# UPPRESSO: An Unlinkable Privacy-PREserving Single Sign-On System

Abstract—As a widely adopted identity management and authentication mechanism in today's Internet, single sign-on (SSO) allows a user to maintain only the credential for the identity provider (IdP), instead of one credential for each relying party (RP), which shifts the burden of user authentication from RPs to the IdP. However, SSO introduces new privacy leakage threats, since (a) a curious IdP could track all the RPs a user has visited, and (b) collusive RPs could learn a user's online profile by linking her identifiers and activities across multiple RPs. Several privacy-preserving SSO solutions have been proposed to defend against either the curious IdP or collusive RPs, however, none of them can address both privacy leakage threats at the same time.

In this paper, we propose a privacy-preserving SSO system, called UPPRESSO, to protect a user's login traces against both the curious IdP and collusive RPs. We first formally analyze the privacy dilemma between SSO security requirements and the new privacy requirements, and convert the SSO privacy problem into an identifier-transformation problem. Then, we design a novel transformed RP designation scheme to transform the identifier of the RP, to which the user requests to log in, into a privacy-preserving pseudo-identifier  $(PID_{RP})$  through the cooperation between the user and the RP. Our trapdoor user identification scheme allows the RP to obtain a trapdoor from the transformation process and use it to derive a unique account of the user at that RP from her privacy-preserving pseudoidentifier  $(PID_U)$  generated by the IdP. The login process of UP-PRESSO follows the service pattern of OpenID Connect (OIDC), a widely deployed SSO system, with minimum modifications and is platform independent. Our analysis shows UPPRESSO provides a comprehensive privacy protection while achieving the same security guarantees of OIDC.

Keywords—Single sign-on, security, privacy.

#### I. Introduction

As a widely deployed identity management and authentication mechanism in the current Internet, single sign-on (SSO) systems such as OpenID Connect [1], OAuth [2] and SAML [3] allow a user to log in to a website, called the relying party (RP), using the account registered at another website, called the identity provider (IdP). The RPs delegate user authentication to a trusted IdP, who generates identity proofs for her visits to these RPs. Thus, the user only needs to remember one credential for the IdP, instead of maintaining different credentials for different RPs. SSO has been widely integrated with many application services. For example, we find that 80% of the Alexa Top-100 websites support SSO [4], and the analysis on the Alexa Top-1M websites identifies 6.30% with the SSO support [5]. Meanwhile, many email and social network providers (such as Google, Facebook, Twitter, etc.) are serving the IdP roles in the Internet.

However, SSO systems have been continuously found vulnerable and insecure [23]–[25], [28], [30]–[32], [36]–[38].

Moreover, the adoption of SSO raises a public concern about user privacy [6], [7], [14], [15], that is whether an adversary is able to track to which RP(s) the user has logged in. Unfortunately, almost all the existing SSO protocols leak user privacy in different ways. Take a widely used SSO protocol OpenID Connect (OIDC) as an example. As shown in Fig. 1, the login process starts when a user sends a login request to the RP, who then constructs a request for identity proof with its identity and redirects the request to the IdP. After authenticating the user, the IdP generates an identify proof with the user's and RP's identities, which is returned to the user and forwarded to the RP. Finally, the RP verifies the identity proof to decide if the user is allowed to log in. In such login instances, by design, an IdP can always see when and where its users log in, in order to generate the identity proof. As a result, a curious IdP can always discover the RPs that a target user has visited over time. This data can be further analyzed to profile users' online activities. Thus, we call this privacy attack IdP-based login tracing, which has also been reported by previous research [14], [15]. Similarly, by design, the RPs can learn users' identities from the identify proofs. If the IdP binds an unique or relevant user identifier(s) to identity proofs generated for the same user but different RPs [8], [9], these RPs can collude to correlate the identifier(s) with the user's identity. We denote this privacy risk as RP-based identity linkage, which allows the adversaries to not only track the user's online activities but also associate her attributes across multiple RPs by linking her login requests [6].

As SSO becomes a popular safeguard for various privacysensitive web services, the privacy concern is considered more prominent and severe than it was in the past. On one hand, privacy-savvy users may provide no or few personal information to web applications to avoid user tracking or profiling. On the other hand, the use of popular SSO services such as Google Account opens a door for IdPs and application providers to recover users' online traces and profiles, which makes users' privacy protection effort in vain. Several large IdPs, especially the social IdPs, are known to be interested in collecting users' online behavioral data for various purposes (e.g., Screenwise Meter [10] and Onavo [11]). Serving the IdP role makes it possible for them to collect such information. Meanwhile, service providers hosting multiple web applications take an advantaged position to correlate users' multiple logins at different RPs through internal information integration. Finally, privacy-preserving record linkage [12] and private set intersection [13] technologies allow multiple RPs to share data without violating their clients' privacy, which pave the path for cross-organizational RP-based identity linkage.

Several solutions have been proposed to protect user privacy in SSO login [6], [7], [14], [15]. However, to the best of our knowledge, none of them provides a comprehensive

protection to defend against IdP-based login tracing and RPbased identity linkage at the same time. For example, as recommended by NIST [7] and specified in several SSO protocols [1], [16], pairwise pseudonymous identifier (PPID) is generated by the IdP to identify a user to an RP, which cannot be correlated with the user's PPID at another RP. Thus, collusive RPs cannot link a user's logins from her PPIDs. However, PPID-based approaches cannot prevent IdP-based login tracing, since the IdP needs to know which RP the user visits in order to generate the correct identify proof. On the contrary, BrowserID [14] and SPRESSO [15] were proposed to defend against IdP-based login tracing. However, both solutions are vulnerable to RP-based identity linkage. In BrowserID (and its prototypes known as Mozilla Persona [17] and Firefox Accounts [9]), the IdP does not know the identity of the requesting RP. Instead, it generates a special "identity proof" to bind the user's unique identifier (e.g., email address) to a public key, so that the user can sign a subsidiary identity proof using the private key, which binds her identity with the RP's identity, and send both identity proofs to the RP. Obviously, when a user logs in to different RPs, the RPs can extract a same user identifier from different identity proofs and correlate these logins. In SPRESSO, the RP creates a one-time pseudo-identifier in each login. The IdP generates an identity proof binding this pseudo-identifier and the user's identity (i.e., email address) and returns it through a trusted third-party entity called forwarder. Similarly, the RPs can correlate a user's logins based on her unique identifier in the identity proofs.

Unfortunately, the techniques proposed by previous research cannot be directly integrated to address the two major types of privacy risks in SSO at the same time. In fact, it requires a non-trivial redesign of the SSO system to defend against IdP-based login tracing and RP-based identity linkage while providing a secure and compatible SSO service. In this paper, we first conceptualize the privacy problem in SSO as an identifier transformation problem and explain the reasons that limit existing solutions from fully protecting user privacy against curious IdPs and collusive RPs. Based on our analysis, we propose an Unlinkable Privacy-PREserving Single Sign-On (UPPRESSO) system to provide a comprehensive protection against both types of privacy attacks.

UPPRESSO designs three one-way identifiertransformation functions based on the discrete logarithm problem. one-way trapdoor Using the function  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}(ID_{RP}, T)$ , the RP converts its identity  $ID_{RP}$  into a privacy-preserving pseudo-identifier  $PID_{RP}$ based on a randomly selected trapdoor T. Similarly, the IdP uses the one-way function  $\mathcal{F}_{ID_U \mapsto PID_U}(ID_U, PID_{RP})$ to generate a privacy-preserving pseudo-identifier  $PID_U$ for the user based on her identity  $ID_U$  and  $PID_{RP}$ . Finally, using a special identifier-transformation function  $\mathcal{F}_{PID_U \mapsto Account}(PID_U, PID_{RP}, T)$ , the RP is able to map all the different privacy-preserving pseudo-identifiers of a user, which are created in her different login sessions to that RP, to a same Account that identifies the user to the RP. The three identifier-transformation functions work cooperatively to ensure: (a) when a user logs in to an RP multiple times, the RP can always map  $PID_U$ s to a unique Account without knowing the user's identity  $ID_U$ ; moreover, when a user logs in to multiple RPs, (b) a curious IdP learns nothing about the identities of these RPs from  $PID_{RP}$ s, and (c) collusive RPs cannot link  $PID_U$ s to a particular user (d) nor correlate Accounts of a same user at different RPs. We summarize our contributions as follows.

- We are among the first to conceptualize the privacy problem in SSO as an identifier-transformation problem and analyze the strengths and limitations of existing SSO privacy protection solutions.
- We propose a comprehensive solution to hide the users' login traces from curious IdPs and collusive RPs. To the best of our knowledge, UPPRESSO is the first SSO system that secures SSO services against IdP-based login tracing and RP-based identity linkage.
- We analyze the security of UPPRESSO based on a formal model of the web infrastructure and formally prove that it provides satisfying security and privacy properties.
- We implement a prototype of UPPRESSO based on an open-source implementation of OIDC, which requires only small modifications to support three identifiertransformation functions for privacy protections. Thus, UPPRESSO is compatible with existing SSO systems. Moreover, our prototype leverages HTML 5 features in the implementation so that it can be used across platforms (e.g., PCs, smart phones and other devices).
- We compare the performance of the UPPRESSO prototype with the state-of-the-art SSO systems (i.e., OIDC [1] and SPRESSO [15]) and demonstrate its efficiency.

The rest of the paper is organized as follows. We first introduce the background and preliminaries in Section II. Then, we describe the identifier-transformation-based approach and the threat model in Sections III and IV. Section V presents the details of our UPPRESSO design, followed by a formal analysis of its security and privacy in Section ??. We explain the implementation specifics and experiment evaluation in Section VII, discuss the extensions and related works in Section VIII and IX, and conclude our work in Section X.

#### II. BACKGROUND AND PRELIMINARIES

UPPRESSO is designed to be compatible with OpenID Connect (OIDC) and provide privacy protections based on the discrete logarithm problem. Here, we provide a brief introduction about OIDC and the discrete logarithm problem.

# A. OpenID Connect (OIDC)

As an extension of OAuth 2.0 for user authentication, OIDC is one of the most popular SSO protocols [1]. As other SSO protocols [16], OIDC involves three entities, i.e., users, the identity provider (IdP), and relying parties (RPs). Both users and RPs register at the IdP with identifiers ( $ID_U$ ,  $ID_{RP}$  and  $PID_U$  in some schemes), and the necessary information such as credentials, RP endpoints (e.g., the URLs to receive identity proofs), etc. The IdP is assumed to maintain these attributes securely. In an OIDC login process, a user is responsible for initiating a login request at an RP, redirecting the SSO messages between the RP and the IdP, and checking the scope of user attributes in the identify proof generated

by the IdP for the visited RP. Usually, the redirection and checking actions are handled by a user-controlled software, known as user agent (e.g., browser). Once receiving a user login request, the RP constructs an identity proof request with its identifier and the scope of requested user attributes, sends the identity proof request to the IdP through the user, and parses the received identity proof to authenticate the user. The IdP authenticates the user based on her  $ID_U$  and credential, maps  $ID_U$  to PPID (i.e., privacy-preserving pseudo-identifier) based on the RP identity (i.e.,  $ID_{RP}$ ), generates an identity proof containing PPID,  $ID_{RP}$  and requested user attributes, and returns the identity proof to the endpoint registered by the RP.

**OIDC Implicit Flow.** OIDC supports three user login flows, which are the implicit flow, authorization code flow and hybrid flow (i.e., a mix-up of the previous two). In the implicit flow, an id token is generated as the identity proof, which contains a user identifier, an RP identifier, the issuer (i.e., IdP), the validity period, and other requested attributes. The IdP signs the id token using its private key to ensure integrity, and sends it to the RP through the user. In the authorization code flow, the IdP binds an authorization code with the RP, and sends it to the RP through the user; then, the RP establishes an HTTPS connection to the IdP and uses the authorization code with the RP's credential to obtain the user's identifier and other attributes. UPPRESSO is compatible with all three flows. For brevity, we will present our design and implementation of UPPRESSO on top of the OIDC implicit flow in details, and discuss the extension to support the authorization code flow in Section VIII.

The original OIDC implicit flow is shown in Figure 1. When a user attempts to log into an RP, the RP constructs an identity proof request and returns it to the user, which gets redirected to the IdP. The request contains  $ID_{RP}$ , the RP endpoint to receive the identity proof, and the scope of requested user attributes. If the user has not yet been authenticated, the IdP initiates an authentication process to authenticate her. For a successfully authenticated user, the IdP generates an id token and returns it to the RP endpoint. If the endpoint is not registered for that RP, the IdP will return a warning to notify the user about potential identity proof leakage. Once the RP receives the identity proof, it makes the authentication decision after verifying the identity proof.

**RP Dynamic Registration.** The RP dynamic registration [18] of OIDC allows an RP to update its information at the IdP. When an RP first registers at the IdP, it obtains a registration token, with which the RP can initiate a dynamic registration process to update its information (e.g., the endpoint). After a successful dynamic registration, the RP obtains a new unique  $ID_{RP}$  from the IdP. UPPRESSO leverages this function and slightly modify the dynamic registration process to enable  $PID_{RP}$  registration, which allows an RP to generate different privacy-preserving identifiers ( $PID_{RP}$ s) and register them at the IdP.

#### B. Discrete Logarithm Problem

Based on the discrete logarithm problem, UPPRESSO designs the identifier-transformation functions. Here, we briefly review the discrete logarithm problem. For the finite field

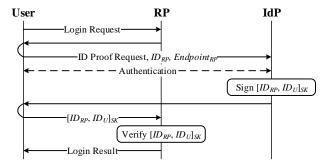


Fig. 1: The implicit flow of OIDC.

GF(p) where p is a large prime, a number g is called a generator of order q, if it constructs a cyclic group of q elements by calculating  $y = g^x \mod p$ . And x is called the discrete logarithm of y modulo p. Given a large prime p, a generator g and a number g, it is computationally infeasible to solve the discrete logarithm (i.e., g) of g [19], which is called the discrete logarithm problem. The hardness of solving discrete logarithms is utilized to design several secure cryptographic primitives, including Diffie-Hellman key exchange and the digital signature algorithm (DSA).

# III. THE PRIVACY DILEMMA AND UPPRESSO OVERVIEW

In this section, we first review the security and privacy requirements of SSO services and discuss the privacy dilemma in designing secure privacy-preserving SSO systems. Then, we provide an overview of the identifier-transformation approach of UPPRESSO. The notations used in this paper are listed in Table I.

## A. Security Requirements of SSO

The primary goal of SSO services is to implement secure user authentication [15], i.e., to ensure that a legitimate user can always log into an honest RP under her unique account. To achieve this, every identity proof generated by the IdP should explicitly specify the user who is authenticated by the IdP (i.e., user identification) and the RP which the user attempts to log into (i.e., RP designation). User identification also requires an RP to be able to recognize every authenticated user under a unique account registered at that RP in multiple logins of the user. Moreover, the identify proof should be generated by the trusted IdP and correctly transmitted to the dedicated RP and the user in some schemes (i.e., confidentiality). In this process, the identify proof should not be modified or forged (i.e., integrity). These are the basic security requirements of SSO systems summarized based on theoretical analysis of SSO designs [20]-[22] and practical attacks [23]-[40].

Many attacks exploit vulnerabilities in SSO design or implementation to break at least one of these security requirements, so that the adversaries can log into an honest RP as a victim user (called *impersonation attacks*), or allure a victim user to log into an honest RP under the attacker's account (called *identity injection attacks*). For example, Friendcaster used to accept every received identity proof (i.e., a violation of RP designation) [35], so a malicious RP could replay the

TABLE I: The notations used in UPPRESSO.

