Question 1:

Union:

 $X \rightarrow Y$ (Initial)

 $X \rightarrow \{X, X\}$ (Reflexivity)

 $\{X, X\} \rightarrow \{X, Y\}$ (Augmentation using $X \rightarrow Y$ with the inclusion of X)

 $\{X, Y\} \rightarrow \{Z, Y\}$ (Augmentation using $X \rightarrow Z$ with the inclusion of Y)

 $X \rightarrow \{Y, Z\}$ (Transitivity based on what we have just shown)

Decomposition:

$$X \rightarrow \{Y, Z\}$$
 (Initial)

$$\{Y, Z\} \rightarrow Y (Reflexivity)$$

 $\{Y, Z\} \rightarrow Z$ (Reflexivity)

$$X \rightarrow Y$$
 (Transitivity)

 $X \rightarrow Z$ (Transitivity)

Pseudo-Transitivity:

 $X \rightarrow Y$ (Initial)

 $\{X, Z\} \rightarrow \{Y, Z\}$ (Augmentation of $X \rightarrow Y$ and Z)

 $\{Y, Z\} \rightarrow A \text{ (Given FD)}$

Question 2: Possible FDs are coloured in green

Α	В	С	D	E
1	Χ	1	М	1
2	Υ	1	М	1
3	Υ	4	N	3
4	W	2	L	5
5	W	2	М	1
6	Т	5	0	2

a) $A \rightarrow B$

b) $B \rightarrow A$

c) $A \rightarrow C$

d) $B \rightarrow C$

e) $C \rightarrow D$

f) $C \rightarrow E$

g) $D \rightarrow E$

h) $\{A, B\} \rightarrow C$

i) $\{B, C\} \rightarrow E$

 $j) \quad \{B, C, D\} \rightarrow E$

Question 3:

Α	В	С	D	E
1	2	1	6	2
1	2	1	4	3
2	4	2	7	4
3	2	1	4	3

Question 4:

- a) Candidate key(s): {A, B}, {A, D}
- b) Candidate key(s): {B, C}, {C, D}, A, E
- c) Candidate key(s): C, {A, B}, D
- d) Candidate key(s): {A, B}
- e) Candidate key(s): {A, B, D}, H, J

Question 5:

- a) Insert anything into B, C, D and E without also inserting a value into A
- b) Deleting the tuple with B = 4 as we lose information for the functional dependency (B \rightarrow {D, E}), specifically (4 \rightarrow {3, 2})
- c) Updating $\{2, 2, 1, 5, 6\}$ to $\{2, 3, 1, 5, 6\}$ creates the inconsistency of $\{B \rightarrow \{D, E\}\}$, creates the inconsistency $\{3 \rightarrow \{5, 6\}\}$ and $\{3 \rightarrow \{5, 4\}\}$