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NUCLEAR THEORY

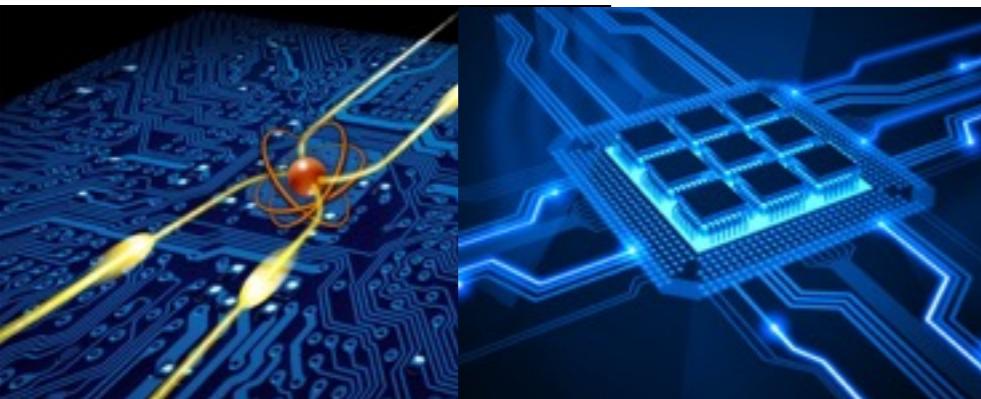


# Quantum Chromodynamics in the Exascale Era with the Emergence of Quantum Computing

Colloquium @ Michigan State University  
April 12, 2018

Martin J Savage

Institute for Nuclear Theory  
University of Washington

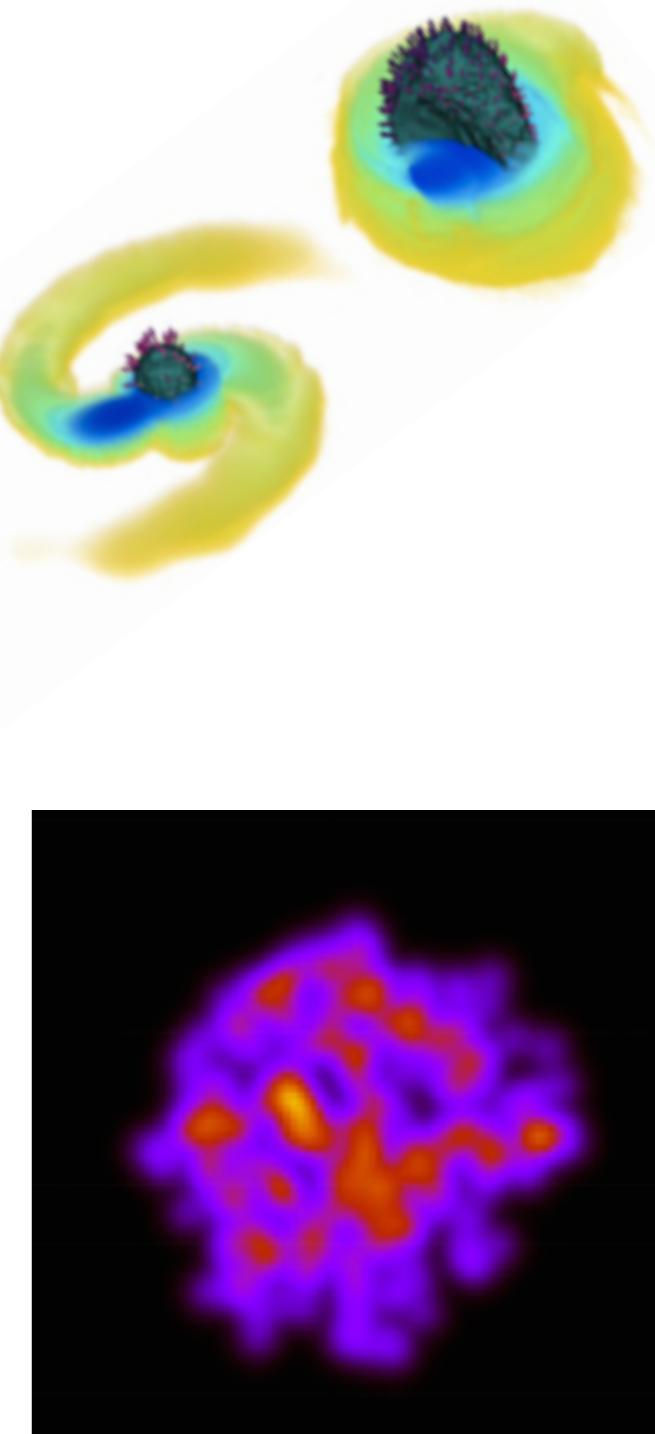
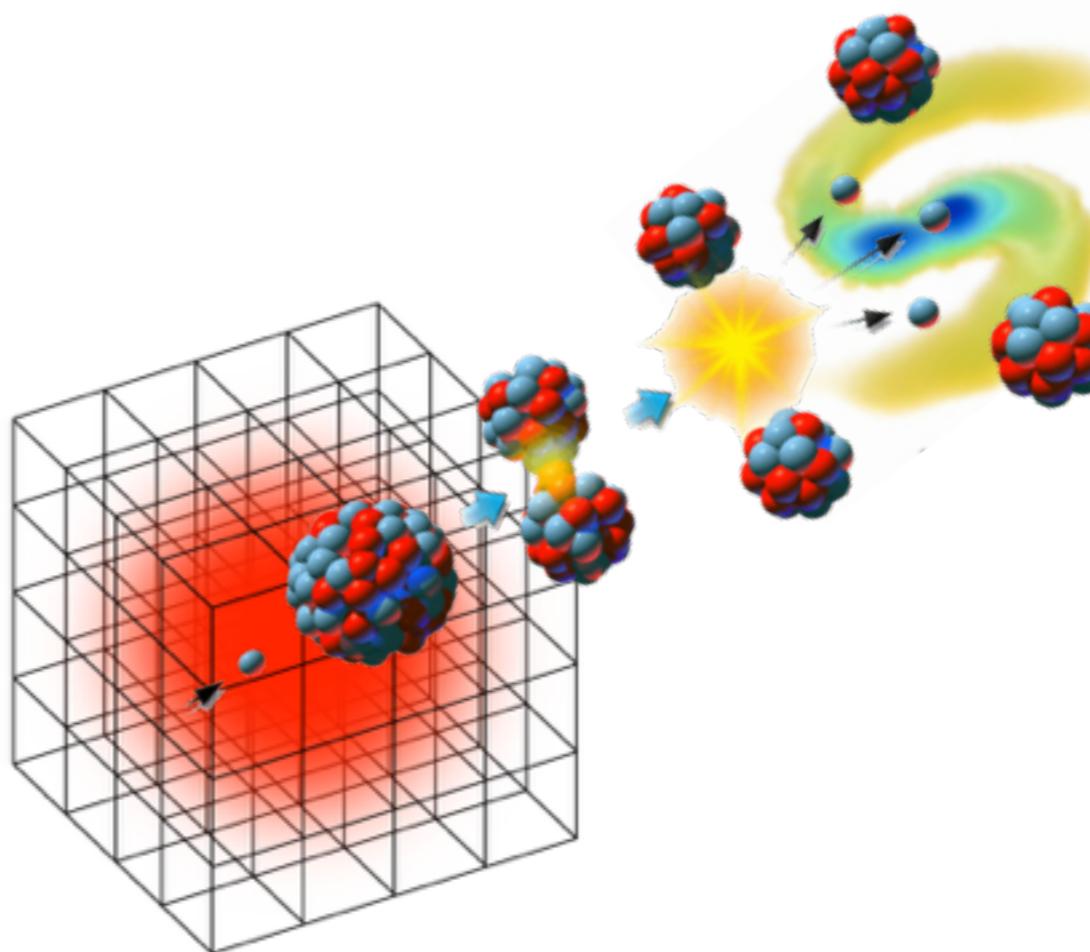


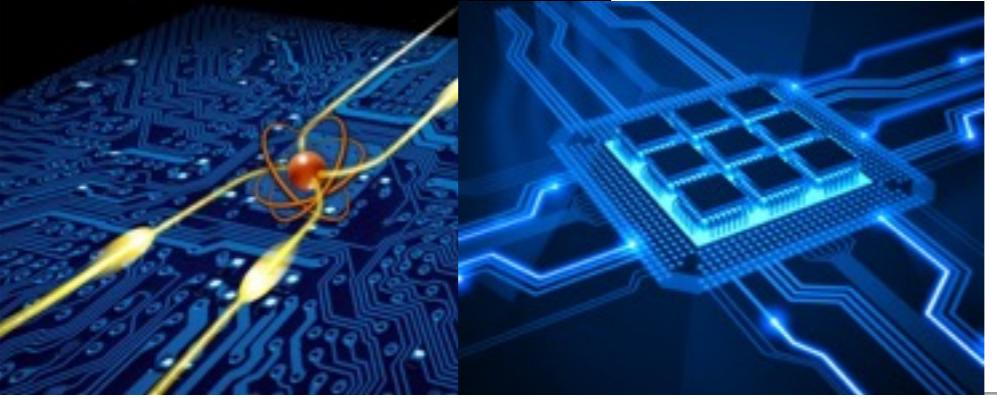
## The Objective

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**Imagine being able to predict — with unprecedented accuracy and precision — the structure of the proton and neutron, and the forces between them, directly from the dynamics of quarks and gluons, and then using this information in calculations of the structure and reactions of atomic nuclei and of the properties of dense neutron stars...**

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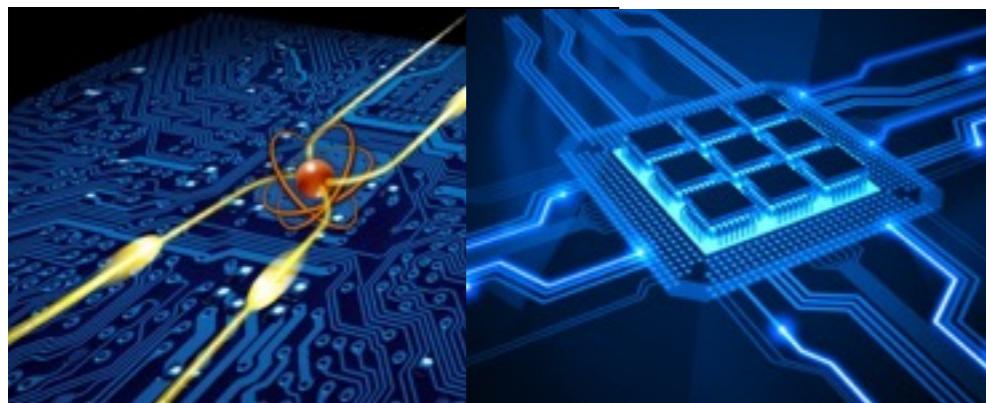


# Nuclear Physics Scientific Objectives and Applications Rely on High-Performance Computing

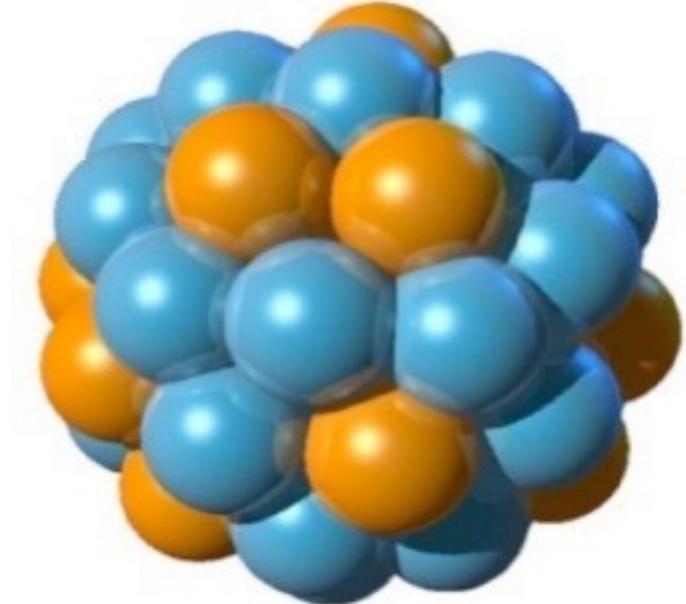
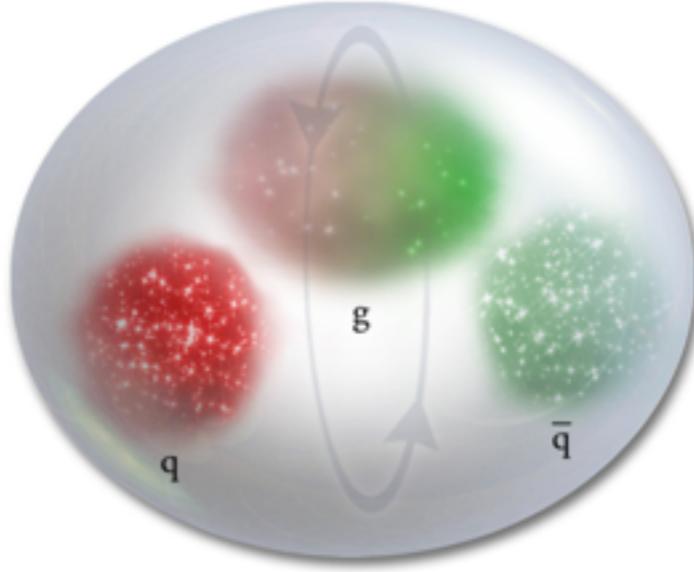
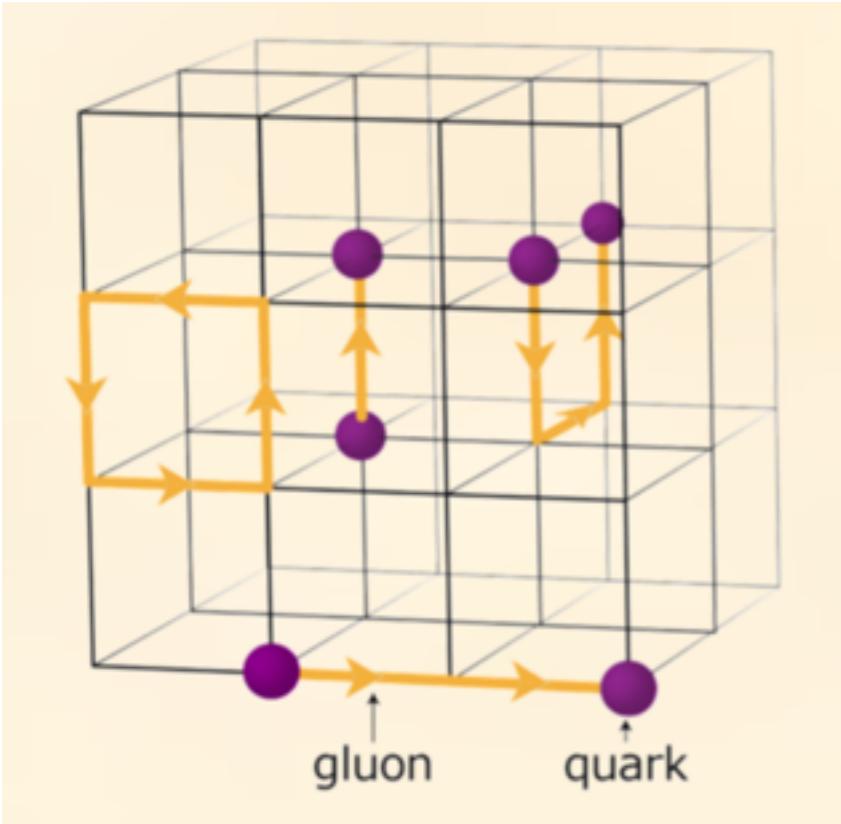
High Performance Computing is essential for NP research program



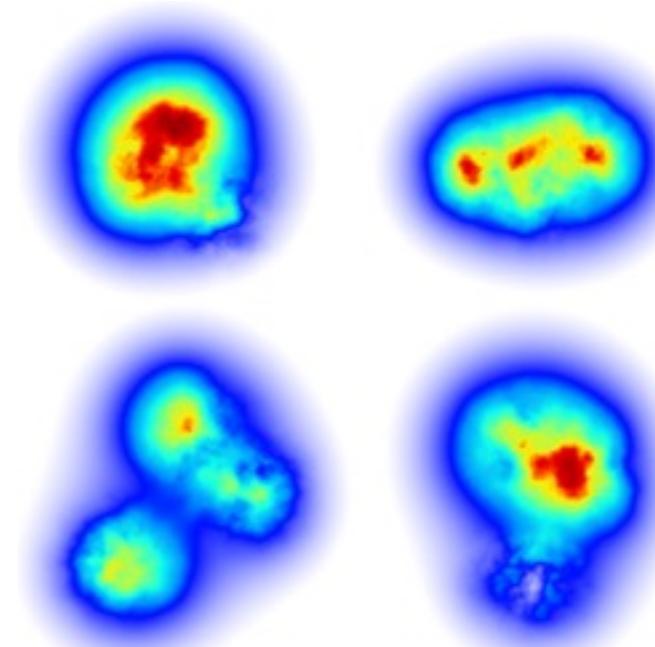
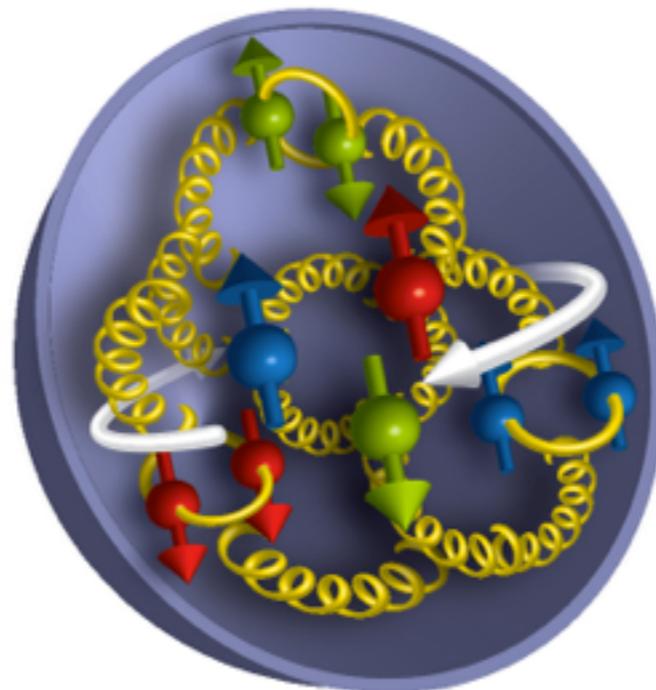
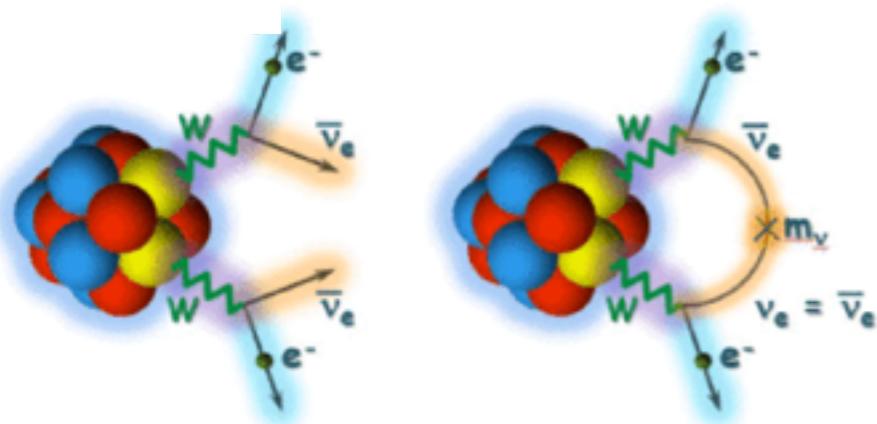
1. Design and Optimization of the vibrant NP experimental program ~ \$1.2 Bn enterprise for construction+operations, ~4000 users
2. Acquisition and handling of experimental data
3. Large-scale simulations and calculations of emergent complex systems from subatomic to cosmological



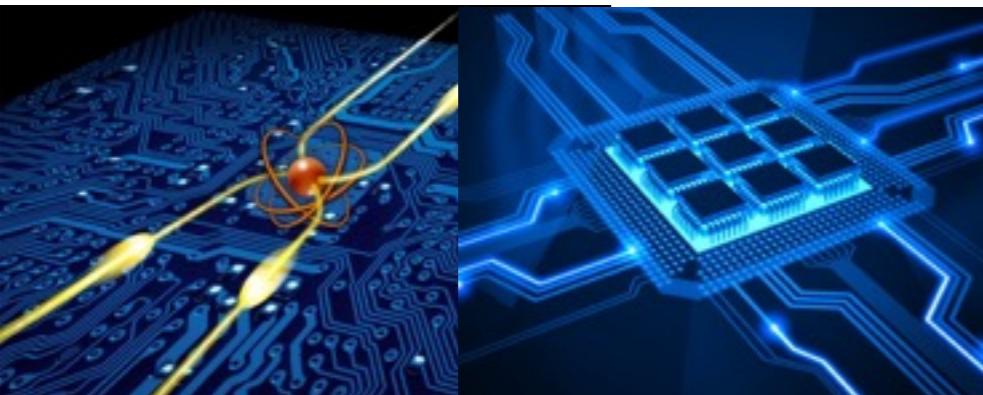
## e.g., Hadrons and Nuclei



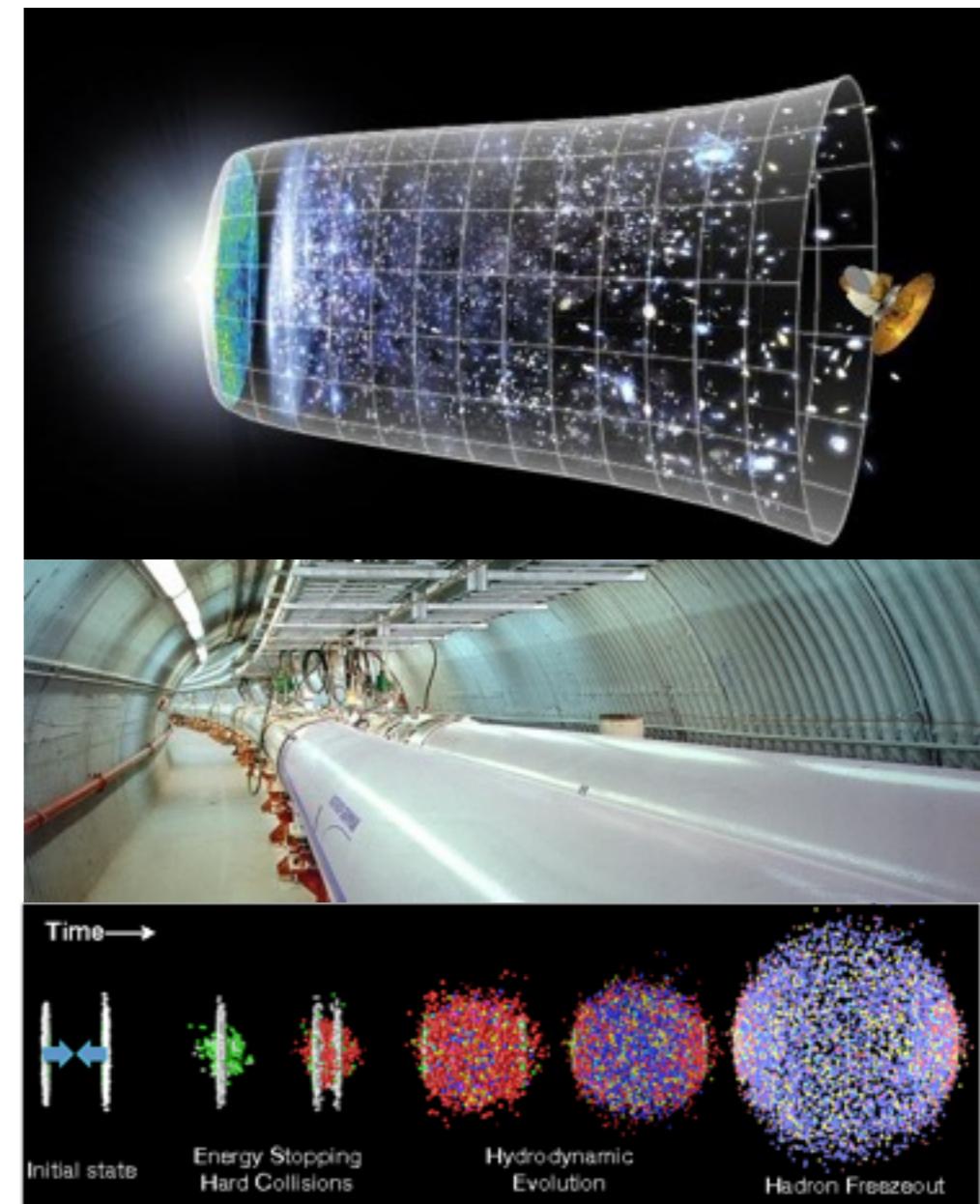
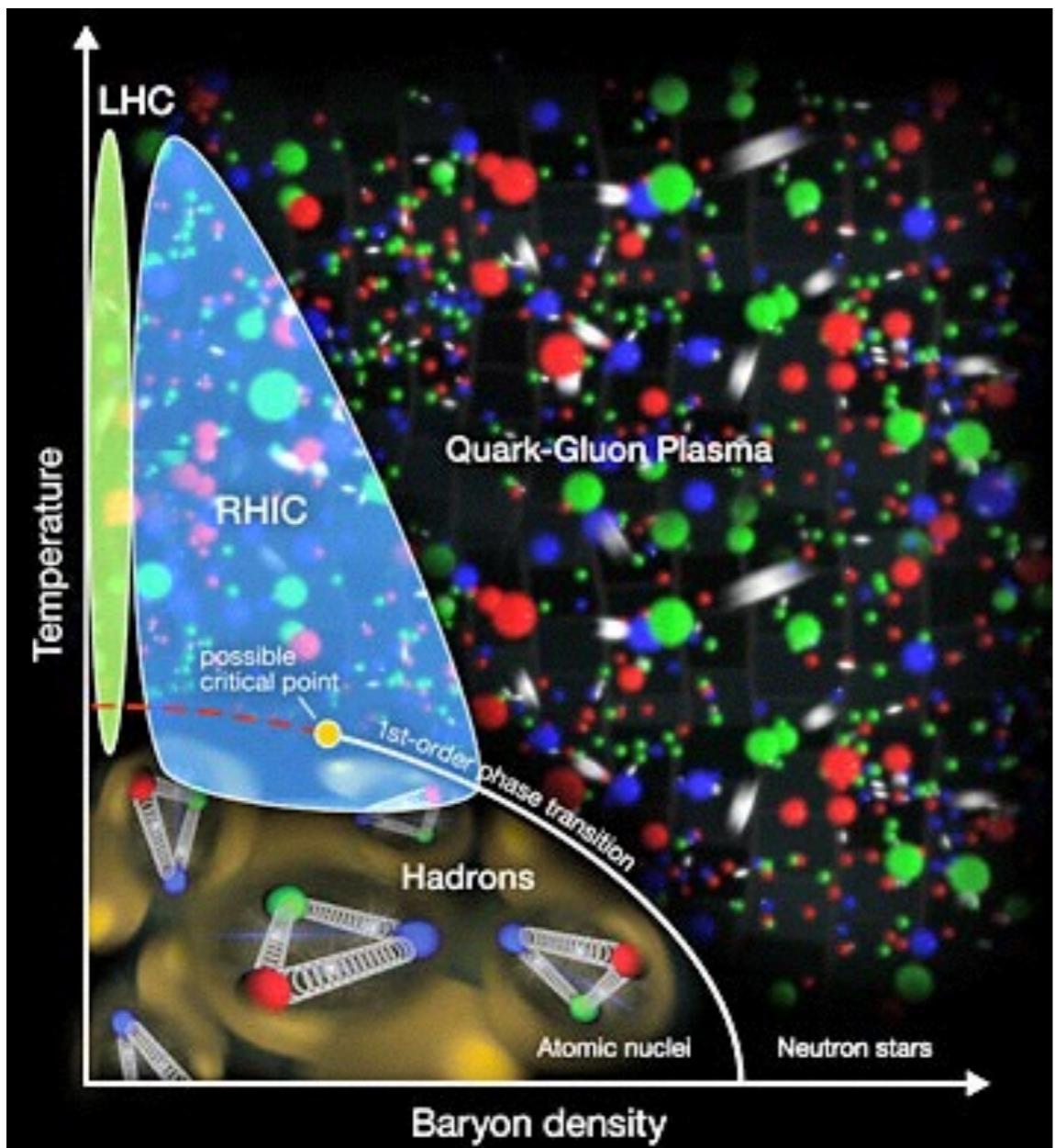
~10% of Leadership Class Computing resources