Notation	Definition	Attribute
p	A large prime.	Long-term constant
q	A large prime factor of $(p-1)$ .	Long-term constant
SK, PK	The private/public key of IdP.	Long-term constant
$ID_{RP}$	An RP's unique identity.	Long-term constant
$Cert_{RP}$	An RP certificate, containing the RP's identity	Long-term constant
	and endpoint.	
$ID_U$	A user's unique identity.	Long-term constant
Account	$A = ID_{RP}^{ID_U} \mod p$ (denoted as A in	Long-term constant
	the equations), a user's identifier at an RP.	
$PID_{RP}$	$PID_{RP} = ID_{RP}^{N_U} \mod p$ , an RP's	One-time variable
	pseudo-identifier.	
$PID_U$	$PID_U = PID_{RP}^{ID_U} \mod p$ , a user's	One-time variable
	pseudo-identifier.	
$N_U$	A user-generated nonce for $PID_{RP}$ .	One-time variable
T	$T = N_U^{-1} \mod q$ , the trapdoor to derive	One-time variable
	Account.	

identity proof received from a user for itself and log into Friendcaster as the victim user. Or, the adversaries could impersonate the victim user with a leaked identity proof (i.e., a violation of confidentiality) [24], [25], [36]–[38]. It was also reported that some RPs of Google ID SSO accepted user attributes that were not tied to the identity proof (i.e., a potential violation of integrity) [24]. As a result, an adversary could insert arbitrary attributes (e.g., an email address) into the identity proof to impersonate another user at the RP.

## B. The Privacy Dilemma in SSO Identity Proofs

As discussed in Section I, existing SSO systems are vulnerable to IdP-based login tracing or RP-based identity linkage privacy leakage. We argue that a secure and privacy-preserving SSO system should prevent *both* types of privacy leakage while satisfying *all* four basic security requirements. However, meeting the security and privacy requirements at the same time incurs a dilemma in the identity proof generation.

In an SSO login instance, the identity proof is generated by the IdP about the authenticated user and the requesting RP. First, to prevent IdP-based login tracing, the identity proof request should not disclose  $ID_{RP}$  to the IdP, since the IdP already knows  $ID_U$  after authenticating the user. However, to ensure RP designation, the IdP should bind each identify proof with a certain transitional pseudo-identifier of the RP (denoted as  $PID_{RP}$ ).  $PID_{RP}$  can be generated by the user or the RP, or together, but it should be computationally infeasible for the IdP to derive  $ID_{RP}$  from  $PID_{RP}$ .

Meanwhile, to prevent RP-based identity linkage, the identity proof should not directly contain  $ID_U$  or disclose it in any means. This requires the IdP to generate a certain transitional pseudo-identifier of the user (denoted as  $PID_U$ ) and bind it to the identity proof. However, to ensure user identification, the requesting RP should be able to recognize the user and associate  $PID_U$  to her unique account at the RP (denoted as Account). Similarly, it should be computationally infeasible for the RP to derive  $ID_U$  from  $PID_U$  or Account.

We illustrate the relationships between the identifiers, pseudo-identifiers, and the identity proof in Figure 2, where red and green blocks respectively represent long-term identities and one-time pseudo-identifiers known to each entity, and the arrows denote how the pseudo-identifiers are obtained. A

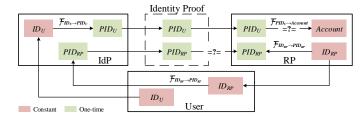


Fig. 2: Identifier transformations in privacy-preserving SSO.

dilemma exists in the SSO login process, that is, the IdP is expected to generate a  $PID_U$  for the authenticated user  $ID_U$  that can be linked to her Account at the requesting RP, without knowing any information about the requesting RP.

#### C. The Identifier-transformation Framework and UPPRESSO

As shown in Figure 2, we convert the privacy-preserving SSO login problem into an identifier-transformation problem, which aims to design three identifier-transformation functions  $\mathcal{F}_{ID_U\mapsto PID_U}$ ,  $\mathcal{F}_{ID_{RP}\mapsto PID_{RP}}$ , and  $\mathcal{F}_{PID_U\mapsto Account}$  to compute  $PID_U$ ,  $PID_{RP}$  and Account that satisfy the desired security and privacy requirements. To solve the dilemma, the key is to pass some information related to the user's Account at the RP to the IdP to assist its generation of  $PID_U$ , so that all  $PID_U$ s of the same user during her multiple logins at the same RP can be correctly linked to her Account. Meanwhile, such information should not provide any additional knowledge for the IdP to infer the RP's identity (i.e.,  $ID_{RP}$ ).

To achieve this goal, UPPRESSO constructs three transformation functions in an integrated way to support transformed RP designation and trapdoor user identification, where (i)  $PID_U$ s and  $PID_{RP}$ s are generated dynamically for different logins to protect user privacy; (ii) in each login,  $PID_{RP}$  helps to link  $PID_U$  to Account; and (iii) in a user's multiple logins to the same RP, an invariant Account can always be derived from different pairs of  $PID_U$ s and  $PID_{RP}$ s.

**Transformed RP designation.** To prevent IdP-based login tracing, the identity proof request should not include  $ID_{RP}$  but a  $PID_{RP}$  dynamically transformed from  $ID_{RP}$ . UP-PRESSO designs a novel trapdoor-based transformation function  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}(ID_{RP},T)$  to compute  $PID_{RP}$  based on  $ID_{RP}$  and a random trapdoor T that is dynamically negotiated between the user and the RP for each login. Then, the user assists the RP to register this  $PID_{RP}$  at the IdP (through OIDC dynamic registration). When an RP receives an identity proof, it can verify if the enclosed  $PID_{RP}$  is transformed from its own  $ID_{RP}$  using the trapdoor it holds.

**Trapdoor user identification.** To prevent RP-based identity linkage, we design a transformation function  $\mathcal{F}_{ID_U \mapsto PID_U}(ID_U, PID_{RP})$  for the IdP to generate  $PID_U$  and include it in the identity proof. When an RP receives an identity proof, another transformation function  $\mathcal{F}_{PID_U \mapsto Account}(PID_U, PID_{RP}, T)$  is designed to help the RP to derive the Account from  $PID_U$  and  $PID_{RP}$  using the trapdoor it holds. Intuitively, the trapdoor T plays a role in the generations of  $PID_{RP}$  and  $PID_U$ , directly or indirectly.

TABLE II: Identifier-transformation in privacy-preserving SSO.

Solution	$PID_U$	$PID_{RP}$	Account
PPID	$\mathcal{F}(ID_U, ID_{RP})$	$ID_{RP}$	$PID_U$
SPRESSO	$ID_U$	$Enc(ID_{RP} nonce)$	$ID_U$
BrowserID <sup>†</sup>	$ID_U$		$ID_U$
UPPRESSO	$\mathcal{F}(ID_U, PID_{RP})$	$\mathcal{F}(ID_{RP},T)$	$\mathcal{F}(PID_U,T)$

 $<sup>\</sup>dagger:$  BrowserID binds null  $PID_{RP}$  in the identity proofs by the IdP, but  $ID_{RP}$  is bound in the subsidiary identity proof signed by the user.

#### D. Existing Privacy-Preserving SSO Solutions

Next, we map three existing privacy-preserving SSO approaches (PPID [1], [16], BrowserID [14] and SPRESSO [15]) to the identifier-transformation framework in Figure 2 and explain their designs and potential privacy issues as shown in Table II. It is worth noting that when  $PID_U = ID_U$  and  $PID_{RP} = ID_{RP}$ , this framework depicts the basic SSO services with no privacy protection.

In PPID approaches, the IdP generates different  $PID_U$ s for a user to log into different RPs and maintains deterministic one-to-many mappings from  $ID_U$  to  $PID_U$ s. Therefore, RP-based identity linkage is prevented. At each RP,  $Account = PID_U$  ensures user identification. However, since  $ID_{RP}$  is directly used in identity proofs  $(PID_{RP} = ID_{RP})$ , they cannot defend against IdP-based login tracing.

In SPRESSO, the RP generates  $PID_{RP}$  by encrypting  $ID_{RP}$  padded with a nonce for each login session and forwards  $PID_{RP}$  to the IdP through the user. With the corresponding nonce, the RP can verify the  $PID_{RP}$  in the identity proof to ensure RP designation, while hiding  $ID_{RP}$  from the IdP to defend against IdP-based login tracing. However, the IdP uses a constant  $ID_U$  to generate identity proofs for each user regardless of which RP she requests to login to. As a result, SPRESSO is vulnerable to RP-based identity linkage, since Account always equals to  $ID_U$ .

The identity proofs in the BrowserID system include  $ID_U$  but no RP information (i.e.,  $PID_{RP} = \bot$ ), therefore, it prevents IdP-based login tracing. To ensure RP designation, BrowserID requires the user to append a *subsidiary* identity proof and sign it, where the identity proof signed by the IdP authorizes the user to sign the subsidiary identity proof. Obviously,  $ID_U$  is tied to a pair of identity proof and subsidiary identity proof and passed to the RP. Therefore,  $Account = ID_U$ , which makes BrowserID vulnerable to RP-based identity linkage.

As we can see, none of these approaches prevents IdP-based login tracing and RP-based identity linkage at the same time. This is because in each approach, three transformation functions  $\mathcal{F}_{ID_U\mapsto PID_U}$ ,  $\mathcal{F}_{ID_{RP}\mapsto PID_{RP}}$  and  $\mathcal{F}_{PID_U\mapsto Account}$  are arbitrarily designed and function separately, which causes either  $PID_{RP}=ID_{RP}$  or  $Account=ID_U$ .

# IV. THREAT MODEL AND ASSUMPTIONS

Similar as other SSO systems (e.g., SAML and OIDC), UPPRESSO consists of an IdP and multiple RPs and users. Next, we describe the threat model and some assumptions.

#### A. Threat Model

In UPPRESSO, we consider the IdP is curious-but-honest, while some users and RPs could be compromised by adversaries. Malicious users and RPs may behave arbitrarily or collude with each other, attempting to break the security and privacy guarantees for benign users.

Curious-but-honest IdP. A curious-but-honest IdP strictly follows the specifications, but may be interested in users' login activities at multiple RPs. It is assumed to be well-protected and never leaks sensitive information. For example, the IdP is trusted to maintain the private key for signing identity proofs and RP certificates (see Section V-B for details), so that the adversaries can never forge an identity proof or an RP certificate. An honest IdP should never collude with other entities (e.g., malicious RPs or users), while a curious IdP tries to break user privacy without violating the protocol. For example, it may store all the received messages to infer the relationship among  $ID_U$ ,  $ID_{RP}$ ,  $PID_U$  and  $PID_{RP}$  and trace a user's login activities.

**Malicious Users.** We assume the adversary can control a set of users, by stealing users' credentials [41], [42] or directly registering sybil accounts at the IdP and RPs, to break the security of UPPRESSO. They may impersonate a benign user at honest RPs, or trick a victim user to log into an honest RP under the account of a malicious user. For example, the malicious users may modify, insert, drop or replay a message, or deviate arbitrarily from the specifications when processing  $ID_{RP}$ ,  $PID_{RP}$  and identity proofs.

**Malicious RPs.** The adversary could also control a set of RPs by directly registering at the IdP as an RP or exploiting software vulnerabilities to compromise some RPs. The malicious RPs may behave arbitrarily to break security and privacy guarantees. For example, a malicious RP may manipulate its  $PID_{RP}$  and trick the users to submit identity proofs for other honest RPs to itself and reply them, or it may manipulate its  $PID_{RP}$  to affect the generation of  $PID_U$  and analyze the relationship between  $PID_U$  and Account.

Collusive Users and RPs. Malicious users and RPs may collude together, attempting to break the security and privacy guarantees. For example, the adversary may firstly acts the RP and allures the honest user to upload her identity proof. Then this adversary may attempt to log in to other honest RPs with this identity proof as the honest user.

# B. Assumptions

We assume the user agent deployed at honest users is correctly implemented and transmits messages to the dedicated receivers as expected. We also assume the IdP and benign RPs and users adopt TLS to ensure confidentiality and integrity in the communications. Meanwhile, the cryptographic algorithms (such as RSA and SHA-256) and building blocks (such as random number generators and the discrete logarithm problem) used in UPPRESSO are assumed to be correctly implemented.

As we consider IdP is always honest, therefore, all the parameters provided by the IdP are assumed to be honest. All the calculations and verifications conducted by IdP are

correct. Meanwhile, the collusion between RPs and IdP is not considered in this paper.

In UPPRESSO, we study the RP-based identity linkage caused by a same user identifier used across different RPs. In this paper, we consider the user attributes hold by IdP can be separated as distinctive and indistinctive message, which is labelled based on whether it can be only associated with specific user. While the RPs may be able to re-identify a user from some distinctive user attributes, such as telephone numbers, addresses, or driver licenses, we consider it out of the scope of UPPRESSO. However, other attributes, such as nickname, birthday and sex can be provided to RPs with the explicit consent form user. Also, we focus on IdP-based login tracing attacks that are enabled by SSO protocols, but do not consider other network attacks such as traffic analysis that trace a user's logins at different RPs.

#### V. THE DESIGN OF UPPRESSO

Next, we present the main design of UPPRESSO. First, we describe our design for the three identifier-transformation functions and the details of the transformed RP designation and trapdoor user identification schemes. Then, we provide an overview of the UPPRESSO system and its login flow. Finally, we discuss the compatibility of UPPRESSO with OIDC.

## A. Identifier-transformation Functions in UPPRESSO

As discussed in Section III, the identifier-transformation functions are essential for privacy-preserving SSO systems. In UPPRESSO, the three functions,  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$ ,  $\mathcal{F}_{ID_{U} \mapsto PID_{U}}$  and  $\mathcal{F}_{PID_{U} \mapsto Account}$ , are all constructed based on the discrete logarithm problem with public parameters p, q, where p is a large prime defining the finite field GF(p), and q is a prime factor of (p-1).

Without loss of generality, we assume the IdP assigns long-term identifiers  $ID_U$  to a user and  $ID_{RP}$  to an RP when they first register at the IdP. In particular, the IdP assigns a unique random number to each user as  $ID_U$ , where  $1 < ID_U < q$ , and  $ID_{RP}$  is a generator of order q in GF(p).

**RP Identifier Transformation.** In each login session, the user negotiates with the RP she tries to log in, and computes a pseudo-identifier  $PID_{RP}$  for the RP cooperatively. The user chooses a random number  $N_{RP}$  ( $1 < N_{RP} < q$ ), and RP provides the  $ID_{RP}$  for user to calculate  $PID_{RP}$  following Equation 1.

$$\mathcal{F}_{ID_{RP} \mapsto PID_{RP}} : PID_{RP} = ID_{RP}^{N_U} \bmod p \qquad (1)$$

The transformation function  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$  satisfies the following requirements. First, it is computationally infeasible for the IdP to derive  $ID_{RP}$  from  $PID_{RP}$  due to the discrete logarithm problem. Moreover, the nonce  $N_U$  ensures that: (a)  $PID_{RP}$  is valid only for this login and for the identity proof generated in this login, and (b)  $PID_{RP}$  is dynamically generated for this login and is different from other  $PID_{RP}$ s generated in other login session between the same user and RP. Therefore, the IdP cannot associate multiple  $PID_{RP}$ s of a same RP.

