

# Numerical Analysis

## Practical File



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**Name:** Kartavya Gupta

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**Roll No.** 1620016

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# Experiment no. 1

Aim:

Program to implement Bisection Method

Algorithm:

1. Start
2. Choose 'a' and 'b' initial guesses such that  $f(a)*f(b)<0$  or they have opposite signs.
3. If  $f(a)*f(b)<0$  then proceed further otherwise choose the value of 'a' and 'b' again.
4. Find:
5.  $x_m = \frac{a+b}{2}$
6. If  $x_m = 0$  then  $x_m$  is the root of the equation otherwise proceed further
7. If  $f(a)*f(x_m)<0$  then  $a=a$  ;  $b=x_m$
8. If  $f(a)*f(x_m)>0$  then  $a=x_m$  ;  $b=b$
9. Check if  $|a-b| \leq 0.0001$  (acceptable error), if it is true then end otherwise go to step 3.

Input:

```
#include<stdio.h>
#include<conio.h>
#include<math.h>

float f(float x)
{
float y=pow(x,3)-18.0;
return y;
}

void main()
{
clrscr();
float a,b,xm;
getthenumber:printf("\nThe Initial Guess a and b:");
scanf("%f%f",&a,&b);

if((f(a)*f(b))>0)
{
printf("The interval is not valid,please enter again");
gotogetthenumber:
}

xm=(a*(f(b)-b*f(b))/(f(b)-f(a)));
int count =0;

//using while loop
while ((b-a)>0.0001)
{
```

```
if ((f(a)*f(xm))<0)
{
b=xm;
}
else if ((f(a)*f(xm))>0)
{
a=xm;
}

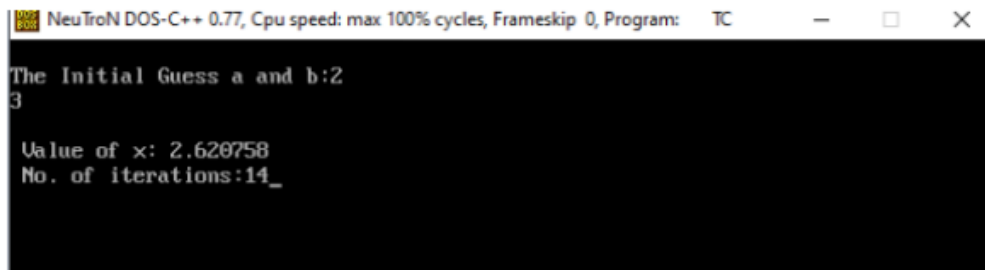
else if ((f(a)*f(xm))==0) {

break;
}

xm=((a+b)/2);
count++;
}

printf("\n Value of x: %f",xm);
printf("\n No. of iterations:%d",count);
getch();
}
```

Output:

A screenshot of a DOS-C++ window titled "NeuTroN DOS-C++ 0.77, Cpu speed: max 100% cycles, Frameskip 0, Program: TC". The window has a black background with white text. The text shows the program's execution: "The Initial Guess a and b:2", followed by a prompt "3" on the next line. Then, the results are displayed: "Value of x: 2.620758" and "No. of iterations:14\_".

```
NeuTroN DOS-C++ 0.77, Cpu speed: max 100% cycles, Frameskip 0, Program: TC
The Initial Guess a and b:2
3
Value of x: 2.620758
No. of iterations:14_
```

## Experiment no. 2

### Aim:

Program to implement Regula falsi method

### Algorithm:

1. Choose 'a' and 'b' initial guesses such that  $f(a)*f(b)<0$  or they have opposite signs.
2. If  $f(a)*f(b)<0$  then proceed further otherwise choose the value of 'a' and 'b' again.
3. Find  $x_n = \frac{af(b)-bf(a)}{f(b)-f(a)}$ .
4. If  $f(a)*f(x_m)<0$  then  $a=a$ ;  $b=x_m$
5. If  $f(a)*f(x_m)>0$  then  $a=x_m$  ;  $b=b$
6. Check if  $|a-b| \leq 0.0001$  (acceptable error), if it is true then end otherwise go to step 3.

### Input:

```
//Program to implement Regula falsi method
#include<stdio.h>

#include<math.h>

#define    f(x)    x*exp(x) - 1

int main()
{
    float a, b, xn, f0, f1, f2, e;
    int itr = 1;

up:
    printf("\nEnter the values of a and b:\n");
    scanf("%f%f", &a, &b);
    printf("Enter error:\n");
    scanf("%f", &e);

    // Calculating Values
    f0 = f(a);
    f1 = f(b);

    /* Checking of valued. */
    if( f0*f1 > 0.0)
    {
        printf("Incorrect Initial Guesses.\n");
        goto up;
    }

    /* using regular falsi method*/
```

}

Output:

```
C:\TURBOC3\BIN>TC

Enter the values of a and b:
0
1
Enter error:
0.1

itr          a          b          xn          f(xn)
1          0.000000      1.000000      0.367879      -0.468536
2          0.367879      1.000000      0.503314      -0.167420
3          0.503314      1.000000      0.547412      -0.053649

Root is: 0.547412_
```

## Experiment no. 3

### Aim:

Program to implement Newton Raphson Method.

