

ALGORITHM-

classmate
Date 15/10/24
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WEEK-2

Implementing A* (A star) search algorithm.

ALGORITHM :

step 1: Initialization:

- start from initial state of puzzle.
- use priority queue to explore nodes based on $f(n) = g(n) + h(n)$

step 2: Expansion:

- expand node with lowest $f(n)$
- generate child nodes by sliding adjacent tiles into blank space

step 3: Evaluation

- for each child node calculate $f(n)$
- continue until goal state is reached.

step 4: Termination

- the search ends when current node corresponds to goal state
- ~~back track~~ to get solution.

Heuristic →

Number of misplaced tiles:

counts of how many tiles are not in current position

Manhattan distance :

sum the distance of each tile from current position to goal state.

OUTPUT:

1. Number of tiles.

solution path using misplaced tiles:

step 0: $h(n)=5$, $g(n)=0$, $f(n)=5$

2	8	3
1	6	4
0	7	5

step 1: $h(n)=4$, $g(n)=1$, $f(n)=5$

2	8	3
1	6	4
7	0	5

step 2: $h(n)=3$, $g(n)=2$, $f(n)=5$

2	8	3
1	0	4
7	6	5

step 3: $h(n)=2$, $g(n)=3$, $f(n)=6$

2	0	3
1	8	4
7	6	5

step 4: $h(n)=2$, $g(n)=4$, $f(n)=6$

0	2	3
1	8	4
7	6	5

step 5: $h(n)=1$ $g(n)=5$ $f(n)=6$

1	2	3
0	8	4
7	6	5

step 6: $h(n)=0$ $g(n)=6$ $f(n)=6$

1	2	3
8	0	4
7	6	5

2. Manhattan distance

step 0: $h(n)=6$ $g(n)=0$ $f(n)=6$

2	8	3
1	6	4
0	7	5

step 1: $h(n)=5$ $g(n)=1$ $f(n)=6$

2	8	3
1	6	4
7	0	5

step 2: $h(n)=4$ $g(n)=2$ $f(n)=6$

2	8	3
1	0	4
7	6	5

step 3: $h(n)=3$ $g(n)=3$ $f(n)=6$

2	0	3
1	8	4
7	6	5

step 4: $h(n) = 2$, $g(n) = 4$, $f(n) = 6$

0	2	3
1	8	4
7	6	5

step 5: $h(n) = 1$, $g(n) = 5$, $f(n) = 6$

1	2	3
0	8	4
7	6	5

step 6: $h(n) = 0$, $g(n) = 6$, $f(n) = 6$

1	2	3
8	0	4
7	6	5

Run
15/10/24

CODE / INPUT -

MISPLACED TILES-

```
goal_state = [
    [1, 2, 3],
    [8, 0, 4], # 0 represents the blank space
    [7, 6, 5]
]
# Function to calculate the number of misplaced tiles
def misplaced_tiles(state, goal_state):
    count = 0
    for i in range(3):
```

```

        for j in range(3):
            if state[i][j] != 0 and state[i][j] != goal_state[i][j]:
                count += 1
        return count
import heapq
def find_blank_tile(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j
def get_possible_moves(state):
    row, col = find_blank_tile(state)
    moves = []
    if row > 0:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row - 1][col] = new_state[row - 1][col],
new_state[row][col]
        moves.append(new_state)
    if row < 2:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row + 1][col] = new_state[row + 1][col],
new_state[row][col]
        moves.append(new_state)
    if col > 0:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row][col - 1] = new_state[row][col - 1],
new_state[row][col]
        moves.append(new_state)
    if col < 2:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row][col + 1] = new_state[row][col + 1],
new_state[row][col]
        moves.append(new_state)
    return moves
def a_star_search_misplaced(initial_state, goal_state, heuristic):
    open_list = [(heuristic(initial_state, goal_state), 0, initial_state, [])] # (f(n), g(n), state, path)
    closed_set = set()
    while open_list:
        f_n, g_n, current_state, path = heapq.heappop(open_list)

