

Final Project; Categorical Data Analysis

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1 Estimates of Killing in Casanare

Casanare is a large, rural state in Colombia that includes 19 municipalities and a population of almost 300,000 inhabitants. Located in the foothills of the Andes, Casanare has a history of violence. Casanare (alongside other states, including Arauca) became pivotal to the Colombian government in the 1980s and 1990s when oil reserves were discovered there. Because of this natural resource, the government targeted opposition to what was perceived as the Colombian interest and modernization and the Union Patriótica (UP) in Casanare (as well as Arauca), who supported people's access to land and workers' rights, became the victim. Multiple armed groups operated in Casanare, including the Colombian military, paramilitaries, and guerrillas, going after "members" (both actual members and merely perceived supporters) of the UP. As a result, many Casanare citizens suffered violent deaths and disappearances. It can be argued that what was seen in Casanare (among other places) in Colombia was "political" genocide (Gomez-Suarez, 2007). But, one of the contentions against framing this episode in Colombian history as a genocide is the low death and disappearances toll.

So how many people have been killed or disappeared? We review the Human Rights Data Analysis Group (HRDAG)'s reporting on this issue of population estimation (Guzman et al., 2007). In this study, the authors used information about victims of killings and disappearances provided by 13 datasets. We have 15 datasets of deaths and disappearances in Casanare from 1998-2007. Any accounting of lethal violence will be incorrect if we assume that any one dataset or combination of datasets contains a comprehensive count of violent acts and disappearances. Registries of violent acts kept by governmental and non-governmental institutions contain some, but not all, of the records of lethal violence. Organizations collecting this data may only have access to certain subsets of a population or geographic areas.

The datasets come from state agencies – including government, security, forensic and judicial bodies – and from civil society organizations. Across these 15 datasets, there are individuals that have been "captured" only by one dataset, and some that have been captured by multiple. How can we disambiguate the patterns of violence?

2 Multiple Systems Estimation (MSE), Capture Re-Capture

The goal is to estimate the overall population of victims by first estimating the victims who are not captured by any of the datasets. MSE estimates the total number of disappearances by comparing the size of the overlap(s) between lists to the sizes of the lists themselves. If the overlap is small, this implies that the population from which the lists were drawn is much larger than the lists. If, on the other hand, most of the cases on the lists overlap, this implies that the overall population is not much larger than the number of cases listed.

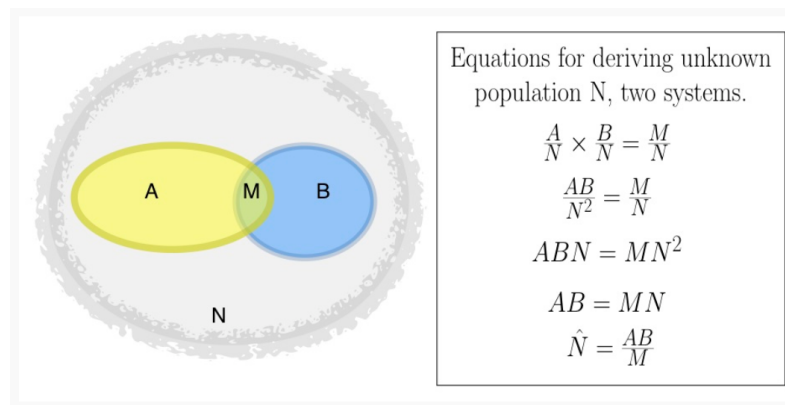


Figure 1: Multiple System Estimation¹

2.1 MSE Assumptions

There are several MSE assumptions that are needed for when there are two “systems” (lists), but not more than that. The assumptions are:

1. *Closed system*: The population of interest does not change during the measurement period. This means that the object of measurement, whether that is a population of persons in a country or a population of violent events that occurred in a state, is a closed system: the target population does not change during the period of measurement. This assumption is generally un-problematical for data on violent events, because events that occurred cannot “un-occur” later.
2. *Perfect matching (record linkage!)*: The overlap between systems (i.e., the group of cases recorded in more than one list) is perfectly identified.
3. *Equal probability of capture*: For every data system, each individual has an equal probability of being captured. For example, every death has probability X of being recorded in list 1, every death has probability Y of being recorded in list 2, and so on. This assumption, the homogeneity of capture probability, is unlikely to hold for any type of violence data. For example, persons with fewer social connections may be both more likely to go missing and less likely to be reported missing; rural locations are more difficult to access than urban ones. Constructing two-sample estimates without accounting for different probabilities of capture leads to conclusions that may be biased.
4. *Independence of lists*: Capture in one list does not affect probability of capture in another list. For example, being reported to one NGO does not change the probability that an individual is reported to another. The third assumption, independence of systems, is similarly difficult to meet.