**User Identifier Transformation.** When the IdP receives an identity proof request for  $ID_U$  and  $PID_{RP}$  from an authenticated user, it follows the transformation function in Equation 2 to calculate  $PID_U$  and includes it in the identity proof.

$$\mathcal{F}_{ID_U \mapsto PID_U} : PID_U = PID_{RP}^{ID_U} \mod p$$
 (2)

**User Account Transformation.** The RP can derive a unique *Account* for each user following Equation 3.

$$\mathcal{F}_{PID_U \mapsto Account} : A = PID_U^T \bmod p \tag{3}$$

Here, we define  $T=N_U^{-1} \bmod q$  as the RP's trapdoor. As q is a prime number and  $1 < N_U < q$ , q is coprime to  $N_U$ . Also, there always exists a T that satisfies  $TN_U=1 \bmod q$ . Moreover, from Equations 1, 2 and 3, we have  $A=ID_{RP}^{ID_U} \bmod p$ , derived as below.

$$A = PID_{U}^{T} = (PID_{RP}^{ID_{U}})^{N_{U}^{-1} \bmod q}$$

$$= ID_{RP}^{ID_{U}N_{U}N_{U}^{-1} \bmod q} = ID_{RP}^{ID_{U}} \bmod p \quad (4)$$

Therefore, when a user logins at an RP multiple times, the RP can always derives the same Account to identity the user. Finally, the transformation function  $\mathcal{F}_{PID_U \mapsto Account}$  satisfies the following requirements: (a) due to the discrete logarithm problem, the RP cannot derive  $ID_U$  from Account, and (b) collusive RPs cannot link a user's Accounts at different RPs.

These three identifier-transformation functions enable transformed RP designation and trapdoor user identification to satisfy all the security and privacy requirements of an SSO.

**Transformed RP Designation.**  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$  ensures that the user and RP cooperatively generate a fresh  $PID_{RP}$  in each login, while  $\mathcal{F}_{ID_U \mapsto PID_U}$  ensures that the IdP generates the exact  $PID_U$  for the  $ID_U$  who logins at  $PID_{RP}$ . The IdP will bind  $PID_U$  with  $PID_{RP}$  in the identity proof, which designates this identity proof to  $PID_{RP}$ . Finally, the transformed RP designation is provided through two phases. The function  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$  prevents the curious IdP from linking  $PID_{RP}$ s of different logins at an RP, and therefore avoids IdP-based login tracing.

**Trapdoor User Identification.** In a user's multiple logins, the RP expresses different  $PID_U$ s and has the corresponding Ts, so that derives the identical Account. The comprehensive design of identifier-transformation functions prevents collusive RPs from linking a user's  $PID_U$ s and Accounts at different RPs, and therefore prevents RP-based identity linkage.

## B. UPPRESSO Overview

The UPPRESSO system has four procedures, namely system initialization, RP initial registration, user registration, and SSO login.

**System Initialization.** System initialization is conducted once by the IdP to establish the entire system. In particular, the IdP generates a large prime p, and a prime factor q of p-1 as

the parameters of the discrete logarithm problem. The IdP also generates one key pair (SK, PK) to sign identity proofs and RP certificates. The lengths of p, q and (SK, PK) should satisfy the required security strength. Then, the IdP keeps SK secret, while announcing p, q and PK are public parameters.

**RP Initial Registration.** RP initial registration is launched by each RP to obtain the necessary configurations from the IdP, including a unique identifier  $ID_{RP}$  and its corresponding RP certificate  $Cert_{RP}$ . Each RP launches this procedure only once. In particular, an RP registers itself at the IdP and requests  $ID_{RP}$  and  $Cert_{RP}$  as follows:

- The RP sends a registration request to the IdP, including the RP endpoint (e.g., URL) to receive identity proofs.
- The IdP generates the unique generator  $ID_{RP}$ , signs  $[ID_{RP}, Endpoint_{RP}, *]$  using SK, where \* denotes the supplementary information such as the RP's common name, and returns  $Cert_{RP} = [ID_{RP}, Endpoint_{RP}, *]_{SK}$  to the RP, where  $[\cdot]_{SK}$  means the message is signed using SK.
- The RP verifies Cert<sub>RP</sub> using PK and accepts ID<sub>RP</sub> and Cert<sub>RP</sub> if they are valid.

Note that,  $ID_{RP}$  cannot be chosen by the RP. It must be generated by the IdP.

**User registration.** UPPRESSO takes the same user registration process as other SSO systems to set up a unique user identifier  $ID_U$  and the corresponding user credential. User registration is launched only once by each user.  $ID_U$  can be chosen by either the user or the IdP, as long as it is unique for each user.

**SSO Login.** Finally, an SSO login procedure will be launched when a user attempts to log into an RP. It is designed on top of the identifier-transformation functions. As shown in Figure 3, the SSO login consists of five phases, namely, scripts downloading, RP identifier transformation,  $PID_{RP}$ registration, identity proof generation and Account calculation. At the scripts downloading phase, browser firstly downloads the scripts from RP and IdP server. In RP identifier transformation, the user and the RP negotiate  $PID_{RP}$  =  $ID_{RP}^{N_U} \mod p$ . Next, the user registers  $PID_{RP}$  at the IdP. It is worth noting that this step has to be conducted by the user but not the RP. Otherwise, the IdP can associate  $PID_{RP}$  and  $ID_{RP}$ . To register  $PID_{RP}$ , the user needs to create a new endpoint and submit it with  $PID_{RP}$  to the IdP. Then, the RP requests the identity proof, and the IdP calculates  $PID_U = PID_{RP}^{ID_U} \mod p$  and signs the identity proof. Finally, in Account calculation, the RP derives  $A = PID_U^{(N_U)^{-1} \mod q} \mod p$  after verifying the identity proof and allows the user to log in under Account.

Moreover, as the IdP is unaware of the visited RP and also the RP's endpoint to receive the identity proof, this endpoint shall be queried by the user from the trusted IdP indirectly to ensure confidentiality; otherwise, an incorrect endpoint leaks the identity proofs. In UPPRESSO this is implemented as an RP certificate signed by the IdP, which is composed of  $ID_{RP}$ , the RP's endpoint and other supplementary information. Then,

the user determines the correct endpoint by itself, while in commonly-used OIDC systems, the endpoint is configured by the IdP.

#### C. SSO Login Flow of UPPRESSO

We illustrate the steps of the SSO login protocol of UPPRESSO in Figure 3, and describe the detailed processes as follows.

**Scripts Downloading.** At the beginning, the user downloads the scripts from RP server and IdP server as follows:

- 1.1 The user visits the RP's script site and downloads the script.
- 1.2 The script opens a new window in the browser visiting the login path at RP server.
- 1.3 The visit to RP's login path is redirected to IdP's script.
- 1.4 The new window visits the IdP's script site and downloads the script.

**RP Identifier Transformation.** In this phase, the user and the RP cooperate to generate  $PID_{RP}$  as follows:

- 2.1 The IdP script chooses a random number  $N_U$  (1 <  $N_U < q$ ) and sends it to RP script through postMessage, then RP script sends  $N_U$  to RP server.
- 2.2 The RP verifies  $N_U \neq 0 \mod q$ , calculates  $PID_{RP}$  with  $N_U$ , derives the trapdoor  $T = (N_U N_{RP})^{-1} \mod q$ ; and acknowledges the negotiation by responding with  $Cert_{RP}$ . The  $Cert_{RP}$  is transmitted from RP script to IdP script through postMessage.
- 2.3 The IdP script verifies  $Cert_{RP}$ , extracts  $ID_{RP}$  from the valid  $Cert_{RP}$ , calculate  $PID_{RP} = ID_{RP}^{N_U} \mod p$ , creates a one-time endpoint to hide the RP's endpoint from the IdP and calculates  $Nonce = Hash(N_U)$ .

The user halts the negotiation, if  $Cert_{RP}$  is invalid.

 $PID_{RP}$  Registration. The user registers  $PID_{RP}$  at the IdP.

- 3.1 The IdP script sends the  $PID_{RP}$  registration request  $[PID_{RP}, Hash(N_U), Endpoint_U]$  to the IdP.
- 3.2 The IdP verifies that  $PID_{RP}$  is unique among unexpired  $PID_{RP}$ s, and then signs the response  $[PID_{RP}, Hash(N_U), Validity]_{SK}$ , where Validity is the validity period.
- 3.3 The IdP script forwards the registration result to the RP server through RP script.
- 3.4 The RP verifies the IdP's signature, and accepts it only if  $PID_{RP}$  and  $Hash(N_U)$  match those in the negotiation and it is in the validity period.

 $Hash(N_U)$  is attached as the nonce to avoid the registration result is accepted by two or more RPs, which have different  $ID_{RP}$ s but generate a same  $PID_{RP}$ . The IdP ensures  $PID_{RP}$  is unique among unexpired ones; otherwise, one

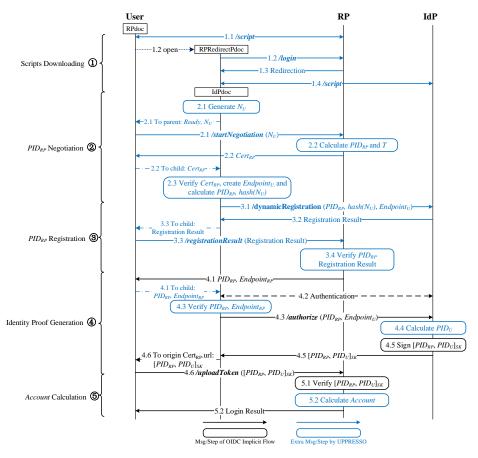


Fig. 3: The flow of a user login in UPPRESSO.

identity proof for one  $PID_{RP}$  might be accepted by other RPs. More details are analyzed in Section ??.

**ID Proof Generation.** In this phase, the user login continues and the IdP signs the identity proof.

- 4.1 The RP uses  $PID_{RP}$  and  $Endpoint_{RP}$  to construct an identity proof request for a set of user's attributes, and the request is forwarded to IdP script through RP script.
- 4.2 The IdP authenticates the user if she has not been authenticated yet.
- 4.3 The user first confirms the scope of the requested attributes. IdP script verifies the  $PID_{RP}$  with the negotiated one and  $Endpoint_{RP} \in Cert_{RP}$ , replaces the endpoint with the registered one-time  $Endpoint_U$  and then sends the modified identity proof request to the IdP server.
- 4.4 The IdP verifies whether  $PID_{RP}$  and  $Endpoint_U$  have been registered and unexpired, and calculates  $PID_U = PID_{RP}^{\ \ ID_U} \mod p$  for the authenticated user.
- 4.5 The IdP constructs and signs the identity proof  $[PID_{RP}, PID_U, Iss, ValTime, Attr]_{SK}$ , where Iss is the identifier of the IdP, ValTime is the validity period, Attr contains the requested attributes.

4.6 Then, the IdP sends the identity proof to the one-time endpoint at the user. The IdP script forwards the identity proof to RP script with the origin  $Endpoint_{RP}$  and RP script sends it to the server.

The user halts the process if  $PID_{RP}$  in the identity proof request is inconsistent with the negotiated one. The IdP rejects the identity proof request, if the pair of  $PID_{RP}$  and  $Endpoint_U$  has not been registered.

**Account calculation.** Finally, RP derives the user's *Account* and completes the user login as follows.

- 5.1 The RP verifies the identity proof, including the signature, validity period, and the consistency between  $PID_{RP}$  and the negotiated one. If any fails, the RP rejects this login.
- 5.2 The RP extracts  $PID_U$ , calculates  $Accout = PID_U^T \mod p$ , and allows the user to log in.

# D. Compatibility with OIDC

As described above, the SSO login protocol of UPPRESSO follows a same logic flow of OIDC login protocol with small modifications to transform the identifiers. Next, we will discuss these necessary modifications and demonstrate its compatibility with OIDC. This indicates that it can be easily integrated with other commonly adopted SSO systems.

First, UPPRESSO does not introduce any new role nor change the security assumptions for each role. Moreover, among the five phases of its SSO login flow, only the scripts downloading and RP identifier transformation phase are newly introduced by UPPRESSO, while the other three ( $PID_{RP}$  registration, identity proof generation and Account calculation) adopt similar communication pattern as OIDC flows.

In particular, the  $PID_{RP}$  registration phase can be viewed as a variant of the RP dynamic registration flow of OIDC [18], where an entity registers its identity and endpoint at the IdP. The RP endpoint is the required parameter for dynamic registration, therefore, here we add the  $Endpoint_U$  to meet the requirement of registration process. Different from OIDC, in UPPRESSO, this process can be launched by any authenticated user who obtains an RP identifier, the registration response includes a signature by the IdP, and the registration will become invalid after a validity period. However, these changes only require small modifications to the RP dynamic registration flow of OIDC.

The identity proof generation and Account calculation phases adopt the same steps and functions as the implicit protocol flow of OIDC but calling a few different parameters. First, in identity proof generation,  $PID_U$  transformed from  $ID_U$  is used to replace  $ID_U$ , which is directly supported by OIDC, similar as in PPID approaches that also convert  $ID_U$  into  $PID_U$ . The calculation of Account from  $PID_U$  can be viewed as a customized step by the RP to derive its user account after the implicit protocol flow of OIDC ends. So,the identity proof generation and Account calculation phases of UPPRESSO can be viewed as a particular but compatible implementation of the implicit protocol flow of OIDC.

It is worth noting that the identity proof generation and *Account* calculation phases of UPPRESSO can be also implemented as the authorization code flow of OIDC with small modifications, which will be discussed in Section VIII.

#### VI. WEB MODEL

Our formal analysis of UPPRESSO is based on the Dolev-Yao style web model [15], which has been widely used in formal analysis of SSO protocol, e.g., OAuth 2.0 [21] and OIDC [22]. To make the description cleaner, we foucus on our modification on OIDC, and assume DNS and HTTPS are secure, which has already been analyzed in [15].

The main entities in the model are atomic processes, which represent the essential nodes in the web systems, such as browsers, web servers and attackers. The atomic processes communicate with each other through the events containing the receiver atomic process's address (IP), the sender atomic process process's address (IP) and the transmitted message. Moreover, there are also dependent scripting processes which runs on the client-side environment relying on the browsers such as JavaScript. The scripting provides the server defined function to the browser. The web system mainly consists of the set of atomic processes and scripting processes. The operation of a system is described as that the system converts its states via step of runs. The state of web system is called configuraton which consists of all the states of the atomic processes in the system and all the event can be accepted by the processes.

#### A. Communication Description

Here we give a brief presentation of generic Dolev-Yaostyle communication model proposed by [15] on which our web model is based.

A  $signature\Sigma$  consists of a finite set of function symbols, such as encrypt, decrypt, and pair, each with an arity. A function symbol with arity 0 (with no arguments) is a constant symbol. The set of terms is defined over a signature  $\Sigma$ , an infinite set of names, and an infinite set of variables.

**Messages** are defined as formal terms without variables (called ground terms). The signature  $\Sigma$  for the messages in the model is considered containing constants (such as ASCII strings and nonce), sequence symbols (such as n-ary sequences  $\langle \rangle, \langle . \rangle, \langle . , . \rangle$  etc.) and further function symbols (such as encryption/decryption and digital signatures). An HTTP request is a common message in the web model, containing a type HTTPReq, a nonce n, a method GET or POST, a domain , a path, URL parameters, request headers, and the body over the  $\Sigma$  in the sequence symbol formate. Here is an example for an HTTP GET request for the domain exa.com/path?para = 1 with the headers and body empty.

$$m := \langle \mathtt{HTTPReq}, n, \mathtt{GET}, exa.com, /path, \langle \langle para, 1 \rangle \rangle, \langle \rangle, \langle \rangle \rangle$$

**Events** are the basic communication elements in the model. An event is the term in the formate  $\langle a, f, m \rangle$ , where the a and f represent the address of sender and receiver, and m is the message transmitted.

**Atomic Processes**. An atomic Dolev-Yao(DY) process is constructed as the tuple  $p=(I^p,Z^p,R^p,s_0^p)$  representing the single node in the web model, such as the server and browser.  $I^p$  is the set of addresses a process listens to, and  $Z^p$  is the set of states (terms) which describes the process.  $R^p$  is the mapping between the pairs  $\langle s,e\rangle$  and  $\langle s',e'\rangle$  where  $s,s'\in Z^p$  It's worth noting that for one process in a state only a finite set of events can be accepted by the process as the state and event are defined as the input of  $R^p$ .