### Algorithm:

1. Define the function and its derivative
2. Define error and maximum number of iterations
3. Read initial guess  $x_0$ ,
4. If  $f(x_0) = 0$  then  $x_0$  is the root of the equation , exit
5. If  $f'(x_0) = 0$  then  $x_0$  is not valid , exit.
6. Find  $x_1 = x_0 - (f(x_0)/f'(x_0))$
7. Find  $|x_1 - x_0|$
8. If  $|x_1 - x_0| < \text{error}$  then  $x_1$  is the root, else
9.  $x_1 = x_0$  and follow all steps from step 4

### Input:

```
#include<stdio.h>
#include<conio.h>
#include<math.h>

float func(float x)
{
float y=pow(x,3)-(5*x)+3.0;
return y;
}
float dif(float x){
float z=3*pow(x,2)-5.0;
return z;}
void main()
{
clrscr();
float x[100];
float a,b;
int count=0;
aa:
printf("Enter the initial value \n");
scanf("%f",&x[0]);

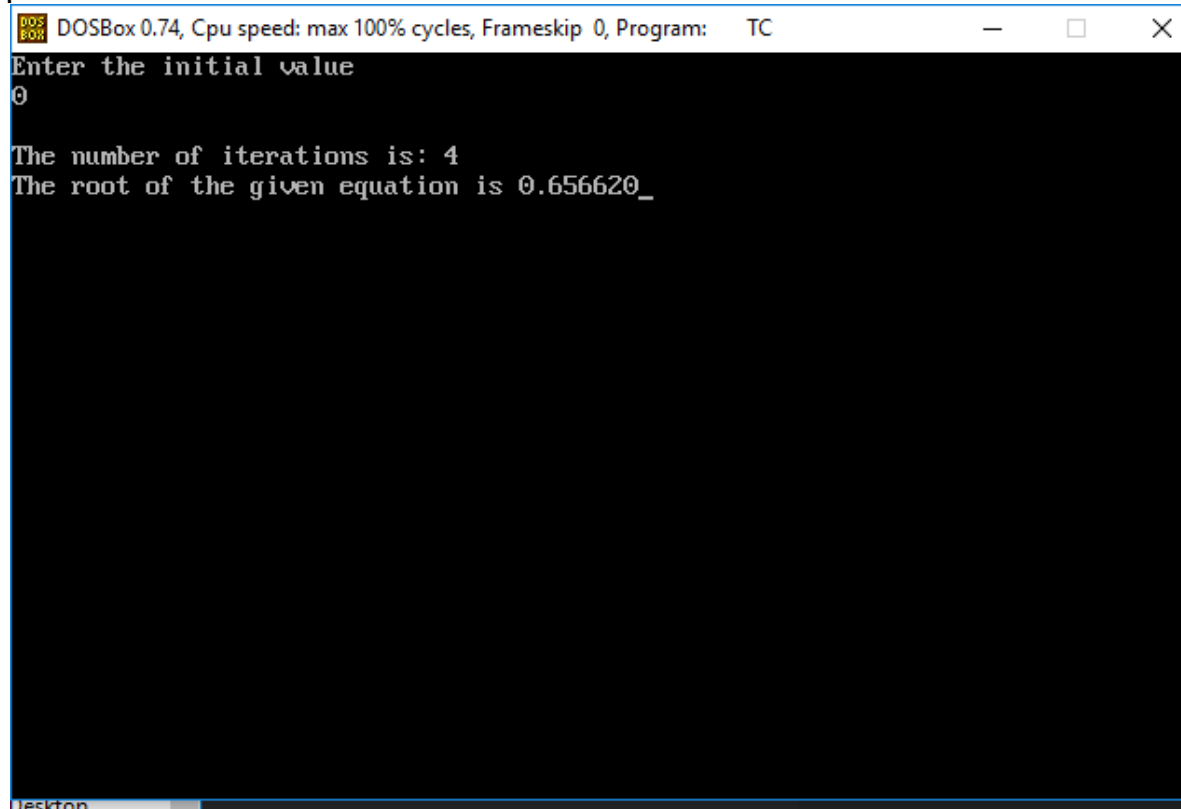
if (dif(x[0])==0){
printf("The value of a is incorrect. \n Press any key to continue!!\n");
goto aa;
}

int n=0;

//using do-while loop
do {
n++;
x[n]=x[n-1]-(func(x[n-1])/dif(x[n-1]));
```

```
count++;
if (dif(x[n])==0){
printf("f(x)=0, Thus, the roots does not exist.\n");
break;}
else{ continue;}
} while (fabs(x[n]-x[n-1])>0.00001);
printf("\nThe number of iterations is: %d",count);
printf("\nThe root of the given equation is %f",x[n]);
getch();
}
```

## Output:



```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC
Enter the initial value
0
The number of iterations is: 4
The root of the given equation is 0.656620_
Desktop
```



# Experiment no. 4

## Aim:

Program to implement Secant Method.

## Algorithm:

1. Define  $f(x)$
2. Choose 'a' and 'b' initial guesses such that  $f(a)*f(b)<0$  or they have opposite signs.
3. If  $f(a)*f(b)<0$  then proceed further otherwise choose the value of 'a' and 'b' again.
4. Find  $x_n = \frac{a+b}{2}$ .
5. If  $f(a)*f(x_m)<0$  then  $a=a$ ;  $b=x_m$ .
6. If  $f(a)*f(x_m)>0$  then  $a=x_m$  ;  $b=b$ .

