

```
knitr::opts_chunk$set(message = FALSE, warning = FALSE)
```

```
library(rstan); rstan_options(javascript=FALSE)
library(bayesplot)
library(dplyr)
options(mc.cores = parallel::detectCores())
rstan_options(auto_write = T)

dat <- read.csv('final_data.csv')
```

```
dat <- dat %>%
  filter(skew != 'control')
dat <- dat %>%
  mutate(cho = ifelse(true_response == 'f', 1, -1))

dat$P_A1 <- dat$P_A1 / 100
dat$P_A2 <- dat$P_A2 / 100
dat$P_B1 <- dat$P_B1 / 100
dat$P_B2 <- dat$P_B2 / 100
```

```
ids <- unique(dat$Prolific_ID)
for(j in 1:length(ids)){
  dat$tid[dat$Prolific_ID==ids[j]] <- j
}
tids <- unique(dat$tid)

dat$rt <- as.numeric(dat$rt/1000)

dat <- dat %>%
  filter(test_part == 'cc' | test_part == 'ss')

dat <- dat %>%
  mutate(con = ifelse(test_part == 'cc', 1 , -1) )
```

```

dat <- dat %>%
  mutate(index1 = as.numeric(ifelse(O_A1>O_A2, 1, -1)) ,
         index2 = as.numeric(ifelse(O_B1>O_B2, 1, -1)),)

dat <- dat %>%
  # Swap values if oa_condition is not 0
  rowwise() %>%
  mutate(
    oa3 = if_else(index1 == 1, O_A1, O_A2),
    oa4 = if_else(index1 == 1, O_A2, O_A1),
    pa3 = if_else(index1 == 1, P_A1, P_A2),
    pa4 = if_else(index1 == 1, P_A2, P_A1),
    ob3 = if_else(index2 == 1, O_B1, O_B2),
    ob4 = if_else(index2 == 1, O_B2, O_B1),
    pb3 = if_else(index2 == 1, P_B1, P_B2),
    pb4 = if_else(index2 == 1, P_B2, P_B1),
  ) %>%
  ungroup()

```

```

oa = as.matrix(dat[, c("oa3", "oa4")])
ob = as.matrix(dat[, c("ob3", "ob4")])
pa = as.matrix(dat[, c("pa3", "pa4")])
pb = as.matrix(dat[, c("pb3", "pb4")])

```

```

dataList = list(cho = dat$cho, rt = dat$rt, participant = dat$tid, N=nrow(dat), L
= length(tids), starting_point=0.5,
  oa = as.matrix(dat[, c("oa3", "oa4")]),
  ob = as.matrix(dat[, c("ob3", "ob4")]),
  pa = as.matrix(dat[, c("pa3", "pa4")]),
  pb = as.matrix(dat[, c("pb3", "pb4")]),