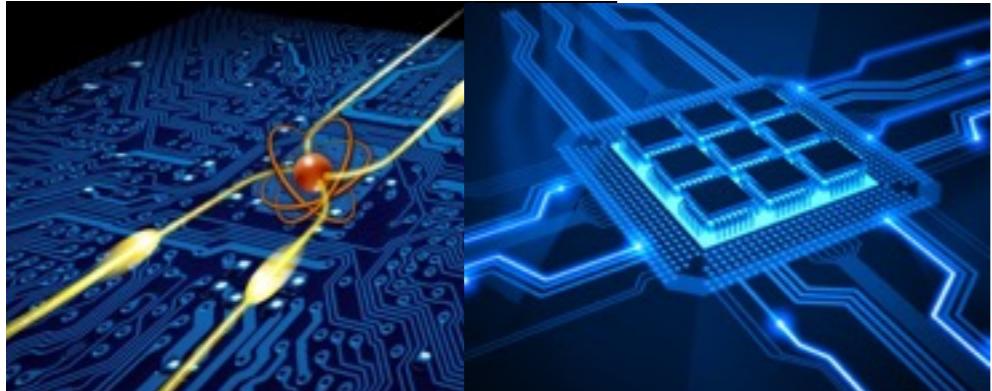


Static quantities with exascale computing ... **reactions and dynamics** remain ``difficult''



# Hot and Dense Matter

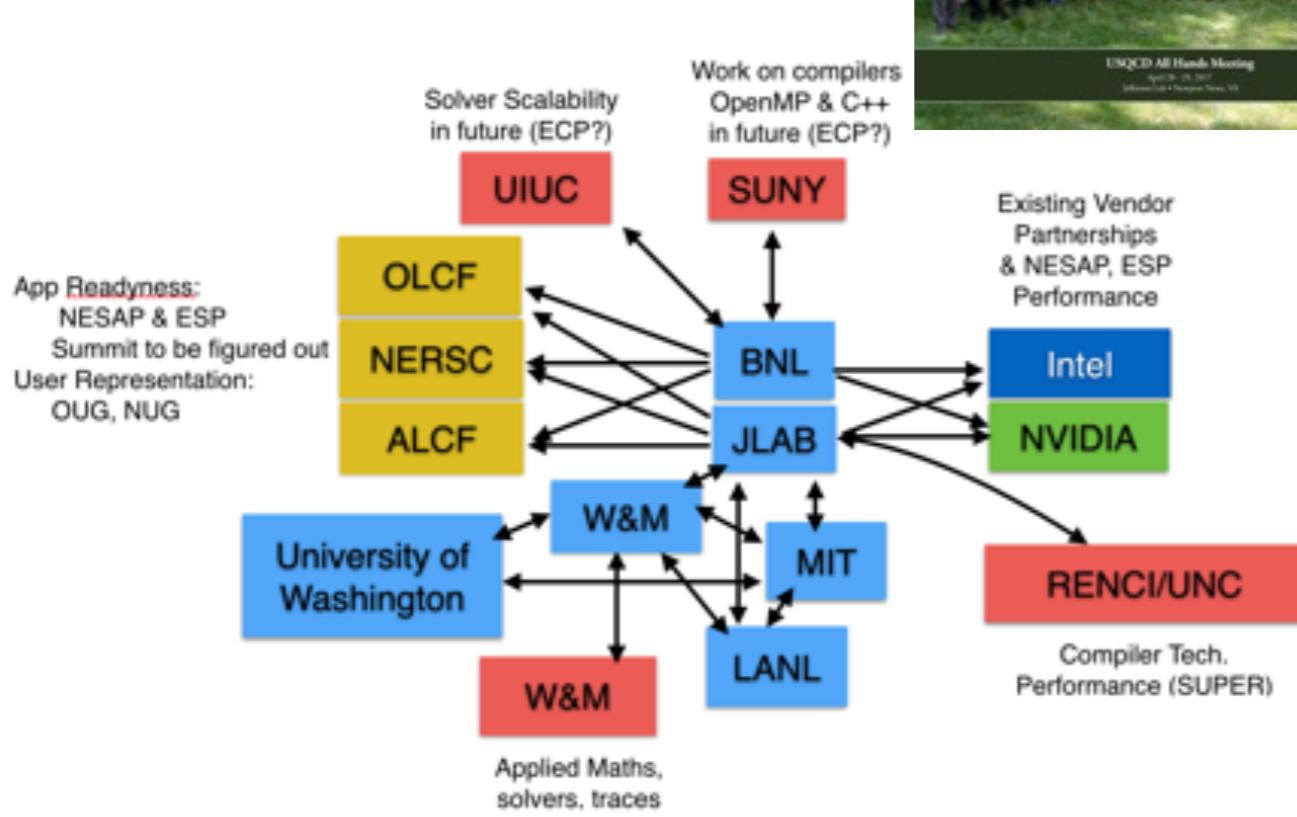




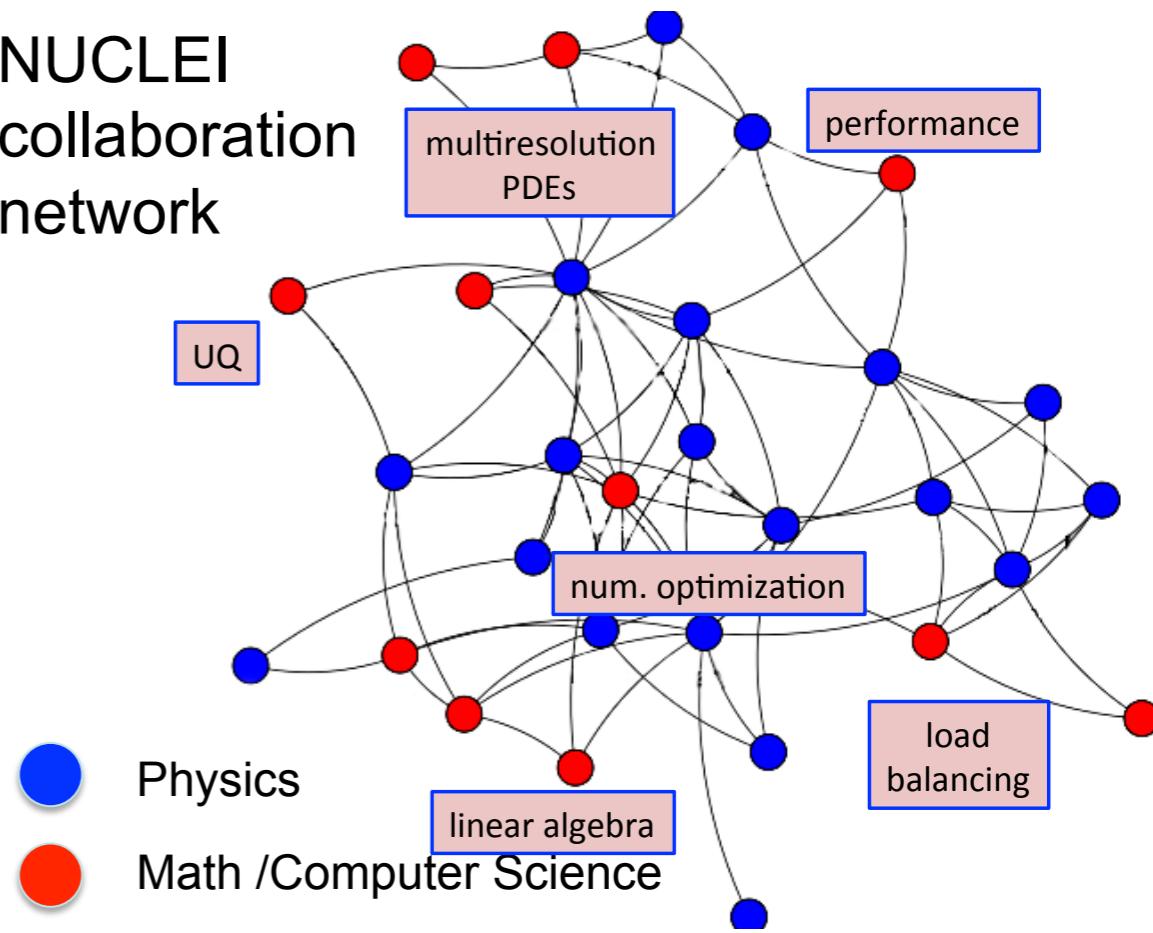
# Essential, Extensive Collaboration

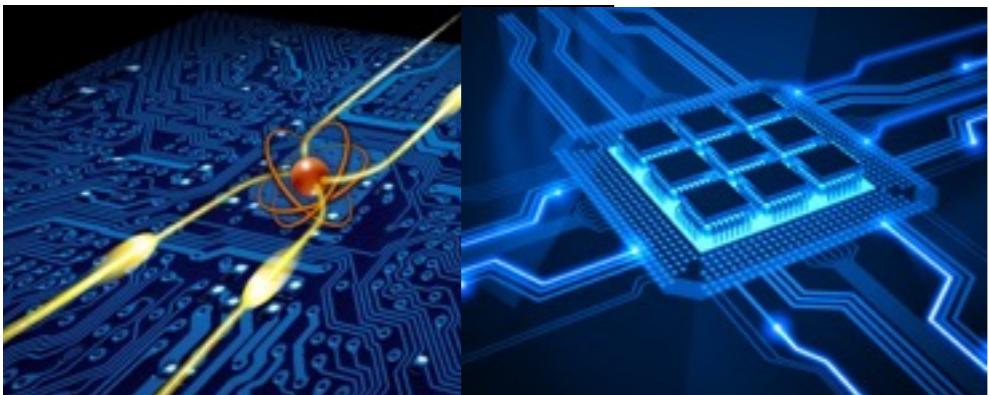


## USQCD-Joint NP-HEP



## NUCLEI collaboration network

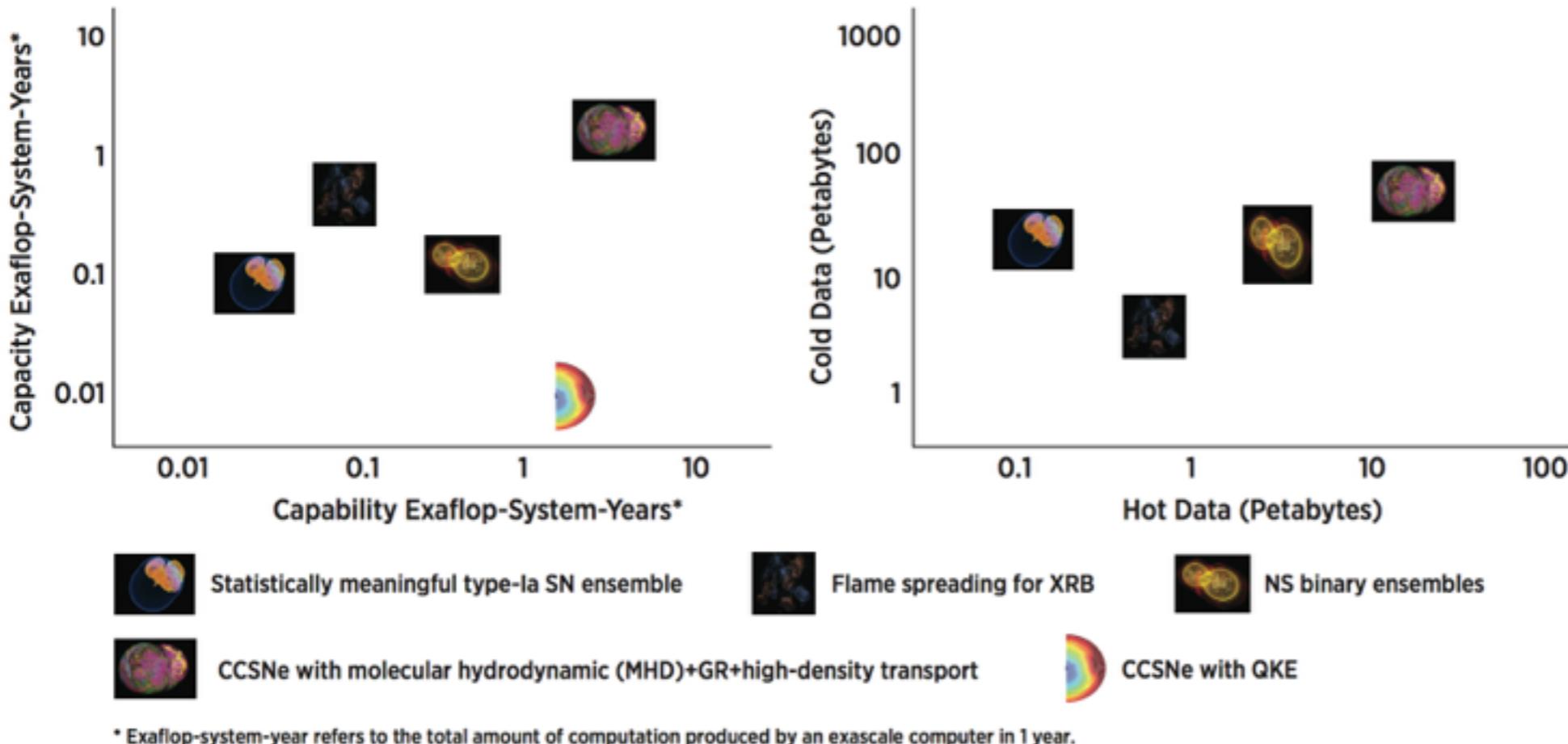




# Exascale Ecosystem for Nuclear Physics

Solve computational problems of extreme complexity and magnitude across a very wide range of physical scales.

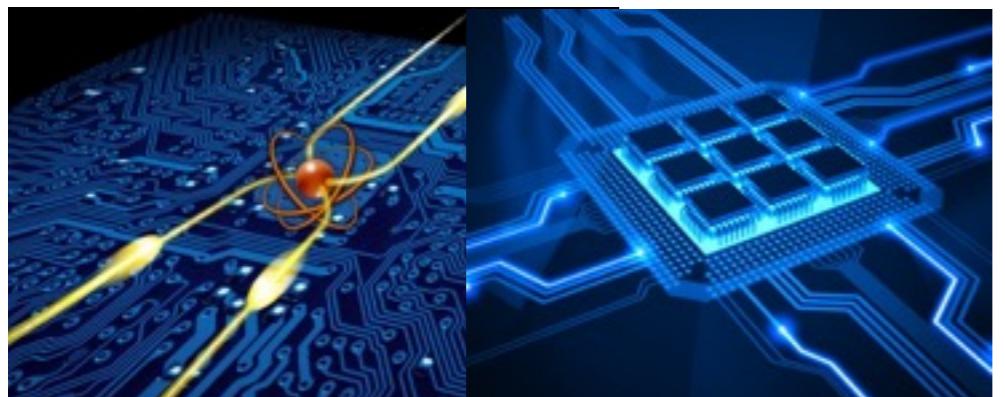
CAPABILITY/CAPACITY RESOURCES VS. HOT/COLD DATA RESOURCES IN 2025  
NUCLEAR ASTROPHYSICS



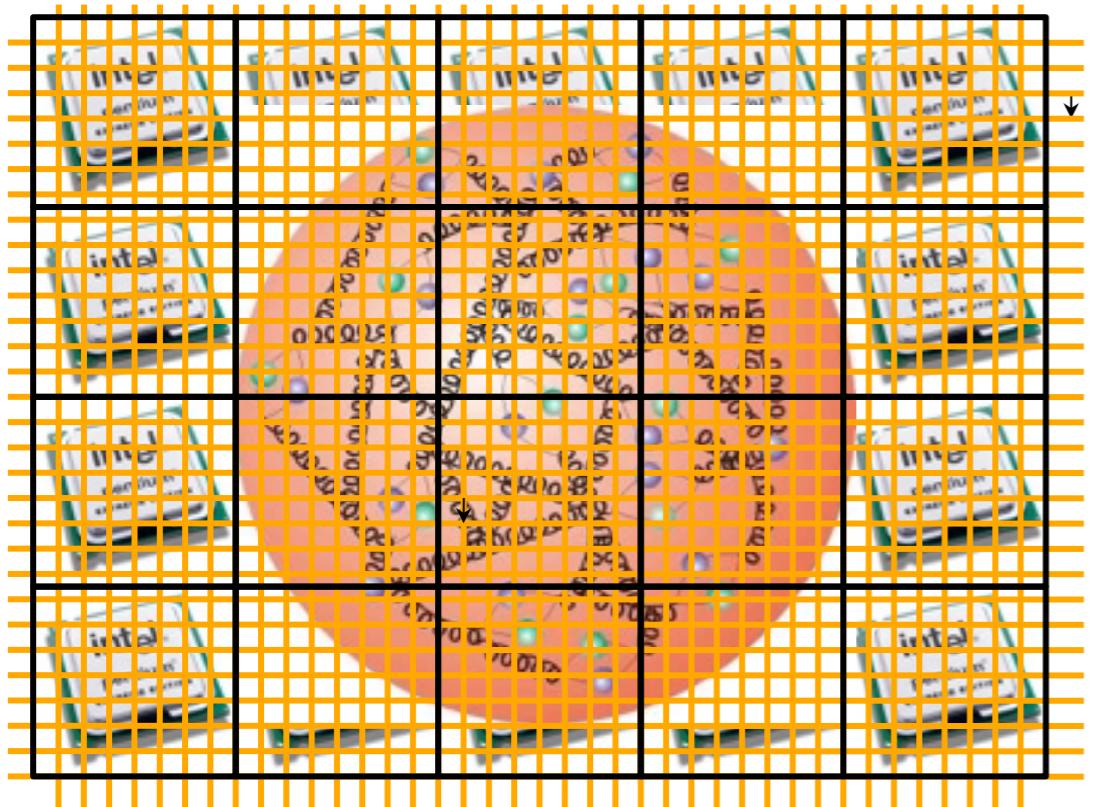
1 Exaflop-System is expected to sustain ~ 100 Petaflops on application code

Multi Exascale need in NP alone, >10x in the US

Exascale machine will be oversubscribed by a large factor



# Lattice Quantum Chromodynamics - Discretized Euclidean Spacetime



Lattice Spacing :

$$a \ll 1/\Lambda\chi$$

(Nearly Continuum)

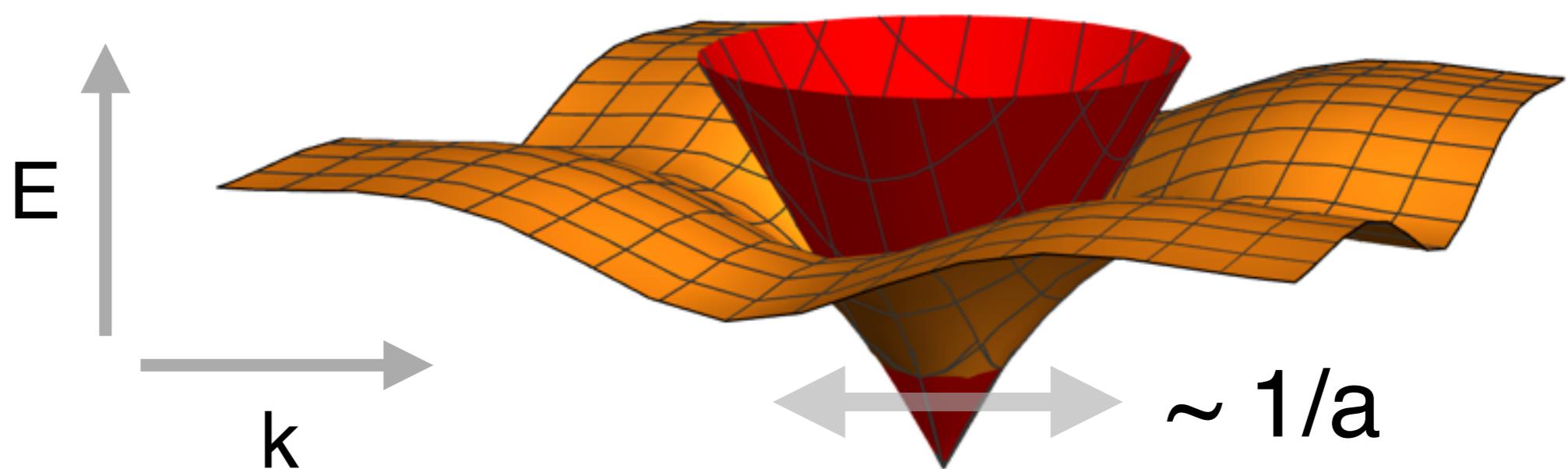
Lattice Volume :

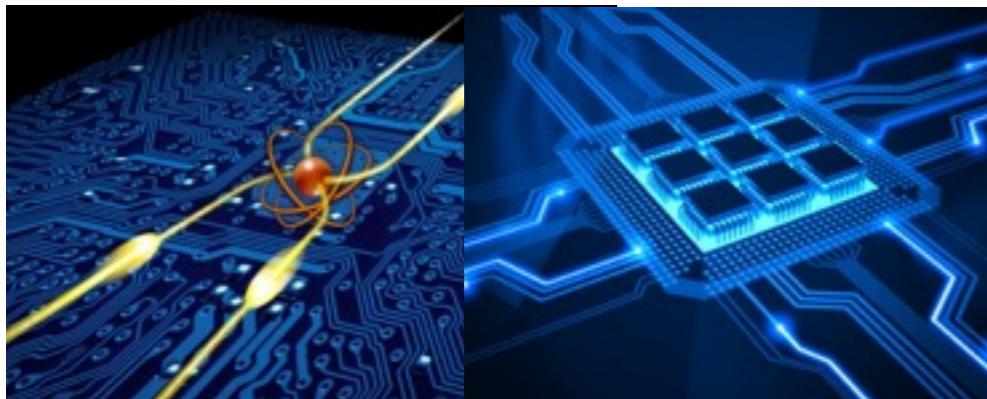
$$m_\pi L \gg 2\pi$$

(Nearly Infinite Volume)

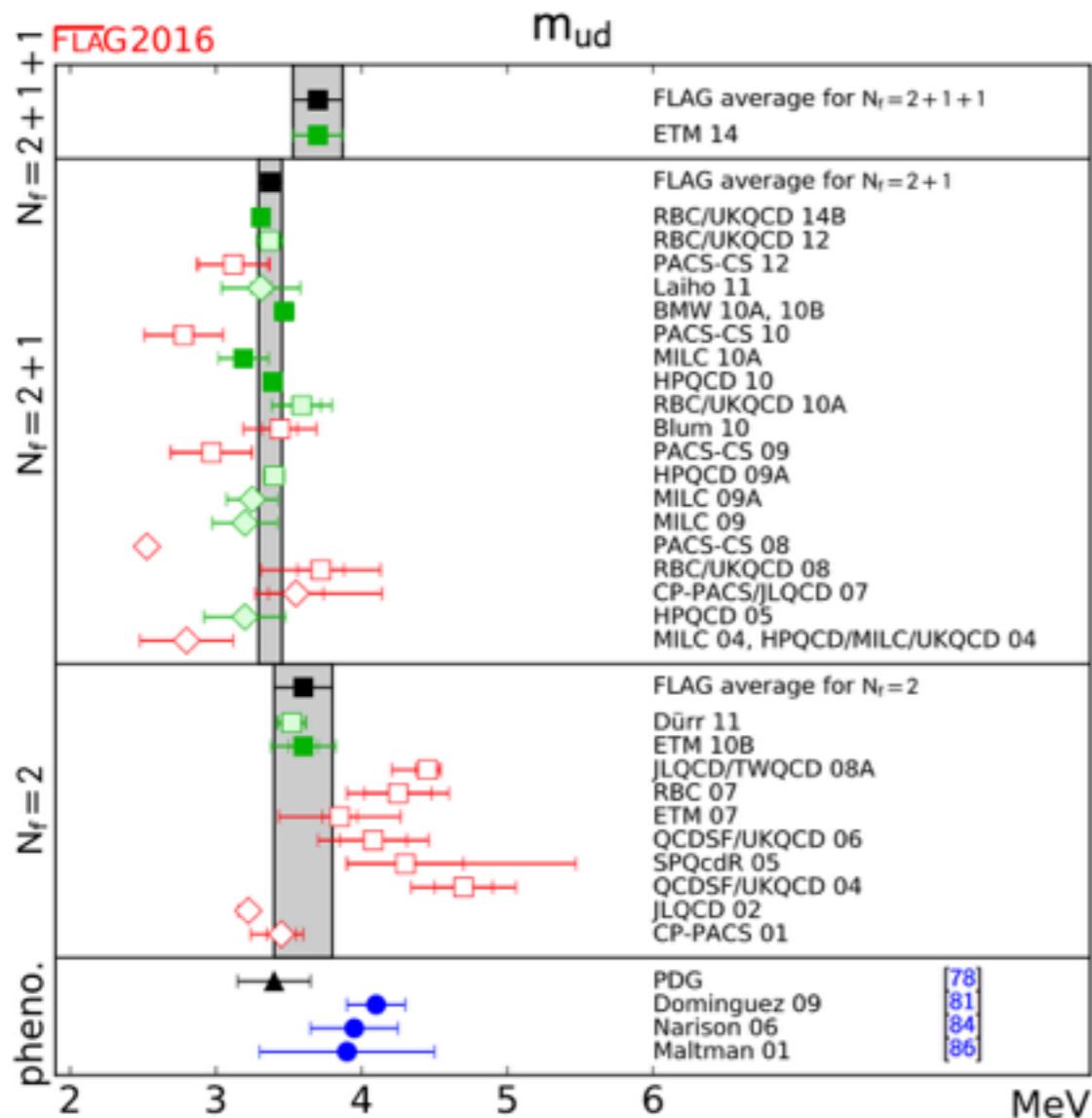
Extrapolation to  $a = 0$  and  $L = \infty$

Systematically remove non-QCD parts of calculation through effective field theories





# Lattice QCD The Quark Masses

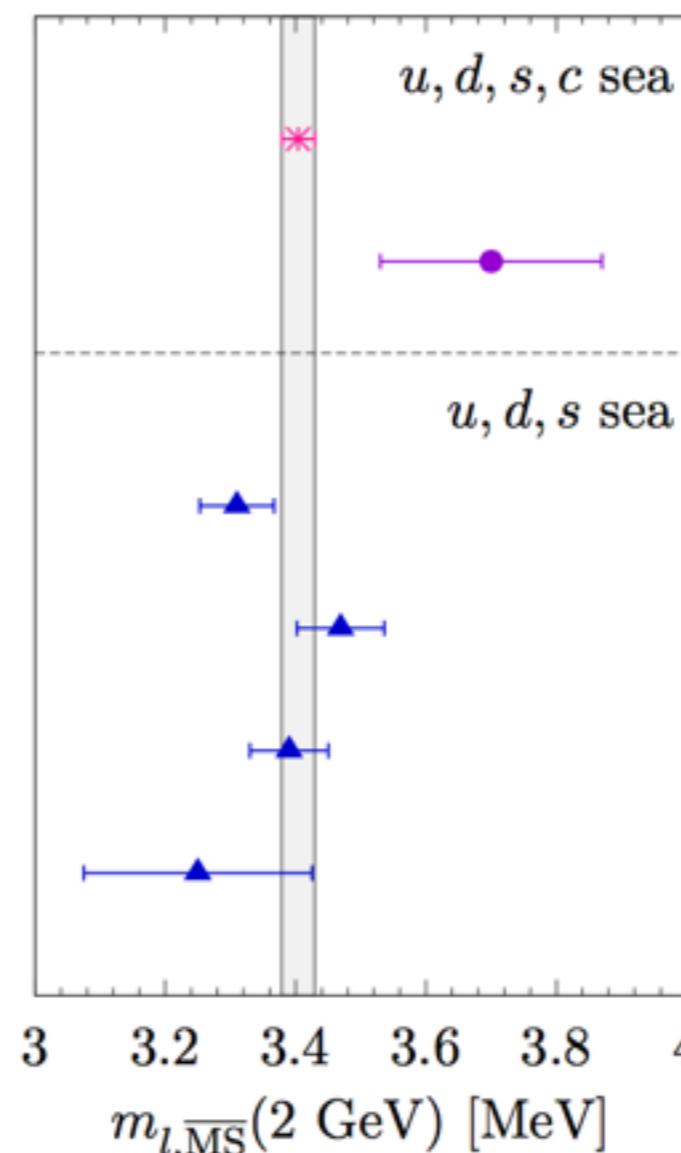


Up-, down-, strange-, charm-, and bottom-quark masses from four-flavor lattice QCD