Like differences in capture probability, dependencies between systems are impossible to account for in the two-system setting. A common example here is the difference between governmental and non-governmental organizations. Because different populations may have different levels of trust in the two organizations, reporting to one type of organization may imply that the witness is very unlikely to report to the other.

¹Green, Amelia Hoover (2013) Multiple Systems Estimation: Stratification and Estimation. Available HTTP: <https://hrdag.org/2013/03/20/mse-stratification-estimation/> (accessed 4 December 2019)

3 Overview of Data

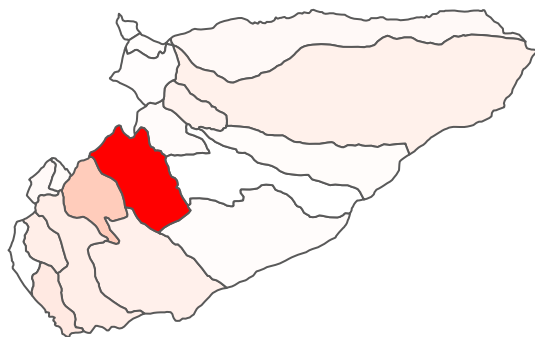
Table 1: Contingency Table

| | Organization | Total Captures | Unique | Type |
|----------|--|----------------|--------|----------|
| d_CCJ.n | Colombian Commission of Jurists | 214 | 48 | judicial |
| d_EQU.n | Equitas | 22 | 0 | civil |
| d_FON.n | Fondelibertad | 304 | 67 | security |
| d_IMLD.n | National Institute of Forensic Medicine Disappearances | 153 | 9 | forensic |
| d_PN0.n | Policía Nacional | 825 | 221 | security |
| d_CIN.n | CINEP | 267 | 91 | civil |
| d_FAM.n | Families of Victims' Organizations | 51 | 1 | civil |
| d_FSR.n | Prosecutor General of Santa Rosa | 151 | 0 | security |
| d_IMLM.n | Instituto Nacional de Medicina Legal | 1878 | 1219 | forensic |
| d_VP.n | Vice Presidency Office | 501 | 284 | judicial |
| d_CCE.n | Colombia-Europe | 72 | 30 | civil |
| d_CTL.n | Technical Investigative Body of the Prosecutor Generals Office | 36 | 0 | judicial |
| d_FDC.n | Prosecutor General list of the Disappeared | 623 | 376 | forensic |
| d_GAU.n | Gaula | 110 | 1 | security |
| d_PL.n | Pais Libre | 9 | 0 | civil |

3.1 Overall Trends

The following graph shows that violence has been concentrated in Yopal. We can see that the *reported* violence (i.e. the counts in the 15 datasets) appears to have intensified across all municipalities in Casanare in 2003-2004 and then dropped.

Total Counts in 15 Datasets by Municipality 1998–2007



Yearly Counts in 15 Datasets by Municipality 1998–2007

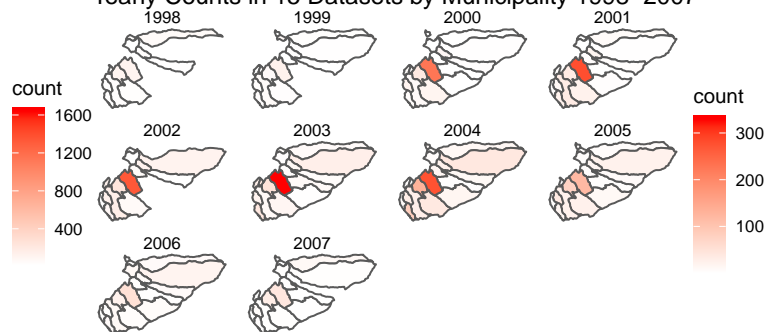


Figure 2: Overall Trends in 15 Datasets by Municipality

Looking just at the totals of the 15 datasets, that data suggest the violence peaked in 2003-2004 and the total number of victims is 3501. However, just looking at the trends among the totals of the 15 datasets does not give the whole picture.

3.2 Heterogeneity Issues

One of the requirements for MSE is for each individual has equal probability of capture for a given list. However, we can see from the figure below this does not seem to be the case. In 2004, the violence was centered around Villanueva, but all three of these lists have very little counts in that location. Since these individual list charts have different gradient trends than the total, that suggest that there is heterogeneity in capture probability. This will make our results more uncertain.