## Input:

```
#include<stdio.h>
#include<conio.h>
#include<math.h>

float f(float x)
{
    float y=pow(x,3)-18.0;
    return y;
}

void main()
{
    clrscr();
    float a,b,xm;
    printf("\nThe Initial Guess a and b:");
    scanf("%f%f",&a,&b);

    int count =0;

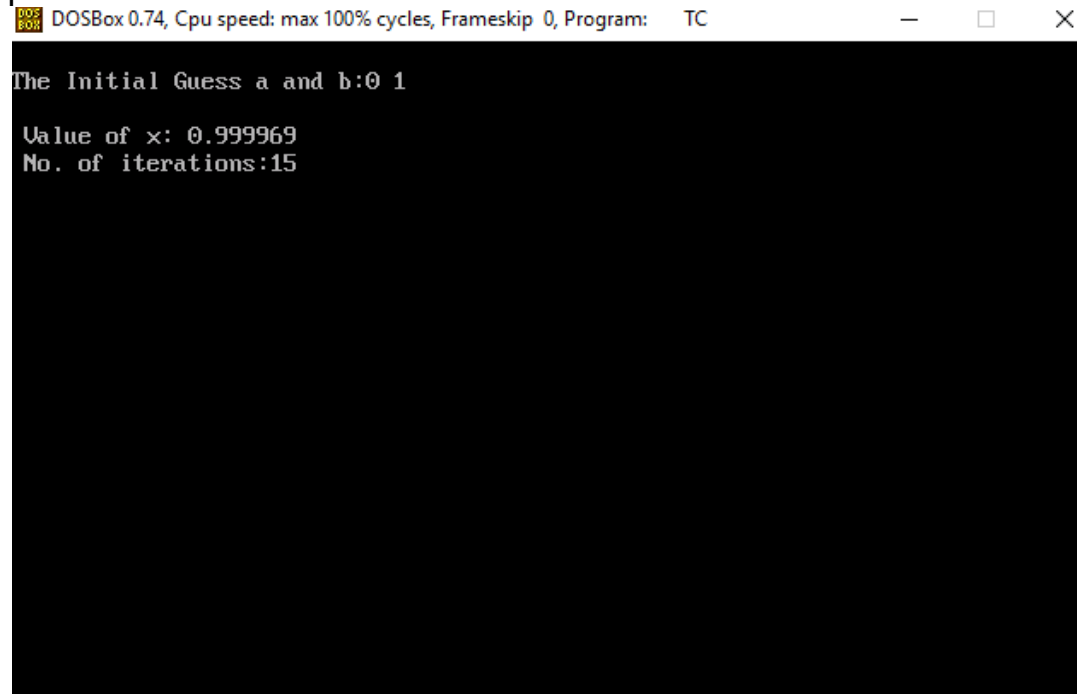
    //using while loop
    while ((b-a)>0.0001)
    {
        if ((f(a)*f(xm))<0)
        {
            b=xm;
        }
        else if ((f(a)*f(xm))>0)
        {
            a=xm;
        }

        else if((f(a)*f(xm))==0){

            break;
        }
    }
```

```
xm = ((a+b)/2);  
count++;  
}  
  
printf("\n Value of x: %f",xm);  
printf("\n No. of iterations:%d",count);  
getch();  
}
```

## Output:

A screenshot of a DOSBox window. The title bar reads "DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC". The window contains a black terminal area with white text. The text displayed is: "The Initial Guess a and b:0 1", "Value of x: 0.999969", and "No. of iterations:15".

```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC  
The Initial Guess a and b:0 1  
Value of x: 0.999969  
No. of iterations:15
```

# Experiment no. 5

## Aim:

Program to solve a problem using LaGrange's interpolation.

## Algorithm:

1. Define two array X and Y, int i, a,y
2. Read the values of arrays X and Y where elements of array Y are the corresponding values of Y for X
3. Read the value of a to be calculated
4. Define the formula
5. Result of the formula will be the desired result
6. End

## Input:

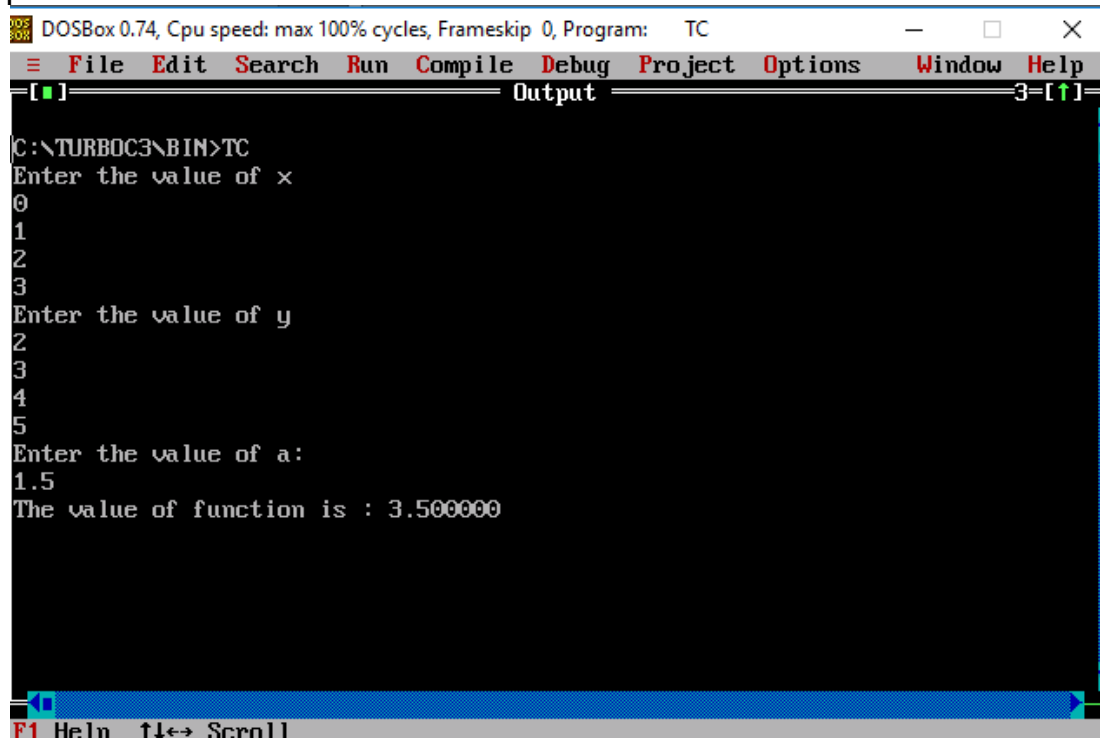
```
#include<stdio.h>
#include<stdlib.h>

void main()
{
    int i,x[4], y[4]; //no of values are 4
    double x1,x2,x3,x4,a,y1;
    printf("Enter the value of x\n");
    for(i=0;i<4;i++)
    {
        scanf("%d",&x[i]);
    }
    printf("Enter the value of y\n");
    for(i=0;i<4;i++)
    {
        scanf("%d",&y[i]);
    }
    printf("Enter the value of a:\n");
    scanf("%lf", &a);

    x1= ((a-x[1])*(a-x[2])*(a-x[3])*y[0])/((x[0]-x[1])*(x[0]-x[2])*(x[0]-x[3]));
    x2=((a-x[0])*(a-x[2])*(a-x[3])*y[1])/((x[1]-x[0])*(x[1]-x[2])*(x[1]-x[3]));
    x3=((a-x[0])*(a-x[1])*(a-x[3])*y[2])/((x[2]-x[0])*(x[2]-x[1])*(x[2]-x[3]));
```

```
x4=((a-x[0])*(a-x[1])*(a-x[2])*y[3])/((x[3]-x[0])*(x[3]-x[1])*(x[3]-x[2]));  
y1 = x1+x2+x3+x4;  
printf("The value of function is : %lf",y1);  
}
```