A. Bazavov,<sup>1</sup> C. Bernard,<sup>2,\*</sup> N. Brambilla,<sup>3,4,†</sup> N. Brown,<sup>2</sup> C. DeTar,<sup>5</sup>  
 A.X. El-Khadra,<sup>6,7</sup> E. Gámiz,<sup>8</sup> Steven Gottlieb,<sup>9</sup> U.M. Heller,<sup>10</sup> J. Komijani,<sup>3,4,11,‡</sup>  
 A.S. Kronfeld,<sup>7,4,§</sup> J. Laiho,<sup>12</sup> P.B. Mackenzie,<sup>7</sup> E.T. Neil,<sup>13,14</sup> J.N. Simone,<sup>7</sup>  
 R.L. Sugar,<sup>15</sup> D. Toussaint,<sup>16,¶</sup> A. Vairo,<sup>3,\*\*</sup> and R.S. Van de Water<sup>7</sup>

(Fermilab Lattice, MILC, and TUMQCD Collaborations)

e-Print: [arXiv:1802.04248 \[hep-lat\]](https://arxiv.org/abs/1802.04248)



$$m_{l,\overline{MS}}(3 \text{ GeV}) = 3.073(13)_{\text{stat}}(07)_{\text{syst}}(10)_{\alpha_s(04)} f_{\pi,\text{PDG}} \text{ MeV},$$

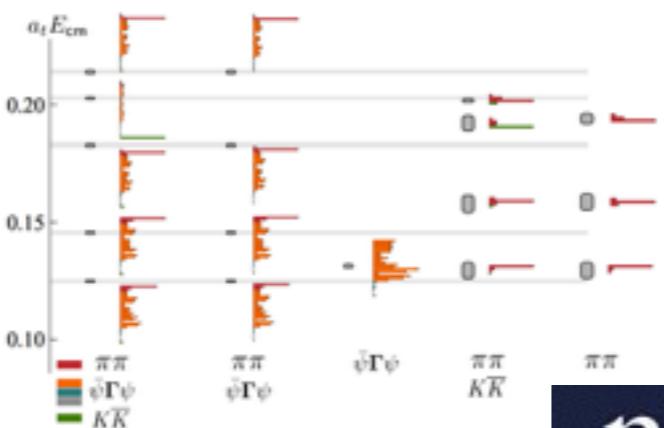
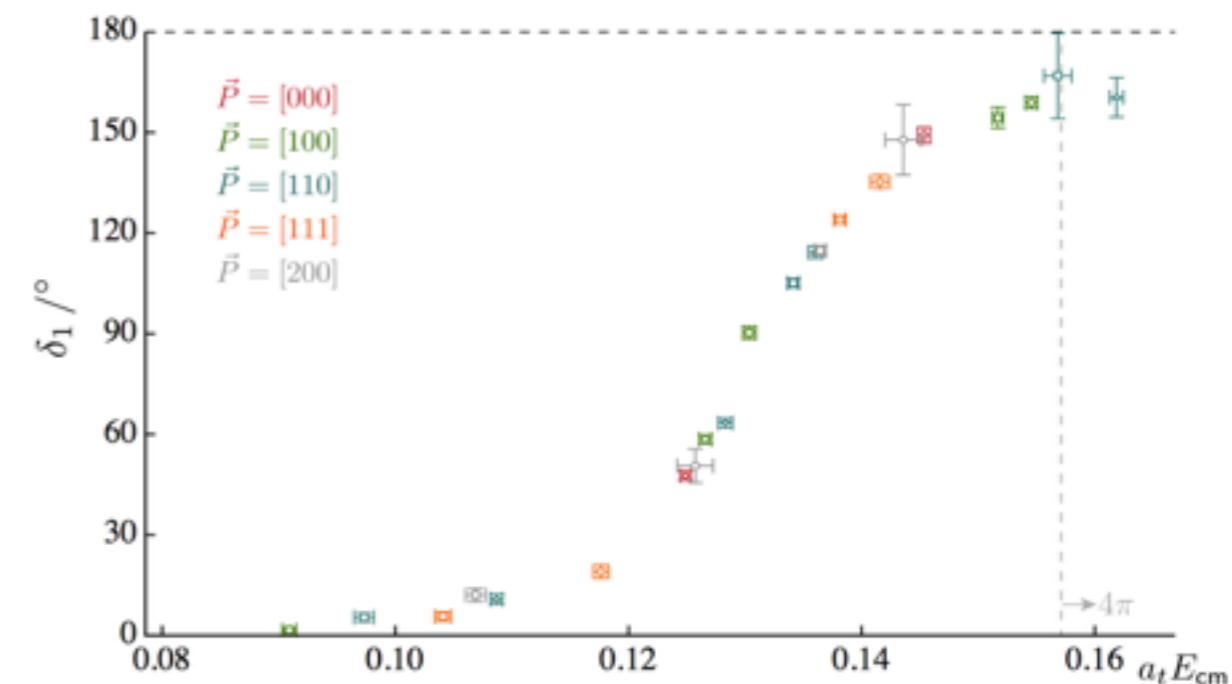
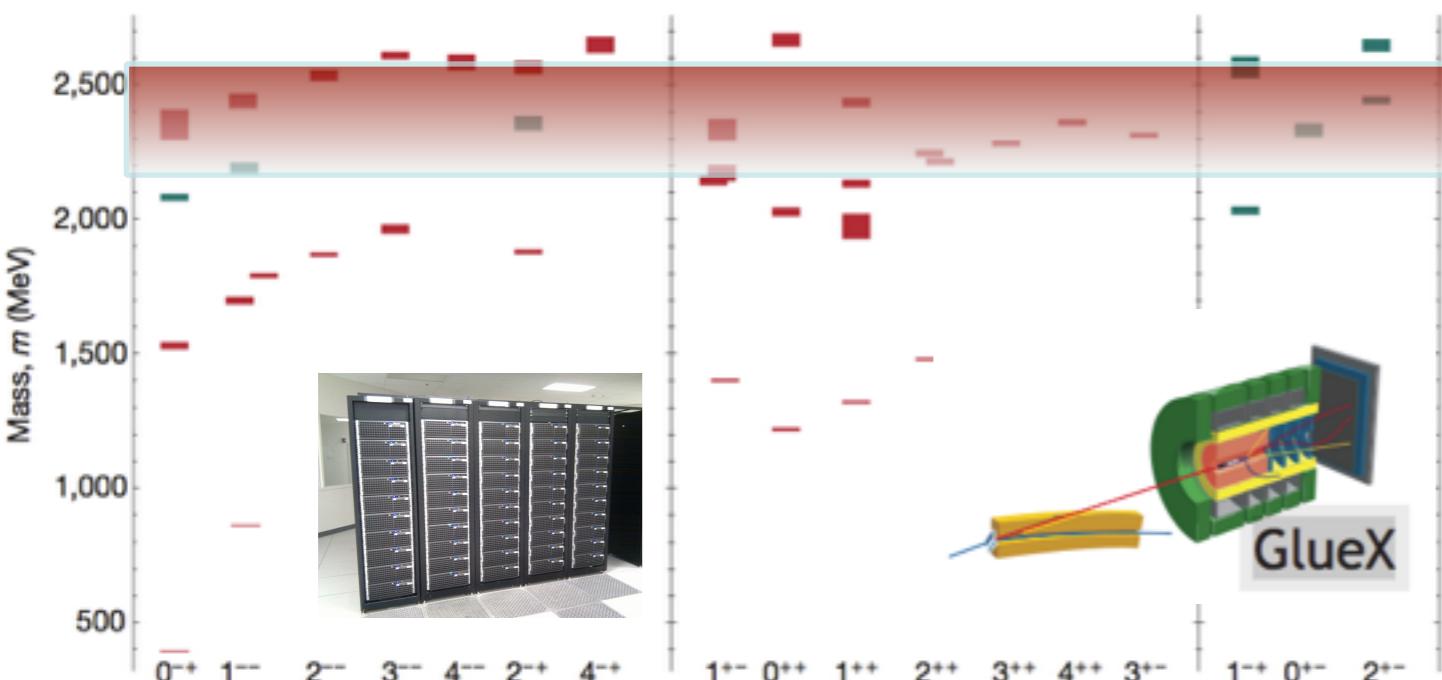
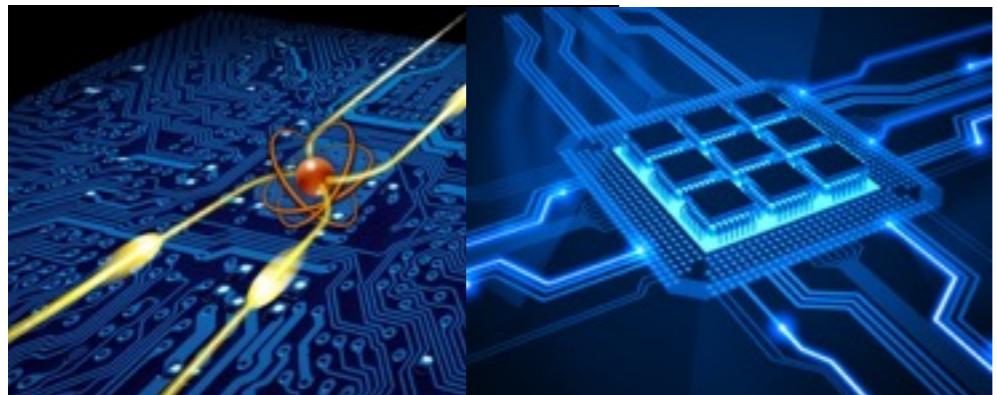
$$m_{u,\overline{MS}}(3 \text{ GeV}) = 1.912(16)_{\text{stat}}(29)_{\text{syst}}(06)_{\alpha_s(03)} f_{\pi,\text{PDG}} \text{ MeV},$$

$$m_{d,\overline{MS}}(3 \text{ GeV}) = 4.234(27)_{\text{stat}}(32)_{\text{syst}}(14)_{\alpha_s(05)} f_{\pi,\text{PDG}} \text{ MeV},$$

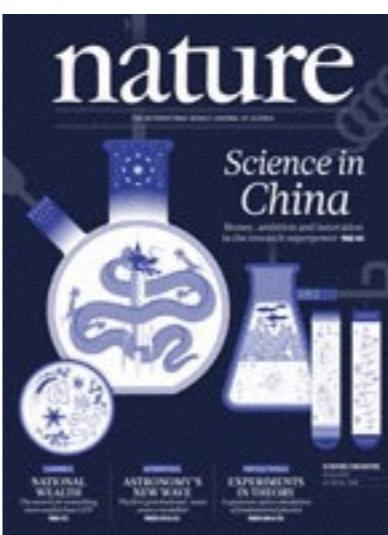
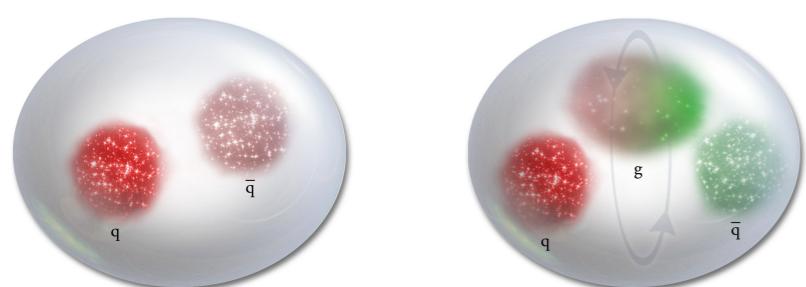
$$m_{s,\overline{MS}}(3 \text{ GeV}) = 83.53(36)_{\text{stat}}(16)_{\text{syst}}(27)_{\alpha_s(11)} f_{\pi,\text{PDG}} \text{ MeV},$$

$$m_{c,\overline{MS}}(3 \text{ GeV}) = 984.3(4.2)_{\text{stat}}(1.6)_{\text{syst}}(3.2)_{\alpha_s(0.6)} f_{\pi,\text{PDG}} \text{ MeV}.$$

# Lattice QCD Spectroscopy and GlueX



Pattern of states suggest gluonic excitations

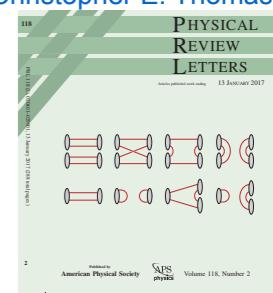


NATURE | REVIEW

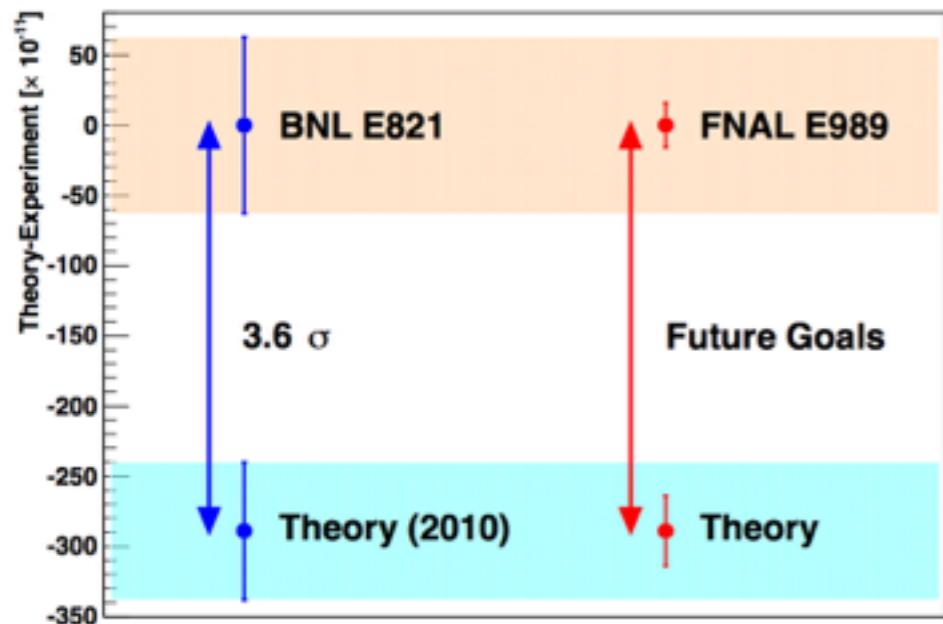
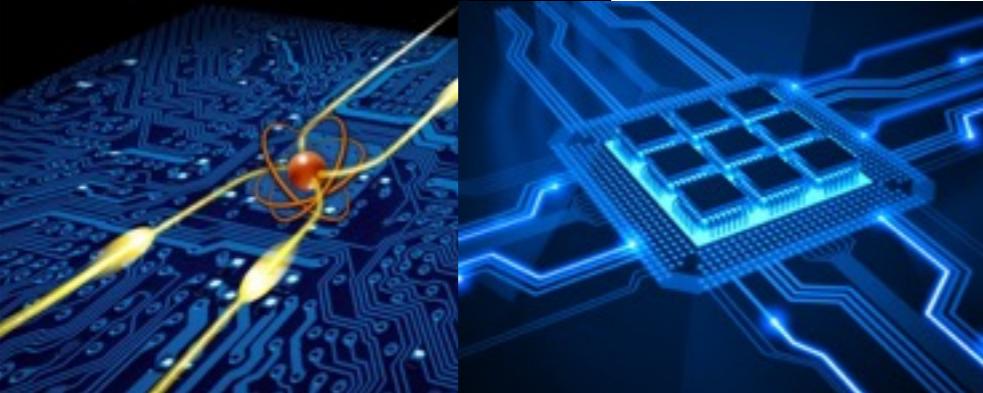
Searching for the rules that govern hadron construction

Matthew R. Shepherd, Jozef J. Dudek & Ryan E. Mitchell

Nature 534, 487–493 (23 June 2016) | doi:10.1038/nature18011



# Lattice QCD Fundamental Symmetries



Dave Hertzog, 2016

**Figure 1.** Comparison of Experiment to Theory at present and expected on completion of future Fermilab E989 and factor of  $\sim 2$  improvements in HVP and HLbL calculations.

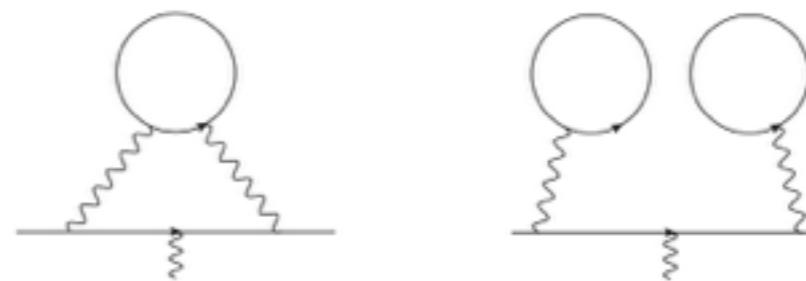
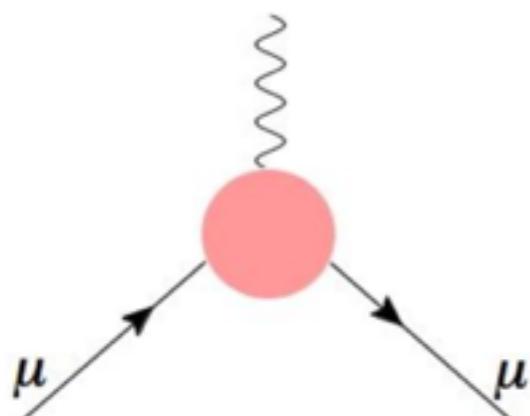
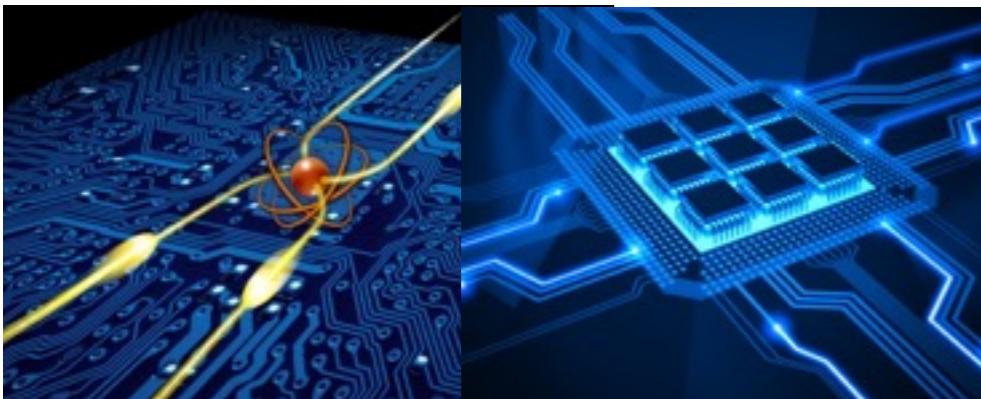


FIG. 1. Quark-connected (left) and quark-disconnected (right) diagram for the calculation of  $a_\mu^{\text{HVP LO}}$ . We do not draw gluons but consider each diagram to represent all orders in QCD.

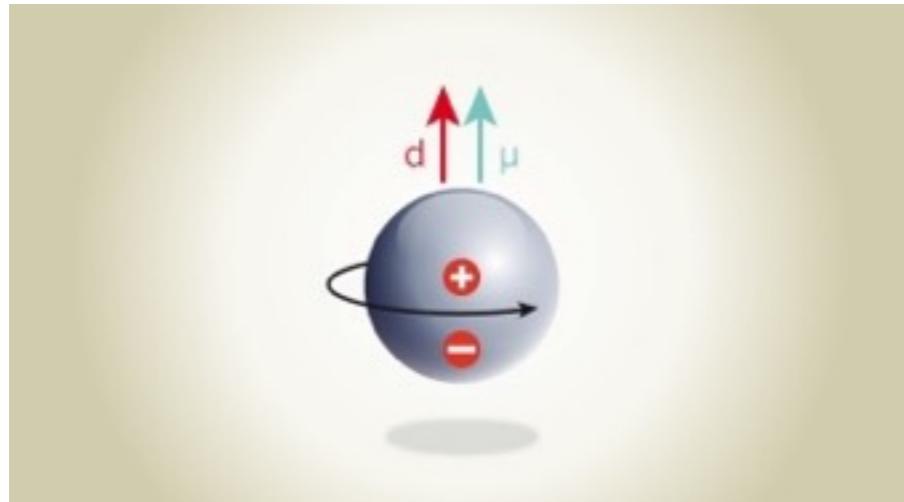


Calculation of the hadronic vacuum polarization contribution to the muon anomalous magnetic moment

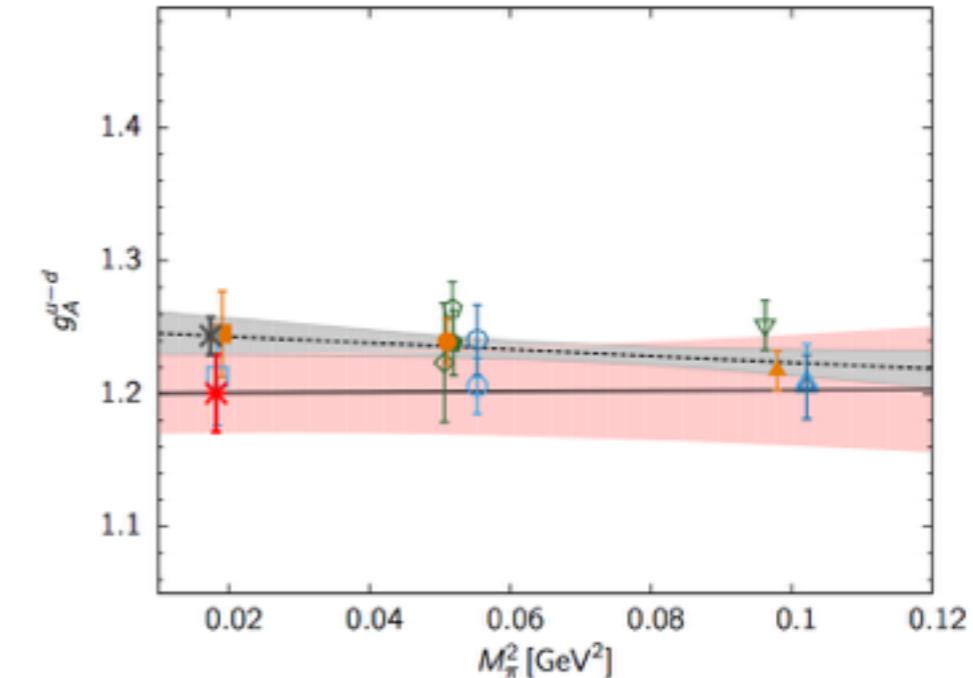
T. Blum,<sup>1</sup> P.A. Boyle,<sup>2</sup> V. Gülpers,<sup>3</sup> T. Izubuchi,<sup>4,5</sup> L. Jin,<sup>1,5</sup>  
C. Jung,<sup>4</sup> A. Jüttner,<sup>3</sup> C. Lehner,<sup>4,\*</sup> A. Portelli,<sup>2</sup> and J.T. Tsang<sup>2</sup>  
(RBC and UKQCD Collaborations)



# Lattice QCD Fundamental Symmetries

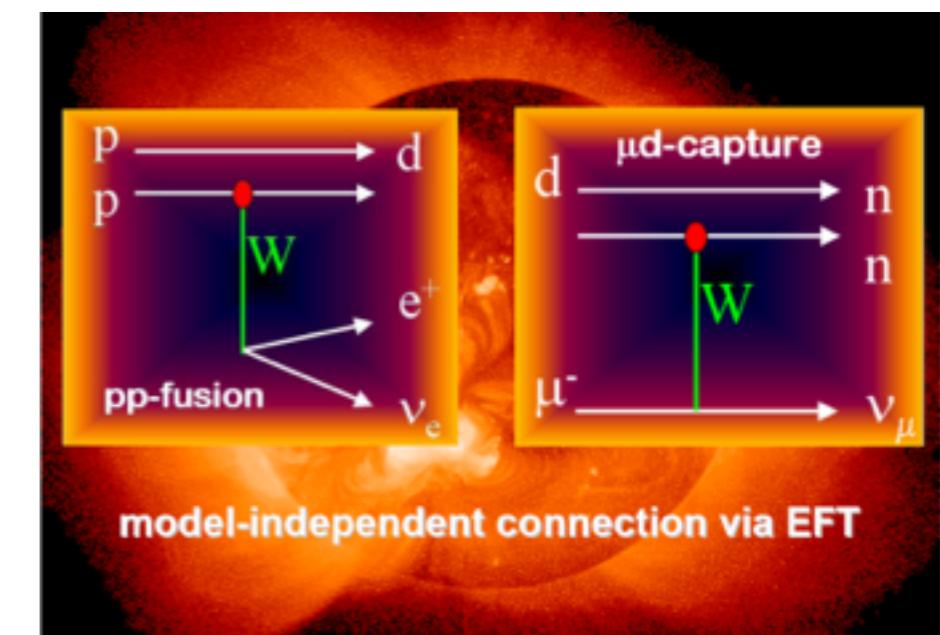
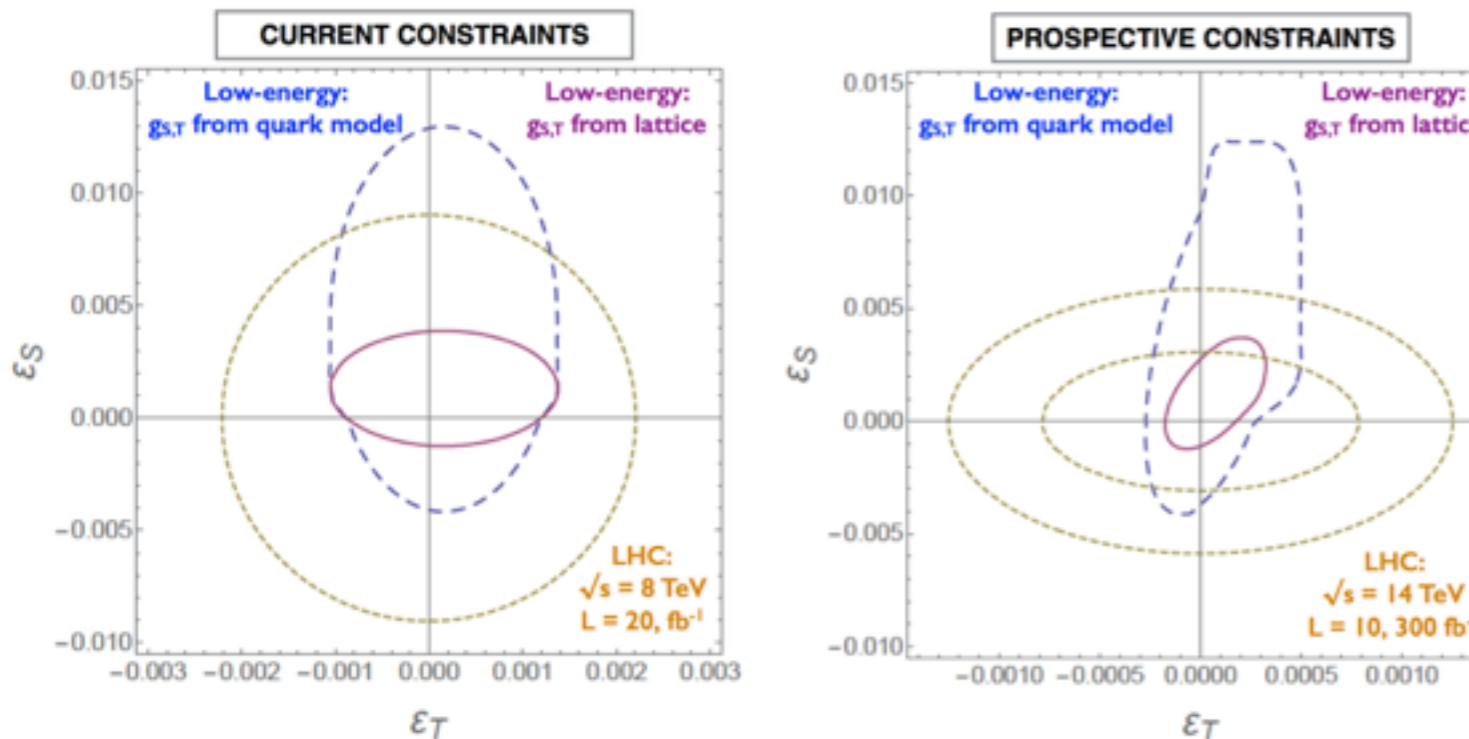


