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# Vector Arithmetic (Section Formula)

## AI24BTECH11021 - Manvik Muthyapu

#### **Question:**

Show that the points  $\mathbf{A}(-6, 10)$ ,  $\mathbf{B}(-4, 6)$  and  $\mathbf{C}(3, -8)$  are collinear and prove that  $AB = \frac{2}{9}AC$ .

### **Solution:**

If this determinant is zero,  $\begin{vmatrix} 1 & 1 & 1 \\ A & B & C \end{vmatrix}$  then A, B, and C are collinear.

Det = 
$$\begin{vmatrix} 1 & 1 & 1 \\ -6 & -4 & 3 \\ 10 & 6 & -8 \end{vmatrix}$$
 =  $1 \cdot (32 - 18) - 1 \cdot (48 - 30) + 1 \cdot (-36 + 40) = 0$ 

 $\therefore$  A, B, and C are collinear.

Using the section formula, if B divides AC in the ratio m:n, then:

$$B\left(\frac{m\cdot 3 + n\cdot (-6)}{m+n}, \frac{m\cdot (-8) + n\cdot 10}{m+n}\right) = (-4, 6)$$

Equating the coordinates, we get

$$\frac{m}{n} = \frac{2}{7}$$

 $\therefore$  It confirms that B divides AC in the ratio 2:7. Since B divides AC in the ratio 2:7, we have:

$$\frac{AB}{AC} = \frac{2}{2+7} = \frac{2}{9}$$

 $\therefore AB = \frac{2}{9}AC$ , Hence proved.