## Output:



```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC  
File Edit Search Run Compile Debug Project Options Window Help  
[ ] Output 3-[↑]  
C:\TURBOC3\BIN>TC  
Enter the value of x  
0  
1  
2  
3  
Enter the value of y  
2  
3  
4  
5  
Enter the value of a:  
1.5  
The value of function is : 3.500000  
F1 Help ↑↓←→ Scroll
```

# Experiment no. 6

## Aim:

To solve the problem using linear regression.

## Algorithm:

1. Read n (no of data points) from the user and declare a,b.
2. Use for loop to read the values of x and y from the user in x[i],y[i].
3. Initailize sumx1=0, sumx2=0, sumy1=0, sumxy=0
4. Use loop to calculate summation-  
 $\text{sumx1} = \text{sumx1} + x[i]$   
 $\text{sumx2} = \text{sumx2} + x[i]*x[i]$   
 $\text{sumy1} = \text{sumy1} + y[i]$   
 $\text{sumxy} = \text{sumxy} + x[i]*y[i]$
5. Use a and b-  
 $a = (n*\text{sumxy} - \text{sumx1}*\text{sumy1}) / (n*\text{sumx2} - \text{sumx1}*\text{sumx1})$   
 $b = (\text{sumy1}*\text{sumx2} - \text{sumx1}*\text{sumxy}) / (n*\text{sumx2} - (\text{sumx1}*\text{sumx1}))$
6. Display value of a and b. Read the values of arrays X and Y where elements of array Y are the corresponding values of Y for X

## Input:

```
// To solve the solution of linear regression
#include<stdio.h>
#include<stdlib.h>
#include<math.h>

int main()
{
    double a0,a1,x[10],y[10];
    double sumx=0,sumxy=0,sumx2=0,sumy=0;
    int i,n;
    printf("Linear Regresion \n");
    printf("Enter the date value of n: ");
    scanf("%d",&n);

    printf("Enter the values of X:\n");
    for(i=0;i<n;i++)
    {
        scanf("%lf",&x[i]);
    }

    printf("Enter the value of Y:\n");
    for(i=0;i<n;i++)
    {
        scanf("%lf",&y[i]);
    }
}
```

```

for(i=0;i<n;i++)
{
sumx= sumx + x[i];
sumx2 = sumx2 + x[i]*x[i];
sumy= sumy + y[i];
sumxy= sumxy + x[i]*y[i];
}

printf("X\t\tY\t\tX^2\t\t\tXY\n");
for(i=0;i<n;i++)
{
printf("%lf\t%lf\t%lf\t\t\t%lf\n",x[i],y[i],x[i]*x[i],x[i]*y[i]);
}

a0= ((sumy*sumx2) - (sumx*sumxy)) / ((n*sumx2)-(sumx*sumx));
a1= ((n*sumxy)-(sumx*sumy)) / ((n*sumx2)-(sumx*sumx));

printf("Y=%lf x + %lf",a1,a0);

}

```

## Output:

DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC

File Edit Search Run Compile Debug Project Options Window Help

Output

```

Enter the date value of n: 5
Enter the values of X:
1
2
3
4
5
Enter the value of Y:
2
4
6
8
10
X          Y          X^2          XY
1.000000   2.000000   1.000000   2.000000
2.000000   4.000000   4.000000   8.000000
3.000000   6.000000   9.000000  18.000000
4.000000   8.000000  16.000000  32.000000
5.000000  10.000000  25.000000  50.000000
Y=2.000000x + 0.000000_

```

F1 Help ↑↓↔ Scroll

# Experiment no. 7

## Aim:

To solve the problem using implement Trapezoidal rule.