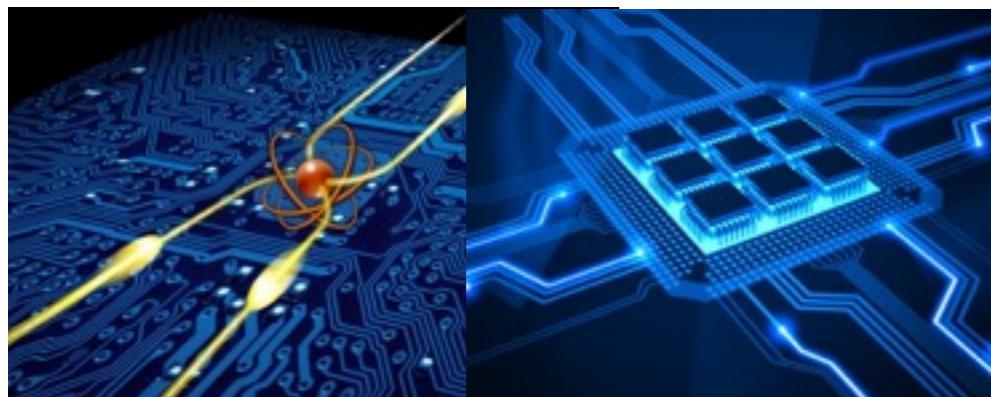
Andrea Shindler and Huey-Wen Lin [MSU]



Isovector and flavor-diagonal charges of the nucleon

Rajan Gupta, Tanmoy Bhattacharya, Yong-Chull Jang, Huey-Wen Lin,  
Boram Yoon e-Print: arXiv:1801.03130 [hep-lat]





# Lattice QCD

## QCD to Nuclear Forces: First Steps



Zohreh Davoudi led this work

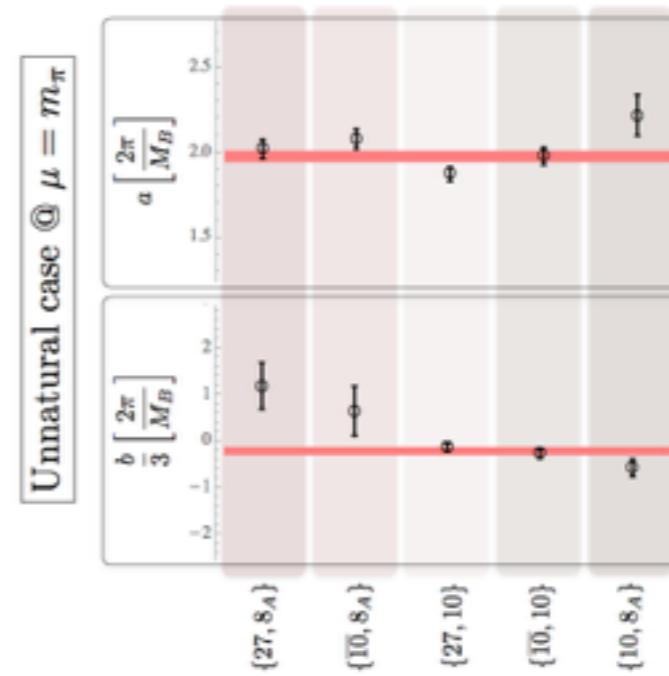


$N_f = 3$ ,  $m_\pi = 0.806$  GeV,  $a = 0.145(2)$  fm



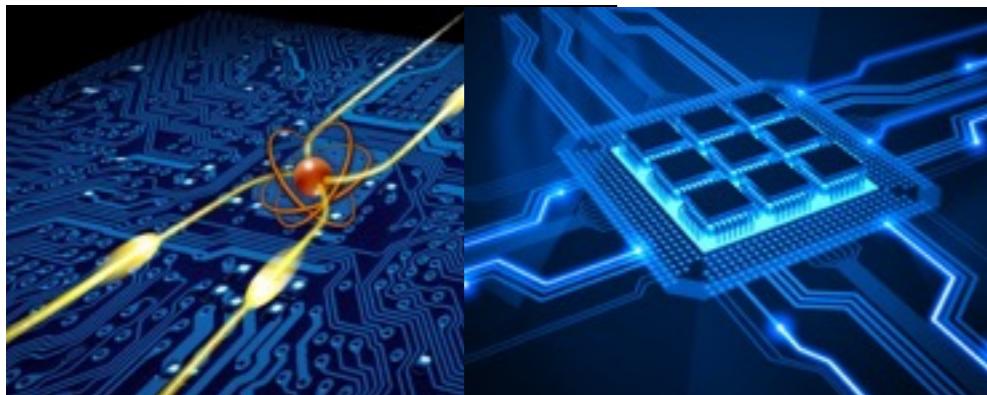
$$\begin{aligned} \mathcal{L}_{BB}^{(0)} = & -c_1 \text{Tr}(B_i^\dagger B_i B_j^\dagger B_j) - c_2 \text{Tr}(B_i^\dagger B_j B_j^\dagger B_i) - c_3 \text{Tr}(B_i^\dagger B_j^\dagger B_i B_j) \\ & - c_4 \text{Tr}(B_i^\dagger B_j^\dagger B_j B_i) - c_5 \text{Tr}(B_i^\dagger B_i) \text{Tr}(B_j^\dagger B_j) - c_6 \text{Tr}(B_i^\dagger B_j) \text{Tr}(B_j^\dagger B_i). \end{aligned}$$

pionless theory, SU(3) symmetric point

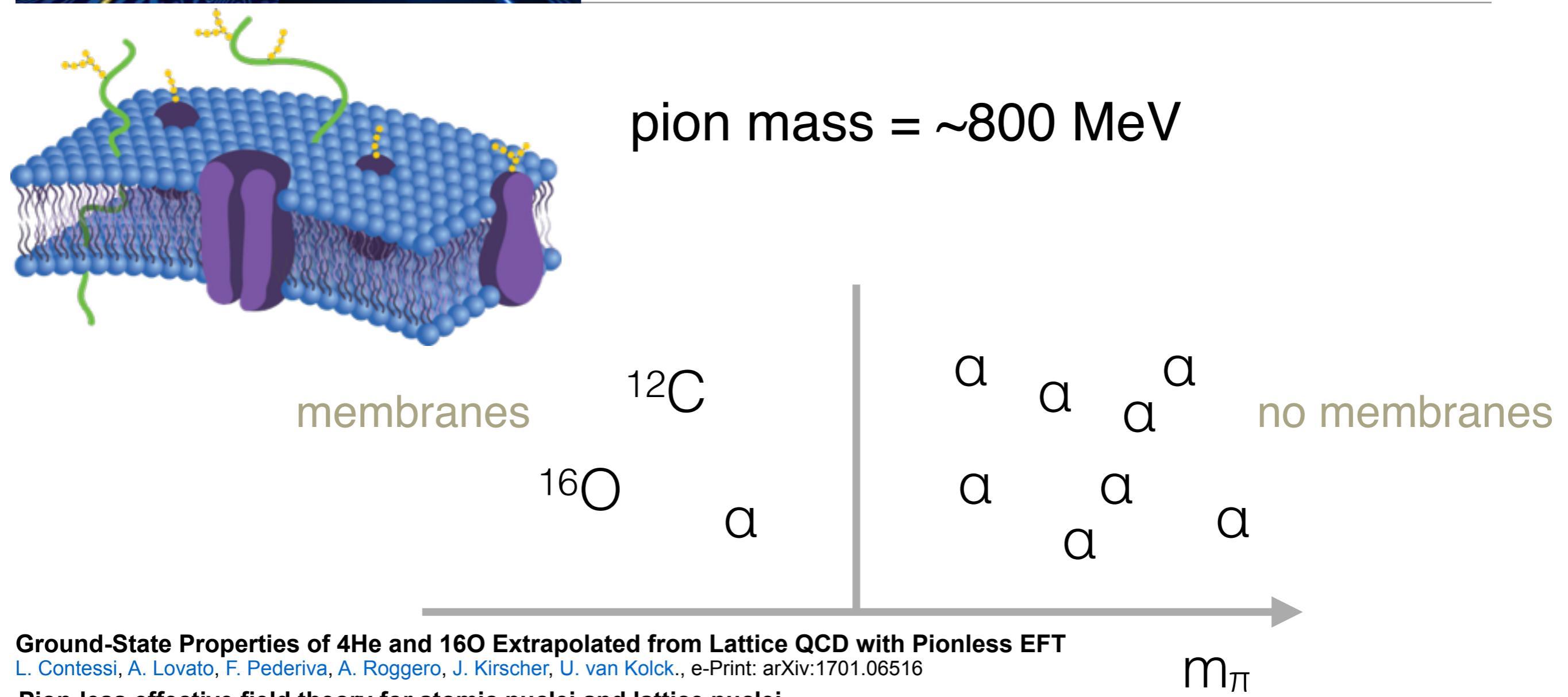


$$\mathcal{L}_{BB}^{(0)} = -a(\Psi_{\mu\nu\rho}^\dagger \Psi^{\mu\nu\rho})^2 - b(\Psi_{\mu\nu\sigma}^\dagger \Psi^{\mu\nu\tau})(\Psi_{\rho\delta\tau}^\dagger \Psi^{\rho\delta\sigma})$$

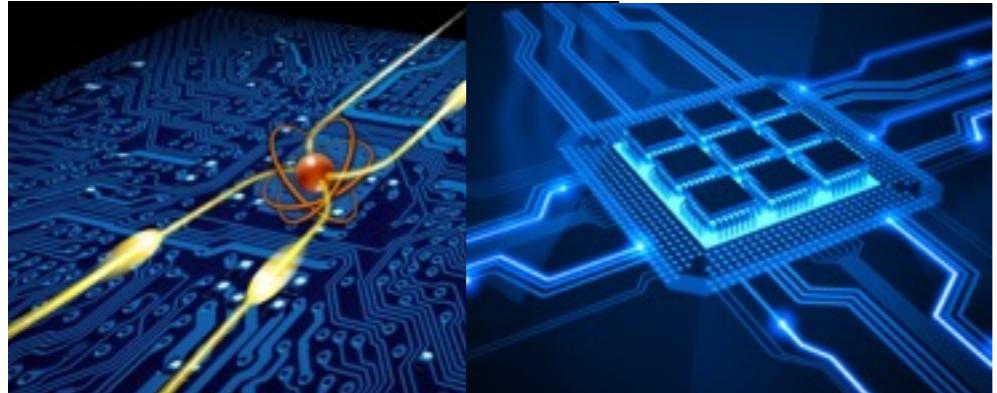
SU(6) spin-flavor symmetry, coefficients indicate very nearly SU(16) symmetry



# The Periodic Table at a Pion Mass of ~800 MeV

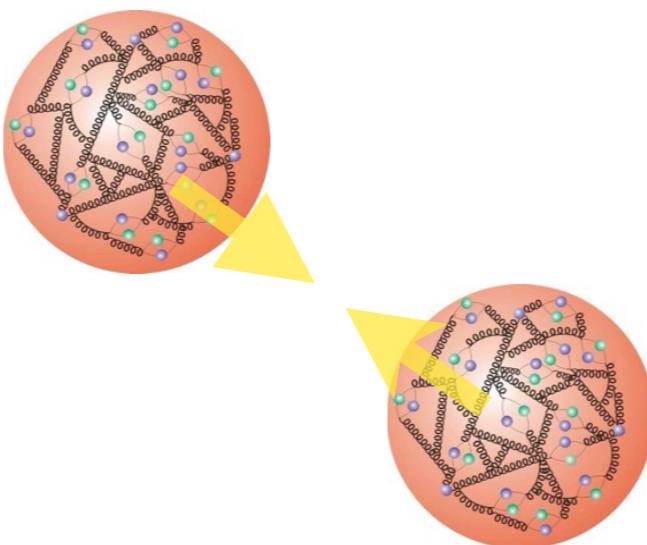
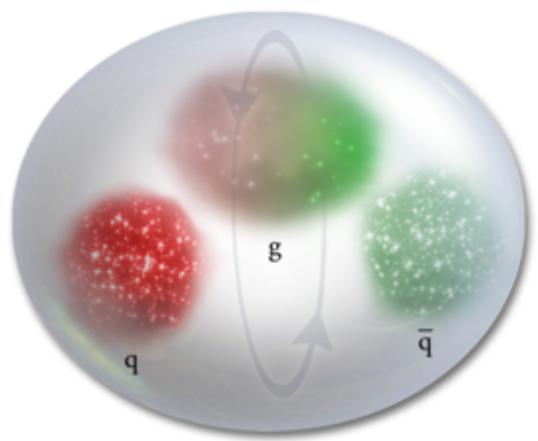


Lattice QCD combined with Nuclear Many-body calculations can explore impact of a significant range of fundamental constants  
- currently limited by precision of lattice QCD results (determined by compute resources !)

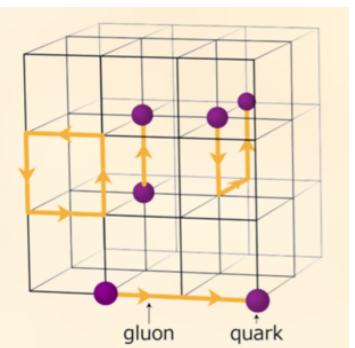


## “ Features “

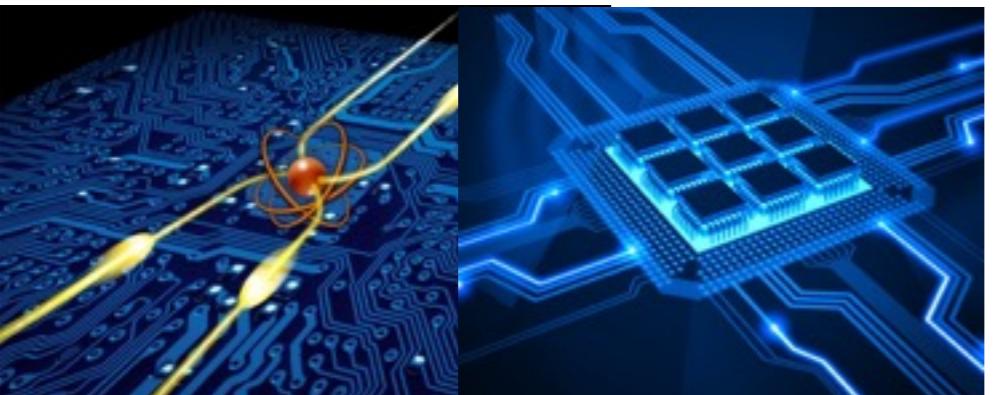
S-matrix elements, equilibrium properties, definite quantum numbers, e.g., 2 neutrons and 1 proton



# Signal to Noise Problem [Sign Problem]

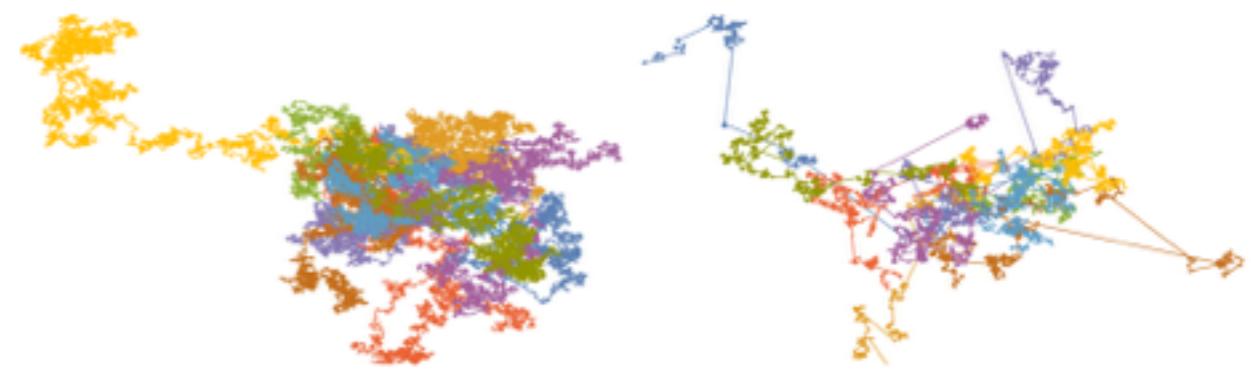
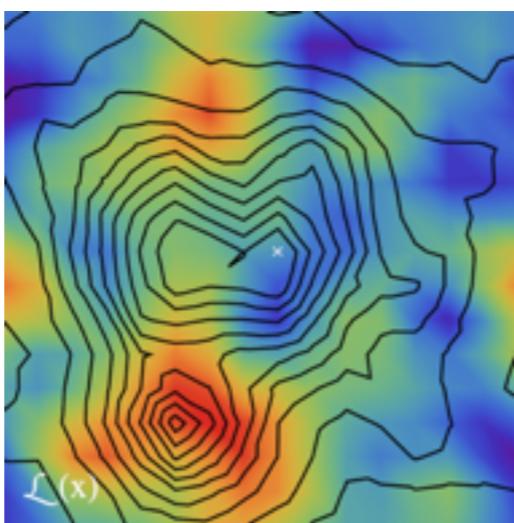
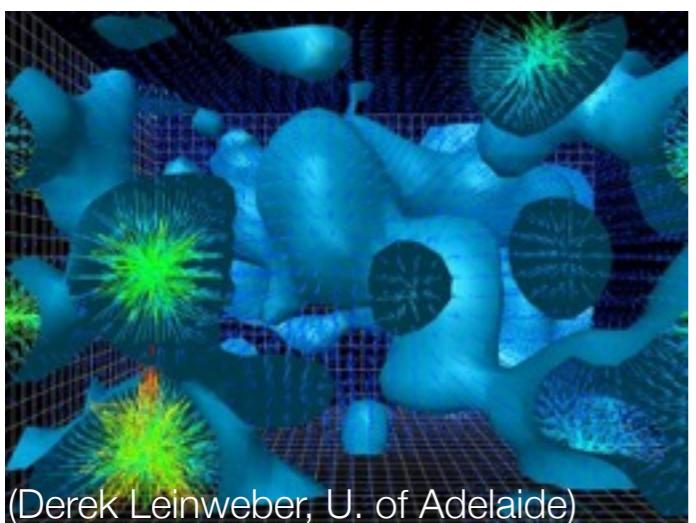


Statistical sampling of the path integral is the limiting element

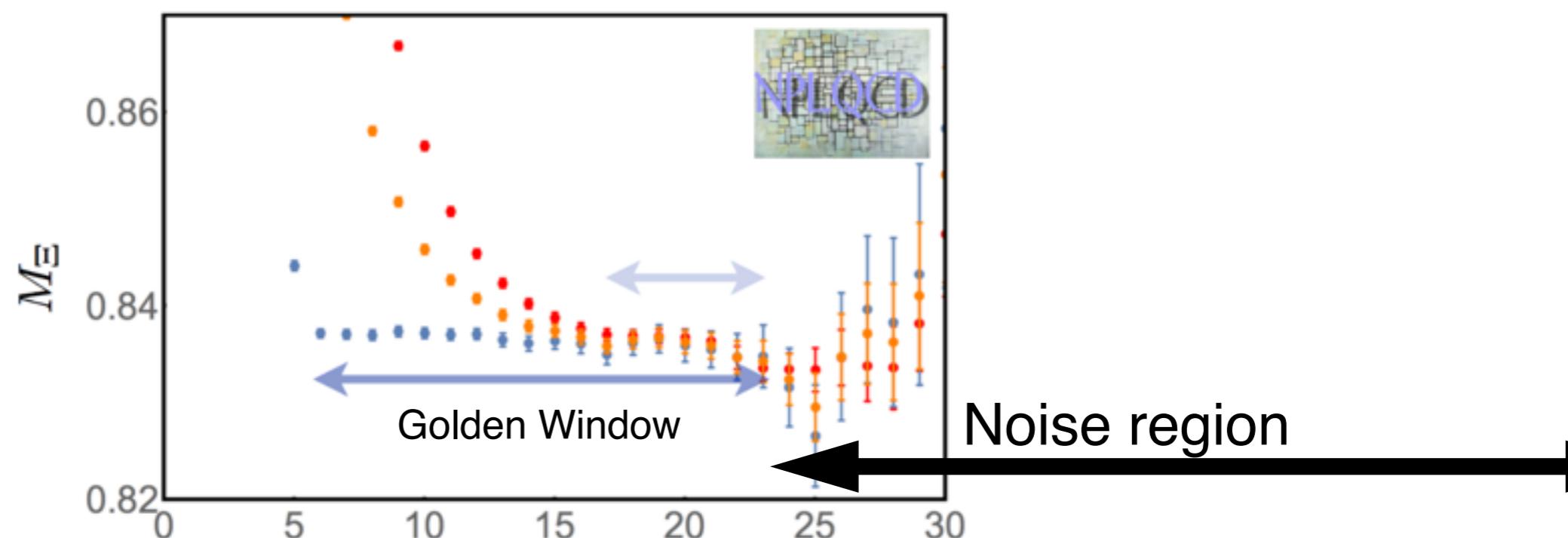
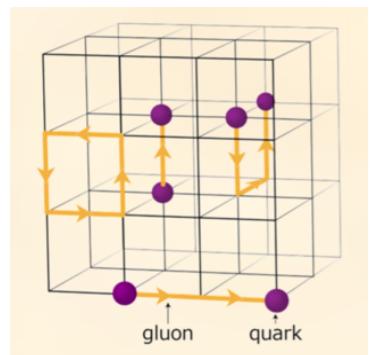


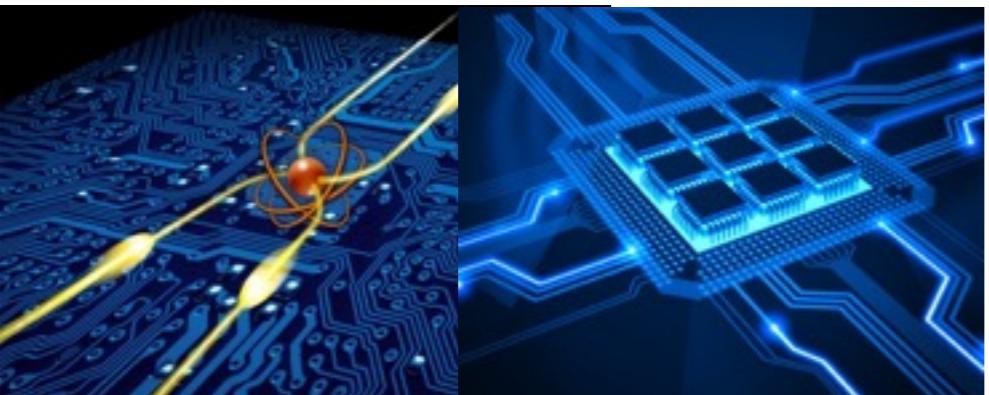
# “ Features “

Michael Wagman, PhD Thesis



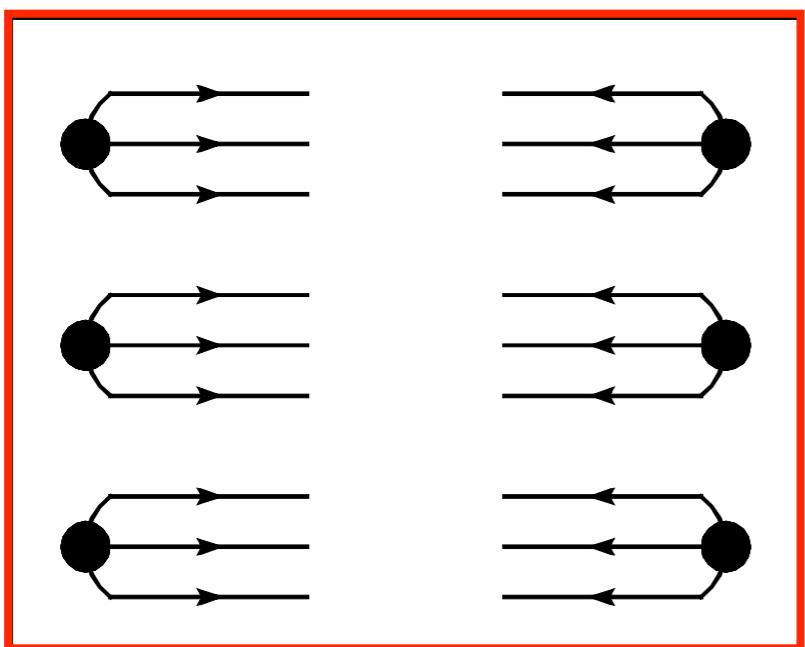
$$C(t) = e^{R(t)+i\theta(t)} \rightarrow \frac{1}{N} \sum_{U_i} e^{R(t;U_i)+i\theta(t;U_i)}$$





## “ Features “

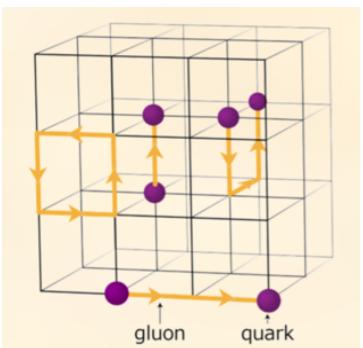
Large number of quark contractions



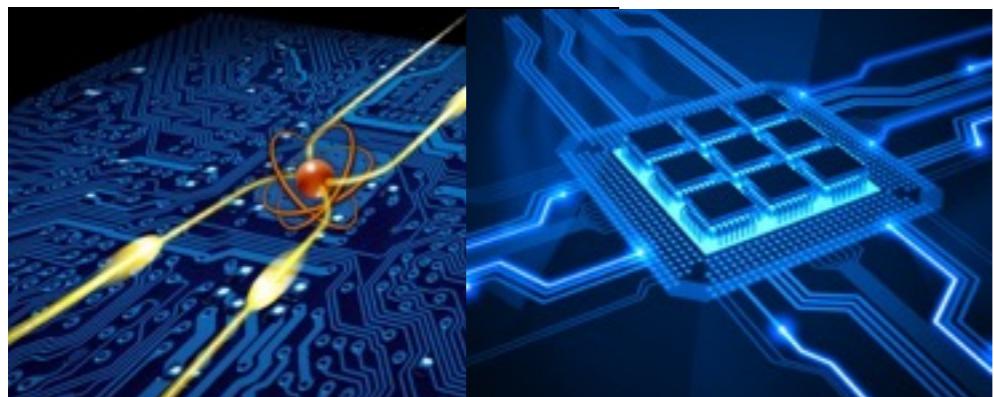
$$\text{Proton : } N^{\text{cont}} = 2$$
$$^{235}\text{U} : N^{\text{cont}} = 10^{1494}$$

$$N_{\text{cont.}} = u!d!s! \text{ (Naive)}$$
$$= (A + Z)!(2A - Z)!s!$$

Symmetries provide significant reduction (NPLQCD, PACS - 2010)

