauth 2.0," in *Proceedings of the 2016 ACM SIGSAC Conference on Computer and Communications Security, Vienna, Austria, October 24-28, 2016*, 2016, pp. 1204–1215.

[16] Juraj Somorovsky, Andreas Mayer, Jörg Schwenk, Marco Kampmann, and Meiko Jensen, "On breaking SAML: be whoever you want to be," in *Proceedings of the 21th USENIX Security Symposium, Bellevue, WA, USA, August 8-10, 2012*, 2012, pp. 397–412.

[17] Rui Wang, Shuo Chen, and XiaoFeng Wang, "Signing me onto your accounts through facebook and google: A traffic-guided security study of commercially deployed single-sign-on web services," in *IEEE Symposium on Security and Privacy, SP 2012, 21-23 May 2012, San Francisco, California, USA*, 2012, pp. 365–379.

[18] Yuchen Zhou and David Evans, "Ssoscan: Automated testing of web applications for single sign-on vulnerabilities," in *Proceedings of the 23rd USENIX Security Symposium, San Diego, CA, USA, August 20-22, 2014.*, 2014, pp. 495–510.

[19] Ronghai Yang, Guanchen Li, Wing Cheong Lau, Kehuan Zhang, and Pili Hu, "Model-based security testing: An empirical study on oauth 2.0 implementations," in *Proceedings of the 11th ACM on Asia Conference on Computer and Communications Security, AsiaCCS 2016, Xi'an, China, May 30 - June 3, 2016*, 2016, pp. 651–662.

[20] Hui Wang, Yuanyuan Zhang, Juanru Li, Hui Liu, Wenbo Yang, Bodong Li, and Dawu Gu, "Vulnerability assessment of oauth implementations in android applications," in *Proceedings of the 31st Annual Computer Security Applications Conference, Los Angeles, CA, USA, December 7-11, 2015*, 2015, pp. 61–70.

[21] Jinguang Han, Yi Mu, Willy Susilo, and Jun Yan, "A generic construction of dynamic single sign-on with strong security," in *Security and Privacy in Communication Networks - 6th Iternational ICST Conference, SecureComm 2010, Singapore, September 7-9, 2010. Proceedings*, 2010, pp. 181–198.

[22] Jinguang Han, Liqun Chen, Steve Schneider, Helen Treharne, and Stephan Wesemeyer, "Anonymous single-sign-on for n designated services with traceability," in *Computer Security - 23rd European Symposium on Research in Computer Security, ESORICS 2018, Barcelona, Spain, September 3-7, 2018, Proceedings, Part I*, 2018, pp. 470–490.

[23] Daniel Fett, Ralf Küsters, and Guido Schmitz, "Analyzing the browserid SSO system with primary identity providers using an expressive model of the web," in *20th European Symposium on Research in Computer Security (ESORICS)*, 2015, pp. 43–65.

[24] Daniel Fett, Ralf Küsters, and Guido Schmitz, "An expressive model for the web infrastructure: Definition and application to the browserid SSO system," *CoRR*, vol. abs/1403.1866, 2014.