  con = dat$con
)

parameters = c("transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt", "transf_mu
_theta", 'transf_mu_delta', 'transf_mu_gamma', 'sd_threshold', "sd_alpha", "sd_ndt",
'sd_theta', 'sd_gamma', 'sd_delta', "alpha_sbj", "threshold_sbj", "ndt_sbj", 'theta_sb
j', 'gamma_sbj', 'delta_sbj', "log_lik")

```

```
initFunc <-function (i) {  
  initList=list()  
  for (ll in 1:i){  
    initList[[ll]] = list(  
      mu_alpha = runif(1,-1.4587,2.5413),  
      sd_alpha = runif(1,0,1),  
      mu_threshold = runif(1,-0.5, 2.5),  
      sd_threshold = runif(1,0,1),  
      mu_ndt = runif(1, -1.5, 0),  
      sd_ndt = runif(1, 0, 1),  
      mu_theta = runif(1,0, 6),  
      sd_theta = runif(1,0,1),  
      mu_gamma = runif(1,-1, 1),  
      sd_gamma = runif(1, 0, 1),  
      mu_delta = runif(1,-1, 1),  
      sd_delta = runif(1, 0, 1),  
      z_alpha = runif(length(tids),-0.1,0.1),  
      z_theta = runif(length(tids),-0.1,0.1),  
      z_threshold = runif(length(tids),-0.1,0.1),  
      z_ndt = runif(length(tids),-0.1,0.1),  
      z_gamma = runif(length(tids),-0.1,0.1),  
      z_delta = runif(length(tids),-0.1,0.1)  
    )  
  }  
  
  return(initList)  
}
```

```
m <- stan_model("EU_prob.stan")
```

```

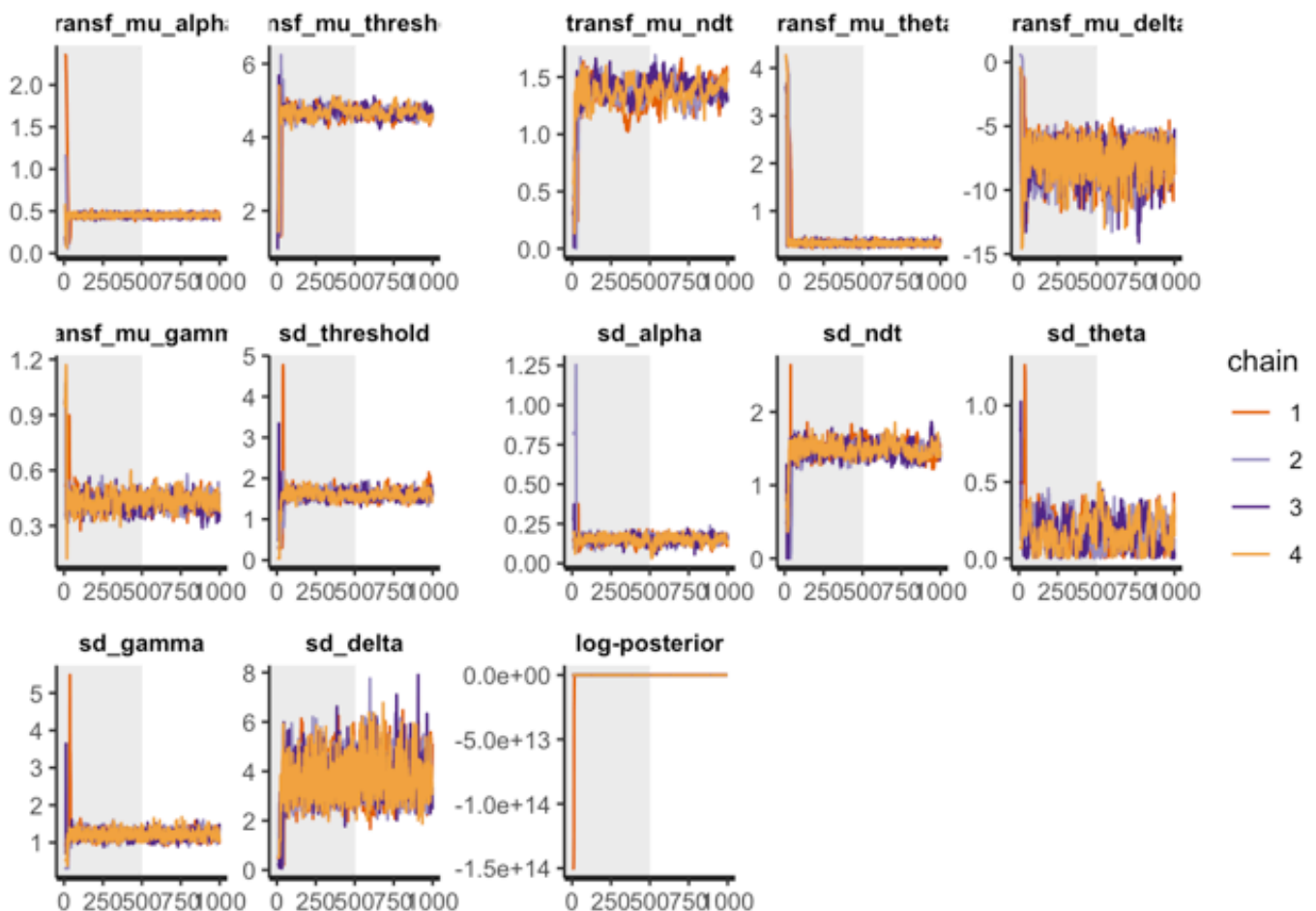
## Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
## clang -mmacosx-version-min=10.13 -I"/Library/Frameworks/R.framework/Resources/i
nclude" -DNDEBUG -I"/Library/Frameworks/R.framework/Versions/4.2/Resources/libra
ry/Rcpp/include/" -I"/Library/Frameworks/R.framework/Versions/4.2/Resources/libra
ry/RcppEigen/include/" -I"/Library/Frameworks/R.framework/Versions/4.2/Resources/
library/RcppEigen/include/unsupported" -I"/Library/Frameworks/R.framework/Version
s/4.2/Resources/library/BH/include" -I"/Library/Frameworks/R.framework/Versions/4.