## Algorithm:

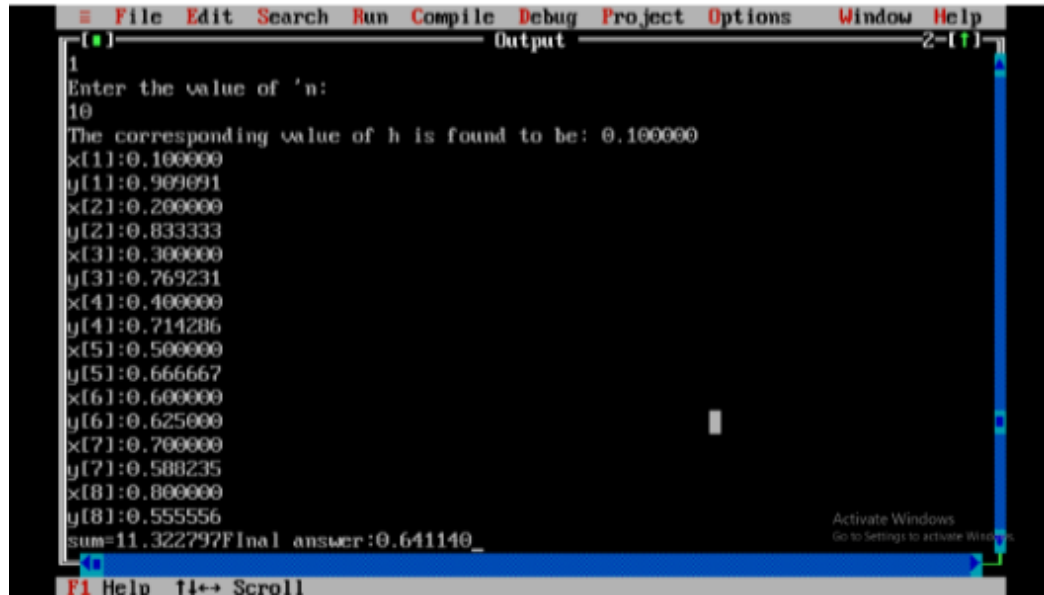
1. Call the function
2. Define h, n,a,b,ans,I,i array X, array Y
3. Define f(x), sum=0
4. Calculate h
5. Using 'for' loop from i=0 to i<n receive the values of array x
6. Using 'for' loop calculate the value of corresponding y as  $y = f(x[i])$
7. Calculate sum of the middle term
8. Calculate integral as  $I = h[y[0] + y[n] + 2 * \text{Sum}] / 2$
9. Print the result.

## Input:

```
#include <math.h>
#include <stdio.h>
#include <conio.h>
float f(float x){
float y=(1/(1+x));
return y;
}
void main(){
float a, b, h;
float x[10], y[10];
int n,i,j;
printf("Enter the value of 'a':\n");
scanf("%f",&a);
printf("Enter the value of 'b':\n");
scanf("%f",&b);
printf("Enter the value of 'n':\n");
scanf("%d",&n);
h=(b-a)/n;
printf("The corresponding value of h is found to be: %f\n",h);
x[0]=a;
x[n-1]=b;
for(i=1;i<(n-1);i++){
x[i]=x[i-1]+h;
y[i]=f(x[i]);
printf("x[%d]:%f\n",i,x[i]);
printf("y[%d]:%f\n",i,y[i]);
}
float sum,integ;
sum=0.0;
integ=0.0;
for (j=1;j<n-1;j++){
sum+=(2*y[j]);
}
printf("sum=%f",sum);
y[0]=f(x[0]);
```

```
y[n-1]=f(x[n-1]);  
integ+=(h/2)*(sum+y[0]+y[n-1]);  
printf("FInal answer:%f",integ);  
}
```

Output:



```
1  
Enter the value of 'n':  
10  
The corresponding value of h is found to be: 0.100000  
x[1]:0.100000  
y[1]:0.909091  
x[2]:0.200000  
y[2]:0.833333  
x[3]:0.300000  
y[3]:0.769231  
x[4]:0.400000  
y[4]:0.714286  
x[5]:0.500000  
y[5]:0.666667  
x[6]:0.600000  
y[6]:0.625000  
x[7]:0.700000  
y[7]:0.588235  
x[8]:0.800000  
y[8]:0.555556  
sum=11.322797FInal answer:0.641140_
```



# Experiment no. 8

## Aim:

To solve the problem using implement simpson's rule.

## Algorithm:

1. Start
2. Define a,b,n,h,z,sum = 0,Result.
3. Find  $h = (b-a)/n$ .
4. Define  $x[i], f[i]$ .
5. Run loop to find  $x[i], f[i]$ .
6. Run if conditional statements to modify the sum of odd and even indexed terms.
7. Compute Result from the formula
8.  $Result = h(f_0 + sum + f(n))/3$ .
9. Stop