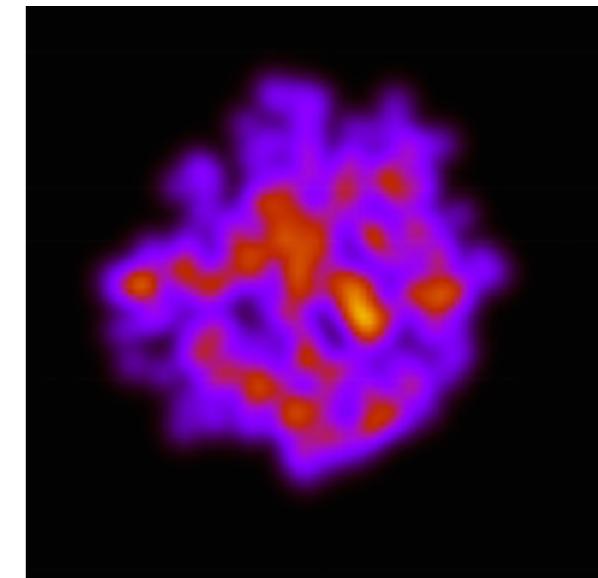
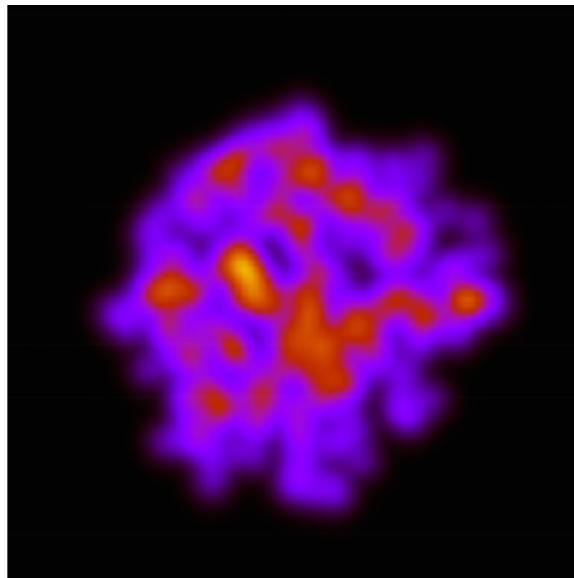
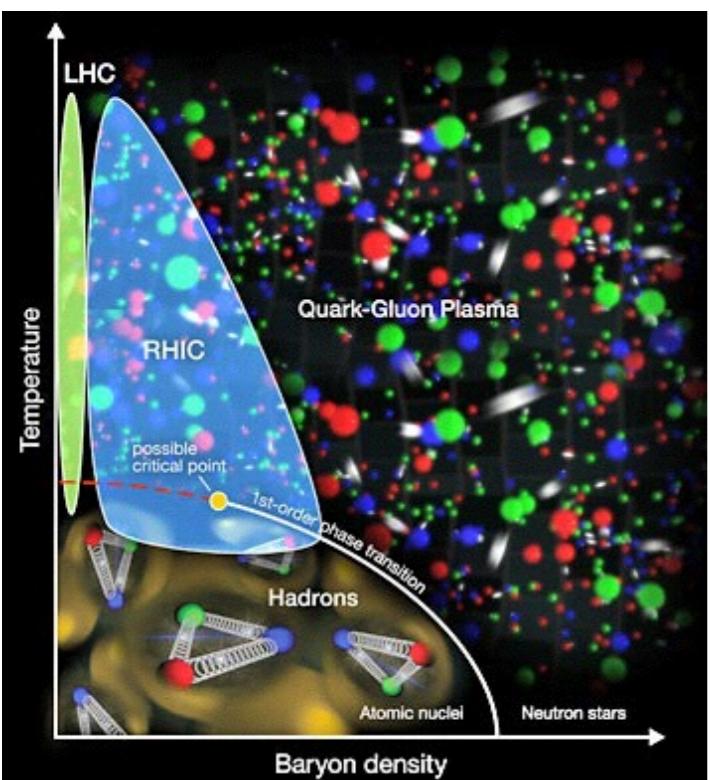


$$^3\text{He} : 2880 \rightarrow 93$$



## “ Features - Finite Density “

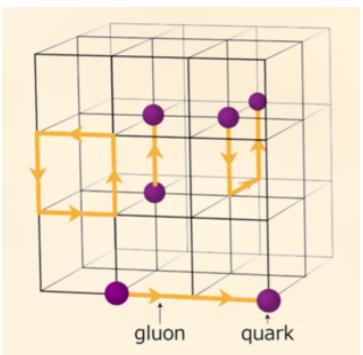
Time evolution of system with baryon number, isospin, electric charge, strangeness, ....  
Currents, viscosity, non-equilibrium dynamics - real-time evolution



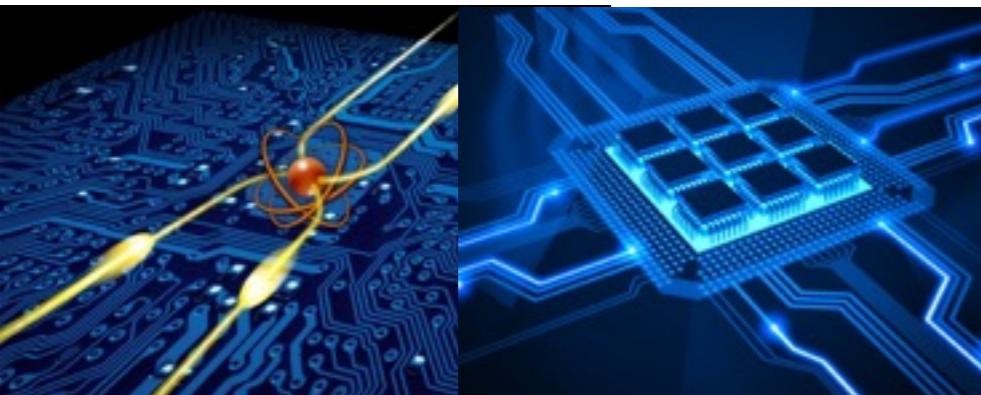
Alexey Bazavov [MSU]

## Sign Problem

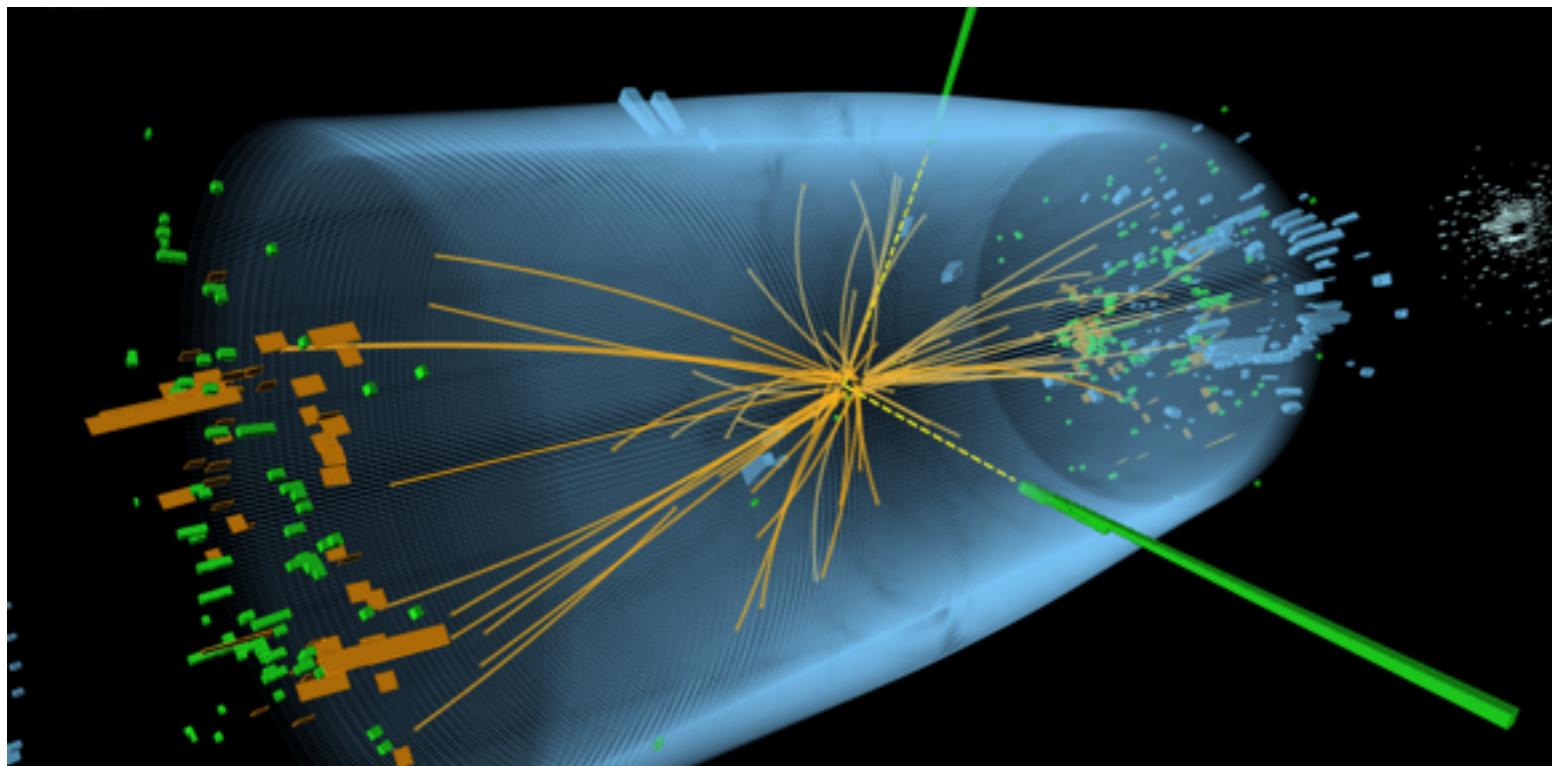
$$\langle \hat{\theta} \rangle \sim \int \mathcal{D}\mathcal{U}_\mu \hat{\theta}[\mathcal{U}_\mu] \det[\kappa[\mathcal{U}_\mu]] e^{-S_{YM}}$$



Complex for non-zero chemical potential



# Fragmentation Vacuum and In-Medium

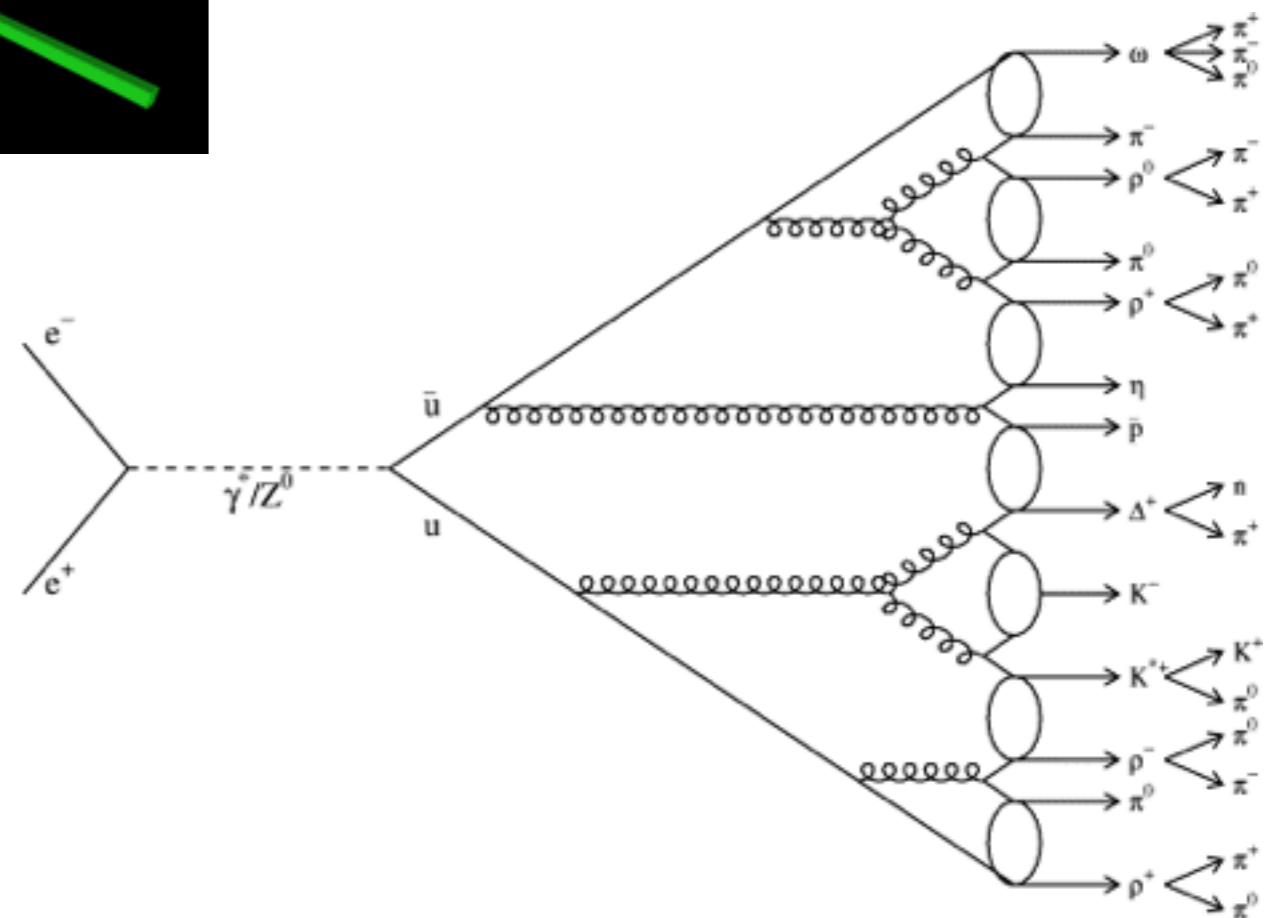


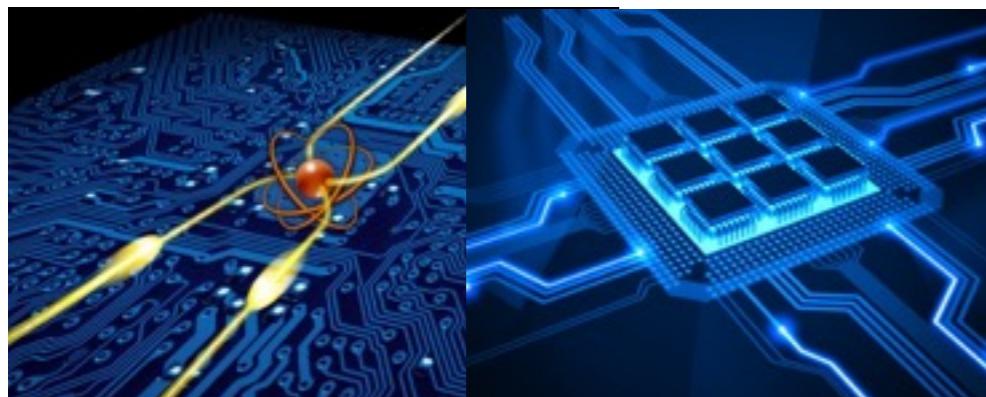
Free-space and in-medium

Diagnostic of state of dense and hot matter

- heavy-ion collisions (e.g., jet quenching)
- finite density and time evolution

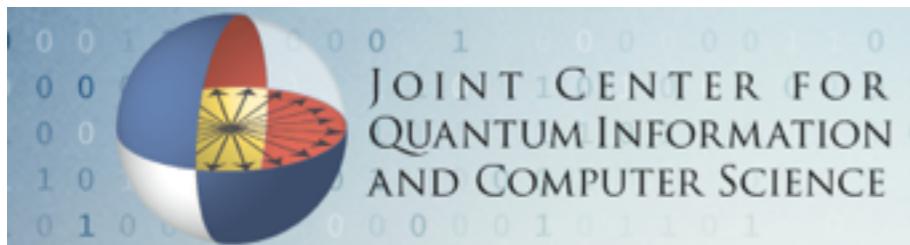
Highly-tuned phenomenology and pQCD calculations





# Why Quantum Computing?

The sign problem and the desire for dynamical evolution of QCD systems, requiring ***beyond exascale classical computing*** resources, lead us to consider the potential of quantum information and computing. [2016-2017]



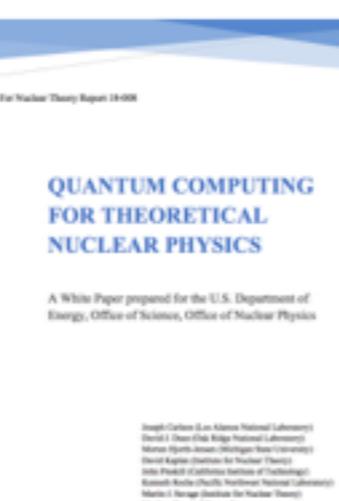
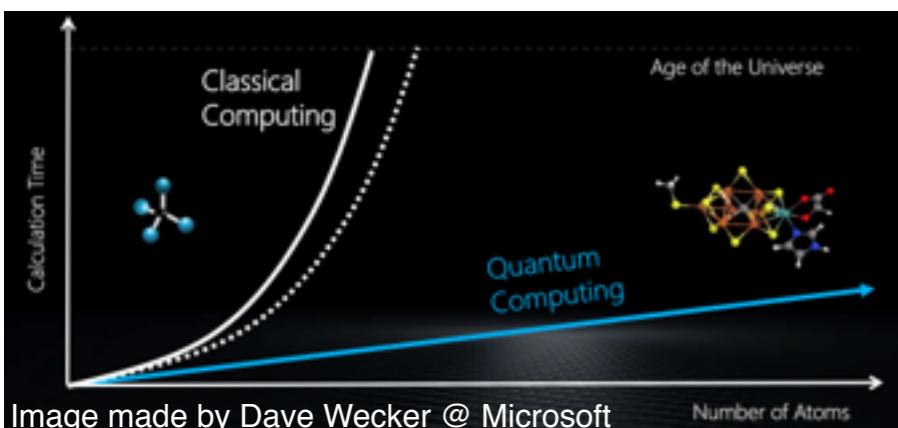
Workshop on Computational Complexity  
and High Energy Physics  
July-31 — August 2, 2017

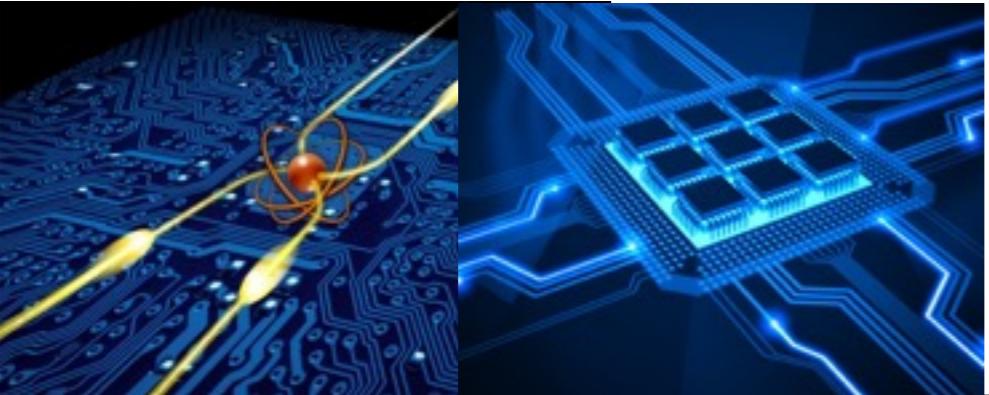


Quantum Computing for Nuclear Physics  
November 14-15, 2017



Intersections Between Nuclear Physics  
and Quantum Information  
November 14-15, 2017





# Quantum Computing

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Maryland

New hole-punched crystal clears a path for quantum light

PHOTONIC CHIP GUIDES SINGLE PHOTONS, EVEN WHEN THERE ARE BENDS IN THE ROAD.

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UPCOMING EVENTS

TIQI

TRAPPED ION QUANTUM INFORMATION

CHRISTOPHER MONROE, Principal Investigator, University of Maryland Department of Physics, Joint Quantum Institute and Center for Quantum Information and Computer Science

Institute for Quantum Information and Matter, a National Science Foundation Physics Frontiers Center

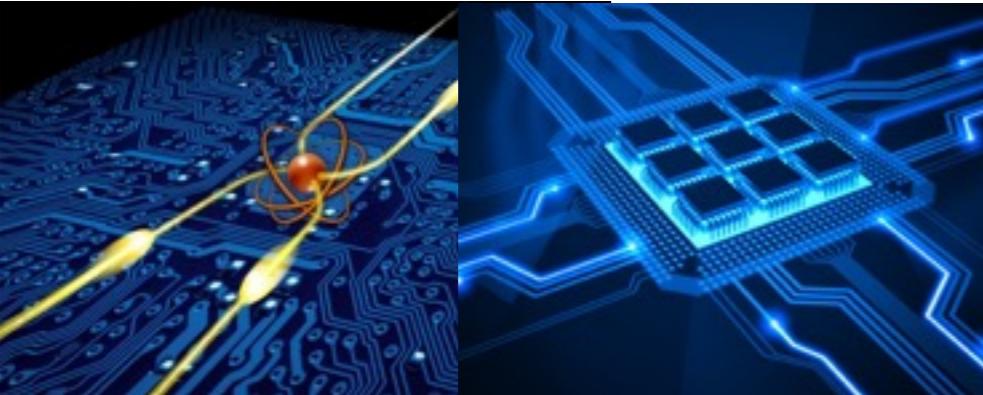
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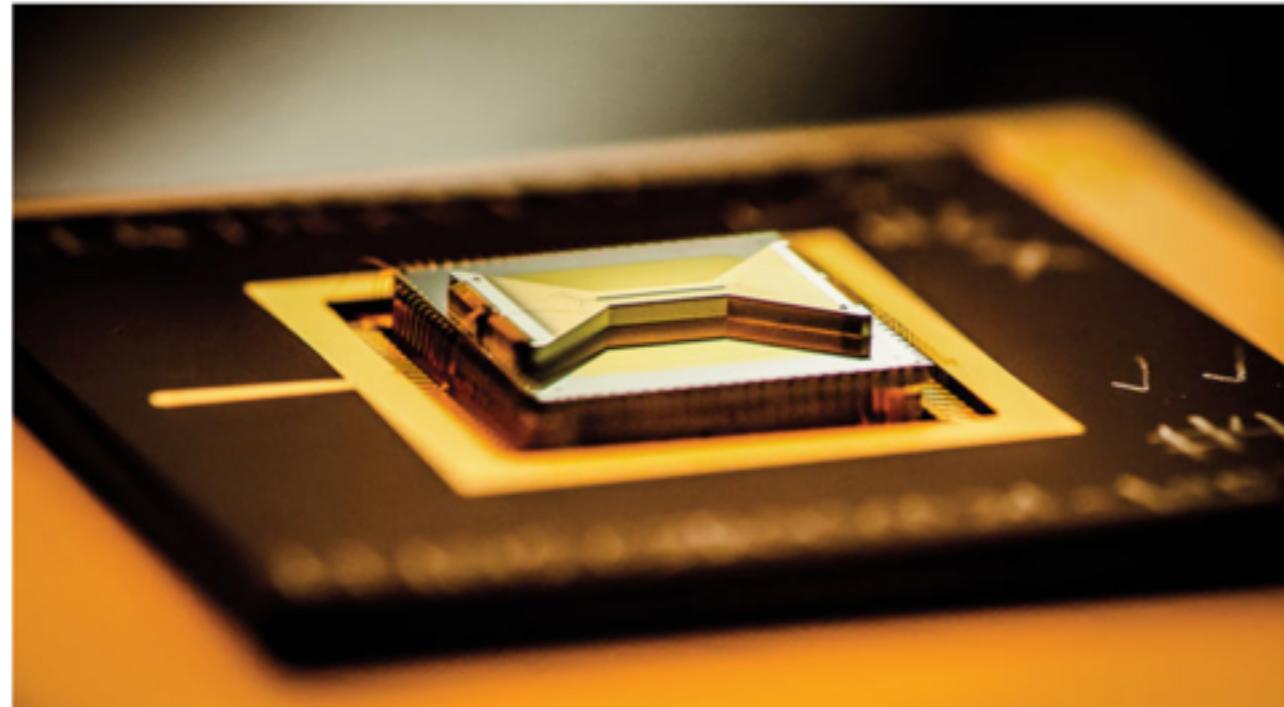
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Microsoft Quantum – Santa Barbara (Station Q)



# Quantum Computing

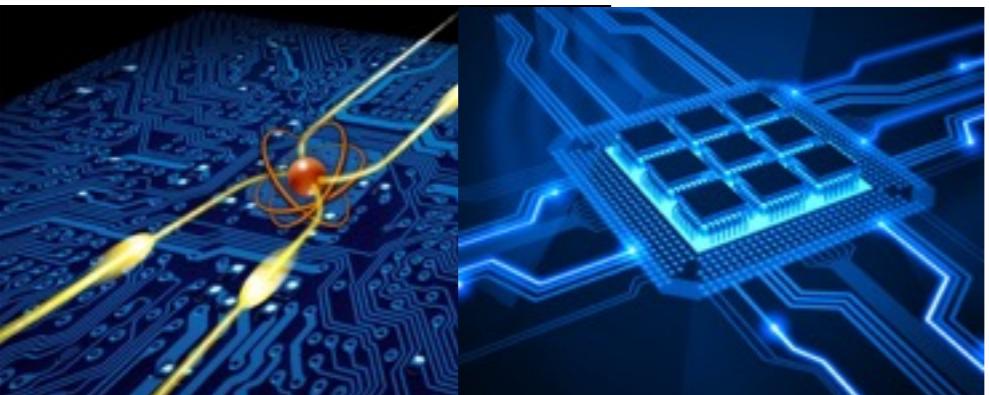


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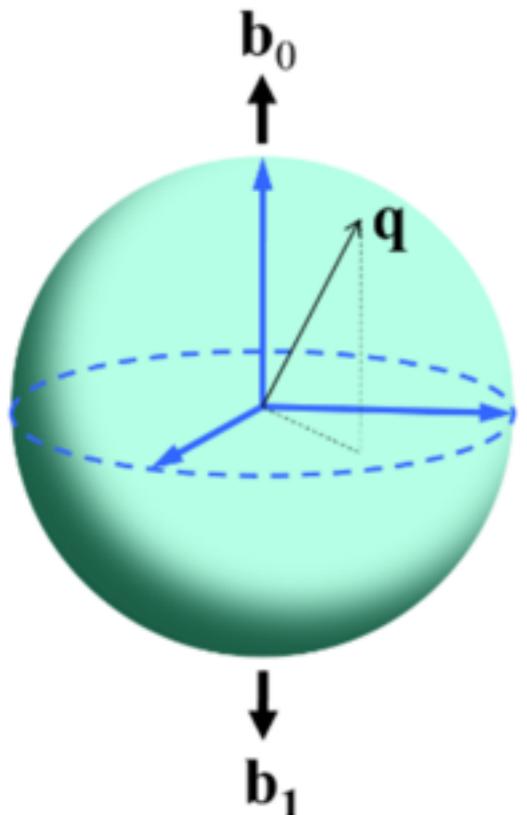
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QUANTUM COMPUTING





# The promise of Quantum Computing



$$|\psi\rangle = a_1|\chi_1\rangle + a_2|\chi_2\rangle + \dots + a_n|\chi_n\rangle + \dots$$

$$H|0\rangle = \frac{1}{\sqrt{2}} |0\rangle + |1\rangle$$

Parallel Processing of quantum states and information

Quantum computation algorithm for many-body studies

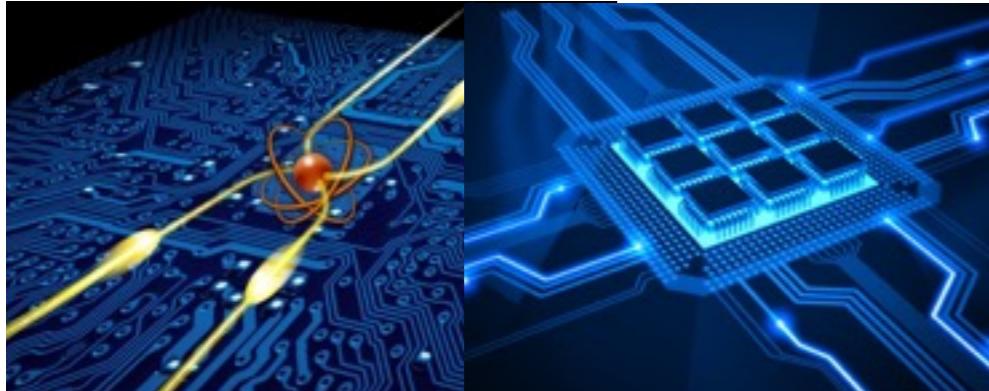
E. Ovrum and M. Hjorth-Jensen

*Department of Physics and Center of Mathematics for Applications, University of Oslo, N-0316 Oslo, Norway*

*(Submitted on 14 May 2007)*

NP's First paper :

We show in detail how the Jordan-Wigner transformation can be used to simulate any fermionic many-body Hamiltonian on a quantum computer. We develop an algorithm based on appropriate qubit gates that takes a general fermionic Hamiltonian, written as products of a given number of creation and annihilation operators, as input. To demonstrate the applicability of the algorithm, we calculate eigenvalues and eigenvectors of two model Hamiltonians, the well-known Hubbard model and a generalized pairing Hamiltonian. Extensions to other systems are discussed.