```

```

    if current_state == goal_state:
        return path + [current_state]
    state_tuple = tuple(map(tuple, current_state))
    if state_tuple in closed_set:
        continue
    closed_set.add(state_tuple)
    for neighbor in get_possible_moves(current_state):
        neighbor_tuple = tuple(map(tuple, neighbor))
        if neighbor_tuple in closed_set:
            continue
        new_g_n = g_n + 1
        new_h_n = heuristic(neighbor, goal_state)
        new_f_n = new_g_n + new_h_n
        heapq.heappush(open_list, (new_f_n, new_g_n, neighbor, path + [current_state]))
    return None

def display_solution_misplaced(path, heuristic, goal_state):
    if path:
        print(f'Solution path using misplaced tiles heuristic:')
        for step, state in enumerate(path):
            h = heuristic(state, goal_state)
            g = step
            f = g + h
            print(f'Step {step}: h(n)={h}, g(n)={g}, f(n)={f}')
            for row in state:
                print(row)
            print()
    else:
        print(f'No solution found using misplaced tiles heuristic.')

initial_state = [
    [2, 8, 3],
    [1, 6, 4],
    [0, 7, 5]
]

solution_path_misplaced = a_star_search_misplaced(initial_state, goal_state, misplaced_tiles)
display_solution_misplaced(solution_path_misplaced, misplaced_tiles, goal_state)

```

OUTPUT-

Solution path using misplaced tiles heuristic:

Step 0: $h(n)=5$, $g(n)=0$, $f(n)=5$

[2, 8, 3]

[1, 6, 4]

[0, 7, 5]

Step 1: $h(n)=4$, $g(n)=1$, $f(n)=5$

[2, 8, 3]

[1, 6, 4]

[7, 0, 5]

Step 2: $h(n)=3$, $g(n)=2$, $f(n)=5$

[2, 8, 3]

[1, 0, 4]

[7, 6, 5]

Step 3: $h(n)=3$, $g(n)=3$, $f(n)=6$

[2, 0, 3]

[1, 8, 4]

[7, 6, 5]

Step 4: $h(n)=2$, $g(n)=4$, $f(n)=6$

[0, 2, 3]

[1, 8, 4]

[7, 6, 5]

Step 5: $h(n)=1$, $g(n)=5$, $f(n)=6$

[1, 2, 3]

[0, 8, 4]

[7, 6, 5]

Step 6: $h(n)=0$, $g(n)=6$, $f(n)=6$

[1, 2, 3]

[8, 0, 4]

[7, 6, 5]

CODE / INPUT -

MANHATTAN DISTANCE-

```
goal_state = [
    [1, 2, 3],
    [8, 0, 4], # 0 represents the blank space
    [7, 6, 5]
]

# Function to calculate Manhattan distance
def manhattan_distance(state, goal_state):
    distance = 0
    for i in range(3):
        for j in range(3):
            if state[i][j] != 0:
                goal_position = [(row, col) for row in range(3) for col in range(3) if
goal_state[row][col] == state[i][j]][0]
                distance += abs(i - goal_position[0]) + abs(j - goal_position[1])
    return distance

import heapq
def find_blank_tile(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def get_possible_moves(state):
    row, col = find_blank_tile(state)
    moves = []
    if row > 0:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row - 1][col] = new_state[row - 1][col],
new_state[row][col]
        moves.append(new_state)
    if row < 2:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row + 1][col] = new_state[row + 1][col],
new_state[row][col]
        moves.append(new_state)
    if col > 0:
```



```

        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row][col - 1] = new_state[row][col - 1],
new_state[row][col]
        moves.append(new_state)
    if col < 2:
        new_state = [r[:] for r in state]
        new_state[row][col], new_state[row][col + 1] = new_state[row][col + 1],
new_state[row][col]
        moves.append(new_state)
    return moves

def a_star_search_manhattan(initial_state, goal_state, heuristic):
    open_list = [(heuristic(initial_state, goal_state), 0, initial_state, [])] # (f(n), g(n), state, path)
    closed_set = set()
    while open_list:
        f_n, g_n, current_state, path = heapq.heappop(open_list)
        if current_state == goal_state:
            return path + [current_state]
        state_tuple = tuple(map(tuple, current_state))
        if state_tuple in closed_set:
            continue
        closed_set.add(state_tuple)
        for neighbor in get_possible_moves(current_state):
            neighbor_tuple = tuple(map(tuple, neighbor))
            if neighbor_tuple in closed_set:
                continue
            new_g_n = g_n + 1
            new_h_n = heuristic(neighbor, goal_state)
            new_f_n = new_g_n + new_h_n
            heapq.heappush(open_list, (new_f_n, new_g_n, neighbor, path + [current_state]))

    return None

def display_solution_manhattan(path, heuristic, goal_state):
    if path:
        print(f'Solution path using Manhattan distance heuristic:')
        for step, state in enumerate(path):
            h = heuristic(state, goal_state)
            g = step
            f = g + h
            print(f'Step {step}: h(n)={h}, g(n)={g}, f(n)={f}')
        for row in state:

```

```
        print(row)
    print()
else:
    print(f'No solution found using Manhattan distance heuristic.')

initial_state = [
    [2, 8, 3],
    [1, 6, 4],
    [0, 7, 5]
]
solution_path_manhattan = a_star_search_manhattan(initial_state, goal_state,
manhattan_distance)
display_solution_manhattan(solution_path_manhattan, manhattan_distance, goal_state)
```

OUTPUT -

```
Solution path using Manhattan distance heuristic:
Step 0: h(n)=6, g(n)=0, f(n)=6
[2, 8, 3]
[1, 6, 4]
[0, 7, 5]

Step 1: h(n)=5, g(n)=1, f(n)=6
[2, 8, 3]
[1, 6, 4]
[7, 0, 5]

Step 2: h(n)=4, g(n)=2, f(n)=6
[2, 8, 3]
[1, 0, 4]
[7, 6, 5]

Step 3: h(n)=3, g(n)=3, f(n)=6
[2, 0, 3]
[1, 8, 4]
[7, 6, 5]
```

[1, 2, 3]

Step 4: $h(n)=2$, $g(n)=4$, $f(n)=6$

[0, 2, 3]

[1, 8, 4]

[7, 6, 5]

Step 5: $h(n)=1$, $g(n)=5$, $f(n)=6$

[1, 2, 3]

[0, 8, 4]

[7, 6, 5]

Step 6: $h(n)=0$, $g(n)=6$, $f(n)=6$

[1, 2, 3]

[8, 0, 4]

[7, 6, 5]

