# Optimal Experimental Design: Psychophysics of change point Detection.

# Manuel Villarreal and Arturo Bouzas Mexico City, Mexico

### Abstract

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Detection

#### 1. Introduction

When we have a new research question, we face the problem of design-

3 ing an experiment in order to address it. Typically, one start's by making

4 decisions about the number of participants, how many and what values of

5 our independent variable should we test or how many times should we test

6 each of those values. Most of the time, these choices are made on the basis of

7 previous research on the field. However, it might be the case that there is not

8 enough information on the literature to make these decisions with confidence,

or that the values that are commonly used, do not allow for strong conclu-

o sions. Optimal Experimental Design (OED) offers an statistical alternative

to solve this kind of problems.

## 2. OUTLINE

Experimental design First we need a research question, then the prolem of

4 designin the experiment arises, how many participants should we test, what

- are the values of the independent variable that we should use, how many
- times should we present each of those values, etc. The problem is when

#### 17 2.1. Optimal experimental design

- 18 Elements:
- Design space: what are the elements of the experimental design that we
- want to optimize Utility Function: function that maps points on the design
- space to the real numbers, this function should reflect the objective of the
- 22 experiment, for example if we want to discriminate between two cognitive
- 23 models, the utility function should assign a greater value to an experimental
- <sup>24</sup> design for which the models give different predictions that to designs for
- <sup>25</sup> which the predictions of the models are indistinguishable from one another.

#### 26 3. Optimal Experimental Design: Example

- 27 Why is is detecting changes important for an organism?
- 28 Change detection in probabilistic series.
- Arising problems with experimental design.
- Research question and its statistical interpretation
- Assumtion about the relationship between a subjects response the depen-
- 32 dent variable under study
- Design space for this problem and how to reduce the dimensionality of
- the space by assuming experimental constraints.
- Utility function and its relationship with the objective of the experiment
- Arising problems with utility function and the proposed response func-
- tion. Bayesian solution, assigning a prior distribution to the parameters, the

- less research in a field the more difficult it is to assign an informative prior,
- 39 however, we could use other cognitive models in order to propose a prior
- 40 distribution.
- 3.1. Using a model to generate prior distributions
- Using the prior distribution, the utility function and the definition of
- a design space we can otimize the experimental design in this case we are
- looking for  $\delta\theta^*$  that maximizes the following equation:

$$U(\delta\theta^*) = \max_{\delta\theta} \int_{\beta} \log(\det(I(\beta|\delta\theta))) \pi(\beta) d\beta \tag{1}$$

The previous integral can be approximated via Monte Carlo sampling

#### 46 4. Results

- 4.1. Consruction of the prior distribution
- Prior over model parameters (Gallistel et al 2014) Results Constructing
- 49 the prior: we take a multivariate normal distribution with mean and covari-
- 50 ance equal to the unbiased estimators for both parameters.
- 51 4.2. Optimal design
- Approximating the utility function (integral) throught Monte Carlo simu-
- lation Utility approximation for 2 Design points
- the approximation returns a smooth curve over the 2 point design space.

# 5. Discussion

- Optimal design for the example Properties of the most useful points (they
- 157 land on the points of the curve where the steepness changes most dramati-
- 58 cally)
- Advantages of Optimal Design
- 60 Using models to generte prior distributions.