**Scripting Processes.** The web model also contains the scripting process representing the client-side script loaded by browser such as JavaScript code. However, the  $scripting\ process$  must rely on an  $atom\ process$  such as browser and provide the relation R witch is called by this  $atomic\ process$ .

**Equational theory** is defined as usual in Dolev-Yao models which introduces the symbol  $\equiv$  representing the congruence relation on terms. For instance,  $dec(enc(m, k), k) \equiv m$ 

## B. Web System

The web system contains a set of processes (including atomic processes and scripting processes) and represents the web infrastructure. A web system is defined as a tuple  $(\mathcal{W}, \mathcal{S}, \mathtt{script}, E^0)$ .  $\mathcal{W}$  is the set of atomic processes containing honest processes and malicious processes,  $\mathcal{S}$  is the set of scripting processes including honest scripts and malicious scripts, script is the set of concrete script code related with specific scripting process in  $\mathcal{S}$ , and  $E^0$  is the set of events which could be accepted by the processes in  $\mathcal{W}$ .

**Configuration**. We firstly define the set of states S of a system, consists of all the current states of processes in  $\mathcal{W}$ . And the set of events E, for each event  $e \in E$ , there is always a state  $s \in S$ , e and s can be accepted by one of the processes as the input. A configuration of the system is defined as the tuple (S, E, N) where N is the mentioned sequence of unused nonces.

**Run Steps**. A run step is the system migrating from the configuration (S, E, N) to (S', E', N') by processing an event  $e \in E$ .

# C. Model Of UPPRESSO

The UPPRESSO model is a web system which is defined as

$$\mathcal{UWS} = (\mathcal{W}, \mathcal{S}, \mathtt{script}, E^0),$$

 ${\cal W}$  is the finite set of atom processes in UPPRESSO system including a single IdP server process, multiple honest RP server processes , the browsers representing the users, and the attacker processes. We assume that all the honest RPs are implemented following the same rule so that the process are considered consistent besides of the addresses they listen to. The browsers controlled by user are considered honest. That is, the browser controlled by attackers can behave as an independent atomic process.  ${\cal S}$  is the finite set of scripting processes consists of  $script\_rp$ ,  $script\_idp$  and  $script\_attacker$ . The  $script\_rp$  and  $script\_idp$  are downloaded from honest RP and IdP processes and the  $script\_attacker$  is downloaded from attacker process considered existing in all browser processes.

We now give a brief description about UPPRESSO model.

- The browser is responsible to send HTTP request, receive HTTP response, handle user behaviour and transmit message between scripting process. As the browser is honest, we only focus on the scripting process running on the browser. The detailed model of browser is shown in [15]
- IdP server process (defined as  $p^i$ ) only accepts the events whose messages are HTTP request and the  $path \in /script$ , /dynamicRegistration, /login, /loginInfo, /authorize. The function of each path is shown in Section V. All the events are accepted by  $p^i$  in any state but the output may be different. The detailed  $R^i$  is shown in \*.
- RP server process (defined as  $p^r$ ) only accepts the events whose messages are HTTP request and the  $path \in \{ \ / script, \ / login, \ / startNegotiation, \ / registrationResult, \ / uploadToken \}$ . The function of each path is shown in Section V. The event with  $path \in \{ \ / script, \ / login, \ / startNegotiation \}$  are accepted in any state. However, the event with  $path \equiv / registrationResult$  is accepted only when the state s is the output for event  $path \equiv / startNegotiation$ . In the same way the following accepted events must be arranged as path in the sequence  $/ registrationResult, \ / uploadToken$ .
- IdP and RP scripting process accepts the events in the formate as HTTP response and postMessage. The details about accepted events are shown in ??.

# D. Security Of UPPRESSO

As we assume that the HTTP requests and responses are well protected by TLS, and the postMeassage are securely implemented in browser, therefore, web attackers are not considered. In this section, we are going to prove the following theorem.

**Theorem 1.** Let UWS be a UPPRESSO web system, then UWS is secure.

Firstly, an SSO system is considered secure **iff** only the legitimate user can always log into an honest RP under her unique account. Based on the model of UPPRESSO, we found that an attacker can visit an honest RP as the honest user only when the attacker own the cookie which is bound to the honest user by RP. Therefore, the definition of a secure UPPRESSO system is,

**Definition 1.** Let  $\mathcal{UWS}$  be a UPPRESSO web system,  $\mathcal{UWS}$  is secure **iff** for any honest RP  $r \in \mathcal{W}$  and the authenticated cookie c for honest u, c is unknown to the attacker a.

Therefore, to prove theorem  $\, 1$ , we are going to prove that an authenticate cookie  $\, c$  is unknown to attacker  $\, a$ . The proof can be separated as two parts, initially  $\, a$  does not know any authenticated cookie, and the following requirements must be met.

- If c is the authenticated cookie owned by u, c cannot be obtained by a.
- If c is an unauthenticated cookie owned by a, c cannot be authenticated by r for u.

**Proof Outline.** Here we introduce the lemmas briefly to prove that  $\mathcal{UWS}$  follows the requirements by Definition 1 so that  $\mathcal{UWS}$  is secure. And the detailed proofs to these lemmas are in 2?

**Lemma 1.** The cookie owned by honest user will not be leaked to any attacker.

*Proof:* That is, due to the Same-Origin policy, the honest browser will not leak the cookies to any attacker. And based on the UPPRESSO model, it is to prove that RP server and RP script will not send any cookies to other processes either. Therefore, the attackers cannot obtain the *u*'s authenticated cookie.

Based on the model of UPPRESSO about RP server process, the procedure of the cookie being authenticated is described as follows.

**Definition 2.** In UWS, the cookie c is to be set authenticated for user u only when RP r receives a valid u's identity proof from the owner of c.

Then we are going to prove that  $\mathcal{UWS}$  follows the requirements that the cookie of the attacker cannot be set authenticated.

Here we propose the lemmas

**Lemma 2.** Attackers cannot obtain the user u's password in  $\mathcal{UWS}$ .

**Lemma 3.** Attackers cannot forge the IdP issued proofs in  $\mathcal{UWS}$ .

*Proof:* Lemma 2 can be easily proved because the password is only sent by honest IdP scripting process to IdP server. Lemma 3 is proved as the IdP issued proofs are well signed and verified. Therefore, the following lemma can be proved base on Lemma 2 and Lemma 3.

**Lemma 4.** Attackers cannot obtain the u's valid identity proof in UWS.

*Proof:* We now give a brief proof about Lemma 4. As the attacker attempts to obtain a valid identity proof, he must receive the proof from one of following processes, IdP server process, RP server process, IdP scripting process and RP scripting process. That is, according to the model we find the honest RP scripting process only send identity proof to honest RP server and RP server will not send the proof to any process. It can be proved that only the process who holds u's password can obtain the u's identity proof from IdP server. As the attacker does not know u's password so that he cannot obtain the identity proof from IdP server. To prove that attacker cannot obtain the identity from IdP scripting process is a little complicated so that we here only give a straightforward conclusion. That is when the honest user u sends the identity proof from the IdP scripting process, the receiver is restricted by the RP Certification  $cert_r$ . And the identity proof is valid in honest RP r only if the  $cert_r$  belongs to r (the full proof is in ??).

Therefore, UWS satisfies the requirements in Definition ??, such that Theorem 1 is proved.

# E. Privacy Of UPPRESSO

Firstly we introduce the definition in [15] about static equivalence.

**Definition 3.** Two messages  $t_1$  and  $t_2$  are statically equivalent, written  $t_1 \approx t_2$ , if and only if, for all terms such as M(x) and N(x) which only contain one variable x without nonces, it is true that  $M(t_1) \equiv N(t_1)$  **iff**  $M(t_2) \equiv N(t_2)$ . For instance, there are the messages m and m', symmetric key k, such that  $enc(m,k) \approx enc(m',k)$  is always true to the attackers without the k.

Here we give the new definitions

**Definition 4.** For a large prime p (2048-bit length) and p-1's prime factor q (256-bit length), there are two constants  $g_1$ ,  $g_2$  as the generators of p and the constants  $n_1$ ,  $n_2$  ( $n_1$ ,  $n_2$  < q). We define the function symbol  $modpow(a,b,p) = a^b \mod p$ , there are  $modpow(g_1,n_1,p) \approx modpow(g_2,n_2,p)$  and  $modpow(g_1,n_1,p) \approx modpow(g_1,n_2,p)$  always true due to the discrete logarithm problem as the  $n_1$  and  $n_2$  are unknown.

**Definition 5. Equivalence of HTTP requests**. There are messages  $m_1$  and  $m_2$ , we say that  $m_1 \approx m_2$  iff the following conditions are met,

• If  $m_1$  and  $m_2$  are HTTPs requests, they are equivalent to the observers besides of the receiver.

- If  $m_1$  and  $m_2$  are HTTPs requests, they are equivalent for the receiver **iff** the value of the Host,Path,Origin and Referer headers in both requests are same, as well as the value of the Parameters and Body are statically equivalent.
- If m<sub>1</sub> and m<sub>2</sub> are HTTP requests, they are equivalent to all the observers as the equivalent HTTPS requests to receivers.

**Definition 6. Equivalence of events.** There are events  $e_1 := \langle a_1, f_1, m_1 \rangle$  and  $e_2 := \langle a_2, f_2, m_2 \rangle$ , we say that  $e_1 \approx e_2$  iff

- $a_1 \equiv a_2$  or  $a_1$  and  $a_2$  belong to random addresses.
- $f_1 \equiv f_2$  or  $f_1$  and  $f_2$  belong to random addresses.
- $m_1$  and  $m_2$  are equivalent.

Then we are going to prove the following theorem

**Theorem 2.** Let UWS be a UPPRESSO web system, then UWS is IdP-Privacy and RP-Privacy.

The definitions about IdP-Privacy and RP-Privacy are designed as follows.

**Definition 7. IdP-Privacy** Let  $\mathcal{UWS}$  be a UPPRESSO web system, there are honest RPs  $r_1, r_2 \in \mathcal{W}$ , IdP  $i \in \mathcal{W}$  and the honest user u, then  $\mathcal{UWS}$  is IdP-Privacy **iff** for every event  $e_1$  received by i during the u logging in to  $r_1$ , there is always an event  $e_2$  for the u logging in to  $r_2$ , and  $e_1$  and  $e_2$  are equivalent.

*Proof:* Here we only give a brief proof that  $\mathcal{UWS}$  meets the conditions defined in Definition 7. Firstly, it is assumed that the HTTPs transmissions well implemented such that all the events to IdP are regarded as equivalent to web attackers. As we consider IdP server is honest but curious, i can only hold the events to IdP server process and does not attempt to steal parameters from other processes or set any illegal parameters in the system.

Here we only focus on the same user's multiple requests to the IdP. IdP server only accepts the events whose messages are HTTP request and the  $path \in /script$ , /dynamicRegistration, /login, /loginInfo, /authorize. All the path will be visited in each login procedure. It can be easily found that the visits to /script and /loginInfo carrying no parameters and bodies so that the events must be equivalent. The visits to /login only carry u's username and password so that the events are equivalent. Moreover, the visits to /dynamicRegistration and /authorize carry the  $PID_{RP}$ s and endpoints where  $PID_{RP}$ s are statically equivalent because of Definition 4 and endpoints are unrelated random constants . Therefore,  $\mathcal{UWS}$  meets the conditions defined in Definition 1, so that theorem 1 is proved.

**Definition 8. RP-Privacy** Let  $\mathcal{UWS}$  be a UPPRESSO web system, there are honest RPs  $r_1, r_2 \in \mathcal{W}$  and the honest users  $u_1$  and  $u_2$ , then  $\mathcal{UWS}$  is RP-Privacy **iff** event through  $r_1$  and  $r_2$  share their states

• for every event  $e_1$  received by  $r_2$  during the  $u_1$  logging in to  $r_2$ , there is always an event  $e_2$  for the  $u_2$  logging in to  $r_2$ , and  $e_1$  and  $e_2$  are equivalent to  $r_1$ .

 for every events received by r<sub>2</sub>, the event cannot be straightforward linked to the existing user's attributes at r<sub>1</sub>.

RP server process only accepts the events whose messages are HTTP request and the  $path \in \{ /script, /login, /startNegotiation, /registrationResult, /uploadToken \}.$  As the RPs may behave malicious so that the events received by RP scripting process should also be considered. However, all of the messages received by RP scripting process are transmitted to RP server. Therefore, we only need to focus on the events received by RP server.

Firstly, we assume that all the parameters are set legally. We give the brief proof. The events visiting to /script and /login carry no parameters and bodies so that the events must be equivalent. The visits to /startNegotiation only carry the nonce so that the events are equivalent. The visits to /registrationResult carry the IdP signed registration result, however, the contents in the result contains the  $PID_{RP}$ ,  $N_U$ and endpint. The contents are all random constants ( $PID_{RP}$ is regarded as same as  $N_U$ ) so that the events are equivalent. The visits to /uploadToken includes the identity proof containing the  $PID_{RP}$ ,  $PID_U$ . According to Definition 4, the  $PID_U$ s are statically equivalent to  $r_1$ . Moreover, with the  $r_2$  shared state,  $Account_{r_1}$ s are known to  $r_1$ . However,  $r_1$  is unable to transform  $Account_{r_1}$ s into the users' account  $Account_{r_2}$  at  $r_2$  so that the events cannot be linked to the existing user. Therefore, the requirements of Definition 8 are met.

However, as the RPs are considered maybe malicious, such that they will attempt to steal the data from other process or set the malicious parameters during the login procedure. That is, according to Definition 4, the  $PID_U$  the Accounts must be equivalent to the attacker as long as the attacker does not know the  $ID_U$ . Therefore the attacker may attempt to steal the  $ID_U$  from UPPRESSO system. But it is easy to be found that IdP will not send the plain  $ID_U$  to any process so that RPs cannot obtain the  $ID_U$ . Another way is that RPs may attempt to treat the Account or  $PID_U$  to be generated insecurely, but we are going to prove it is impossible.

- RP may lead the login using the forged  $ID_{RP}$  or  $PID_{RP}$  so that  $PID_{U}$ s and Accounts are no more equivalent. However,  $ID_{RP}$  are provided by the Cert, protected by the IdP's signature and verified by IdP script.  $PID_{RP}$  is generated by the  $ID_{RP}$  and the honest user generated nonce. Therefore, it is impossible to lead the honest user to use the illegal  $ID_{RP}$  and  $PID_{RP}$ .
- RP may also lead the same user to upload the identity proof with same  $PID_U$  or Account so that the system is not RP-Privacy according to Definition 8. However, the  $PID_U$  is generated with the user's nonce  $N_U$  so that it is not controlled by the RP. Account is generated as the form  $ID_{RP}^{ID_U} \mod p$ , while RPs may lead the user to use the same  $ID_{RP}$  to generate identity proof. However, the  $ID_{RP}$  is bound with Cert which is verified by the user and it is easy for user to find out the login RP does not coincide the RP name shown on her browser.

Therefore, we consider that W meet all the requests defined in Definition 8 so that theorem 2 is proved.

# VII. IMPLEMENTATION AND PERFORMANCE EVALUATION

We have implemented the UPPRESSO prototype, and evaluated its performance by comparing with the original OIDC which only prevents RP-based identity linkage, and SPRESSO which only prevents IdP-based login tracing.

# A. Implementation

We adopt SHA-256 for digest generation, and RSA-2048 for signature generation. We randomly choose a 2048-bit prime as p, a 256-bit prime as q, and the q-order generators as  $ID_{RP}$ .  $N_U$  and  $ID_U$  are 256-bit random numbers. Then, the discrete logarithm problem provides equivalent security strength (i.e., 112 bits) as RSA-2048 [43]. UPPRESSO includes the processing at the IdP, users and the RPs. The implementations at each entity are as follows.