# time=0 for Quantum Computing in Nuclear Physics

## Cloud Quantum Computing of an Atomic Nucleus\*

E. F. Dumitrescu,<sup>1</sup> A. J. McCaskey,<sup>2</sup> G. Hagen,<sup>3,4</sup> G. R. Jansen,<sup>5,3</sup> T. D. Morris,<sup>4,3</sup>  
T. Papenbrock,<sup>4,3,†</sup> R. C. Pooser,<sup>1,4</sup> D. J. Dean,<sup>3</sup> and P. Lougovski<sup>1,‡</sup>

<sup>1</sup>Computational Sciences and Engineering Division,

Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

<sup>2</sup>Computer Science and Mathematics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

<sup>3</sup>Physics Division, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

<sup>4</sup>Department of Physics and Astronomy, University of Tennessee, Knoxville, TN 37996, USA

<sup>5</sup>National Center for Computational Sciences, Oak Ridge National Laboratory, Oak Ridge, TN 37831, USA

We report a quantum simulation of the deuteron binding energy on quantum processors accessed via cloud servers. We use a Hamiltonian from pionless effective field theory at leading order. We design a low-depth version of the unitary coupled-cluster ansatz, use the variational quantum eigensolver algorithm, and compute the binding energy to within a few percent. Our work is the first step towards scalable nuclear structure computations on a quantum processor via the cloud, and it sheds light on how to map scientific computing applications onto nascent quantum devices.

<http://arxiv.org/abs/1801.03897>

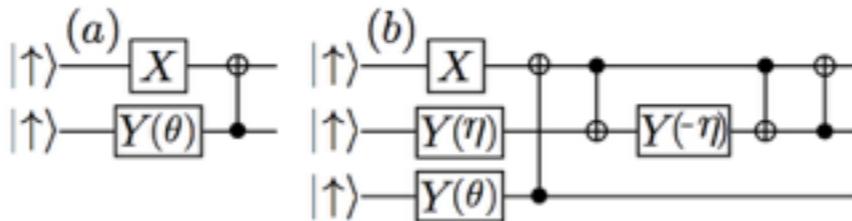
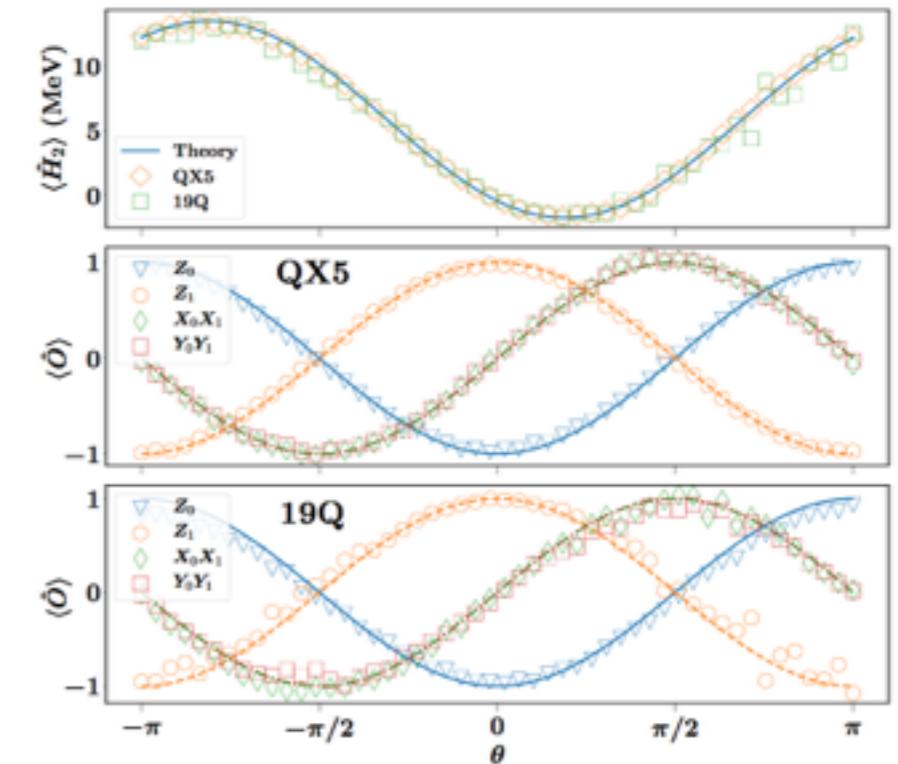
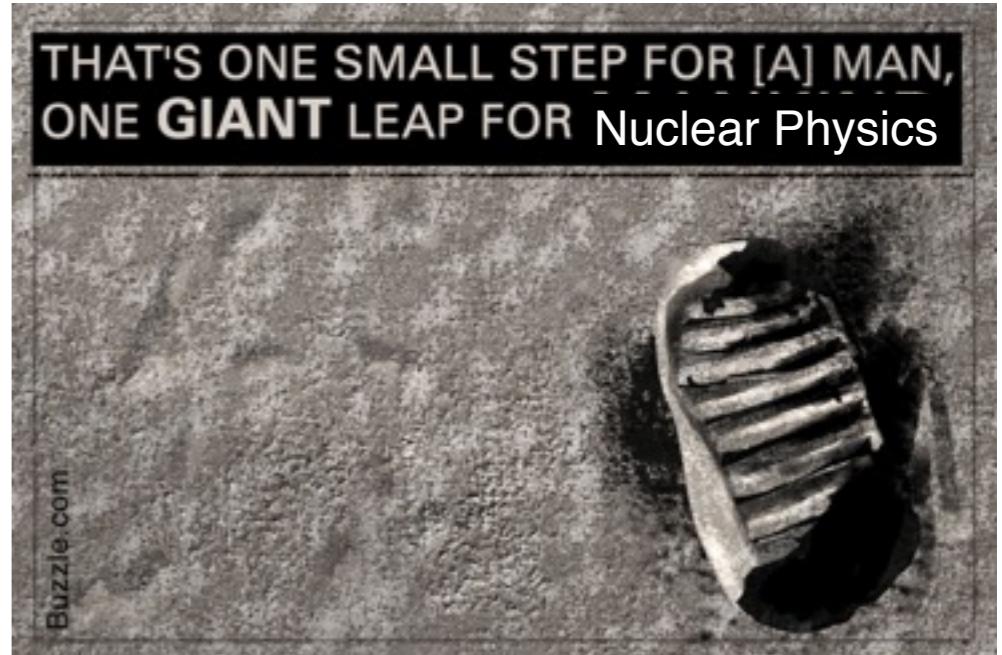
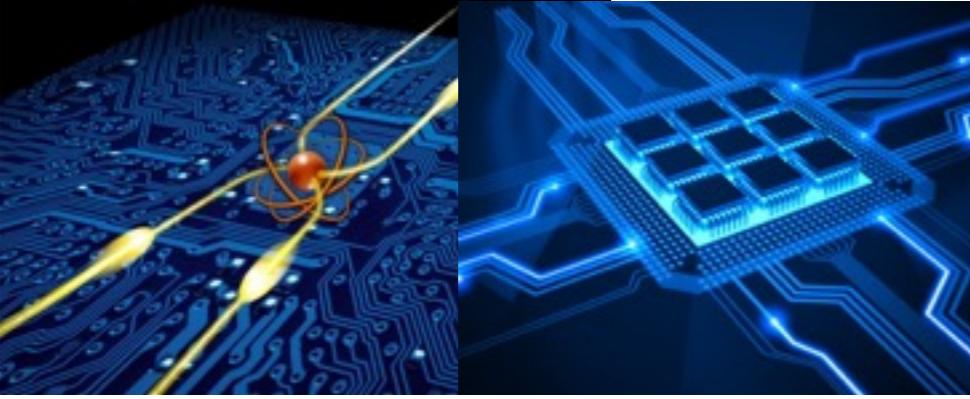


FIG. 1. Low-depth circuits that generate unitary rotations in Eq. (7) (panel a) and Eq. (8) (panel b). Also shown are the single-qubit gates of the Pauli  $X$  matrix, the rotation  $Y(\theta)$  with angle  $\theta$  around the  $Y$  axis, and the two-qubit CNOT gates.

of a Hamiltonian is to use UCC ansatz in tandem with the VQE algorithm [12, 15, 21]. We adopt this strategy for the Hamiltonians described by Eqs. (4) and (5). We define unitary operators entangling two and three orbitals,

$$U(\theta) \equiv e^{\theta(a_0^\dagger a_1 - a_1^\dagger a_0)} = e^{i\frac{\theta}{2}(X_0 Y_1 - X_1 Y_0)}, \quad (7)$$





# Quantum Field Theory with Quantum Computers - Foundational Works

## Simulating lattice gauge theories on a quantum computer

Tim Byrnes\*

National Institute of Informatics, 2-1-2 Hitotsubashi, Chiyoda-ku, Tokyo 101-8430, Japan

Yoshihisa Yamamoto

E. L. Ginzton Laboratory, Stanford University, Stanford, CA 94305 and  
National Institute of Informatics, 2-1-2 Hitotsubashi, Chiyoda-ku, Tokyo 101-8430, Japan

(Dated: February 1, 2008)

We examine the problem of simulating lattice gauge theories on a universal quantum computer. The basic strategy of our approach is to transcribe lattice gauge theories in the Hamiltonian formulation into a Hamiltonian involving only Pauli spin operators such that the simulation can be performed on a quantum computer using only one and two qubit manipulations. We examine three models, the U(1), SU(2), and SU(3) lattice gauge theories which are transcribed into a spin Hamiltonian up to a cutoff in the Hilbert space of the gauge fields on the lattice. The number of qubits required for storing a particular state is found to have a linear dependence with the total number of lattice sites. The number of qubit operations required for performing the time evolution corresponding to the Hamiltonian is found to be between a linear to quadratic function of the number of lattice sites, depending on the arrangement of qubits in the quantum computer. We remark that our results may also be easily generalized to higher  $SU(N)$  gauge theories.

Phys.Rev. A73 (2006) 022328

## Quantum Computation of Scattering in Scalar Quantum Field Theories

Stephen P. Jordan,<sup>†§</sup> Keith S. M. Lee,<sup>†§</sup> and John Preskill <sup>§ \*</sup>

<sup>†</sup> National Institute of Standards and Technology, Gaithersburg, MD 20899

<sup>‡</sup> University of Pittsburgh, Pittsburgh, PA 15260

<sup>§</sup> California Institute of Technology, Pasadena, CA 91125

### Abstract

Quantum field theory provides the framework for the most fundamental physical theories to be confirmed experimentally, and has enabled predictions of unprecedented precision. However, calculations of physical observables often require great computational complexity and can generally be performed only when the interaction strength is weak. A full understanding of the foundations and rich consequences of quantum field theory remains an outstanding challenge. We develop a quantum algorithm to compute relativistic scattering amplitudes in massive  $\phi^4$  theory in spacetime of four and fewer dimensions. The algorithm runs in a time that is polynomial in the number of particles, their energy, and the desired precision, and applies at both weak and strong coupling. Thus, it offers exponential speedup over existing classical methods at high precision or strong coupling.

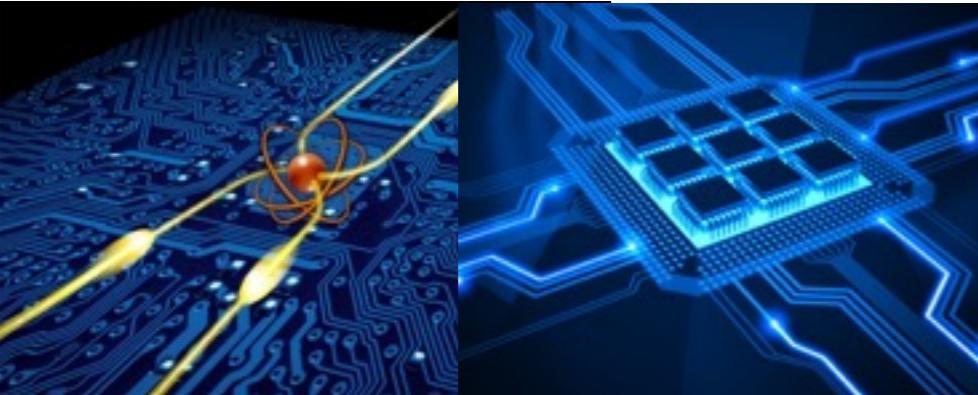
Quantum Information and Computation 14, 1014-1080 (2014)

## Detailed formalism for 3+1 Hamiltonian Gauge Theory

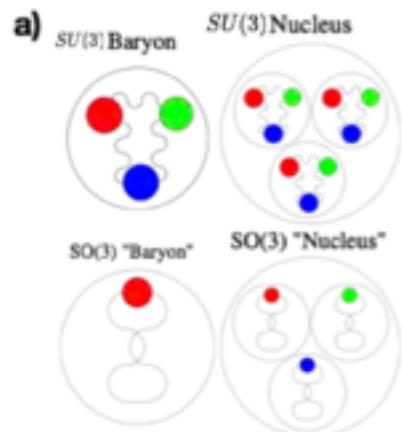
## Discretized spatial volume - no quarks

$10^4$  spatial lattice sites would require  $10^5 * D$  qubits ,  
 $D$ =size of register defining value of the field

Scalar Field Theory - Hamiltonian is nice



# Quantum Field Theory



**b)**

	3-d QCD	1-d $SO(3)$	2-d $SO(3)$
gauge symmetry	$SU(3)$	$SO(3)$	$SO(3)$
chiral symmetry	$SU(2)_L \times SU(2)_R$	$\mathbb{Z}_2$	$\mathbb{Z}_2 \times \mathbb{Z}_2$
flavor symmetry	$SU(2)_{L=R}$	$\mathbb{I}$	$\mathbb{Z}_2$
baryon symmetry	$U(1)$	$U(1)$	$U(1)$
charge conjugation	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_2$
parity	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_2$

## Quantum Link Models and Quantum Simulation of Gauge Theories

Uwe-Jens Wiese

Albert Einstein Center for Fundamental Physics  
Institute for Theoretical Physics, Bern University



**Winter School:**  
Intersections Between QCD and Condensed Matter  
Schladming, Styria, 2015



arXiv:1802.00022v1 [cond-mat.quant-gas] 31 Jan 2018

## SO(3) “Nuclear Physics” with ultracold Gases<sup>☆</sup>

E. Rico<sup>a,\*</sup>, M. Dalmonte<sup>b</sup>, P. Zoller<sup>c</sup>,  
D. Banerjee<sup>d,e</sup>, M. Bögli<sup>d</sup>, P. Stebler<sup>d</sup>, U.-J. Wiese<sup>d</sup>

<sup>a</sup>*IKERBASQUE, Basque Foundation for Science, Maria Diaz de Haro 3, E-48013 Bilbao, Spain and Department of Physical Chemistry, University of the Basque Country UPV/EHU, Apartado 644, E-48080 Bilbao, Spain*

<sup>b</sup>*International Center for Theoretical Physics, 34151 Trieste, Italy*

<sup>c</sup>*Institute for Theoretical Physics, Innsbruck University, and Institute for Quantum Optics and Quantum Information of the Austrian Academy of Sciences, A-6020 Innsbruck, Austria*

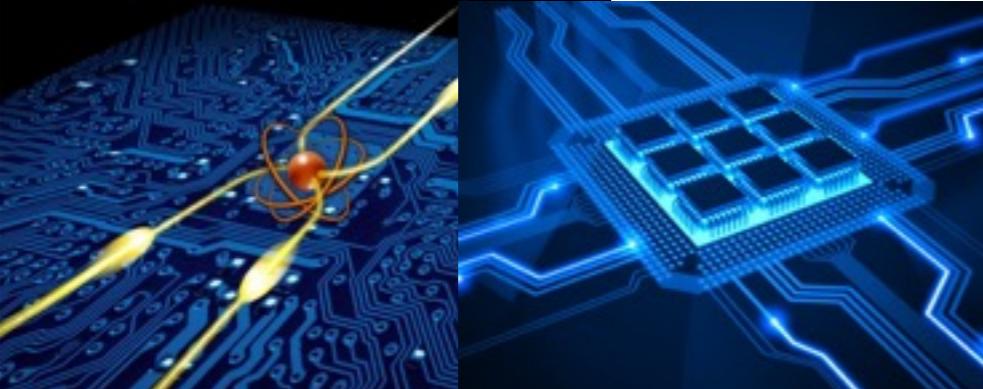
<sup>d</sup>*Albert Einstein Center for Fundamental Physics, Institute for Theoretical Physics, University of Bern, Sidlerstrasse 5, CH-3012 Bern, Switzerland*

<sup>e</sup>*NIC, DESY, Platanenallee 6, 15738 Zeuthen, Germany*

### Abstract

An *ab initio* calculation of nuclear physics from Quantum Chromodynamics (QCD), the fundamental  $SU(3)$  gauge theory of the strong interaction, remains an outstanding challenge. Here, we discuss the emergence of key elements of nuclear physics using an  $SO(3)$  lattice gauge theory as a toy model for QCD. We show that this model is accessible to state-of-the-art quantum simulation experiments with ultracold atoms in an optical lattice. First, we demonstrate that our model shares characteristic many-body features with QCD, such as the spontaneous breakdown of chiral symmetry, its restoration at finite baryon density, as well as the existence of few-body bound states. Then we show that in the one-dimensional case, the dynamics in the gauge invariant sector can be encoded as a spin  $S = \frac{3}{2}$  Heisenberg model, i.e., as quantum magnetism, which has a natural realization with bosonic mixtures in optical lattices, and thus sheds light on the connection between non-Abelian gauge theories and quantum magnetism.

**Keywords:** ultracold atoms | Lattice gauge theories | Quantum simulation



# Quantum Field Theory - recent examples

## Quantum sensors for the generating functional of interacting quantum field theories

A. Bermudez,<sup>1,2,\*</sup> G. Aarts,<sup>1</sup> and M. Müller<sup>1</sup>

<sup>1</sup>*Department of Physics, College of Science, Swansea University, Singleton Park, Swansea SA2 8PP, United Kingdom*

<sup>2</sup>*Instituto de Física Fundamental, IFF-CSIC, Madrid E-28006, Spain*

Difficult problems described in terms of interacting quantum fields evolving in real time or out of equilibrium are abound in condensed-matter and high-energy physics. Addressing such problems via control in atomic, molecular, and optical physics would be a breakthrough in the field of quantum simulation. In this work, we present a quantum-sensing protocol to measure the generating functional of an interacting field theory and, with it, all the relevant information about its in or out of equilibrium phenomena. This can be understood as a collective interferometric scheme based on a generalization of the notion of sources in quantum field theories, which make it possible to probe the generating functional. We show that this scheme can be realized in crystals of trapped ions acting as analog quantum simulators of self-interacting quantum field theories.

arXiv:1702.05492  
proposed method

## Dynamics of entanglement in expanding quantum fields

Jürgen Berges,<sup>a</sup> Stefan Floerchinger<sup>a</sup> and Raju Venugopalan<sup>b</sup>

arXiv:1802.07347 [quant-ph]

## Quantum simulation of the universal features of the Polyakov loop

Jin Zhang<sup>1</sup>, J. Unmuth-Yockey<sup>2</sup>, A. Bazavov<sup>3</sup>, S.-W. Tsai<sup>1</sup>, and Y. Meurice<sup>4</sup>

<sup>1</sup>*Department of Physics and Astronomy, University of California, Riverside, CA 92521, USA*

<sup>2</sup>*Department of Physics, Syracuse University, Syracuse, New York 13244, USA*

<sup>3</sup>, *Department of Physics and Astronomy, Michigan State University, East Lansing, Michigan, 48824, USA and*

<sup>4</sup>*Department of Physics and Astronomy, The University of Iowa, Iowa City, IA 52242, USA*

arXiv:1704.02877

## Quantum Simulation of the Abelian-Higgs Lattice Gauge Theory with Ultracold Atoms

Daniel González-Cuadra<sup>1,2</sup>, Erez Zohar<sup>2</sup> and J. Ignacio Cirac<sup>2</sup>

<sup>1</sup> ICFO – The Institute of Photonic Sciences, Av. C.F. Gauss 3, E-08860, Castelldefels (Barcelona), Spain

<sup>2</sup> Max-Planck-Institut für Quantenoptik, Hans-Kopfermann-Straße 1, D-85748 Garching, Germany

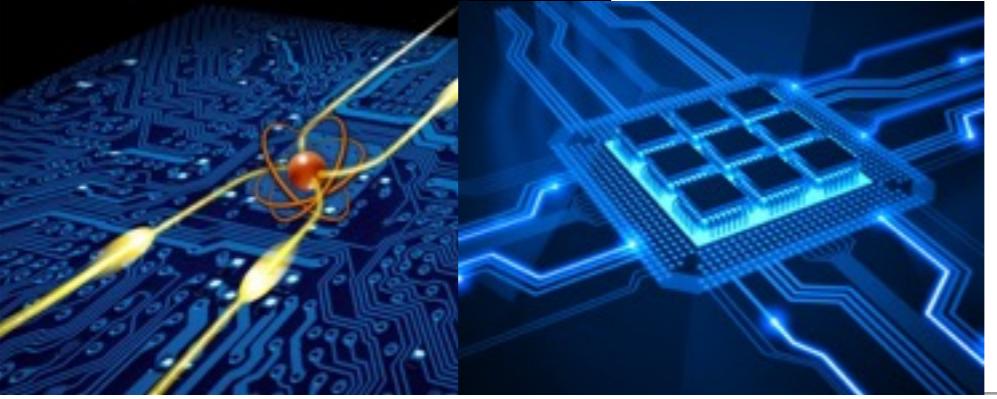
arXiv:1712.09362 [hep-th]

## Electron-Phonon Systems on a Universal Quantum Computer

Alexandru Macridin, Panagiotis Spentzouris, James Amundson, Roni Harnik

Batavia, Illinois 60510, USA

arXiv:1803.11166 [hep-lat]

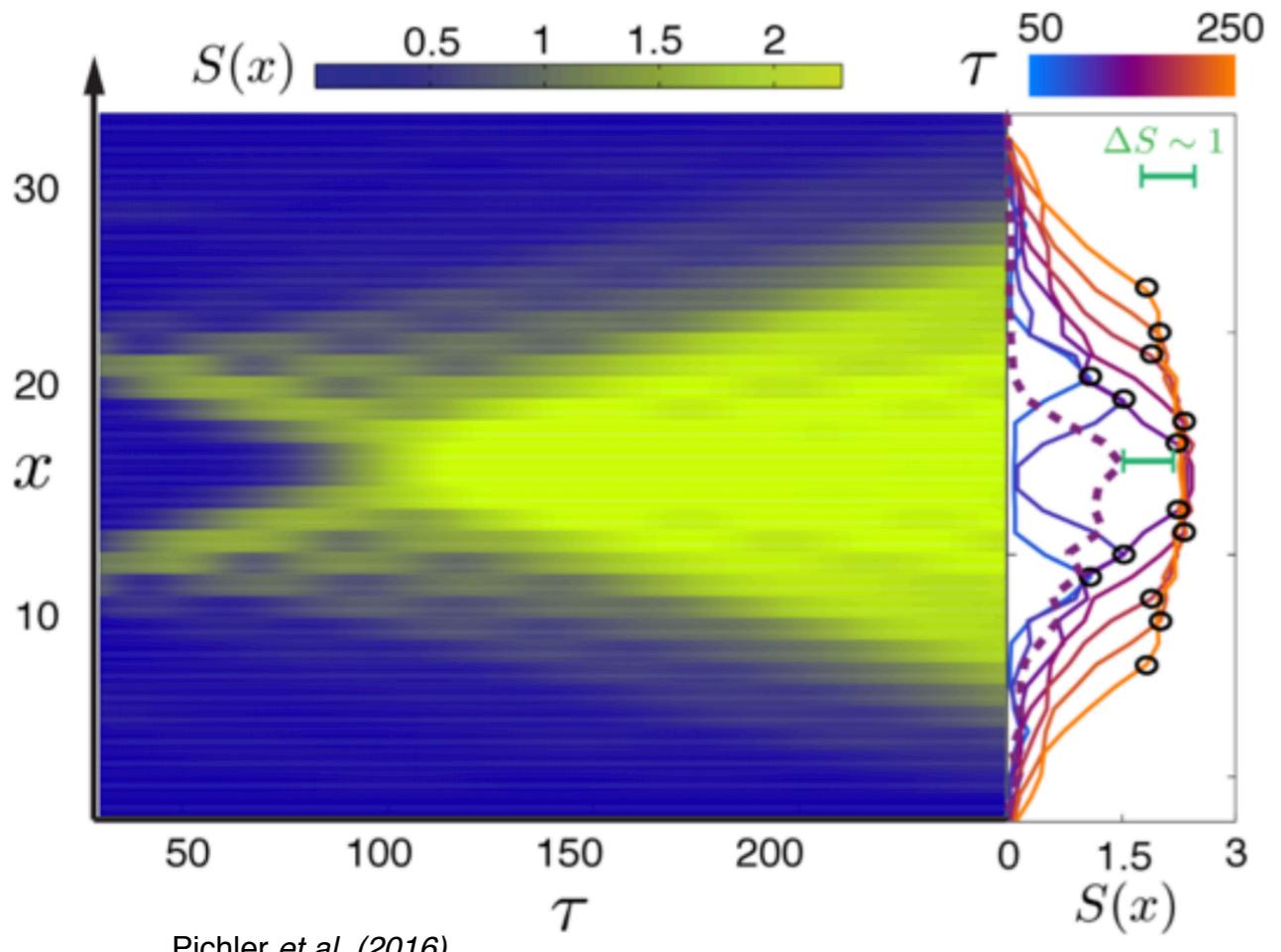


# Quantum Field Theory and Quantum Information

Are there new insights into the forces of nature and/or calculational techniques to be had by thinking in terms of quantum information?

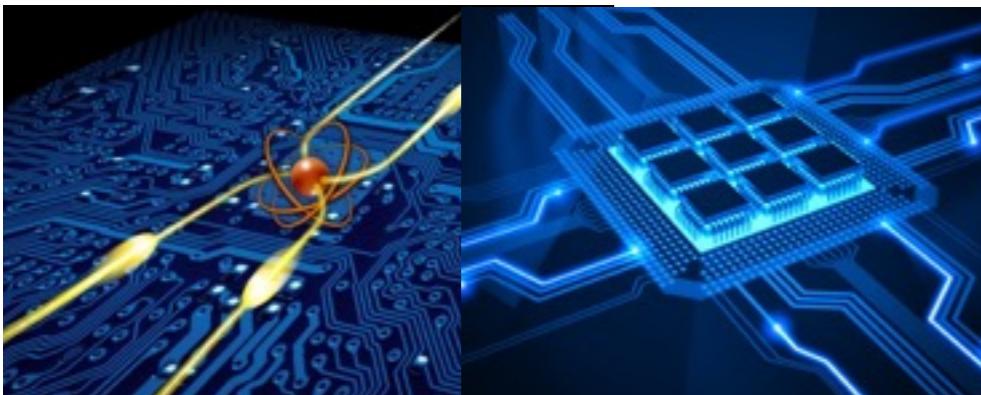
Preskill, Swingle, and others

Entanglement entropy in scattering (tensor networks)



New ways to arrange QCD calculations ?  
New ways to address QCD analytically ?