## Input:

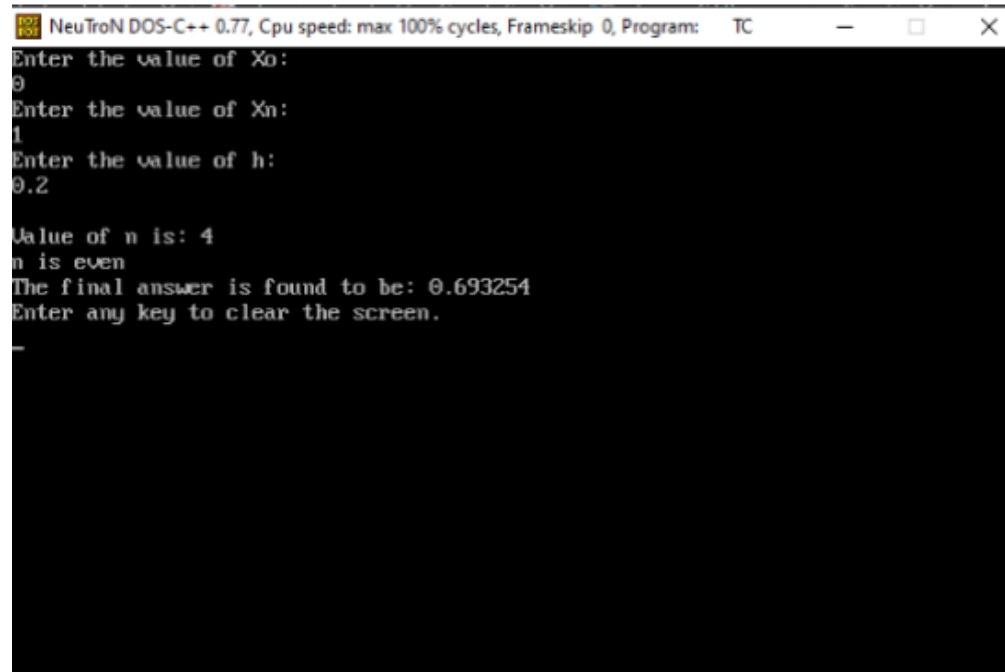
```
#include <stdio.h>
#include <conio.h>
#include <math.h>

float f(float x){
return (1/(1+x));
}

void main(){
int i,n;
float x0, xn, h, y[20], x[20], so, se, ans;
printf("Enter the value of Xo:\n");
scanf("%f", &x0);
printf("Enter the value of Xn:\n");
scanf("%f",&xn);
printf("Enter the value of h: \n");
scanf("%f",&h);
n=(xn-x0)/h;
printf("\nValue of n is: %d",n);
if (n%2==1){
printf("\nn is odd");
n=n+1;
}else{
printf("\nn is even");
}
h=(xn-x0)/n;
for (i=0;i<(n+1);i++){
x[i]=x[0]+(i*h);
y[i]=f(x[i]);
}
se=0;
so=0;
for (i=1;i<n;i++){
if (i%2==1){
so+=y[i];
}
```

```
}  
else{  
se+=y[i];  
}  
}  
ans=(h/3)*(y[0]+y[n]+(4*so)+(2*se));  
printf("\nThe final answer is found to be: %f",ans);  
printf("\nEnter any key to clear the screen.\n");  
getch();  
clrscr();  
}
```

Output:



The screenshot shows a Turbo C++ DOS window titled "NeuTroN DOS-C++ 0.77, Cpu speed: max 100% cycles, Frameskip 0, Program: TC". The window has a black background with white text. The output of the program is as follows:

```
Enter the value of Xo:  
0  
Enter the value of Xn:  
1  
Enter the value of h:  
0.2  
  
Value of n is: 4  
n is even  
The final answer is found to be: 0.693254  
Enter any key to clear the screen.  
-
```

# Experiment no. 9

## Aim:

To solve the problem using implement Euler's method.

## Algorithm:

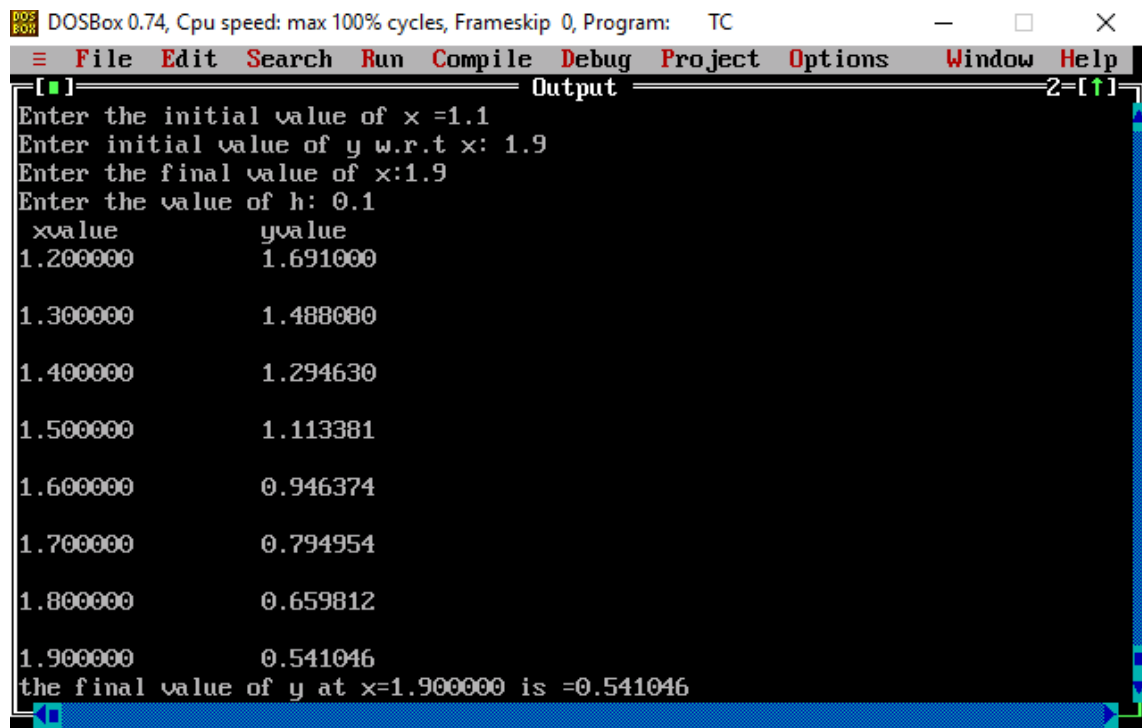
1. Start
2. Declare  $f(x,y)$ .
3. Read  $x_0, y_0, x_n, h$  from the user (where  $x_n$  is the final value of  $x$ ).
4. Apply for ( $x=x_0; x < x_n; x+=h$ ) for computing values of  $y$  by using formula-  $y_{n+1} = y_n + h * f(x_n, y_n)$ .
5. Display the values of  $x$  and  $y$  on the screen.
6. Print the final value of  $y$ .
7. Stop