The implementation of the IdP only needs small modifications on the existing OIDC implementation. The UPPRESSO IdP is implemented based on MITREid Connect [44], an open-source OIDC Java implementation certificated by the OpenID Foundation [45]. We add 3 lines of Java code to calculate  $PID_U$ , about 20 lines to change the way identity proof responded, about 50 lines to the function of dynamic registration to support  $PID_{RP}$  registration, i.e., checking  $PID_{RP}$  and adding a signature and validity period in the response. The calculations of  $ID_{RP}$ ,  $PID_U$  and RSA signature are implemented based on Java built-in cryptographic libraries (e.g., BigInteger).

The user-side processing is implemented as a JavaScript code provided by IdP and RP server, respectively containing about 200 lines and 150 lines of codes, to provide the functions in Steps 2.1, 2.3 and 4.3. The cryptographic computations, e.g.,  $Cert_{RP}$  verification and  $PID_{RP}$  negotiation, are implemented based on jsrsasign [46], an efficient JavaScript cryptographic library.

We provide a Java SDK for RPs to integrate UPPRESSO. The SDK provides 2 functions to encapsulate RP's processings: one for RP identifier transformation,  $PID_{RP}$  registration and identity proof request generation; while the other for identity proof verification and Account calculation. The SDK is implemented based on the Spring Boot framework with about 1000 lines code, and cryptographic computations are implemented based on Spring Security library. An RP only needs to invoke these two functions for the integration.

#### B. Performance Evaluation

**Environment.** The evaluation was performed on 3 machines, one (3.4GHz CPU, 8GB RAM, 500GB SSD, Windows 10) as IdP, one (3.1GHz CPU, 8GB RAM, 128GB SSD, Windows 10) as an RP, and the last one (2.9GHz CPU, 8GB RAM, 128GB SSD, Windows 10) as a user. The user agent is Chrome v75.0.3770.100. And the machines are connected by an isolated 1Gbps network.

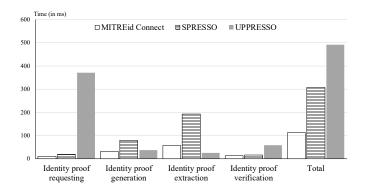


Fig. 4: The Evaluation.

**Setting.** We compare UPPRESSO with MITREid Connect [44] and SPRESSO [15], where MITREid Connect provides opensource Java implementations [44] of IdP and RP's SDK, and SPRESSO provides the JavaScript implementations based on node.js for all entities [15]. We implemented a Java RP based on Spring Boot framework for UPPRESSO and MITREid Connect, by integrating the corresponding SDK respectively. The RPs in all the three schemes provide the same function, i.e., extracting the user's account from the identity proof. We have measured the time for a user's login at an RP, and calculated the average values of 1000 measurements. For better analysis, we divide a login into 4 phases according to the lifecycle of identity proof: Identity proof requesting (Steps 1.1-4.3 in Figure 3), the RP (and user) constructing and transmitting the request to IdP; **Identity proof generation** (Steps 4.4 and 4.5 in Figure 3), the IdP generating identity proof (no user authentication); **Identity proof extraction** (Steps 4.5 and 4.6 in Figure 3), the RP server extracts the identity proof from the IdP; and **Identity proof verification** (Steps 5.1 and 5.2 in Figure 3), the RP verifying and parsing the identity proof.

**Results.** The evaluation results are provided in Figure 4. The overall processing times are 113 ms, 308 ms and 492 ms for MITREid Connect, SPRESSO and UPPRESSO, respectively. The part in UPPRESSO takes the longest time is opening the new window and downloading the script which totally cost about 255 ms. The time cost can be cut down as the browser can implicitly conduct this procedure while user visit the RP website. The details are as follows.

In the requesting, UPPRESSO requires firstly user downloads the RP script, opens the IdP window and downloads the IdP script, then both the user and RP to perform 1 modular exponentiations for RP identifier transformation and complete  $PID_{RP}$  registration at the IdP, which totally need 371 ms, where SPRESSO needs 19 ms for the RP to obtain IdP's public key and encrypt its domain; while MITREid Connect only needs 10 ms.

In the generation, UPPRESSO needs an extra 6 ms for computing  $PID_U$ , compared to MITREid Connect which only needs 32 ms. SPRESSO requires 71 ms, as it implements the IdP based on node.js and therefore can only adopt a JavaScript cryptographic library, while others adopt a more efficient Java library. As the processings in SPRESSO and MITREid Connect are the same, the processing time in SPRESSO may

be reduced to 32 ms.

In the identity proof extraction, UPPRESSO only needs about 25 ms where the scripts relay the identity proof to the RP server. MITREid Connect requires the IdP to send the identity proof to the RP's web page which then sends the proof to the RP server through a JavaScript function, and needs 57 ms. SPRESSO needs the longest time (193 ms) due to a complicated processing at the user's browser, which needs the browser to obtain identity proofs from the IdP, download the JavaScript program from a trusted entity (forwarder), execute the program to decrypt RP's endpoint, send identity proofs to this endpoint (an RP's web page) who finally transmits the proof to RP server. In the evaluation, the forwarder and IdP are deployed in one machine, which doesn't introduce performance degradation based on the observation.

In the verification, UPPRESSO needs an extra calculation for *Account*, which then requires 58 ms, compared to 14 ms in MITREid Connect and 17 ms in SPRESSO.

#### VIII. DISCUSSIONS AND FUTURE WORK

In this section, we discuss some related issues and our future work.

Scalability. The adversary cannot exhaust  $ID_{RP}$  and  $PID_{RP}$ . For  $ID_{RP}$ , it is generated only in RP's initial registration. For  $PID_{RP}$ , in practice, we only need to ensure all  $PID_{RP}$ s are different among the unexpired identity proof (the number denoted as n). We assume that IdP doesn't perform the uniqueness check, and then calculate the probability that at least two  $PID_{RP}$ s are equal in these n ones. The probability is  $1-\prod_{i=0}^{n-1}(1-i/q)$  which increases with n. For an IdP with throughput  $2*10^8$  req/s, when the validity period of the identity proof  $(PID_{RP})$  is set as 5 minutes, n is less than  $2^{36}$ , then the probability is less than  $2^{-183}$  for 256-bit q. Moreover, as this probability is negligible, the uniqueness check of  $PID_{RP}$ , i.e., the  $PID_{RP}$  registration, could be removed in the SSO login process, and this optimization can be adopted when this negligible probability is acceptable by the users and RPs.

Security against DoS attack. The adversary may attempt to perform DoS attack on the IdP and RP. For example, the adversary may act as a user to invoke the  $PID_{RP}$  registration (Step 2.1) and identity proof generation (Step 3.2) at the IdP, which requires the IdP to perform two signature generations and one modular exponentiation. However, as the user has already been authenticated at the IdP, the IdP could identify the malicious users based on audit, in addition to the existing DoS mitigation schemes. The adversary may act as a user requesting to log into an RP, and make the RP perform two modular exponentiations. The RP could previously calculated a set of  $Y_{RP}$ s to mitigate this attack.

OIDC authorization code flow support. The privacy-preserving functions  $\mathcal{F}_{ID_U \mapsto PID_U}$ ,  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$  and  $\mathcal{F}_{PID_U \mapsto Account}$  can be integrated into OIDC authorization code flow directly, therefore RP-based identity linkage and IdP-based login tracing are still prevented during the construction and parsing of identity proof. The only privacy leakage is introduced by the transmission, as RP servers obtain the identity proof directly from the IdP in this flow, which allows the IdP to obtain RP's network information (e.g., IP address).

UPPRESSO needs to integrate existing anonymous networks (e.g., Tor) to prevent this leakage.

**Malicious IdP mitigation.** The IdP is assumed to assign a unique  $ID_{RP}$  in  $Cert_{RP}$  for each RP and generate the correct  $PID_U$  for each login. The malicious IdP may attempt to provide the incorrect  $ID_{RP}$  and  $PID_U$ , which could be prevented by integrating certificate transparency [47] and user's identifier check [15]. With certificate transparency [47], the monitors check the uniqueness of  $ID_{RP}$  among all the certificates stored in the log server. To prevent the malicious IdP from injecting any incorrect  $PID_U$ , the user could provide a nickname to the RP for an extra check as in SPRESSO [15].

Identity linkage through cookie. In UPPRESSO, IdP does not provide any distinctive user message, such as  $ID_U$ , to RP to avoid RP-based identity linkage. However, the cookie of each user may be exploited by RPs to correlate the same user. For instance, while user has logged in to  $RP_A$  with  $Account_A$ , RP may redirect user's  $Account_A$  to  $RP_B$  through the hidden iframe. That is, as long as the user has logged in to  $RP_B$  with  $Account_B$ , the user would be correlated. Moreover, this attack is not only appeared in SSO systems, but also existed in all user-account systems. However, this attack can be easily detected by multiple methods, such as checking the iframe in script, observing redirection flow through browser network tool, and detecting the redirection based on the browser extension.

# IX. RELATED WORKS

Various SSO protocols have been proposed, such as, OIDC, OAuth 2.0, SAML, Central Authentication Service (CAS) [48] and Kerberos [49]. These protocols are widely adopted in Google, Facebook, Shibboleth project [50], Java applications and etc. And, plenty of works have been conducted on privacy protection and security analysis for SSO systems.

# A. Privacy protection for SSO systems.

Privacy-preserving SSO systems. As suggested by NIST [7], SSO systems should prevent both RP-based identity linkage and IdP-based login tracing. The pairwise user identifier is adopted in SAML [3] and OIDC [1], and only prevents RP-based identity linkage; while SPRESSO [15] and BrowserID [14] only prevent IdP-based login tracing. BrowserID is adopted in Persona [17] and Firefox Accounts [9], however an analysis on Persona found IdP-based login tracing could still succeed [14], [51]. UPPRESSO prevents both the RP-based identity linkage and IdP-based login tracing, and could be integrated into OIDC which has been formally analyzed [22].

Anonymous SSO systems. Anonymous SSO schemes are designed to allow users to access a service (i.e. RP) protected by a verifier (i.e., IdP) without revealing their identities. One of the earliest anonymous SSO systems was proposed for Global System for Mobile (GSM) communication in 2008 [52]. The notion of anonymous SSO was formalized [53] in 2013. And, various cryptographic primitives, such as group signature, zero-knowledge proof and etc., were adopted to design anonymous SSO schemes [53], [54]. Anonymous SSO schemes are designed for the anonymous services, and not applicable to common services which need user identification.

B. Security analysis of SSO systems.

Formal analysis on SSO standards. The SSO standards (e.g., SAML, OAuth and OIDC) have been formally analyzed. Fett et al. [21], [22] have conducted the formal analysis on OAuth 2.0 and OIDC standards based on an expressive Dolev-Yao style model [51], and proposed two new attacks, i.e., 307 redirect attack and IdP Mix-Up attack. When the IdP misuses HTTP 307 status code for redirection, the sensitive information (e.g., credentials) entered at the IdP will be leaked to the RP by the user's browser. While, IdP Mix-Up attack confuses the RP about which IdP is used and makes the victim RP send the identity proof to the malicious IdP, which breaks the confidentiality of the identity proof. Fett et al. [21], [22] have proved that OAuth 2.0 and OIDC are secure once these two attacks prevented. UPPRESSO could be integrated into OIDC, which simplifies its security analysis. [20] formally analyzed SAML and its variant proposed by Google, and found that Google's variant of SAML doesn't set RP's identifier in the identity proof, which breaks RP designation.

**Single sign-off.** In SSO systems, once a user's IdP account is compromised, the adversary could hijack all her RPs' accounts. A backwards-compatible extension, named single sign-off, is proposed for OIDC. The single sign-off allows the user to revoke all her identity proofs and notify all RPs to freeze her accounts [5]. The single sign-off could also be achieved in UPPRESSO, where the user needs to revoke the identity proofs at all RPs, as the IdP doesn't know which RPs the user visits.

Analysis on SSO implementations. Various vulnerabilities were found in SSO implementations, and then exploited for impersonation and identity injection attacks by breaking the confidentiality [24], [25], [36]–[38], integrity [23], [24], [28], [30], [31], [38] or RP designation [28], [30]-[32], [38] of identity proof. Wang et al. [24] analyzed the SSO implementations of Google and Facebook from the view of the browser relayed traffic, and found logic flaws in IdPs and RPs to break the confidentiality and integrity of identity proof. An authentication flaw was found in Google Apps [25], allowing a malicious RP to hijack a user's authentication attempt and inject the malicious code to steal the cookie (or identity proof) for the targeted RP, breaking the confidentiality. The integrity has been tampered with in SAML, OAuth and OIDC systems [23], [24], [28], [30], [31], due to various vulnerabilities, such as XML Signature wrapping (XSW) [23], RP's incomplete verification [24], [28], [31], IdP spoofing [30], [31] and etc. And, a dedicated, bidirectional authenticated secure channel was proposed to improve the confidentiality and integrity of identity proof [39]. The vulnerabilities were also found to break the RP designation, such as the incorrect binding at IdPs [28], [32], insufficient verification at RPs [30]-[32]. Automatical tools, such as SSOScan [26], OAuthTester [29] and S3KVetter [32], have been designed to detect vulnerabilities for breaking the confidentiality, integrity or RP designation of identity proof.

Analysis on mobile SSO systems. In mobile SSO systems, the IdP App, IdP-provided SDK (e.g., an encapsulated WebView) or system browser are adopted to redirect identity proof from IdP App to RP App. However, none of them was trusted to ensure that the identity proof could be only sent to the designated RP [27], [35], as WebView and system browser cannot authenticate RP App while the IdP App may be repackaged. Moreover, the SSO protocols needed to be modified to provide

SSO services for mobile Apps, however these modifications were not well understood by RP developers [33], [35]. The top Android applications have been analyzed [27], [33]–[35], [40], and vulnerabilities were found to break the confidentiality [27], [33]–[35], [40], integrity [33], [35], and RP designation [34], [35] of identity proof.

# X. CONCLUSION

In this paper, we propose UPPRESSO, an unlinkable privacy-preserving single sign-on system, which protects a user's login activities at different RPs against both curious IdP and collusive RPs. To the best of our knowledge, UPPRESSO is the first approach that defend against both IdP-based login tracing and RP-based identity linkage privacy threats at the same time. To achieve these goals, we convert the privacy problem in SSO services into an identifier-transformation problem and design three transformation functions based on the discrete logarithm problem, where  $\mathcal{F}_{ID_{RP} \mapsto PID_{RP}}$  prevents curious IdP from knowing the identity of the RP,  $\mathcal{F}_{ID_U\mapsto PID_U}$ prevents collusive RPs from linking a user based on her identifier, and  $\mathcal{F}_{PID_U \mapsto Account}$  allows each RP to derive an identical account for a user in her multiple logins. The three functions could be integrated with existing SSO protocols, such as OIDC, to enhance the protection of user privacy, without breaking any security guarantee of SSO. Moreover, the evaluation on the prototype of UPPRESSO demonstrates that it supports an efficient SSO service, where a single login takes only 254 ms on average.

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# APPENDIX A WEB MODEL

#### A. Data Formate

Here we provide the details of formate of some messages we use to construct the UPPRESSO model.

HTTP Messages. An HTTP request message is the term of the form

 $\langle HTTPReq, nonce, method, host, path, parameters, headers, body \rangle$ 

An HTTP response message is the term of the form

 $\langle \mathtt{HTTPResp}, nonce, status, headers, body \rangle$ 

The details are dined as follows:

- HTTPReq and HTTPResp are the type of messages.
- nonce is the constant nonce mapping the response with the specific request.
- *method* is the HTTP method, such as GET and POST.
- host is the constant string domain of visited server.
- path is the constant string representing the concrete resource of the server.
- parameters contains the parameters carried by the url as the form  $\langle\langle name, value \rangle, \langle name, value \rangle, \ldots \rangle$ , for example the parameters HTTP request sent to the url http: //www.example.com?type = confirm is  $\langle\langle type, confirm \rangle\rangle$ .
- headers is the header content of each HTTP messages as the form  $\langle \langle name, value \rangle, \langle name, value \rangle, \ldots \rangle$ , such as  $\langle \langle Referer, http: //www.example.com \rangle, \langle Cookies, c \rangle \rangle$ .
- body is the body content carried by HTTP POST request or HTTP response in the form  $\langle \langle name, value \rangle, \langle name, value \rangle, \ldots \rangle$ .
- status is the HTTP status code defined by HTTP standard.