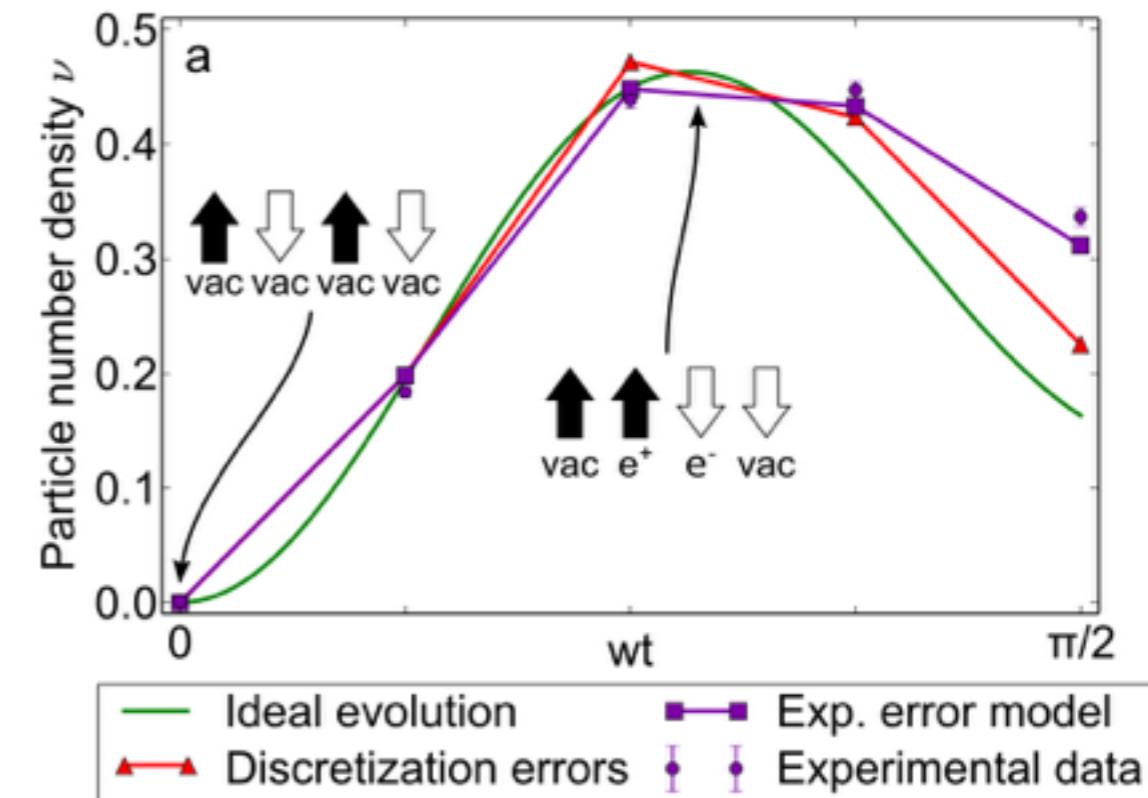
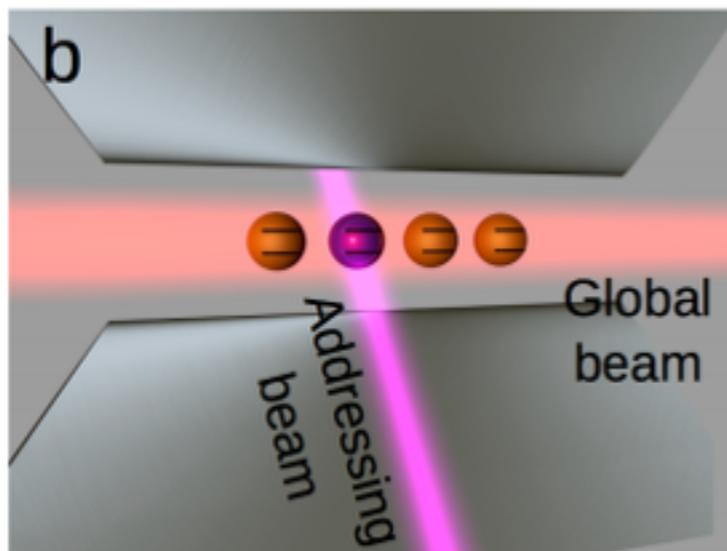
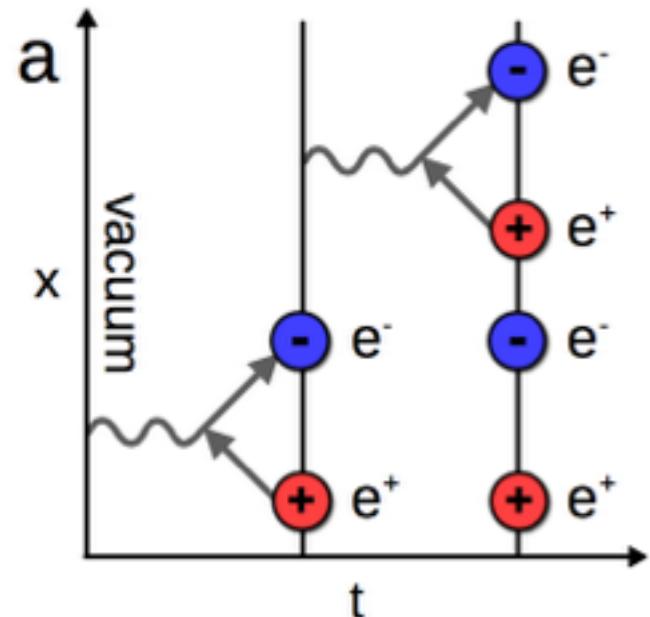
Entanglement in HEP and NP systems  
is starting to be considered,  
e.g. fragmentation



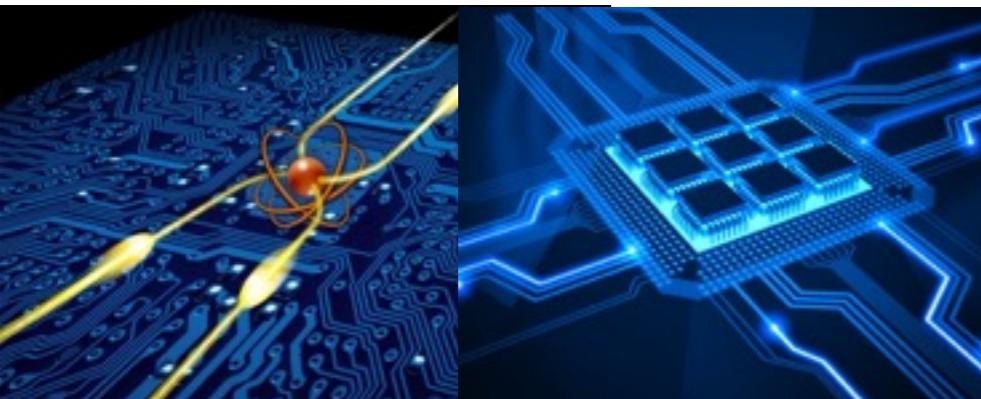
# Starting Simple 1+1 Dim QED - Pivotal Paper

Real-time dynamics of lattice gauge theories with a few-qubit quantum computer

Esteban A. Martinez,<sup>1,\*</sup> Christine Muschik,<sup>2,3,\*</sup> Philipp Schindler,<sup>1</sup> Daniel Nigg,<sup>1</sup> Alexander Erhard,<sup>1</sup> Markus Heyl,<sup>2,4</sup> Philipp Hauke,<sup>2,3</sup> Marcello Dalmonte,<sup>2,3</sup> Thomas Monz,<sup>1</sup> Peter Zoller,<sup>2,3</sup> and Rainer Blatt<sup>1,2</sup> (2016)

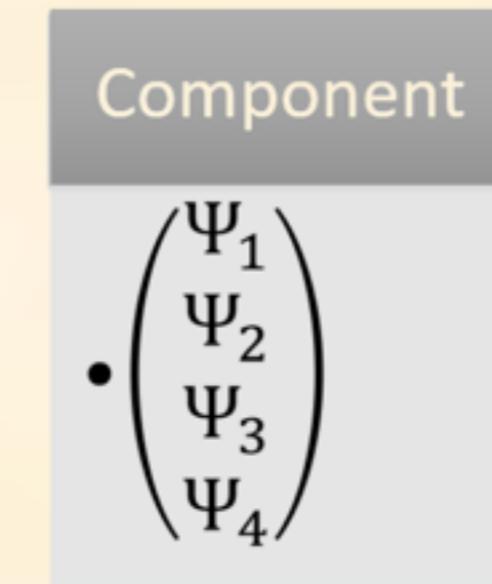
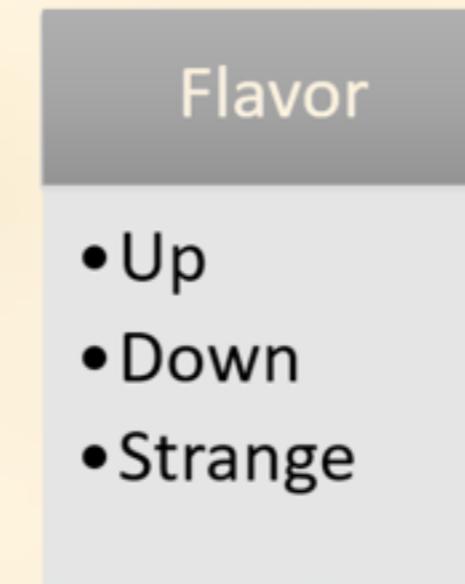
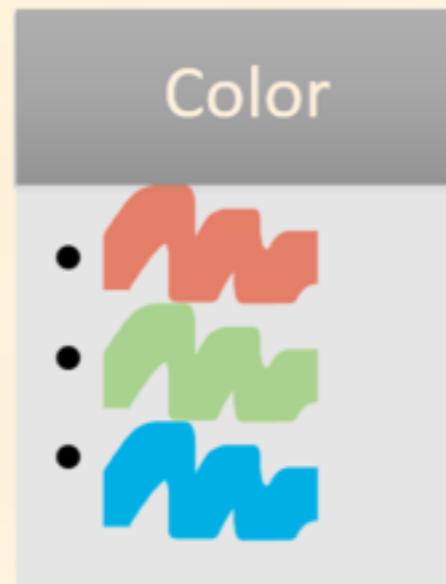
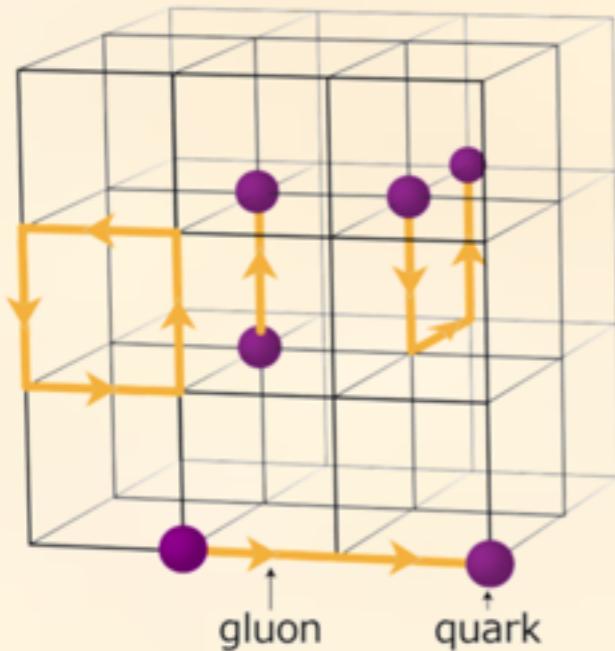


Based upon a string of  $^{40}\text{Ca}^+$  trapped-ion quantum system  
Simulates 4 qubit system with long-range couplings = 2-spatial-site Schwinger Model  
> 200 gates per Trotter step



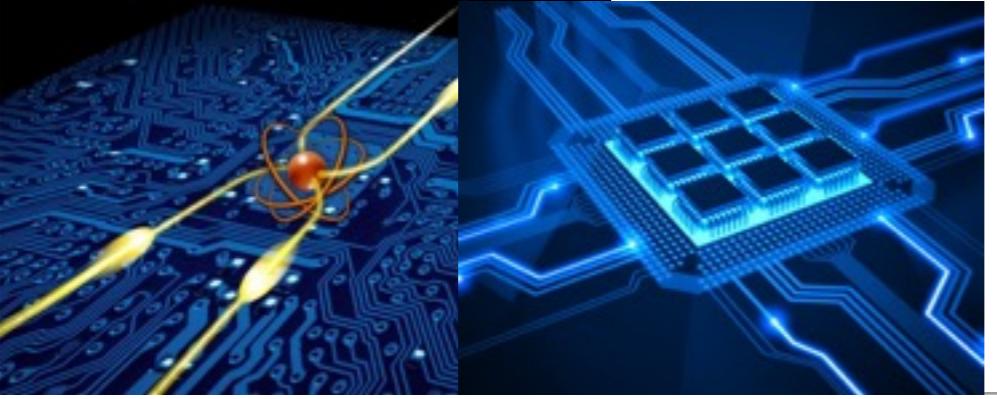
# Gauge Field Theories

e.g. QCD



Natalie Klco

$32^3$  lattice requires naively  $> 4$  million qubits !

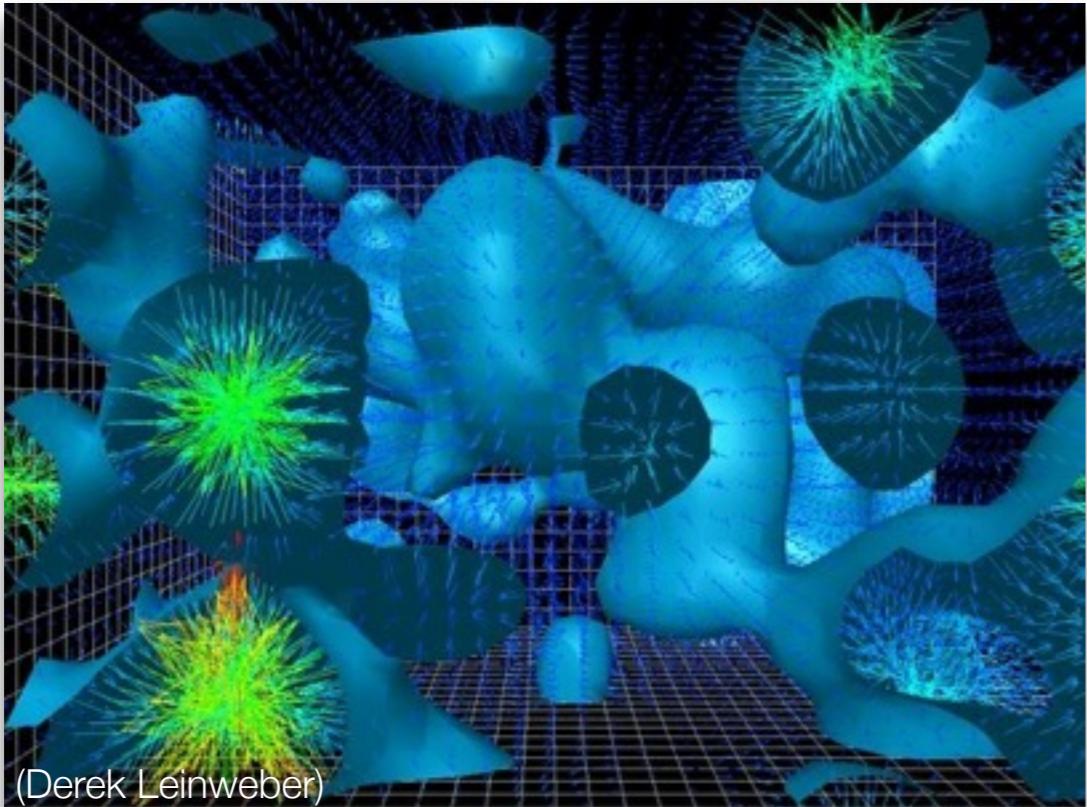


# What is the QCD Vacuum : $E^a |0\rangle = 0$ ?

Random fields at each point in spacetime is far from ground state.

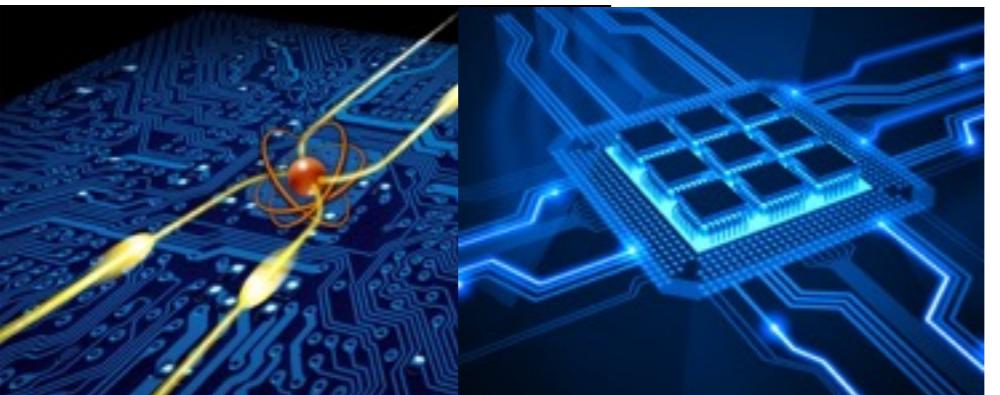
- generally all  $0^{++}$  states will be populated with some amplitude

$$| \text{random} \rangle = a | 0 \rangle + b | (\pi \pi) \rangle + c | (\pi \pi \pi \pi) \rangle + \dots + d | (GG) \rangle + \dots$$



1 vacuum configuration  
Probability  $e^{-S_{\text{QCD}}}$

**Classical Lattice QCD calculations will likely be required to provide initialization of vacuum. How to do this ? What are the algorithms?**  
e.g. parallel or tensor methods in 1-dim ?  
but no explicit fermions,..

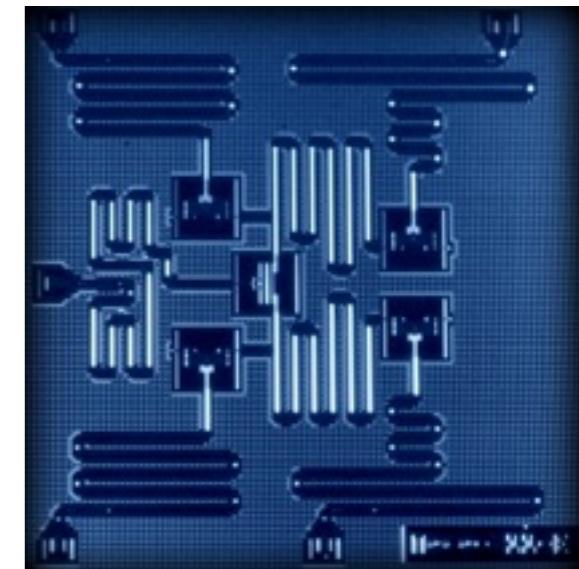


# QC for QFT Start Simple

Two ORNL-led research teams receive \$10.5 million to advance quantum computing for scientific applications



ORNL's Pavel Lougovski (left) and Raphael Pooser will lead research teams working to advance quantum computing for scientific applications. Credit: Oak Ridge National Laboratory, U.S. Dept. of Energy (hi-res image)



DOE-ASCR

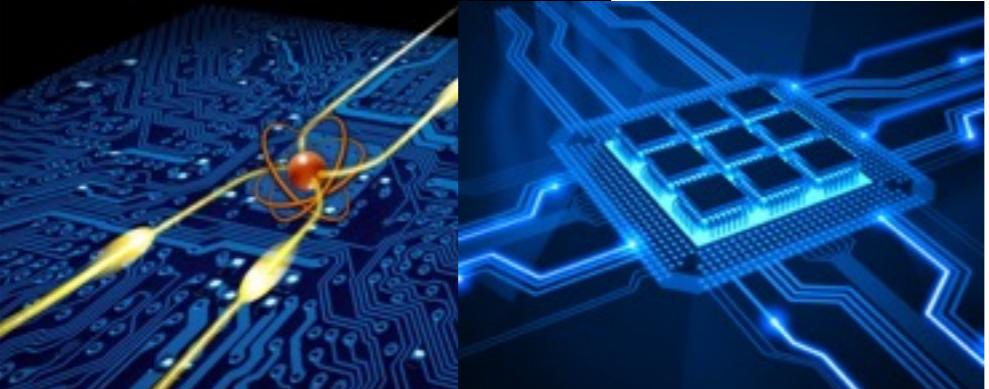
Heterogeneous Digital-Analog Quantum Dynamics Simulations  
Methods and Interfaces for Quantum Acceleration of Scientific Applications

**Quantum-Classical Dynamical Calculations of the Schwinger Model using Quantum Computers**

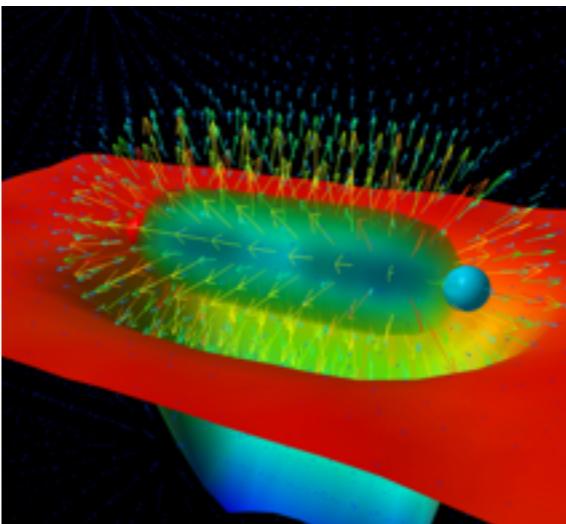
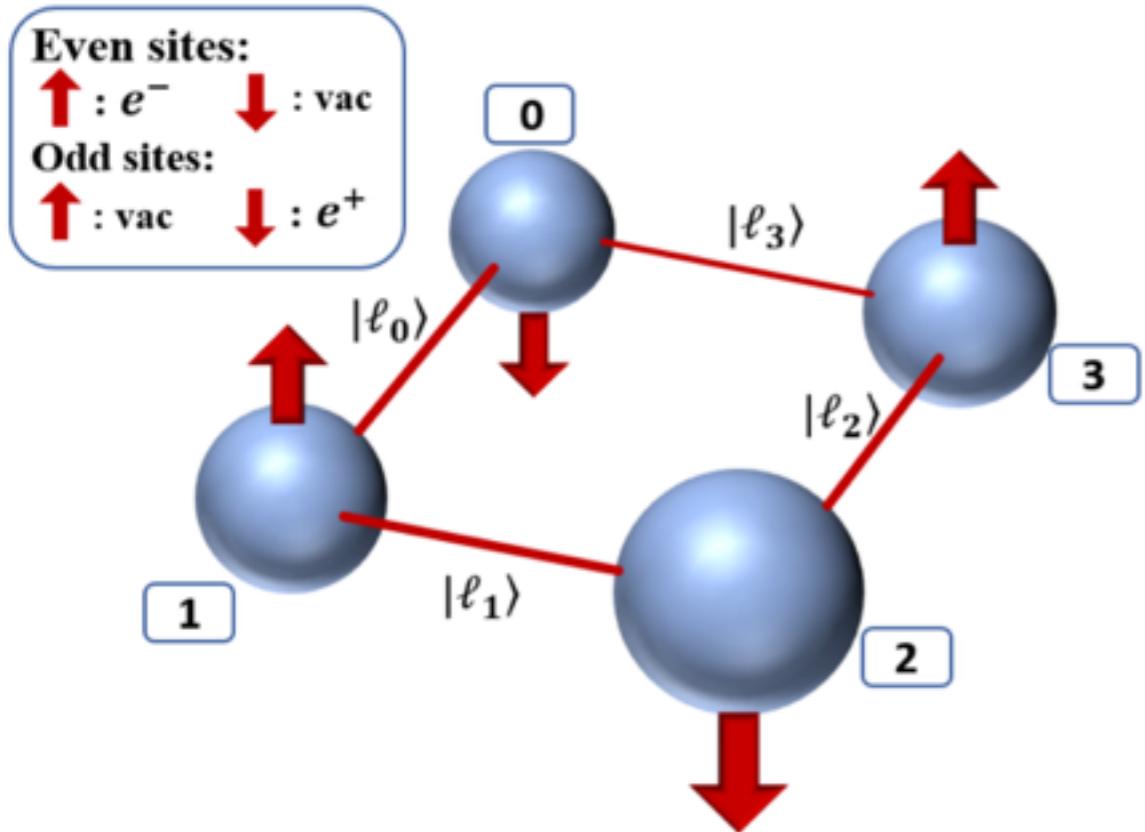
N. Klco, E.F. Dumitrescu, A.J. McCaskey, T.D. Morris, R.C. Pooser, M. Sanz, E. Solano, P. Lougovski, M.J. Savage.

arXiv:1803.03326 [quant-ph]

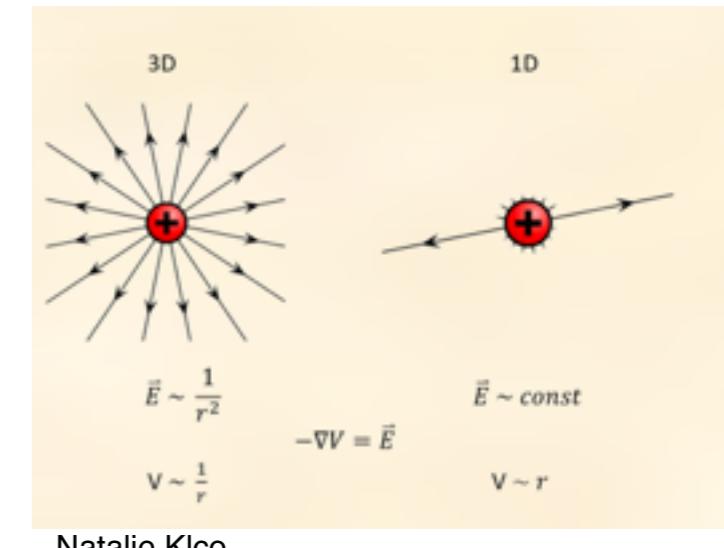
# Starting Simple 1+1 Dim QED Construction



"Quantum computing makes you think about your calculations very differently than programming a classical computer," says Natalie Klco.  
MEDIA CREDIT: WHITNEY SANCHEZ



Derek Leinweber

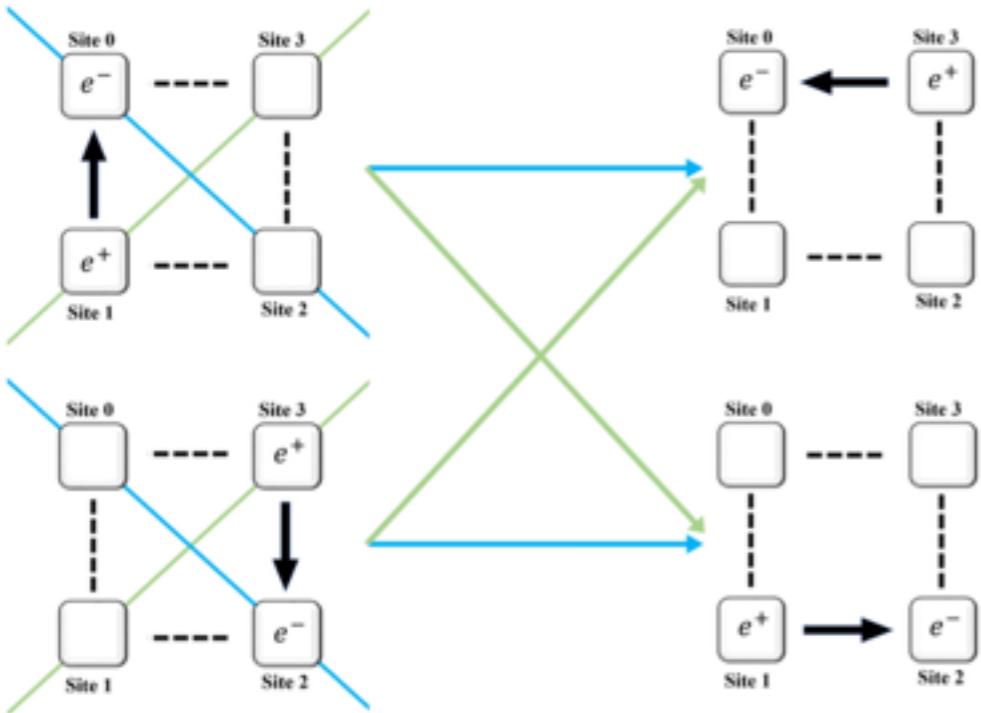
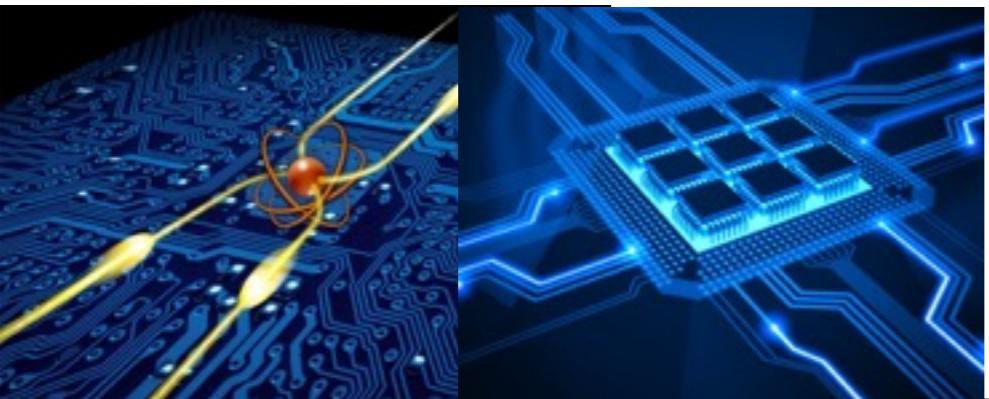