## Input:

```
#include<stdio.h>
#include<math.h>
void main()
{
    double x0,y0,xn,h,x,y;
    double f(double x, double y);
    printf("Enter the initial value of x =");
    scanf("%lf",&x0);
    printf("Enter initial value of y w.r.t x: ");
    scanf("%lf",&y0);
    printf("Enter the final value of x:");
    scanf("%lf",&xn);
    printf("Enter the value of h: ");
    scanf("%lf",&h);
    printf(" xvalue \t yvalue");
    for(x=x0;x<xn;x+=h)
    {
        y=y0+h*f(x,y0);
        printf("\n");
        printf("%lf \t %lf \n",x+h,y);
        y0=y;
    }
    printf("the final value of y at x=%lf is =%lf",x,y);
}

double f(double x, double y)
{
    return -(x*y);
}
```

## Output:



```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC
File Edit Search Run Compile Debug Project Options Window Help
[ ] Output 2-[ ]
Enter the initial value of x =1.1
Enter initial value of y w.r.t x: 1.9
Enter the final value of x:1.9
Enter the value of h: 0.1
xvalue      yvalue
1.200000    1.691000
1.300000    1.488080
1.400000    1.294630
1.500000    1.113381
1.600000    0.946374
1.700000    0.794954
1.800000    0.659812
1.900000    0.541046
the final value of y at x=1.900000 is =0.541046
```

# Experiment no. 10

## Aim:

To solve the problem using implement Gauss seidel Iteration method.

## Algorithm:

1. Start
2. Define function  $f(x,y,z), s(x,y,z), t(x,y,z)$
3. Choose initial guesses  $x_0, y_0, z_0$ .
4. Choose pre-specified tolerable error.
5. Run do while loop changing the values of  $x_1, y_1, z_1$  by using the assumed given values/guesses.
6. While  $|dx-x_1| > \text{error}, |dy-y_1| > \text{error}, |dz-z_1| > \text{error}$  then goto (5) otherwise goto (7).
7. Display  $x_1, y_1, z_1$  as root.
8. Stop

## Input:

```
/* Program to implement Gauss Scidel Method */
#include<stdio.h>
#include<conio.h>
#include<math.h>

float f(float x, float y, float z)
{
    x = ( (9 - (2*y) - z) / 10 );
    return x;
}

float s(float x, float y, float z)
{
    y = ( (-44 - (2*x) + (2*z)) / 20 );
    return y;
}

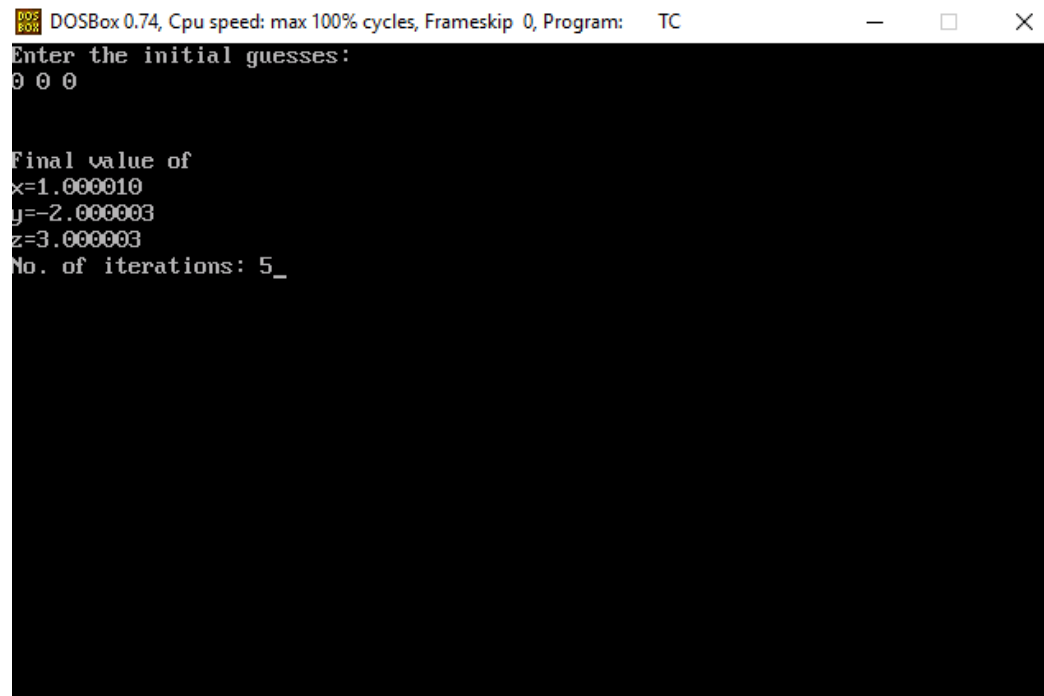
float t(float x, float y, float z)
{
    z = ( (-22 - (2*x) + (3*y)) / (-10) );
    return z;
}

void main()
{
    clrscr();
    float x0, y0, z0, x1=0, y1=0, z1=0, tempx, tempy, tempz, acc=0.0001;
    int i=0;
    printf("Enter the initial guesses:\n");
    scanf("%f %f %f", &x0, &y0, &z0);
    do{
        tempx=x1;
        tempy=y1;
        tempz=z1;
        x1=f(x0, y0, z0);
        y1=s(x1, y0, z0);
        z1=t(x1, y1, z0);
```

```
i++;
x0=x1;
y0=y1;
z0=z1;
}
while (fabs (tempx-x1)>acc&&fabs (tempy-y1)>acc&&fabs (tempz-z1)>acc);

printf("\n\nFinal value of\n");
printf("x=%f \ny=%f \nz=%f \n",x1,y1,z1);
printf("No. of iterations: %d",i);
getch();
}
```