**URL**. A URL is a term  $\langle \text{URL}, protocol, host, path, parameters \rangle$ , where URL is the type, protocol is chosen in  $\{S, P\}$  as S stands for HTTPS and P stands for HTTP. The host, path, and parameters are same as in HTTP message.

**Origin**. An Origin is a term  $\langle host, protocol \rangle$  that stands for the specific domain used by the HTTP CORS policy, where host and protocol are defined as same as in URL.

**POSTMESSAGE**. PostMessage is used in the browser for transmitting messages between scripts from different origins. We define the postMessage as the form  $\langle POSTMESSAGE, target, Content, Origin \rangle$ , where POSTMESSAGE is the type, target is the constant nonce which stands the for the receiver, Content is the message transmitted and Origin is restricts the receiver's origin.

**XMLHTTPREQUEST.** XMLHTTPRequest is the HTTP message transmitted by scripts in the browser. That is the XMLHTTPRequest is converted with the HTTP message by the browser. The XMLHTTPRequest in the form  $\langle XMLHTTPREQUEST, URL, methods, Body, nonce \rangle$  can be converted into HTTP request message by the browser, and  $\langle XMLHTTPREQUEST, Body, nonce \rangle$  is converted from HTTP response message.

**Data Operation**. The data used in UPPRESSO are defined in the following forms:

- Standardized Data is the data in the fixed format, for instance the HTTP request is the standardized data in the form  $\langle \text{HTTPReq}, nonce, method, host, path, parameters, headers, body} \rangle$ . We assume there is an HTTP request  $r := \langle \text{HTTPReq}, n, \text{GET}, example.com, /path, <math>\langle \rangle, \langle \rangle, \langle \rangle \rangle$ , here we define the operation on the r. That is the elements in r can be accessed in the form r.name, such that  $r.method \equiv \text{GET}, r.path \equiv /path$  and  $r.body \equiv \langle \rangle$ .
- **Dictionary Data** is the data in the form  $\langle \langle name, value \rangle, \langle name, value \rangle, ... \rangle$ , for instance the *body* in HTTP request is dictionary data. We assume there is a  $body := \langle \langle username, alice \rangle, \langle password, 123 \rangle \rangle$ , here we define the operation on the *body*. That is we can access the elements in *body* in the form body[name], such that  $body[username] \equiv alice$  and  $body[password] \equiv 123$ . We can also add the new attributes to the dictionary, for example after we set body[age] := 18, the body are changed into $\langle \langle username, alice \rangle, \langle password, 123 \rangle, \langle age, 18 \rangle \rangle$ .

**Patten Matching**. We define the term with the variable  $\star$  as the pattern, such as  $\langle a, b, \star \rangle$ . That is the pattern matches any terms which is in the same form of the pattern but replacing the  $\star$  with other terms. For instance,  $\langle a, b, \star \rangle$  matches  $\langle a, b, c \rangle$ .

#### B. Browser Model

As we consider that the browsers are honest in UPPRESSO model, therefore, we only focus on how the browsers interactive with the scripts.

We firstly introduce the windows and documents of the browser model.

**Window**. A window w is a term of the form  $w = \langle nonce, documents, opener \rangle$ , representing the concrete browser window in the system. The nonce is the window reference to identify each windows. The documents is the set of documents (defined below) including the current document and cached documents (for example, the documents can be viewed via the "forward" and "back" buttons in the browser). The opener represents the widow is created in which document, for instance, while a user clicks the href in document d and it creates a new window w, there is  $w.opener \equiv d.nonce$ .

#### **Document.** A document d is a term of the form

 $\langle nonce, location, referrer, script, script state, script inputs, subwindows, active \rangle$ 

where document is the HTML content in the window. The *nonce* is to locate the document. *Location* is the URL where the document is loaded. *Referrer* is same as the Referer header defined in HTTP standard. *script* is the scripting process downloaded from each servers. *scriptstate* is define by the script, different in each scripts. *scriptinputs* is the message transmitted into the scripting process. *subwindows* is the set of *nonce* of document's created windows. *active* represents whether this document is active or not.

A scripting process is the dependent process relying on the browser, which can be considered as a relation R mapping a message input and a message output. And finally the browser will conduct the command in the output message. Here we give the description of the form of input and output.

• Scripting Message Input. The input is the term in the form

 $\langle tree, docnonce, scriptstate, state inputs, cookies, local Storage, session Storage, ids, secret \rangle$ 

• Scripting Message Output. The output is the term in the form

 $\langle scriptstate, cookies, localStorage, sessionStorage, command \rangle$ 

The tree is the relations of the opened windows and documents, which are visible to this script. Docnonce is the document nonce. The Scriptstate is a term of the form defined by each script. Scriptinputs is the message transmitted to script. However, the scriptinputs are defined as standardized forms, for example postMessage is one of the forms of scriptinputs. Cookies is the set of cookies belong to the document's origin. LocalStorage is the storage space for browser and sessionStorage is the space for each HTTP sessions. Ids is the set of user IDs while secret is the password to corresponding user ID. The command is the operation which is to be conducted by the browser. Here we only introduce the form of commands used in UPPRESSO system. We have defined the postMessage and XMLHTTPRequest (for HTTP request) message which are the commands. Moreover, a term in the form  $\langle IFRAME, URL, WindowNonce \rangle$  asks the browser to create this document's subwindow and it visits the server with the URL.

# C. Model Of UPPRESSO

In this section, we will introduce the model of processes in UPPRESSO system, containing IdP server process, RP server process, IdP scripting process and RP scripting process. We will focus on the state form and relation R. They can describe that what kind of event can be accepted by the process in each states, and the content of new output events and states.

#### D. IdP Server Process

The state of IdP server process is a term in the form  $\langle ID, p, SignKey, sessions, users, RPs, Validity, Tokens \rangle$ . Other data stored at IdP but not used during SSO authentication are not mentioned here.

- *ID* is the identifier of IdP.
- p is the large prime mentioned before.
- SignKey is the private key used by IdP to generate signatures.
- sessions is the term in the form of  $\langle\langle Cookie, session\rangle\rangle$ , the Cookie uniquely identify the session and sessions store the browser uploaded message.
- users is the set of user information. And each user informations contains the username, password, uid and other user attributes.
- RPs is the set of RP information which consists of ID of RP  $(PID_{RP})$ , Endpoints the set of RP's validity endpoints and Validity.

- Validity is the validity for IdP generated signatures.
- *Tokens* is the set of IdP generated Identity proofs.

To make the description clearer, we also provide the functions to define the complicated procedure.

- SecretOfID(u) is used to search the user u's password.
- UIDOfUser(u) is used to search the user u's uid.
- ListOfPID() is the set of IDs of registered RP.
- EndpointsOfRP(r) is the set of endpoints registered by the RP with ID r.
- ModPow(a, b, c) is the result of  $a^b \mod c$ .
- CurrentTime() is the system current time.

The relation of IdP process  $R^i$  is shown as Algorithm 1.

# Algorithm 1 $R^i$

```
Input: \langle a, f, m \rangle, s
 1: let s := s'
 2: let n, method, path, parameters, headers, body such that
       \langle \mathtt{HTTPReq}, n, method, path, parameters, headers, body \rangle \equiv m
       if possible; otherwise stop \langle \rangle, s'
 3: if path \equiv /script then
        let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{IdPScript} \rangle
        stop \langle f, a, m' \rangle, s'
 6: else if path \equiv /login then
       let cookie := headers[Cookie]
       let session := s'.sessions[cookie]
 8:
       let username := body[username]
 9:
        let password := body[password]
10:
        if password \not\equiv \texttt{SecretOfID}(username) then
11:
12:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{LoginFailure} \rangle
           stop \langle f, a, m' \rangle, s'
13:
14:
        let session[uid] := UIDOfUser(username)
15:
        let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{LoginSucess} \rangle
16:
        stop \langle f, a, m' \rangle, s'
18: else if path \equiv /loginInfo then
        let cookie := headers[Cookie]
19.
        let session := s'.sessions[cookie]
20:
        let username := session[username]
21:
        if username \not\equiv null then
22:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Logged} \rangle
23:
           stop \langle f, a, m' \rangle, s'
24:
25:
        end if
        let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Unlogged} \rangle
26:
        stop \langle f, a, m' \rangle, s'
27:
28: else if path \equiv /dynamicRegistration then
       let PID_{RP} := body[PID_{RP}]
29:
        let Endpoint := body[Endpoint]
30:
        let Nonce := body[Nonce]
31:
        if PID_RP \in \texttt{ListOfPID}() then
32:
           let Content := \langle Fail, PID_{RP}, Nonce \rangle
33:
           let Sig := Sig(Content, s'.SignKey)
34:
           let RegistrationResult := \langle Content, Sig \rangle
35:
           let m' := \langle \text{HTTPResp}, n, 200, \langle \rangle, RegistrationResult \rangle
36:
           stop \langle f, a, m' \rangle, s'
37:
38:
        end if
39:
        let Validity := CurrentTime() + s'.Validity
        let s'.RPs := s'.RPs + \langle PID_{RP}, Endpoint, Validity \rangle
40:
        let Content := \langle OK, PID_{RP}, Nonce, Validity \rangle
41:
```

```
let Sig := Sig(Content, s'.SignKey)
42:
       let RegistrationResult := \langle Content, Sig \rangle
43:
       let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, RegistrationResult \rangle
44:
        stop \langle f, a, m' \rangle, s'
45:
46: else if path \equiv /authorize then
       let cookie := headers[Cookie]
47:
       let session := s'.sessions[cookie]
48:
       let username := session[username]
49:
        if username \equiv null then
50:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
51:
52:
           stop \langle f, a, m' \rangle, s'
53:
        let PID_{RP} := parameters[PID_{RP}]
54:
        let Endpoint := parameters[Endpoint]
55:
        if PID_{RP} \notin \texttt{ListOfPID}() \vee Endpoint \notin \texttt{EndpointsOfRP}(PID) then
56:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
57:
           stop \langle f, a, m' \rangle, s'
58:
        end if
59:
        let UID := session[uid]
60:
       let PID_U := ModPow(PID_{RP}, UID, s'.p)
61:
       let Validity := CurrentTime() + s'.Validity
62:
       let Content := \langle PID_{RP}, PID_U, s'.ID, Validity \rangle
63:
64:
       let Sig := Sig(Content, s'.SignKey)
65:
       let Token := \langle Content, Sig \rangle
       let s'.Tokens := s'.Tokens + \langle \rangle Token
66:
       let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \langle Token, Token \rangle \rangle
67:
       stop \langle f, a, m' \rangle, s'
68:
69: end if
70: stop \langle \rangle, s'
```

#### E. RP process

The state of RP server process is a term in the form  $\langle ID_{RP}, Endpoints, IdP, Cert, sessions, users \rangle$ . Other attributes are not mentioned here.

- $ID_{RP}$  and Endpoints are RP's registered information at IdP.
- Cert is the IdP signed RP information containing  $ID_{RP}$ , Endpoints and other attributes.
- IdP is the term of the for  $\langle ScriptUrl, p, q, PubKey \rangle$ , where ScriptUrl is the site to download IdP script, p and q are large prime defined before, and PubKey is used to verify the IdP signed content.
- sessions is same as it in RP process.
- users is the set of RP registered user which is uniquely identified by the Account.

The new functions are defined as follows

- ExEU(a,q) is the Extended Euclidean algorithm, of which the result in RP process the  $a^{-1} \mod q$ .
- Random() is a newly generated random number.
- RegisterUser(Account) add the new user with Account into RP's user list.

The relation of RP process  $R^r$  is shown as Algorithm 2.

#### Algorithm 2 $R^r$

```
Input: \langle a, f, m \rangle, s

1: let s := s'

2: let n, method, path, parameters, headers, body such that \langle \mathsf{HTTPReq}, n, method, path, parameters, headers, body \rangle \equiv m if possible; otherwise \mathsf{stop}\ \langle \rangle, s'

3: if path \equiv /script then

4: let m' := \langle \mathsf{HTTPResp}, n, 200, \langle \rangle, \mathsf{RPScript} \rangle

5: \mathsf{stop}\ \langle f, a, m' \rangle, s'
```

```
6: else if path \equiv /login then
       let m' := \langle \mathtt{HTTPResp}, n, 302, \langle \langle Location, s'. IdP. ScriptUrl \rangle \rangle, \langle \rangle \rangle
       stop \langle f, a, m' \rangle, s'
 9: else if path \equiv /startNegotiation then
       let cookie := headers[Cookie]
10:
       let session := s'.sessions[cookie]
11:
       let N_U := parameters[N_U]
12:
       let PID_{RP} := ModPow(s'.ID_{RP}, N_U, s'.IdP.p)
13:
       let t := \text{ExEU}(N_U, s'.IdP.q)
14:
15:
       let session[N_U] := N_U
       let session[PID_{RP}] := PID_{RP}
16:
        let session[t] := t
17:
       let session[state] := expectRegistration
18:
       let m' := \langle \text{HTTPResp}, n, 200, \langle \rangle, \langle Cert, s'.Cert \rangle \rangle
19:
        stop \langle f, a, m' \rangle, s'
20:
21: else if path \equiv /registrationResult then
        let cookie := headers[Cookie]
        let session := s'.sessions[cookie]
23:
        if session[state] \not\equiv expectRegistration then
24:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
25:
           stop \langle f, a, m' \rangle, s'
26:
        end if
27:
       let RegistrationResult := body[RegistrationResult]
28:
29:
        let Content := RegistrationResult.Content
        if checksig(Content, RegistrationResult.Sig, s'.IdP.PubKey) \equiv FALSE then
30:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
31:
           \mathbf{let}\ session := \mathtt{null}
32:
           stop \langle f, a, m' \rangle, s'
33:
        end if
34:
        if Content.Result \not\equiv OK then
35:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
36:
37:
           let session := null
           stop \langle f, a, m' \rangle, s'
38:
        end if
39:
        let PID_{RP} := session[PID_{RP}]
40:
41:
       let N_U := session[N_U]
42:
       let Nonce := \operatorname{Hash}(N_U)
        let Time := CurrentTime()
43:
        if PID_{RP} \not\equiv Content.PID_{RP} \lor Nonce \not\equiv Content.Nonce \lor Time > Content.Validity then
44:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
45:
           let \ session := null
46:
           stop \langle f, a, m' \rangle, s'
47:
        end if
48:
        let session[PIDValidity] := Content.Validity
49:
        let Endpoint \in s'.Endpoints
50:
        let session[state] := expectToken
51:
       let Nonce' := Random()
52:
       let session[Nonce] := Nonce'
53:
54:
       let Body := \langle PID_{RP}, Endpoint, Nonce' \rangle
       let m' := \langle \text{HTTPResp}, n, 200, \langle \rangle, Body \rangle
       stop \langle f, a, m' \rangle, s'
57: else if path \equiv /uploadToken then
       let cookie := headers[Cookie]
58:
       let session := s'.sessions[cookie]
59:
       if session[state] \not\equiv expectToken then
60:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
61:
           stop \langle f, a, m' \rangle, s'
62:
        end if
63:
       let Token := body[Token]
64.
        if checksig(Token.Content, Token.Sig, s'.IdP.PubKey) \equiv FALSE then
65:
           let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
66:
67:
           stop \langle f, a, m' \rangle, s'
```

```
end if
68:
       let PID_{RP} := session[PID_{RP}]
69:
       let Time := CurrentTime()
70:
       let PIDValidity := session[PIDValidity]
71:
       let Content := Token.Content
72:
       if PID_{RP} \not\equiv Content.PID_{RP} \lor Time > Content.Validity \lor Time > PIDValidity then
73:
          let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{Fail} \rangle
74:
          stop \langle f, a, m' \rangle, s'
75:
       end if
76:
       let PID_U := Content.PID_U
77:
       let t := session[t]
       let Account := ModPow(PID_U, t, s'.IdP.p)
79:
       if Account \in ListOfUser() then
80:
          let RegisterUser(Account)
81:
       end if
82:
       let session[user] := Account
83:
       let m' := \langle \mathtt{HTTPResp}, n, 200, \langle \rangle, \mathtt{LoginSuccess} \rangle
       stop \langle f, a, m' \rangle, s'
86: end if
87: stop \langle \rangle, s'
```

# F. IdP scripting process

The state of IdP scripting process scriptstate is a term in the form  $\langle IdPDomain, Parameters, p, q, refXHR \rangle$ , where

- *IdPDomain* is the IdP's host.
- Parameters is used to store the parameters received from other process.
- p is the large prime defined before.
- q is used to label the procedure point in the login.
- $\bullet$  refXHR is the nonce to mapping HTTP request and response.