STATE SPACE TREE-

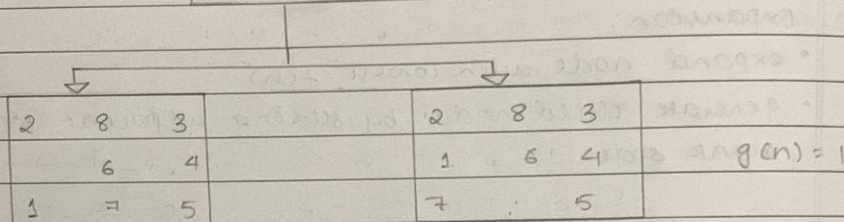
STATE SPACE TREES

1. Number of misplaced tiles.

$$f(n) = g(n) + h(n)$$

Initial state →	2 8 3	Goal state →	1 2 3
	1 6 4		8 4
	7 5		7 6 5

$g(n) = 0$

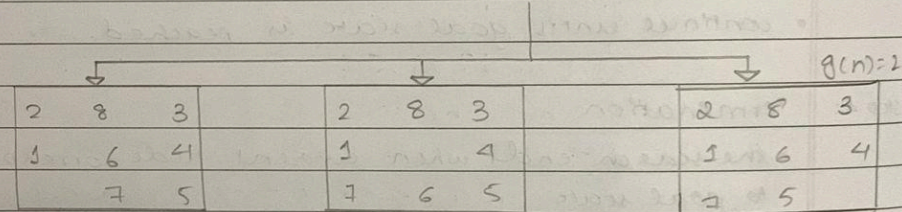


$h(n) = 5$

$$f(n) = 1 + 5 = 6$$

$h(n) = 4$

$$f(n) = 1 + 4 = 5$$



$h(n) = 5$

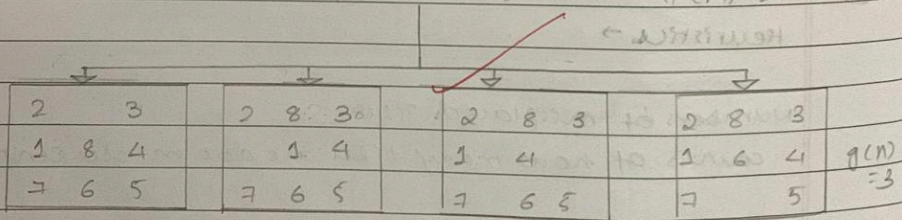
$$f(n) = 1 + 5 = 6$$

$h(n) = 3$

$$f(n) = 2 + 3 = 5$$

$h(n) = 5$

$$f(n) = 2 + 5 = 7$$



$h(n) = 3$

$$f(n) = 3 + 3 = 6$$

$h(n) = 3$

$$f(n) = 3 + 3 = 6$$

$h(n) = 4$

$$f(n) = 3 + 4 = 7$$

$h(n) = 4$

$$f(n) = 3 + 4 = 7$$

①

②

2 3	2 3	2 8 3	2 8 3
1 8 4	1 8 4	1 4	2 1 4
7 6 5	7 6 5	7 6 5	7 6 5

$$h(n) = 2$$

$$h(n) = 4$$

$$h(n) = 3$$

$$h(n) = 3$$

$$f(n) = 4 + 2 = 6$$

$$f(n) = 4 + 4 = 8$$

$$f(n) = 4 + 3 = 7$$

$$f(n) = 4 + 3 = 7$$

2 3	2 8 3	2 8 3
1 8 4	1 4	7 1 4
7 6 5	7 6 5	6 5

$$g(n) = 4$$

$$h(n) = 3$$

$$h(n) = 4$$

$$f(n) = 4 + 3 = 7$$

$$f(n) = 4 + 4 = 8$$

2 3	1 2 3
1 8 4	8 4
7 6 5	7 6 5

$$h(n) = 3$$

$$h(n) = 1$$

$$f(n) = 5 + 3 = 8$$

$$f(n) = 5 + 1 = 6$$

2 3	1 2 3	1 2 8
1 8 4	8 4	7 8 4
7 6 5	7 6 5	6 5

$$h(n) = 2$$

$$h(n) = 0$$

$$h(n) = 2$$

$$f(n) = 6 + 2 = 8$$

$$f(n) = 6 + 0 = 6$$

$$f(n) = 6 + 2 = 8$$

Goal state reached

2. Manhattan method.

$$f(n) = g(n) + h(n)$$

Initial state →	2 8 3	goal state →	1 2 3
	1 6 4		8 4
	7 5	$g(n) = 0$	7 6 5

↓	2 8 3	↓	2 8 3
	1 6 4		6 4
	7 5		1 7 5

$g(n) = 1$

$$h(n) = 1 + 1 + 2 = 5 \quad h(n) = 1 + 2 + 1 + 1 + 2$$

$$f(n) = 1 + 5 = 6 \quad f(n) = 1 + 7 = 8$$

↓	2 8 3	↓	2 8 3	↓	2 8 3
	1 6 4		1 4		1 6 4
	7 5		7 6 5		7 5

$g(n) = 2$

$$h(n) = 1 + 1 + 2 + 1 + 1 \quad h(n) = 1 + 1 + 2 \quad h(n) = 1 + 1 + 2 + 1 + 1$$

$$f(n) = 2 + 6 = 8 \quad f(n) = 2 + 4 = 6 \quad f(n) = 2 + 6 = 8$$

↓	2 3	↓	2 8 3	↓	2 8 3	↓	2 8 3
	1 8 4		1 4		1 4		1 6 4
	7 6 5		7 6 5		7 6 5		7 5

$g(n) = 3$

$$h(n) = 1 + 1 + 1 \quad h(n) = 1 + 2 + 2 \quad h(n) = 1 + 1 + 2 + 1 \quad h(n) = 1 + 1 + 2 + 1$$

$$f(n) = 3 + 3 = 6 \quad f(n) = 3 + 5 = 8 \quad f(n) = 3 + 5 = 8 \quad f(n) = 3 + 5 = 8$$

①

2 3	2 3	2 8 3	$g(n) = 4$
1 8 4	1 8 4	1 4	
7 6 5	7 6 5	7 6 5	

$$h(n) = 1 + 1$$

$$f(n) = 4 + 2 = 6$$

$$h(n) = 1 + 1 + 1 + 1$$

$$f(n) = 4 + 4 = 8$$

$$h(n) = 1 + 2 + 1$$

$$f(n) = 4 + 4 = 8$$

1 2 3	2 3	$g(n) = 5$
8 4	1 8 4	
7 6 5	7 6 5	

$$h(n) = 1$$

$$f(n) = 5 + 1 = 6$$

$$h(n) = 1 + 1 + 1$$

$$f(n) = 5 + 3 = 8$$

1 2 3	2 3	1 2 3	$g(n) = 6$
8 4	1 8 4	7 8 4	
7 6 5	7 6 5	6 5	

$$h(n) = 0$$

$$f(n) = 6$$

$$h(n) = 1 + 1$$

$$f(n) = 6 + 2 = 8$$

$$h(n) = 1 + 1$$

$$f(n) = 6 + 2 = 8$$

goal state
reached