## Output:



```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC
Enter the initial guesses:
0 0 0

Final value of
x=1.000010
y=-2.000003
z=3.000003
No. of iterations: 5_
```

# Experiment no. 11

## Aim:

To solve the problem using implement Runge-Kutta method.

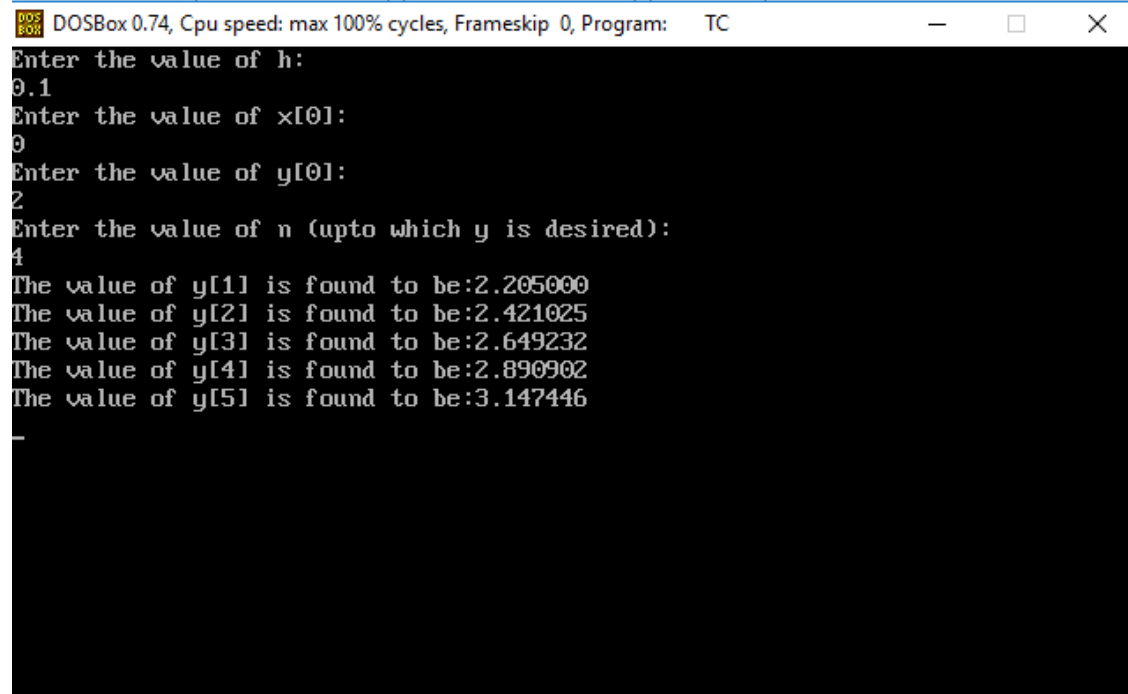
## Input:

```
#include <stdio.h>
#include <conio.h>
#include <math.h>

float f(float x,float y){
float a=y-x;
return a;
}

void main(){
clrscr();
float h,k1,k2,k3,k4,a,b;
int n,i;
float x[20], y[20];
printf("Enter the value of h:\n");
scanf("%f",&h);
printf("Enter the value of x[0]:\n");
scanf("%f",&a);
x[0]=a;
printf("Enter the value of y[0]:\n");
scanf("%f",&b);
y[0]=b;
printf("Enter the value of n (upto which y is desired):\n");
scanf("%d",&n);
for (i=0;i<(n+1);i++){
k1=h*f(x[i],y[i]);
x[i+1]=x[i]+h;
k2=h*f(x[i+1],(y[i]+k1));
y[i+1]=y[i]+(0.5*(k1+k2));
printf("The value of y[%d] is found to be:%f\n",(i+1),y[i+1]);
}
getch();
}
```

## Output:

A screenshot of a DOSBox window. The title bar reads "DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC". The window contains a black terminal area with white text. The text shows a series of prompts and user inputs, followed by calculated values for y[1] through y[5].

```
DOSBox 0.74, Cpu speed: max 100% cycles, Frameskip 0, Program: TC
Enter the value of h:
0.1
Enter the value of x[0]:
0
Enter the value of y[0]:
2
Enter the value of n (upto which y is desired):
4
The value of y[1] is found to be:2.205000
The value of y[2] is found to be:2.421025
The value of y[3] is found to be:2.649232
The value of y[4] is found to be:2.890902
The value of y[5] is found to be:3.147446
_
```