CS520 Theory of Programming Languages

Introduction

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How to analyze programming languages (their constructs, type systems, implementations, etc) formally?

We will study mathematical tools for doing such analysis.

Preview 1:
Abstract syntax

- What is a program? What kind of syntactic object is it?

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- Bad answer: a sequence of characters.

Preview 1: Abstract syntax

- What is a program? What kind of syntactic object is it?
- Bad answer: a sequence of characters.
- Our answer: an instance of an abstract syntax.
- Mathematically, an element of an initial algebra.

Preview 2: Domain theory

```
>>> def F(g): return g
...
```

- Which mathematical object does the program F denote?

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...
```

- Which mathematical object does the program F denote?
- Identity function in [D→D] for some D.

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>>> def F(g): return g
...
>>> F(F)
<function F at 0x10c573410>
```

- Which mathematical object does the program F denote?
- Identity function in [D→D] for some D.
- But D should include [D→D]. Impossible if D is a set.

Preview 2: Domain theory

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>>> def F(g): return g
...
>>> F(F)
<function F at 0x10c573410>
```

- Which mathematical object does the program F denote?
- Identity function in [D→D] for some D.
- But D should include [D→D]. Impossible if D is a set.
- Possible if D is a domain & [D→D] has only continuous fns.

Preview 3: Evaluation order

```
>>> def f(x): return (x+x)
...
>>> f(f(3))
12
```

- Should we compute f(3) before applying f to f(3)?

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- Should we compute f(3) before applying f to f(3)?
- Yes. Eager evaluation. Python, OCaml, Scheme, etc.
- No. Normal-order evaluation or lazy evaluation. Haskell.

Preview 3: Evaluation order

```
>>> def f(x): return 3
...
>>> f(f(3))
12
```

- Should we compute f(3) before applying f to f(3)?
- Yes. Eager evaluation. Python, OCaml, Scheme, etc.
- No. Normal-order evaluation or lazy evaluation. Haskell.

Preview 3: Evaluation order

```
>>> def f(x): return 3
...
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12
```

- Should we compute f(3) before applying f to f(3)?
- Yes. Eager evaluation. Python, OCaml, Scheme, etc.
- No. Normal-order evaluation or lazy evaluation. Haskell.
- To be analysed via operational and denotational semantics.

Preview 4:
Type system

```
import typing
from typing import Callable

def twice(f : Callable[[int],int], x : int) -> int:
  return(f(f(x)))
```

- Types help develop correct programs.

Preview 4:
Type system

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import typing
from typing import Callable

def twice(f : Callable[[int],int], x : int) -> int:
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```

- Types help develop correct programs.
- Can we infer types automatically?
- What mathematical objects do types denote?

Preview 4:
Type system

```
import typing
from typing import Callable

def twice(f : Callable[[int],int], x : int) -> int:
  return(f(f(x)))
```

- Types help develop correct programs.
- Can we infer types automatically? Type inference algo.
- What mathematical objects do types denote? Partial equivalence relation.

- Predicate Logic (Ch1).
- The Simple Imperative Language (Ch2).
- Program Specification and Their Proofs (Ch3).
- Failure, Input-Output, and Continuation (Ch5).
- Transition Semantics (Ch6).
- An Introduction to Category Theory (Tennent Ch8).
- Recursively-Defined Domains (Tennent Ch10).
- The Lambda Calculus (Ch10).
- An Eager Functional Language (Ch11).
- Continuation in a Functional Language (Ch12).
- A Normal-Order Language (Ch14).
- The Simple Type System (Ch15).

Imperative Languages

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Functional Languages

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Math tools

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Functional Languages

Course webpage

https://github.com/hongseok-yang/graduatePL20

- Primary source of information about the course.

Blackboard lectures

- Nearly all the lectures will use blackboard, not slides.

- My handwritten notes will be available in the course webpage.

Evaluation

- Final exam — 40%.
- Homework (4 problem sheets) — 30%.
- Two critical surveys — 30%.

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- Homework (4 problem sheets) — 30%.
- Two critical surveys — 30%.

Final exam

- 12 hour take-home exam.
- From 10am on 12 Dec (Sat) until 10pm on 12 Dec (Sat).
- The exam paper will be distributed at KLMS.
- Solutions should be submitted at KLMS.

Evaluation

- Final exam — 40%.
- Homework (4 problem sheets) — 30%.
- Two critical surveys — 30%.

Critical surveys

- Study an assigned topic for yourself.
- Write a review (up to 3 pages) excluding bibliography.
- Try to go beyond simple survey. Your own thoughts. Connection with other PL concepts. In-depth study.
- Writing (20%). Understanding (40%). Originality (40%).

Critical survey 1

- Deadline: 30 Oct (Friday). By 23:59.
- Topic: Concurrent separation logic.
- Look at the course webpage for guideline.

Critical survey 2

- Deadline: 7 Dec (Monday). By 23:59.
- Topic: Relational parametricity.
- Look at the course webpage for guideline.

Honour code

- We adopt a strict policy for handling plagiarism and academically dishonest behaviours.
- A student will get F if
  - she or he is found to copy texts from papers and books without rephrasing them properly; or
  - he or she is found to cheat in an exam or copy answers or code from friends' or other sources.

Teaching staffs

- Prof Hongseok Yang (Lecturer). hongseok00@gmail.com. Office hour: 6pm-7pm at ZOOM.
- Mr Hyoungjin Lim (TA1). lmkmkr@kaist.ac.kr
- Mr Dongwoo Oh (TA2). dongwoo@kaist.ac.kr
- TAs’ office hours will be announced shortly.