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DEPT: BSCS

DLD: ASSIGNMENT: 02

1) PROBLEM 1:-

a) Develop a truth table for each of the following standard SOP expressions.

$$\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}C + ABC$$

Soln-

	A	B	C	X	
	0	0	0	1	$\bar{A}\bar{B}\bar{C}$
→	0	0	1	0	
	0	1	0	1	$\bar{A}B\bar{C}$
	0	1	1	1	$\bar{A}BC$
→	1	0	0	0	
	1	0	1	1	$A\bar{B}C$
→	1	1	0	0	$AB\bar{C}$
	1	1	1	1	ABC

b) Convert the SOP expression in part a) to an equivalent POS expression.
So Soln.

We can write POS expression from above truth table where $X=0$.
So,

$$(A + B + \bar{C})(\bar{A} + B + C)(\bar{A} + \bar{B} + C).$$

This is standard POS expression from SOP expression.

2) PROBLEM 2:

From truth table, derived a standard SOP and a standard POS expression.

	A	B	C	D	X
1)	0	0	0	0	1 ✓
2)	0	0	0	1	1 ✓
3)	0	0	1	0	0
4)	0	0	1	1	1 ✓
5)	0	1	0	0	0
6)	0	1	0	1	1 ✓
7)	0	1	1	0	1 ✓
8)	0	1	1	1	0
9)	1	0	0	0	0
10)	1	0	0	1	1 ✓
11)	1	0	1	0	0
12)	1	0	1	1	0
13)	1	1	0	0	1 ✓
14)	1	1	0	1	0
15)	1	1	1	0	0
16)	1	1	1	1	0

Sol.

i) SOP expression from above truth table

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD + \bar{A}BC\bar{D} + \bar{A}BCD + ABC\bar{D} + ABCD$$

ii) POS expression from above truth table,

$$\begin{aligned} & (A+B+\bar{C}+D)(A+\bar{B}+C+D)(\bar{A}+\bar{B}+\bar{C}+\bar{D}) \\ & (\bar{A}+B+C+D)(\bar{A}+B+\bar{C}+D)(\bar{A}+B+\bar{C}+\bar{D}) \\ & (\bar{A}+\bar{B}+C+\bar{D})(\bar{A}+\bar{B}+\bar{C}+D)(\bar{A}+\bar{B}+\bar{C}+\bar{D}). \end{aligned}$$

3) PROBLEM 3:-

a) Use a Karnaugh map to reduce the given expression to a minimum SOP form.

$$\bar{A}B(\bar{C}\bar{D} + \bar{C}D) + AB(\bar{C}\bar{D} + \bar{C}D) + A\bar{B}\bar{C}D$$

Sol:

$$\Rightarrow \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D} + A\bar{B}\bar{C}\bar{D} + A\bar{B}C\bar{D} + A\bar{B}\bar{C}D$$

0100 1100 1100 ~~0110~~ 1001

1101

AB \ CD

	00	01	11	10
00				
01	1	1		
11	1		1	
10			1	

$$B\bar{C} + A\bar{C}D$$

b) Convert each of the following POS expressions to minimum SOP expressions using a Karnaugh map.

$$(\bar{A} + B)(\bar{A} + \bar{B} + \bar{C})(B + \bar{C} + D)(A + \bar{B} + C + \bar{D})$$

Sol.

$$\begin{array}{cccc}
 (\bar{A} + B) & (\bar{A} + \bar{B} + \bar{C}) & (B + \bar{C} + D) & (A + \bar{B} + C + \bar{D}) \\
 1. & 0 & 0 & 0 \\
 1 & 0 & 0 & 1 \\
 1 & 0 & 1 & 0 \\
 1 & 0 & 1 & 1
 \end{array}$$

AB \ CD	00	01	11	10
00	1	1	1	0
01	1	0	1	1
11	1	1	0	0
10	0	0	0	0

$$\bar{A}\bar{C}D + \bar{A}\bar{B}D + A\bar{B}\bar{C} + \bar{A}BC$$