The new functions are defined as follows

- PARENTWINDOW(tree, docnonce). The first parameter is the input relation tree defined before, and the second parameter
  is the nonce of a document. The output returned by the function is the current window's opener's nonce if it exists and
  is visible to this document.
- CHOOSEINPUT(inputs, pattern). The first parameter is a set of messages, and the second parameter is a pattern. The result returned by the function is the message in inputs matching the pattern.
- RandonUrl() returns a newly generated host string.

The relation of IdP scripting process  $script\_idp$  is shown as Algorithm 3.

# Algorithm 3 script\_idp

```
Input: \langle tree, docnonce, scriptstate, scriptinputs, cookies, local Storage, session Storage, ids, secret \rangle
 1: let s' := script state
 2: let command := \langle \rangle
 3: let target := PARENTWINDOW(tree, docnonce)
 4: let IdPDomain := s'.IdPDomain
 5: switch s'.q do
       case start:
 6:
          let N_U := \mathtt{Random}()
 7:
          \textbf{let} \ command := \langle \texttt{POSTMESSAGE}, target, \langle \langle N_U, N_U \rangle \rangle, \texttt{null} \rangle
 8:
          let s'.Parameters[N_U] := N_U
 9:
          let s'.q := expect Cert
10:
       case expectCert:
11:
          let pattern := \langle POSTMESSAGE, *, Content, * \rangle
12:
          let input := CHOOSEINPUT(scriptinputs, pattern)
13:
          if input \not\equiv \texttt{null} then
14:
15:
             let Cert := input.Content[Cert]
```

```
if checksig(Cert.Content, Cert.Sig, s'.PubKey) \equiv null then
16:
               let stop (
17:
             end if
18:
             let s'.Parameters[Cert] := Cert
19:
            let N_U := s'.Parameters[N_U]
20:
             let PID_{RP} := ModPow(Cert.Content.ID_{RP}, N_U, s'.p)
21:
            let s'.Parameters[PID_{RP}] := PID_{RP}
22:
            let Endpoint := RandomUrl()
23:
            let s'.Parameters[Endpoint] := Endpoint
24:
            let Nonce := \operatorname{Hash}(N_U)
25:
26:
            let Url := \langle URL, S, IdPDomain, /dynamicRegistration, \langle \rangle \rangle
             let s'.refXHR := Random()
27:
            let command := \langle XMLHTTPREQUEST, Url, POST,
28:
                  \langle PID_{RP}, PID_{RP} \rangle, \langle Nonce, Nonce \rangle, \langle Endpoint, Endpoint \rangle \rangle, s'.refXHR \rangle
            let s'.q := expectRegistrationResult
29:
          end if
30:
       case expectRegistrationResult:
31:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
32:
33:
          let input := CHOOSEINPUT(scriptinputs, pattern)
          if input \not\equiv null \land input.Content[RegistrationResult].type \equiv OK then
34.
             \textbf{let} \ RegistrationResult := input.Body[RegistrationResult]
35:
             if RegistrationResult.Content.Result \not\equiv OK then
36:
               let s'.q := stop
37:
38:
               let stop \langle \rangle
             end if
39:
            \textbf{let} \ command := \langle \texttt{POSTMESSAGE}, target, \langle \langle RegistrationResult, RegistrationResult \rangle \rangle, \texttt{null} \rangle
40:
            let s'.q := expectProofRquest
41:
          end if
42:
       case expectProofRquest:
43:
          let pattern := \langle POSTMESSAGE, *, Content, * \rangle
44:
          let input := CHOOSEINPUT(scriptinputs, pattern)
45:
          if input \not\equiv \text{null then}
46:
            let PID_{RP} := input.Content[PID_{RP}]
47:
            let Endpoint_{RP} := input.Content[Endpoint]
48:
            let s'.Parameters[Nonce] := input.Content[Nonce]
49:
            let Cert := s'.Parameters[Cert]
50:
             if Endpoint_{RP} \notin Cert.Content.Endpoints \lor PID_{RP} \not\equiv s'.Parameters[PID_{RP}] then
51:
52:
               let s'.q := stop
               let stop \langle \rangle
53:
             end if
54:
            let s'.Parameters[Endpoint_{RP}] := Endpoint_{RP}
55:
            let Url := \langle URL, S, IdPDomain, /loginInfo, \langle \rangle \rangle
56:
            let s'.refXHR := Random()
57:
            let command := \langle XMLHTTPREQUEST, Url, GET, \langle \rangle, s'.refXHR \rangle
58:
59:
             let s'.q := expectLoginState
          end if
60:
       case expectLoginState:
61:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
62:
          let input := CHOOSEINPUT(scriptinputs, pattern)
63:
64:
          if input \not\equiv \text{null then}
             if input.Body \equiv Logged then
65:
               let username \in ids
66:
               let Url := \langle URL, S, IdPDomain, /login, \langle \rangle \rangle mystates'.refXHR := Random()
67:
               \textbf{let} \ command := \langle \texttt{XMLHTTPREQUEST}, Url, \texttt{POST}, \langle \langle username, username \rangle, \langle password, secret \rangle \rangle, s'.refXHR \rangle
68:
               let s'.q := expectLoginResult
69:
             else if input.Body \equiv Unlogged then
70:
               let PID_{RP} := s'.Parameters[PID_{RP}]
71:
               let Endpoint := s'.Parameters[Endpoint]
72:
               let Nonce := s'.Parameters[Nonce]
73:
               \textbf{let } Url := \langle \mathtt{URL}, \mathtt{S}, IdPDomain, / authorize,
74:
                     \langle PID_{RP}, PID_{RP} \rangle, \langle Endpoint, Endpoint \rangle, \langle Nonce, Nonce \rangle \rangle \rangle
75:
               let s'.refXHR := Random()
```

```
\mathbf{let}\ command := \langle \mathtt{XMLHTTPREQUEST}, Url, \mathtt{GET}, \langle \rangle, s'.refXHR \rangle
76:
                let s'.q := expectToken
77:
              end if
78:
          end if
79:
       case expectLoginResult:
80:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
81:
          let input := CHOOSEINPUT(scriptinputs, pattern)
82:
          if input \not\equiv \texttt{null} then
83:
             if input.Body \not\equiv \texttt{LoginSuccess} then
84:
85:
                let stop \langle \rangle
86:
              end if
              let PID_{RP} := s'.Parameters[PID_{RP}]
87:
             let Endpoint := s'.Parameters[Endpoint]
88.
             let Nonce := s'.Parameters[Nonce]
89:
             let Url := \langle URL, S, IdPDomain, /authorize,
90:
                   \langle PID_{RP}, PID_{RP} \rangle, \langle Endpoint, Endpoint \rangle, \langle Nonce, Nonce \rangle \rangle \rangle
              let s'.refXHR := Random()
91:
             let command := \langle \texttt{XMLHTTPREQUEST}, Url, \texttt{GET}, \langle \rangle, s'.refXHR \rangle
92:
              let s'.q := expect Token
93:
          end if
94.
       case expectToken:
95:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
96:
97:
          let input := CHOOSEINPUT(scriptinputs, pattern)
98:
          if input \not\equiv \text{null then}
              let Token := input.Body[Token]
99:
              let RPOringin := \langle s'.Parameters[Endpoint_{RP}], S \rangle
100:
              \textbf{let} \ command := \langle \texttt{POSTMESSAGE}, target, \langle Token, Token \rangle, RPOrigin \rangle
101:
              let s.q := stop
102:
           end if
103:
104: end switch
105: let stop \langle s', cookies, localStorage, sessionStorage, command \rangle
```

# G. RP scripting process

The state of RP scripting process scriptstate is a term in the form  $\langle IdPDomain, RPDomain, Parameters, q, refXHR \rangle$ . The RPDomain is the host string of the corresponding RP server, and other terms are defined same as them in IdP scripting process.

Here we define another new function SUBWINDOW(tree, docnonce). This function takes the tree define above and the current document's nonce as the input. And it selects the nonce of the first window opened by this document as the output. However, if there is not the opened windows, it will return the null.

The relation of RP scripting process  $script\_rp$  is shown as Algorithm 4.

# Algorithm 4 script\_rp

```
Input: \langle tree, docnonce, script state, script inputs, cookies, local Storage, session Storage, ids, secret \rangle
 1: let s' := script state
 2: let command := \langle \rangle
 3: let IdPWindow := SUBWINDOW(tree, docnonce).nonce
 4: let RPDomain := s'.RPDomain
 5: let IdPOringin := \langle s'.IdPDomian, S \rangle
 6: switch s'.q do
       case start:
 7:
          let Url := \langle URL, S, RPDomain, /login, \langle \rangle \rangle
 8:
          let command := \langle IFRAME, Url, \_SELF \rangle
 9:
          let s'.q := expect N_U
10:
       case expectN_U:
11:
          let pattern := \langle POSTMESSAGE, *, Content, * \rangle
12:
          \textbf{let}\ input := \texttt{CHOOSEINPUT}(scriptinputs, pattern)
13:
          if input \not\equiv \texttt{null} then
14:
             let N_U := input.Content[N_U]
15:
16:
             let Url := \langle URL, S, RPDomain, / startNegotiation, \langle \rangle \rangle
```

```
let s'.refXHR := Random()
17:
             let command := \langle XMLHTTPREQUEST, Url, POST, \langle \langle N_U, N_U \rangle \rangle, s'.refXHR \rangle
18:
19:
             let s'.q := expectCert
          end if
20:
       case expectCert:
21:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
22:
          let input := CHOOSEINPUT(scriptinputs, pattern)
23:
          if input \not\equiv \text{null then}
24:
             let Cert := input.Content[Cert]
25:
             \textbf{let} \ command := \langle \texttt{POSTMESSAGE}, IdPWindow, \langle \langle Cert, Cert \rangle \rangle, IdPOringin \rangle
26:
27:
             let s'.q := expectRegistrationResult
          end if
28:
       case expectRegistrationResult:
29:
          let pattern := \langle POSTMESSAGE, *, Content, * \rangle
30:
          let input := CHOOSEINPUT(scriptinputs, pattern)
31:
          if input \not\equiv \text{null then}
32:
             let RegistrationResult := input.Content[RegistrationResult]
33:
             let Url := \langle URL, S, RPDomain, /registrationResult, \langle \rangle \rangle
34:
             let s'.refXHR := Random()
35:
             \textbf{let} \ command := \langle \texttt{XMLHTTPREQUEST}, Url, \texttt{POST}, \langle \langle RegistrationResult, RegistrationResult \rangle \rangle, s'.refXHR \rangle
36:
             let s'.q := expectTokenRequest
37:
          end if
38:
       case expectTokenRequest:
39:
40:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
          \textbf{let} \ input := \texttt{CHOOSEINPUT}(scriptinputs, pattern)
41:
          if input \not\equiv \texttt{null} then
42:
             let PID_{RP} := input.Content.Body[PID_{RP}]
43:
             let Endpoint := input.Content.Body[Endpoint]
44:
             let Nonce := input.Content.Body[Nonce]
45:
             let command := \langle POSTMESSAGE, IdPWindow,
46:
                 \langle\langle PID_{RP}, PID_{RP}\rangle, \langle Endpoint, Endpoint\rangle, \langle Nonce, Nonce\rangle\rangle, IdPOringin\rangle
             let s'.q := expectToken
47:
          end if
48.
       case expectToken:
49:
          \mathbf{let}\ pattern := \langle \mathtt{POSTMESSAGE}, *, Content, * \rangle
50:
          let input := CHOOSEINPUT(scriptinputs, pattern)
51:
52:
          if input \not\equiv \text{null then}
             let Token := input.Content[Token]
53:
             let Url := \langle URL, S, RPDomain, /uploadToken, \langle \rangle \rangle
54:
             let s'.refXHR := Random()
55:
             \textbf{let} \ command := \langle \texttt{XMLHTTPREQUEST}, Url, \texttt{POST}, \langle \langle Token, Token \rangle \rangle, s'.refXHR \rangle
56:
             let s'.q := expectLoginResult
57:
          end if
58:
       case expectLoginResult:
59:
          let pattern := \langle XMLHTTPREQUEST, Body, s'.refXHR \rangle
60:
          let input := CHOOSEINPUT(scriptinputs, pattern)
61:
          if input \not\equiv \texttt{null} then
62:
             if input.Body \equiv \texttt{LoginSuccess} then
63:
64:
                let LoadHomepage
65:
             end if
          end if
67: end switch
```

#### H. Proof of Theorem 1

We assume that all the network messages are protected by HTTPS and postMessage messages are protected by the browser, and the browsers are all honest, such that web attackers listening the network flow are not considered.

In this section, we will give a full version of proof about UPPRESSO security. Firstly, we recall the security requirements of UPPRESSO. That is, the system must ensure that only a legitimate user can log into an honest RP under her unique account. We consider the visits to RP's resource paths are controlled by the visitors' cookie, so that the attacker can break the security only when he own the cookie bound to the honest user. Therefore, we can propose the definition 1 about the secure UPPRESSO system.

**Definition 1.** Let  $\mathcal{UWS}$  be a UPPRESSO web system,  $\mathcal{UWS}$  is secure **iff** for any honest RP  $r \in \mathcal{W}$  and the authenticated cookie c for honest u, c is unknown to the attacker a.

Therefore, the proof of Theorem 1 is converted into whether the UPPRESSO system meet the requirement in definition 1. However, as we consider the attacker initially knows any honest users' cookies, the requirement of definition 1 can be separated as following requirements. Before describe the requirements, we firstly define the user u's authenticated cookie for RP r as c(u, r).

**Requirement 1.** If c(u,r) is the authenticated cookie owned by u, c(u,r) cannot be obtained by a.

**Requirement 2.** If c is an unauthenticated cookie owned by a, c cannot be set as c(u,r).

**Requirement 3.** The user u does not use the attacker's cookie (defined as c(a, r)).

To prove that UPPRESSO meets the requirements, we now show some lemmas. The first lemma here can prove that the UPPRESSO system meets requirement 1.

Lemma 1. Attacker does not learn users' cookies.

*Proof:* As the Brute-force attacks, such as exhausting the possible users' cookies, are not considered, the attackers can only try to obtain the cookies from honest processes in the system. For an honest user u and the honest RP r, the valid cookie c(u,r) can only be obtained by u's browser  $b_u$ , the r's script  $script\_rp$  and RP's server  $P^r$ . Here we only need to prove that attacker cannot receive the event from these processes carrying c(u,r).

- b. The browsers used by users are considered honest and well implemented. Therefore, based on the same-origin policy,  $b_u$  only sends r's cookie to RP's domain, so that attackers cannot receive the cookie.
- $script_rp$ . According to Algorithm 4, the  $script_rp$  does not send any cookie.
- $P^r$ . According to Algorithm 2, the  $P^r$  does not send any cookie.

