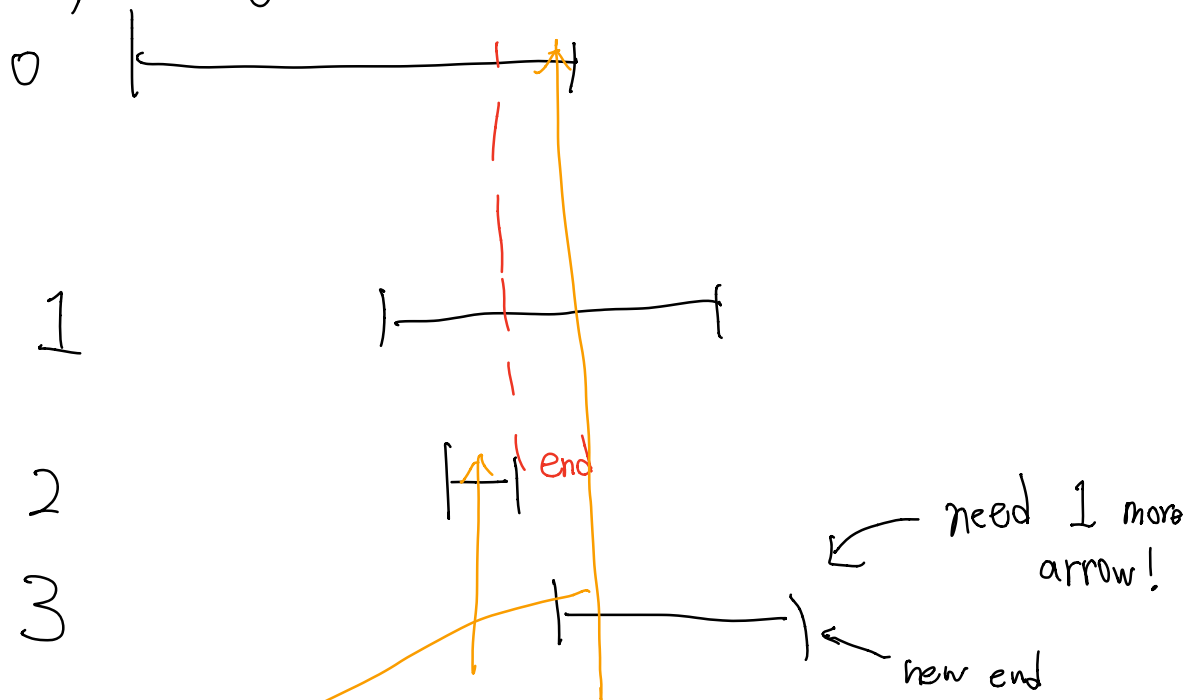


My thinking process:



And because 'start' will only become greater, our arrow used before 'end' can never be reused !!

⇒ Update to `points[3].end`

Q: Why don't we shoot here?

A: I think if we want to shoot 0, 1, 3, this arrow's right end will be $\leq \text{points}[3].\text{end}$. And that will benefit us nothing!

That's why we let the new arrow shoot in range $[\text{points}[3].\text{start}, \text{points}[3].\text{end}]$

Proof by induction: (Adapt a leetcode discuss post)

Assume my algorithm works on $[0, t)$ balloons

Let balloons = $[(s_0, e_0), \dots, (s_t, e_t), \dots, (s_{n-1}, e_{n-1})]$

And let end_{t-1} be the result computed after the balloon $t-1$ (s_{t-1}, e_{t-1}).

By induction hypothesis, the arrow r_{t-1} can be shot within: $[s_{t-1}, end_{t-1}]$

Case 1: $s_t \in [s_{t-1}, end_{t-1}]$

$\Rightarrow r_{t-1}^{th}$ arrow can be reused $\Rightarrow r_t = r_{t-1}$

$$end_t = \min(end_t, e_t)$$

Case 2: $s_t > end_{t-1}$

$\Rightarrow r_{t-1}^{th}$ arrow cannot be reused

and $0 \sim r_{t-1}^{th} - 1$ arrows cannot help too! (They are all $\leq end_{t-1}$)