2/Resources/library/StanHeaders/include/src/" -I"/Library/Frameworks/R.framework/
Versions/4.2/Resources/library/StanHeaders/include/" -I"/Library/Frameworks/R.fra
mework/Versions/4.2/Resources/library/RcppParallel/include/" -I"/Library/Framework
s/R.framework/Versions/4.2/Resources/library/rstan/include" -DEIGEN_NO_DEBUG -DB
OOST_DISABLE_ASSERTS -DBOOST_PENDING_INTEGER_LOG2_HPP -DSTAN_THREADS -DUSE_STAN
C3 -DSTRICT_R_HEADERS -DBOOST_PHOENIX_NO_VARIADIC_EXPRESSION -D_HAS_AUTO_PTR_ETC
=0 -include '/Library/Frameworks/R.framework/Versions/4.2/Resources/library/StanH
eaders/include/stan/math/prim/fun/Eigen.hpp' -D_REENTRANT -DRCPP_PARALLEL_USE_TBB
=1 -I/usr/local/include -fPIC -Wall -g -O2 -c foo.c -o foo.o
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.2/Resources/li
brary/StanHeaders/include/stan/math/prim/fun/Eigen.hpp:22:
## In file included from /Library/Frameworks/R.framework/Versions/4.2/Resources/li
brary/RcppEigen/include/Eigen/Dense:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.2/Resources/li
brary/RcppEigen/include/Eigen/Core:88:
## /Library/Frameworks/R.framework/Versions/4.2/Resources/library/RcppEigen/includ
e/Eigen/src/Core/util/Macros.h:628:1: error: unknown type name 'namespace'
## namespace Eigen {
## ^
## /Library/Frameworks/R.framework/Versions/4.2/Resources/library/RcppEigen/includ
e/Eigen/src/Core/util/Macros.h:628:16: error: expected ';' after top level declara
tor
## namespace Eigen {
## ^
## ;
## In file included from <built-in>:1:
## In file included from /Library/Frameworks/R.framework/Versions/4.2/Resources/li
brary/StanHeaders/include/stan/math/prim/fun/Eigen.hpp:22:
## In file included from /Library/Frameworks/R.framework/Versions/4.2/Resources/li
brary/RcppEigen/include/Eigen/Dense:1:
## /Library/Frameworks/R.framework/Versions/4.2/Resources/library/RcppEigen/includ
e/Eigen/Core:96:10: fatal error: 'complex' file not found
## #include <complex>
## ^~~~~~
## 3 errors generated.
## make: *** [foo.o] Error 1

```

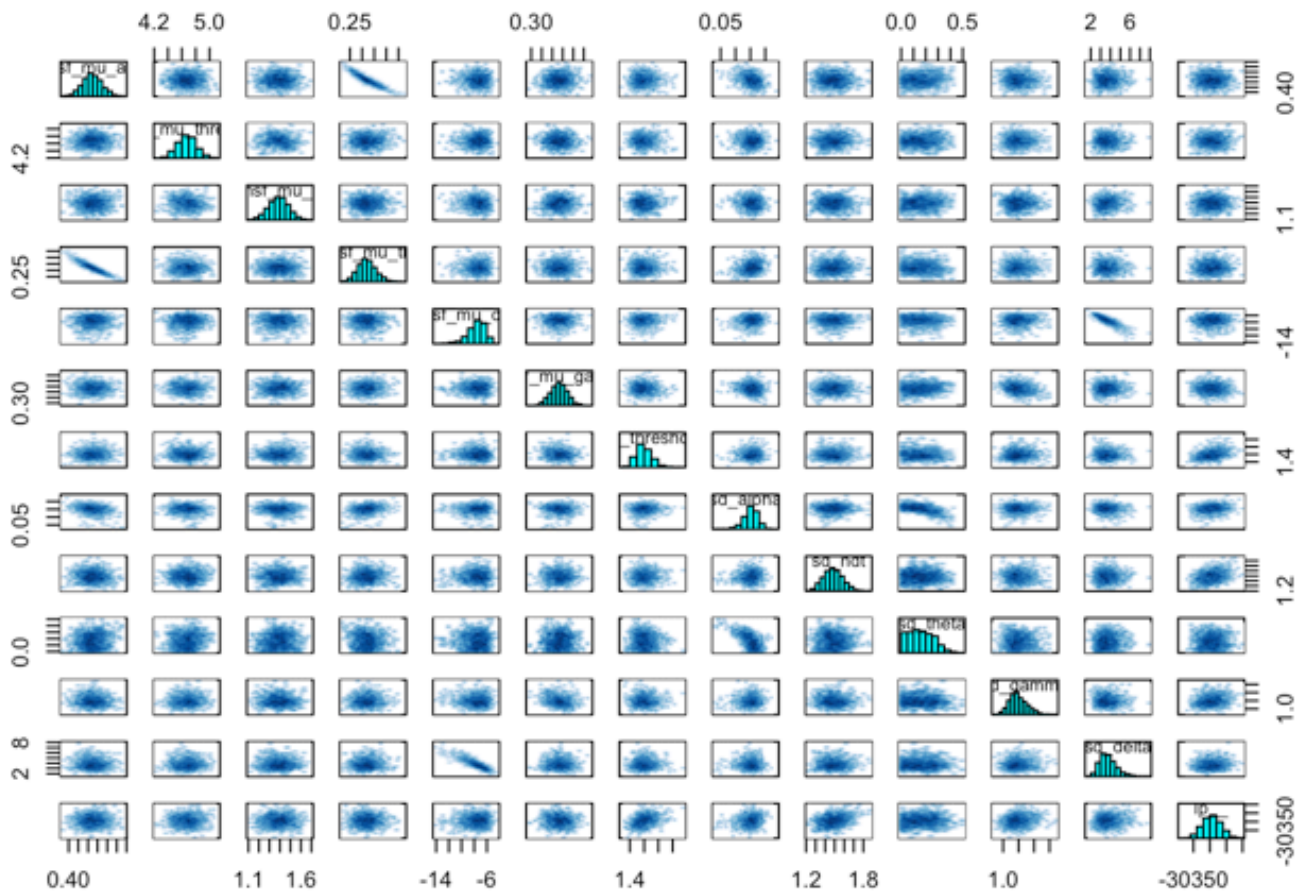
```
dsamples <- sampling(m,
  data=dataList,
  pars=parameters,
  iter=1000,
  chains=4, #If not specified, gives random inits
  init = initFunc(4),
  warmup = 500, # Stands for burn-in; Default = iter/2
  seed = 12

)
```

```
#"transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt", "transf_mu_theta", 'transf_mu_delta', 'transf_mu_gamma', 'sd_threshold', "sd_alpha", "sd_ndt", 'sd_theta', 'sd_gamma', 'sd_delta', "alpha_sbj", "threshold_sbj", "ndt_sbj", 'theta_sbj', 'gamma_sbj', 'delta_sbj',
rstan::traceplot(dsamples, pars=c("transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt", "transf_mu_theta", 'transf_mu_delta', 'transf_mu_gamma', 'sd_threshold', "sd_alpha", "sd_ndt", 'sd_theta', 'sd_gamma', 'sd_delta', "lp__"), inc_warmup = TRUE, nrow = 3)
```



```
pairs(dsamples, pars = c("transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt",
"transf_mu_theta", 'transf_mu_delta', 'transf_mu_gamma', 'sd_threshold', "sd_alph
a", "sd_ndt", 'sd_theta', 'sd_gamma', 'sd_delta', "lp__"))
```



```
print(dsamples, pars = c("transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt",
"transf_mu_theta", 'transf_mu_delta', 'transf_mu_gamma', 'sd_threshold', "sd_alph
a", "sd_ndt", 'sd_theta', 'sd_gamma', 'sd_delta', "lp__"))
```