Therefore, lemma 1 is proved.

To prove UPPRESSO system meets the requirement 2, firstly we need to know how the cookie can be set as c(u, r). Based on the algorithm 2, we propose the new definition.

**Definition 2.** In  $\mathcal{UWS}$ , the cookie c is to be set asc(u), r only when RP r receives a valid u's identity proof, here we defined as t(u, r), from the owner of c.

To prove that t(u, r) cannot be obtained by attackers, we firstly show some lemmas.

Lemma 2. Attacker does not learn users' passwords.

*Proof:* Same as the proof to lemmas 1, we only need to prove that attackers cannot receive the message form honest processes carrying password. The honest IdP server is defined as  $P^i$  and the IdP script is defined as  $script\_idp$ . Here we give the proof about each processes.

- script\_rp. According to algorithm 4, we can prove that RP script does not send any stored passwords.
- $P^r$ . According to algorithm 2, it is easy to find out that RP server does not receive or send any stored passwords.
- script\_rp. Based on algorithm 3, we can find that IdP script sends the user's password at line 68. The target of this message is Url whose host is IdPDoaim set at line 67. The IdPDomian is set at line 4 and the value is defined by the script initially with no modification. Therefore the password can only be sent to IdP server. The IdP server obtain the password at algorithm 1 line 10 and does not send this parameter to any other processes.
- $P^i$ . Based on algorithm 1, we can find that IdP server does not send any stored passwords.

Therefore, no attackers can obtain the password from honest processes, so that this lemma is proved.

Lemma 3. Attacker cannot forge or modify the IdP issued proofs.

*Proof:* Here we only consider the Cert used in  $script\_idp$ , the RegistrationResult and Token used in  $P^r$ . First of all, we can easily find that the IdP does not send the private key to any processes so that the attackers cannot obtain the private key.

• Cert is used at algorithm 3 line 21, 52. At line 21, the Cert has already been verified at line 16. At line 52, the Cert is picked from the state parameters, and the cert parameter is set at line 19. At line 19, the Cert has already been verified at line 16. At line 16 the Cert is verified with the public key in the scriptstate, where the key is considered initially honest and the key is not modified at algorithm 3. Therefore, Cert cannot be forged or modified.

- RegistrationResult is used at algorithm 2 from line 35 to 55 after line 30 where it is verified. The public key is initially set in the RP and never modified so that it is considered honest. Therefore, RegistrationResult cannot be forged or modified.
- *Token* is used at algorithm 2 from line 69 to 84 after line 65 where it is verified. And the public has been proved honest. Therefore, *Token* cannot be forged or modified.

Therefore, this lemma is proved.

Here we now show the lemma to prove that UPPRESSO meets the requirements in definition 2.

Lemma 4. Attacker cannot learn users' valid identity proofs.

*Proof:* As the Token has been proved that it can not be gorged by the attackers, here we only need to prove attackers cannot receive Token from other honest processes.

- Attacker cannot obtain the *Token* from RP server. We check all the messages sent by the RP server at algorithm 2 line 4, 7, 19, 25, 31, 36, 45, 55, 61, 66, 74, 84. It is easy to proved that the RP server does not sent any *Token* to other processes.
- Attacker cannot obtain the *Token* from RP script. The messages sent by RP script can be classified into two classes. The messages at algorithm 4 line 18, 36, 56 are sent to the RPDomain set at line 4, so that attackers cannot receive these messages. However, the messages at line 26, 46 only carry the contents received from RP server. We have already that RP server does not send any *Token*. Therefore, attackers cannot receive the *Token* from RP script.
- Attacker cannot obtain the *Token* from IdP server. Considered the messages at algorithm 1 line 4, 12, 16, 23, 26, 36, 44, 51, 67, it can be found that only the message at line 67 carries the *Token*. This *Token* is generated at line 65, following the trace where the *Content* at line 63, the *PID<sub>U</sub>* at line 61, the *UID* at line 60, the *session* at line 48, and finally the *cookie* at line 47. That is the *Token* receive must be the owner of the *cookie* the session of which save the parameter *UID*. The *UID* is set at line 15 after verifying the password and never modified. As we have already proved that the cookies and passwords cannot be known to attackers, so that attackers cannot obtain the *Token* from IdP server.
- Attacker cannot obtain the Token from IdP script. As the proof above, only IdP sends the Token with the message at algorithm 1 line 67, the IdP script can only receive the Token at algorithm 3 line 99. Here we are going to proof that the token t(u,r) can be only sent to the corresponding RP server through IdP script. The receiver of t(u,r) is restricted by the RPOrigin at line 100, which is set at line 55. The host in the RPOrigin is verified included in Cert at line 51. If the Cert belong to r, the attacker cannot obtain the t(u,r). Now we give the proof that the Cert belong to r. Firstly we define the negotiated  $PID_{RP}$  in t(u,r) as p. That is the  $PID_{RP}$  at algorithm 2 line 69 must equals with p and the  $PID_{RP}$  is verified at line 44 with the RegistrationToken. This verification cannot be passed due to the state check at line 60. At the same validity period, the IdP script need to send the registration request with same p and receive the successful registration result. As the IdP checks the uniqueness of  $PID_{RP}$  at algorithm 1 line 32. Therefore the r and IdP script must share the same RegistrationToken. As the RegistrationToken contains the  $Hash(N_U)$ , the IdP script and r must share the same  $ID_{RP}$ . Therefore, the the Cert saved as the IdP scriptstate parameter must belong to r.

Therefore, attackers cannot learn users' valid identity proofs.

Here we confirm that UPPRESSO meet the requirement 3. As the browser follows the same-origin policy, we consider that the attackers cannot set its cookie to user's browser at RP's origin. Therefore, due to definition 2, the user only sets her cookie as c(a,r) when RP receives the Token containing the attacker's PIDRP and a valid  $PID_{RP}$  negotiated by u and r. It requires that the attackers must know a valid  $PID_{RP}$ . Here we give a lemma.

**Lemma 5.** Attacker does not know a valid  $PID_{RP}$  negotiated by user u and RP r.

*Proof:* Here we give the proof that attacker cannot obtain the  $PID_{RP}$  and  $N_U$  from each processes.

- $P^i$ . We can find at algorithm 1 IdP only returns the message containing  $PID_{RP}$  to other processes when the  $PID_{RP}$  is included in the request message.
- $P^r$ . Same as IdP server, RP server only send the message containing  $PID_{RP}$  at algorithm at line 55, and the  $PID_{RP}$  is contained in the RegistrationResult received at line 28 and werified at line 44.  $script\_rp$ . We can find at algorithm 4, RP script only sends the messages to RP server and IdP script. The receivers' identities are ensured at line 3, 4. Therefore, attackers cannot obtains the  $PID_{RP}$  and  $N_U$ .  $script\_idp$ . The HTTP requests sent by IdP script are forwarded to the domain set at algorithm 3 line 4. The HTTP requests are ensured sent to IdP server. The postMessages are sent to the target set at line 3, and we will prove the target cannot be attacker. According to algorithm 2 line 44, the  $PID_{RP}$  is valid at RP server only when server receives the registration result. The Hash $(N_U)$  in the result ensure the result must

issued for the correct  $ID_{RP}$ . As the registration result is  $PID_{RP}$ -unique due to algorithm 1 line 32, the registration result received by IdP script at algorithm 3 line 35 must be same as it in RP server. This HTTP response is related with the HTTP request at line 28, carrying  $PID_{RP}$  and  $\operatorname{Hash}(N_U)$  at line 21, 25. It ensure the Cert obtained at line 15 must belong to RP not the attacker. As the target at line 3 is the window which opens the IdP script window and asks for user's login consent, user can easily find out the target site is not coincident with the consent requirement. Therefore, the target cannot be the attacker.

Here we have proved that UPPRESSO meets the requirements in definition 2. Therefore the requirement 2 is met, so that the theorem 1 is proved.

#### I. Proof of Theorem 2

In this section, we will give a full version of proof about UPPRESSO privacy. That is, if UPPRESSO is a privacy-preserving system, the system must be IdP-Privacy and RP-Privacy. Firstly we recall the requirements of IdP-Privacy and RP-Privacy system. Then we will give the proof that UPPRESSO system meets these requirements.

**Requirement 4. IdP-Privacy**. There are honest RPs  $r_1, r_2$ , IdP i and the honest user u. We define the event sets containing each users' login procedure, for instance, the  $events_{(u,r_1)}$  consists of all the events generated during the u logging in to  $r_1$  in correct procedure. It requires that for every every event  $e_1 \in events_{(u,r_1)}$  received by IdP, there is always an an event  $e_2 \in events_{(u,r_2)}$ , and  $e_1$  and  $e_2$  are equivalent.

Here we give the proof that UPPRESSO system meets the requirement 4.

*Proof:* Here we consider the IdP behave honestly, therefore, we only focus on all events sent to the IdP and prove the equivalence of these events. As the IdP only accepts the HTTP requests to the path /script, /synamicRegistration, /login, loginInfo and /authorize, we will examine each of these paths.

- /script. Based on algorithm 1, we can find that every requests to this path does not carry any parameters and bodies. Therefore, for event  $e_1 \in events_{(u,r_1)}$  and  $e_2 \in events_{(u,r_2)}$ , the HTTPS messages in  $e_1$  and  $e_2$  meet the requirements in definition 5, such that  $e_1$  and  $e_2$  are equivalent.
- /loginInfo. As it defined in algorithm 1, no parameters and bodies are sent to this path. The proof is same as it in path /script.
- /login. According to algorithm 1, the requests carry the body including u's username and password. For event  $e_1 \in events_{(u,r_1)}$  and  $e_2 \in events_{(u,r_2)}$ , the usernames and passwords must be the same. Therefore,  $e_1$  and  $e_2$  are equivalent.
- /dynamicRegistration. As defined in algorithm 1, the requests should carry the body containing  $PID_{RP}$ , Endpoint and Nonce. That is the  $PID_{RP}$  is the result of  $ID_{RP}^{N_U} \mod p$ , where  $N_U$  is unknown to IdP, so that based on definition 4 the  $PID_{RP}$  in  $e_1$  and  $e_2$  are equivalent. The Endpoints and Nonces are all randomly generated unrelated, therefore, they are equivalent in each events. It is proved that  $e_1$  and  $e_2$  are equivalent.
- /authorize. Based on the algorithm 1, it is easy to find that the requests to this path carry the body including  $PID_{RP}$  and Endpoint same as in path /dynamicRegistration. The proof of equivalence is also same as above.

Therefore, we prove that UPPRESSO meets the requirement 4.

**Requirement 5. IRP-Privacy**. There are honest RPs  $r_1, r_2$ , IdP i and the honest users  $u_1, u_2$ . It requires that for every every event  $e_1 \in events_{(u_1, r_2)}$  received by IdP. The following requirements are proposed even if  $r_1$  and  $r_2$  share their states.

- There is always an an event  $e_2 \in events_{(u_2,r_2)}$ , and  $e_1$  and  $e_2$  are equivalent.
- For any user u, the event  $e \in events_{(u_2,r_2)}$  can not linked with specific Account.

Here we give the proof that UPPRESSO system meets the requirement 5.

*Proof:* As the RPs are considered maybe malicious, at the beginning of the proof we only focus on the procedure with legal parameters. Then the RPs are considered able to use illegal parameters and conduct illegal processes.

The events known to the RPs contains the postMessages form IdP script to RP script, and the HTTPS messages from RP script to RP server. However, we can find at algorithm 2 that all the postMessages received by RP script are transmitted to RP server, so that we can only focus on the RPs paths for HTTPS requests. The proof when RPs behave honestly is described as follows.

/script. As it is defined at algorithm 2, every requests to this path does not carry any parameters and bodies. The HTTPS messages in event  $e_1 \in events_{(u_1,r_2)}$  and  $e_2 \in events_{(u_2,r_2)}$  must be equivalent based on definition 5, such that  $e_1$  and  $e_2$  are equivalent.

- /login. According to algorithm 2, the requests to this path do not carry any parameters and bodies. Therefore, same as it in path /script,  $e_1$  and  $e_2$  must be equivalent.
- /startNegotiation. Based on algorithm 2, we can find that the requests to this path only carry the body including  $N_U$ . As  $N_U$  is the new generated random constant number, the messages in  $e_1$  and  $e_2$  are equivalent, so that  $e_1$  and  $e_2$  are equivalent.
- /registrationResult. According to algorithm 2, the requests to this path contains the RegistrationResult in the body. The RegistrationResult's content contains  $PID_{RP}$ , Endpoint, Nonce and the Validity. However, the  $PID_{RP}$  is considered equal with  $N_U$ , and Nonce is the hash of  $N_U$ , so that  $PID_{RP}$ s and Nonces are equivalent. Endpoint is newly generated random string. Validity is generated based on the current time. Therefore, all the parameters in  $e_1$  and  $e_2$  are considered equivalent, such that  $e_1$  and  $e_2$  are equivalent.
- /uploadToken. As it defined algorithm 2, the requests to this path carry the Token. Token consists of  $PID_{RP}$ ,  $PID_U$  and Validity. As it is proved above,  $PID_{RP}$ s and Validitys in each events are equivalent.  $PID_U$  is the result of  $ID_{RP}^{ID_U} \mod p$ , so that  $PID_U$ s are equivalent to RP without knowing  $ID_U$  sue to definition 4. Therefore,  $e_1$  and  $e_2$  are equivalent.

Moreover, with the r2 shared states, users' Accounts at  $r_2$  are known to  $r_1$ . However, as  $ID_{RP}$ s of  $r_1$  and  $r_2$  have the relation  $ID_{RP_{r_1}} \equiv ID_{RP_{r_2}}^n \mod p$ . But n is unknown to RPs due to the discrete logarithm problem. Therefore, the Account at  $r_2$  cannot be linked with the Account at  $r_1$ .

Therefore, the UPPRESSO meets the requirement 5 while RPs behave honestly.

Then we prove that UPPRESSO meets the RP-Privacy requirements even though RPs behave maliciously. The malicious RPs will attempt to steal the data from other process or set the malicious parameters during the login procedure. That is, according to Definition 4, the  $PID_U$ s the Accounts must be equivalent to the attacker as long as the attacker does not know the  $ID_U$ . However, based on algorithm 1 we can find out that IdP does not send  $ID_U$  to any processes, so that  $PID_U$ s the Accounts must be equivalent in each events.

Moreover, another way is that RPs may attempt to treat the Account or  $PID_U$  to be generated incorrectly, but we are going to prove it is impossible.

- RP may lead the login using the forged  $ID_{RP}$  or  $PID_{RP}$  so that  $PID_{U}$ s and Accounts are no more equivalent. However,  $ID_{RP}$  are provided by the Cert which is verified at algorithm 3 line 17, by the IdP's public key set initially and not modified.  $PID_{RP}$  is generated by the  $ID_{RP}$  at line 21 using the honest user generated nonce at line 20. Therefore, it is impossible to lead the honest user to use the illegal  $ID_{RP}$  and  $PID_{RP}$ .
- RP may also lead the same user to upload the identity proof with same  $PID_U$  or Account so that the system is not RP-Privacy according to requirement 5. However, the  $PID_U$  is generated containing the user's generated nonce  $N_U$  so that it is not controlled by the RP. Account is generated as the form  $ID_{RP}^{ID_U} \mod p$ , while RPs may lead the user to use the same  $ID_{RP}$  to generate identity proof. However, the  $ID_{RP}$  is bound with Cert which is verified by the user and it is easy for user to find out the login RP does not coincide the RP name shown on her browser.

In conclusion, we prove that UPPRESSO system meets the requirement 5.

As we have proved the UPPRESSO system meets the requirement 4 and 5, the theorem 2 is proved.