Natalie Klco

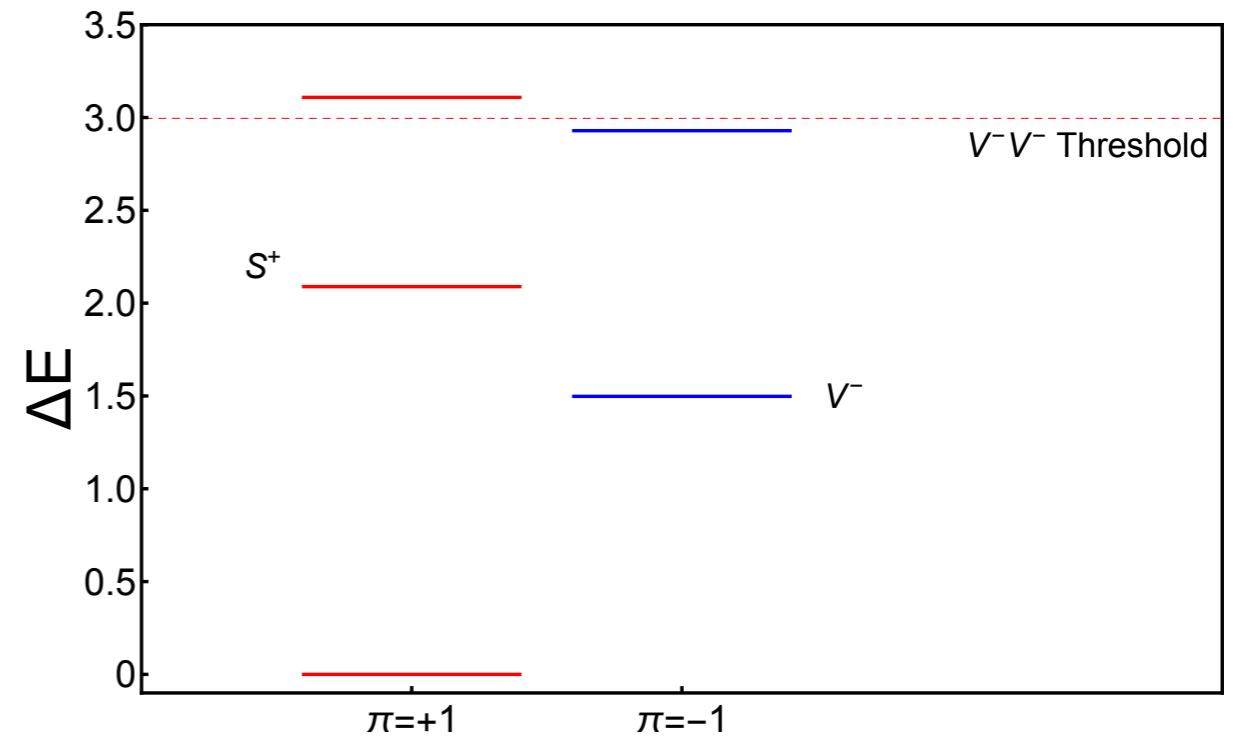
$$\begin{aligned} \hat{H} = & x \sum_{n=0}^{N_{fs}-1} (\sigma_n^+ L_n^- \sigma_{n+1}^- + \sigma_{n+1}^+ L_n^+ \sigma_n^-) \\ & + \sum_{n=0}^{N_{fs}-1} \left( l_n^2 + \frac{\mu}{2} (-)^n \sigma_n^z \right) . \end{aligned}$$

- Clearly, this is just a start - far from infinite-volume and continuum limits
- Will require improved (Symanzik-like) actions, effective field theories, etc

# Starting Simple 1+1 Dim QED Symmetries



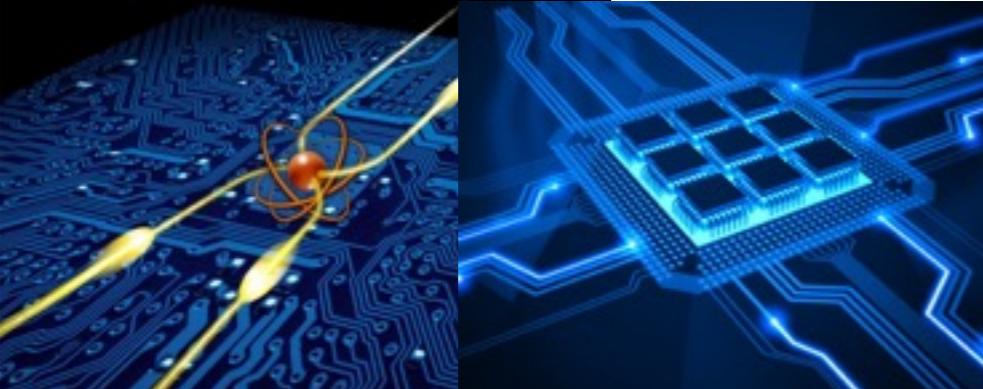
- Gauss's Law
- (Angular) Momentum
- Parity



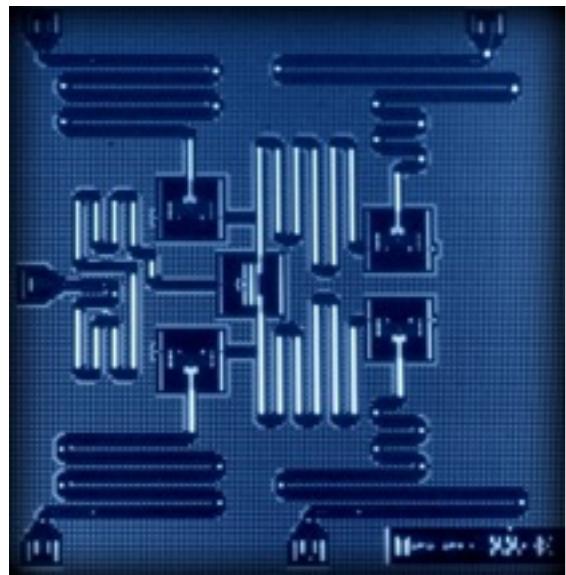
physical sites	$Nq_{\text{lattice}}$	$D_{\text{lattice}}$	$D_{\text{physical}}$	$D_{\mathbf{k}=0}$	$D_{\text{even}}$	$D_{\text{odd}}$	$Nq_{\text{even}}^{\mathbf{k}=0}$	$Nq_{\text{odd}}^{\mathbf{k}=0}$
1	6	64	5	-	3	2	2	1
2	12	$4.1 \times 10^3$	13	9	5	4	3	2
4	24	$1.7 \times 10^7$	117	35	19	16	5	4
6	36	$6.9 \times 10^{10}$	1,186	210	110	100	7	7
8	48	$2.8 \times 10^{14}$	12,389	1,569	801	768	10	10
10	60	$1.2 \times 10^{18}$	130,338	13,078	6,593	6,485	13	13
12	72	$4.7 \times 10^{21}$	1,373,466	114,584	57,468	57,116	16	16

Classical pre-processing  
Can this be done *in situ*?

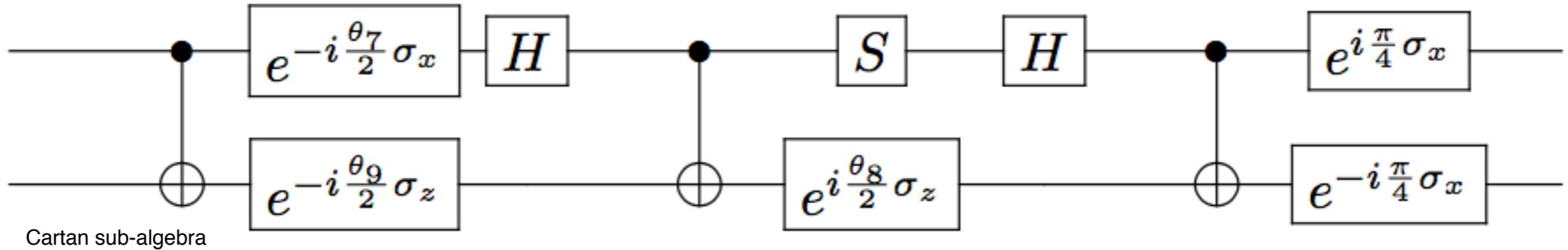
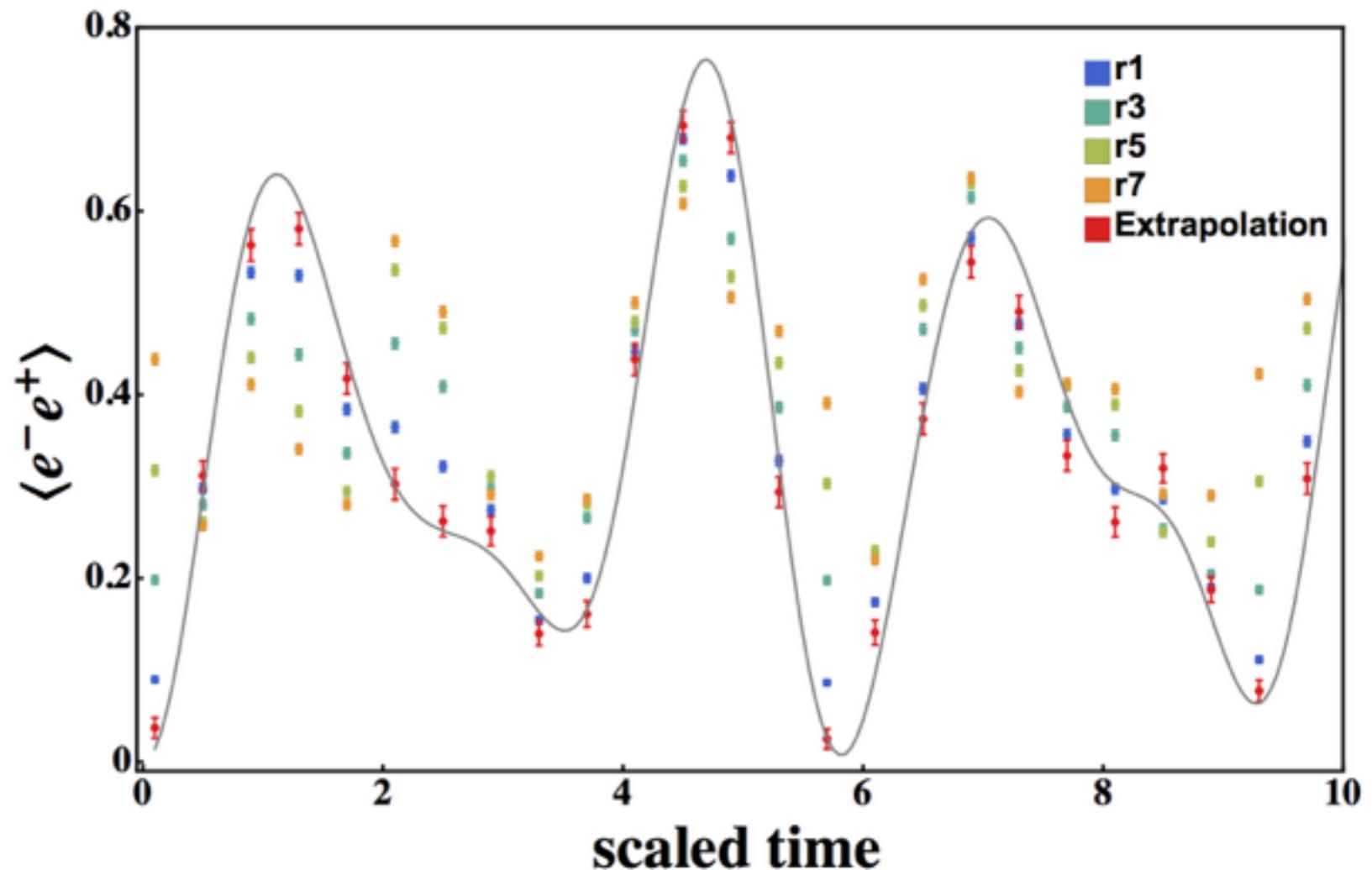
Classical post-processing



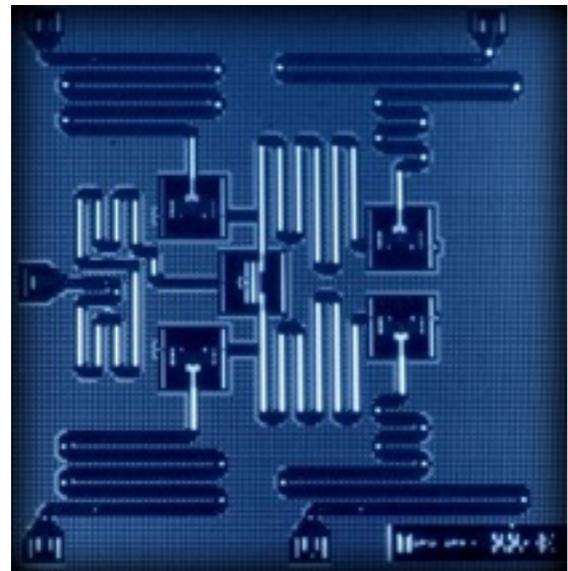
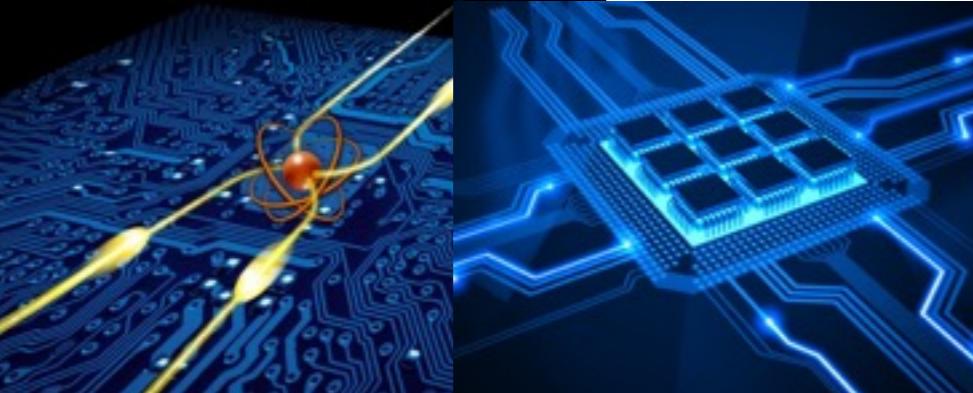
# Starting Simple 1+1 Dim QED Living NISQ - IBM Classically Computed $U(t)$



ibmqx2  
8K shots per point

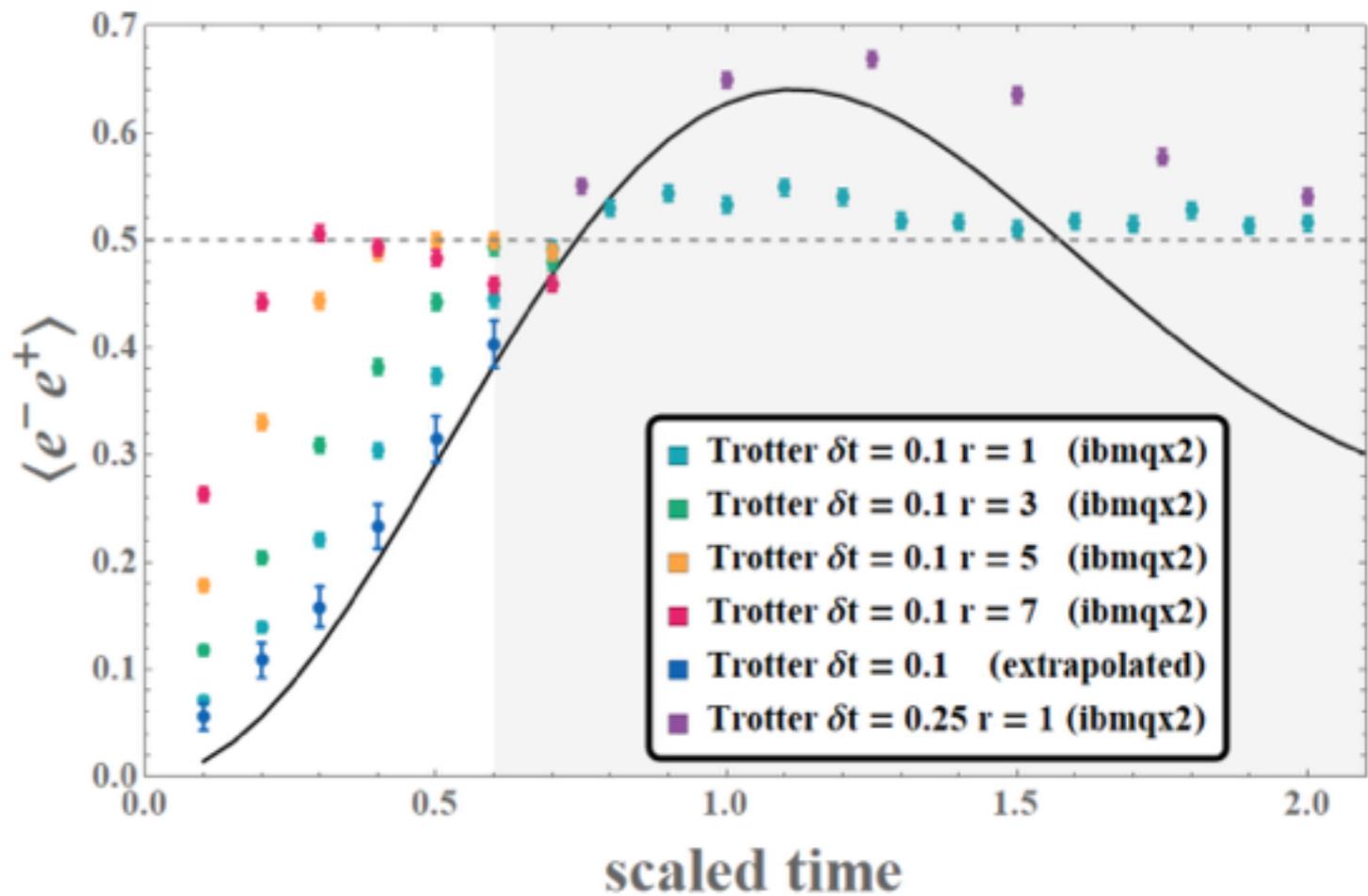


# Starting Simple 1+1 Dim QED Living NISQ - IBM Trotter U(t)



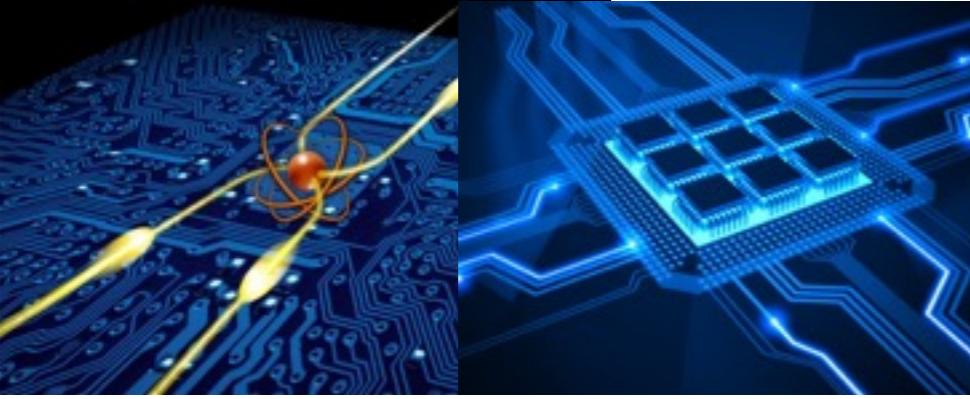
T2 ( $\mu\text{s}$ )      55.20    65.10    47.00    35.10    37.60

$$\begin{aligned} H = & \frac{x}{\sqrt{2}} \sigma_x \otimes \sigma_x + \frac{x}{\sqrt{2}} \sigma_y \otimes \sigma_y - \mu \sigma_z \otimes \sigma_z \\ & + x \left(1 + \frac{1}{\sqrt{2}}\right) I \otimes \sigma_x - \frac{1}{2} I \otimes \sigma_z \\ & - (1 + \mu) \sigma_z \otimes I + x \left(1 - \frac{1}{\sqrt{2}}\right) \sigma_z \otimes \sigma_x \end{aligned}$$



3.6 QPU-s and 260 IBM units

[ ``Capacity computing'' - required only 2 of the 5 qubits on the chip - 5 CNOT gates per step]



# Starting Simple 1+1 Dim QED

## Simple Coding

### Chroma Vs Python3

```
// $Id: HigherLpions_w.cc,v 1.0 SAVAGE Dec 2012 Exp $
/*!
 * \brief Calculate the Two Pion Phase Shift in higher partial waves
 */

#include "chromabase.h"
#include "util/ft/sftmom.h"
#include "HigherLpions_w.h"
#include <iostream>
#include <string>

namespace Chroma {

// pion-pion interactions in higher L
/*!
 * \ingroup hadron
 *
 * This routine is specific to Wilson fermions!
 *
 * Construct propagators for mesons with "u" and "d" quarks.
 * Calculate the correlators for pion (p1) pion (p2) from displaced sources
 *
 * \param u gauge field (Read)
 * \param quark_prop1 quark propagator 1 ( Read )
 * \param quark_prop2 quark propagator 2 ( Read )
 * \param src_coord cartesian coordinates of the source ( Read )
 * \param phases object holds list of momenta and Fourier phases ( Read )
 * \param xml xml file object ( Read )
 * \param xml_group group name for xml data ( Read )
 */
void PIPIints(const multild<LatticeColorMatrix>& u,
               const LatticePropagator& quark_prop1,
               const LatticePropagator& quark_prop2,
               const multild<int>& src_coord1,
               const multild<int>& src_coord2,
               const SftMom& phases,
               XMLWriter& xml,
               const string& xml_group)
{
    START_CODE();

    if ( Ns != 4 || Nc != 3 ){ /* Code is specific to Ns=4 and Nc=3. */
        QDPIO::cerr << "HigherLpions code only works for Nc=3 and Ns=4\n";
        QDP_abort(111);
    }
}
```

Lattice QCD application **chroma** code written by Savage (2012) for NPLQCD, adapted from other **chroma** codes written by Robert Edwards and Balint Joo [JLab, USQCD, SciDAC].

c++

Displaced propagator sources generate hadronic blocks projected onto cubic irreps. to access meson-meson scattering amplitudes in L>0 partial waves.

```
for ii in range(0,len(NTrotter)):
    p0=qp.get_circuit(pidtab[ii])
    ntrott = NTrotter[ii]
    print("Calculating ntrott = ",ii," : = ",ntrott)

    for jjTT in range(0,ntrott):
        print("ii = ",ii," jjTT = ",jjTT, "ntrott =",ntrott)

        # One Trotter Step
        # acting with Cartan sub-algebra to describe a1,a2,a3 = h1,h2,h3

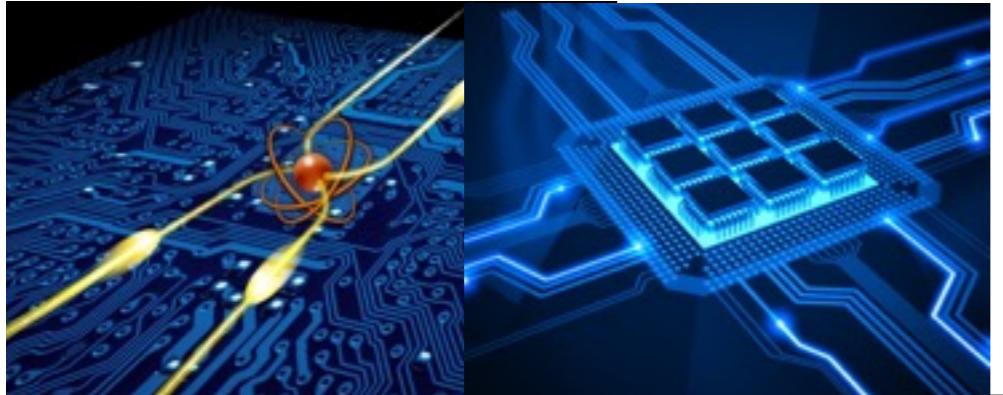
        p0.cx(qr[0],qr[1])
        p0.u3(a1,-halfpi,halfpi,qr[0])
        p0.h(qr[0])
        p0.u3(0,0,a3,qr[1])
        p0.cx(qr[0],qr[1])
        p0.s(qr[0])
        p0.h(qr[0])
        p0.u3(0,0,-a2,qr[1])
        p0.cx(qr[0],qr[1])
        p0.u3(-halfpi,-halfpi,halfpi,qr[0])
        p0.u3(halfpi,-halfpi,halfpi,qr[1])

        # I x sigmax to describe h4

        p0.u3(a4,-halfpi,halfpi,qr[1])
```

**Python3** code written by Savage (2018) to access IBM quantum devices through ``the cloud'' (through ORNL). IBM templates and example codes.

Calculates Trotter evolution of +ve parity sector of the 2-spatial-site Schwinger Model.



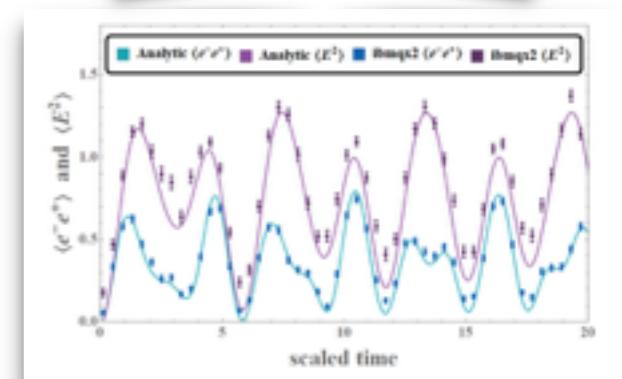
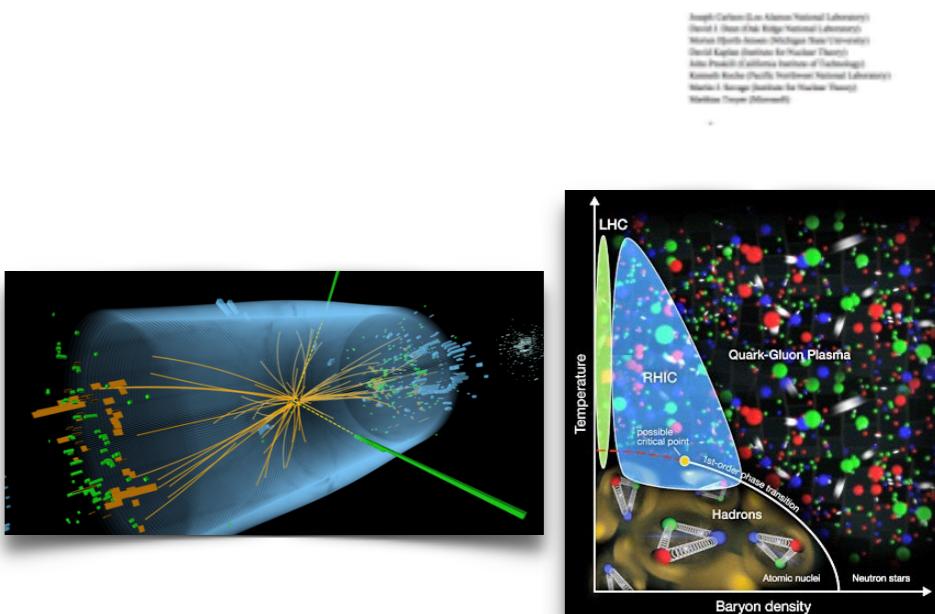
# Summary



## QUANTUM COMPUTING FOR THEORETICAL NUCLEAR PHYSICS

A White Paper prepared for the U.S. Department of Energy, Office of Science, Office of Nuclear Physics

- Exascale conventional computing will provide required precision for many experimentally important quantities in NP and HEP.
- Important **finite density** systems (including modest size nuclei) and **dynamics** require exponentially large conventional computing resources.
- QFTs on QCAs are important for NP and HEP ... start simple ... explore all architectures
- Workforce development is essential - competing with tech. companies for junior scientists is challenging
- NISQ-era coherence times and noise present challenges



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**FIN**