```
## Inference for Stan model: anon_model.
## 4 chains, each with iter=1000; warmup=500; thin=1;
## post-warmup draws per chain=500, total post-warmup draws=2000.
##
##
```

	mean	se_mean	sd	2.5%	25%	50%
transf_mu_alpha	0.45	0.00	0.02	0.41	0.44	0.45
transf_mu_threshold	4.67	0.01	0.14	4.41	4.58	4.67
transf_mu_ndt	1.39	0.01	0.09	1.20	1.32	1.39
transf_mu_theta	0.32	0.00	0.04	0.25	0.29	0.32
transf_mu_delta	-7.65	0.05	1.39	-11.12	-8.39	-7.46
transf_mu_gamma	0.43	0.00	0.04	0.35	0.40	0.43
sd_threshold	1.60	0.01	0.11	1.41	1.52	1.59
sd_alpha	0.15	0.00	0.02	0.10	0.14	0.15
sd_ndt	1.48	0.01	0.10	1.30	1.41	1.48
sd_theta	0.16	0.01	0.10	0.01	0.08	0.16
sd_gamma	1.20	0.01	0.12	0.99	1.12	1.18
sd_delta	3.75	0.03	0.86	2.39	3.13	3.63
lp__	-30294.68	1.71	28.26	-30347.42	-30314.57	-30294.58

```
##
##      75%      97.5% n_eff Rhat
transf_mu_alpha      0.46      0.49   796 1.01
transf_mu_threshold  4.76      4.93   104 1.01
transf_mu_ndt        1.45      1.57    56 1.08
transf_mu_theta      0.34      0.40   894 1.01
transf_mu_delta     -6.65     -5.54   725 1.01
transf_mu_gamma      0.46      0.51   144 1.03
sd_threshold         1.67      1.84   144 1.02
sd_alpha             0.17      0.19   108 1.03
sd_ndt              1.55      1.69    78 1.03
sd_theta             0.24      0.36    89 1.03
sd_gamma            1.27      1.45   434 1.01
sd_delta            4.25      5.84   616 1.01
lp__                -30275.39 -30240.09  274 1.00
##
## Samples were drawn using NUTS(diag_e) at Mon Jan  8 13:09:01 2024.
## For each parameter, n_eff is a crude measure of effective sample size,
## and Rhat is the potential scale reduction factor on split chains (at
## convergence, Rhat=1).
```

```
library(ggplot2)
library(tidyverse) # for the gather function

samples_matrix <- as.matrix(dsamples)
means <- colMeans(samples_matrix)
hpd_interval <- t(apply(samples_matrix, 2, function(x) quantile(x, probs=c(0.025,
0.975))))

parameters <- c("transf_mu_alpha", "transf_mu_threshold", "transf_mu_ndt", "transf_m
```

```

u_theta", 'transf_mu_delta', 'transf_mu_gamma')

# Reshape data to a long format
df_long <- as.data.frame(samples_matrix) %>%
  gather(key = "parameter", value = "value", parameters)

# Convert hpd_interval to a data frame and name the columns
hpd_interval_sub <- hpd_interval[parameters, ]
hpd_df <- as.data.frame(hpd_interval_sub)
colnames(hpd_df) <- c("lower", "upper")
rownames(hpd_df) <- parameters
hpd_df$parameter <- rownames(hpd_df)

# Aesthetic enhancements
theme_set(theme_minimal(base_size = 14)) # Set the default theme

custom_palette <- c("density_fill" = "lightgray",
                    "mean_line" = "blue",
                    "hpd_line" = "darkgreen")

# Add text labels for mean, lower, and upper HPD values
df_long <- df_long %>%
  group_by(parameter) %>%
  mutate(mean = means[parameter])

hpd_df <- hpd_df %>%
  mutate(mid = (lower + upper) / 2)

p <- ggplot(df_long, aes(x = value)) +
  geom_density(aes(fill = "density_fill")) +
  scale_fill_manual(values = custom_palette, guide = FALSE) +
  geom_vline(aes(xintercept = mean, color = "mean_line"), linetype = "dashed", size = 1, alpha = 0.7) +
  geom_text(data = df_long, aes(x = mean, y = 0, label = round(mean, 2)), vjust = -0.5, hjust = 0.5, size = 4, color = custom_palette["mean_line"]) +
  geom_vline(data = hpd_df, aes(xintercept = lower, color = "hpd_line"), linetype = "solid", size = 1, alpha = 0.5) +
  geom_text(data = hpd_df, aes(x = lower, y = 0, label = round(lower, 2)), vjust = -0.5, hjust = -0.5, size = 4, color = custom_palette["hpd_line"]) +
  geom_vline(data = hpd_df, aes(xintercept = upper, color = "hpd_line"), linetype = "solid", size = 1, alpha = 0.5) +
  geom_text(data = hpd_df, aes(x = upper, y = 0, label = round(upper, 2)), vjust = -0.5, hjust = 1.5, size = 4, color = custom_palette["hpd_line"]) +
  facet_wrap(~ parameter, scales = "free", ncol = 2) +
  scale_color_manual(values = custom_palette, guide = 'none') +
  labs(title = "Posterior distributions")

print(p)

```


Posterior distributions

