

$$a_0 a_1 a_2 a_3 \dots a_i \leq \dots a_j \leq a_{n-1}$$

If a_i, a_j are swapped

$$a_{i-1} \underline{a_i} a_{i+1} \dots a_{j-1} \underline{a_j}$$

$$\rightarrow a_{i-1} \leq \underline{a_j} a_{i+1} \dots a_{j-1} \leq \underline{a_i} a_{j+1}$$

contradicts

sorted
property

① $a_j = a_{i+1}, a_{j-1} = a_i \Rightarrow$ no need to do anything

② $a_j > a_{i+1}, a_{j-1} = a_i \Rightarrow a_i = a_{i+1} = a_{i+2} \dots a_{j-1}$


$a_i \neq a_{j+1} \Rightarrow$ otherwise contradiction

③ $a_j = a_{i+1}, a_{j-1} > a_i \Rightarrow a_{i+1} = a_{i+2} \dots a_{j-1} = a_j$

$a_{i-1} \neq a_j \Rightarrow$ otherwise contradiction

④ $a_j > a_{i+1}, a_{j-1} > a_i \Rightarrow$ normal case

② Ex. 1 2 2 2 2 2 3



③ Ex. 1 2 3 3 3 3 3



→ 1 2 3 2 2 2 2

→ 1 3 3 3 3 2 3



cannot be 3