## Section-B JEE Main-Quadratic Equations

## AI24BTECH11021 - Manvik Muthyapu

- 1) The number of real solutions of the equation  $x^2 3|x| + 2 = 0$  is
  - a) 3
  - b) 2
  - c) 4
  - d) 1
- 2) The real number x when added to its inverse gives the minimum value of the sum at x equal to [2003]
  - a) -2
  - b) 2
  - c) 1
  - d) -1
- 3) Let two numbers have arithmetic mean 9 and geometric mean 4. Then these numbers are the roots of the quadratic equation [2004]
  - a)  $x^2 18x 16 = 0$
  - b)  $x^2 18x + 16 = 0$
  - c)  $x^2 + 18x 16 = 0$
  - d)  $x^2 + 18x + 16 = 0$
- 4) If (1 p) is a root of quadratic equation  $x^2 + px + (1 p) = 0$  then its root are [2004]
  - a) -1, 2
  - b) -1, 1
  - c) 0, -1
  - d) 0, 1
- 5) If one root of the equation  $x^2 + px + 12 = 0$  is 4, while the equation  $x^2 + px + q = 0$  has equal roots, then the value of 'q' is [2004]
  - a) 4
  - b) 12
  - c) 3
  - d)  $\frac{49}{4}$
- 6) In a triangle PQR,  $\angle R = \frac{\pi}{2}$ . If  $\tan\left(\frac{P}{2}\right)$  and  $-\tan\left(\frac{Q}{2}\right)$  are the roots of  $ax^2 + bx + c = 0$ ,  $a \ne 0$  then [2005]
  - a) a = b + c
  - b) c = a + b
  - c) b = c
  - d) b = a + c

7) If both the roots of the quadratic equation  $x^2 - 2kx + k^2 + k - 5 = 0$  are less than 5, then k lies in the interval [2005]

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- a) (5,6]
- b)  $(6, \infty)$
- c)  $(-\infty,4)$
- d) [4,5]
- 8) If the roots of the quadratic equation  $x^2 + px + q = 0$  are  $\tan 30^\circ$  and  $\tan 15^\circ$ , respectively, then the value of 2 + q p is [2006]
  - a) 2
  - b) 3
  - c) 0
  - d) 1
- 9) All the values of m for which both roots of the equation  $x^2 2mx + m^2 1 = 0$  are greater than -2 but less than 4, lie in the interval [2006]
  - a) -2 < m < 0
  - b) m > 3
  - c) -1 < m < 3
  - d) 1 < m < 4
- 10) If *x* is real, the maximum value of  $\frac{3x^2+9x+17}{3x^2+9x+7}$  is [2006]
  - a)  $\frac{1}{2}$
  - b) 41
  - c) 1
  - d)  $\frac{17}{7}$
- 11) If the difference between the roots of the equation  $x^2 + ax + 1 = 0$  is less than  $\sqrt{5}$ , then the set of possible values of a is [2007]
  - a)  $(3, \infty)$
  - b)  $(-\infty, -3)$
  - c) (-3,3)
  - d)  $(-3, \infty)$
- 12) **Statement-1**: For every natural number  $n \ge 2$ ,

$$\frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \dots + \frac{1}{\sqrt{n}} > \sqrt{n}$$

**Statement-2**: For every natural number  $n \ge 2$ ,

$$\sqrt{n(n+1)} < n+1$$

[2008]

- a) Statement-1 is false, Statement-2 is true
- b) Statement-1 is true, Statement-2 is true, Statement-2 is a correct explanation for Statement-1
- c) Statement-1 is true, Statement-2 is true, Statement-2 is not a correct explanation for Statement-1
- d) Statement-1 is true, Statement-2 is false
- 13) The quadratic equations  $x^2 6x + a = 0$  and  $x^2 cx + 6 = 0$  have one root in common. The roots of the first and second equations are integers in the ratio 4:3. Then the common root is [2009]
  - a) 1
  - b) 4
  - c) 3
  - d) 2
- 14) If the roots of the equation  $bx^2 + cx + a = 0$  be imaginary, then for all the real values of x, the expression

$$3b^2x^2 + 6bcx + 2c^2$$
 is: [2009]

- a) less than 4ab
- b) greater than -4ab
- c) less than -4ab
- d) greater than 4ab
- 15) If  $\left|z \frac{4}{z}\right| = 2$ , then the maximum value of |Z| is equal to: [2009]
  - a)  $\sqrt{5} + 1$
  - b) 2
  - c)  $2 + \sqrt{2}$
  - d)  $\sqrt{3} + 1$
- 16) If  $\alpha$  and  $\beta$  are the roots of the equation  $x^2 x + 1 = 0$ , then  $\alpha^{2009} + \beta^{2009} = [2010]$ 
  - a) -1
  - b) 1
  - c) 2
  - d) -2