Disappearances/Kidnappings Across Municipalities by Different Organizations, in 2004

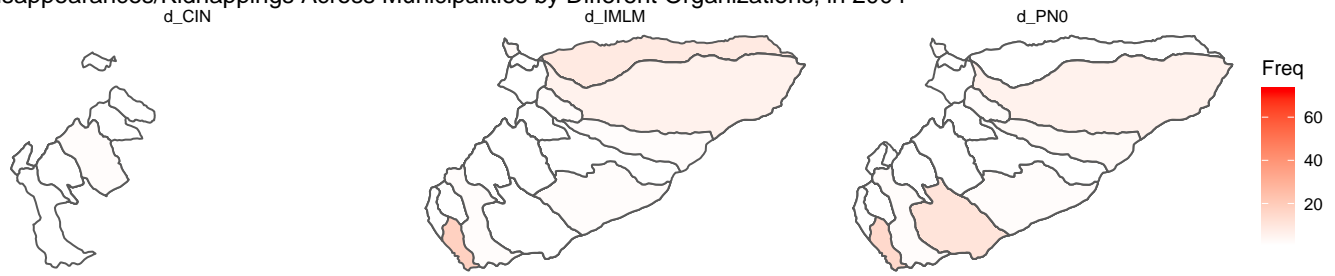


Figure 3: Counts from Three Different Datasets in 2004

3.3 Different Datasets - Different Stories

We motivate our need for a more sophisticated analysis by showing the reporting patterns of 3 different organizations across 1998-2007. If we relied on just one organization or even a combination of two we could tell different stories regarding the violence. Relying on FAM shows a peak in violent incidents in 2003, while reports by IMLM show a peak in 2004. Using multiple systems estimation allows us to parse both the reported and unreported violent in Casanare.

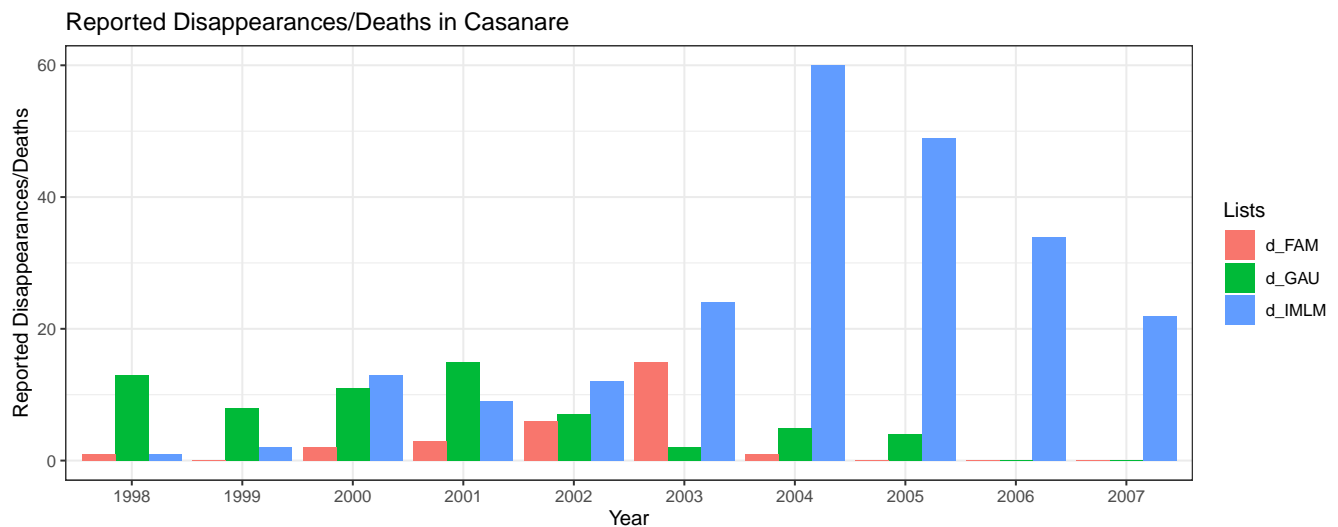


Figure 4: Count Trends for Three Organizations

4 Loglinear Modelling

In order to do our estimation, we will use loglinear modeling. We will describe the model as if we had two datasets (for simplicity). We know the victims “captured” by only dataset 1, only dataset 2, and both datasets. However, we don’t know the amount of victims that are not captured by either list. Estimate this value allows us to estimate the total count of victims.

| | | Captured in Dataset #2 | |
|------------------------|-----|--------------------------|----------------------------|
| | | Yes | No |
| Captured in Dataset #1 | Yes | n_{11} <i>Known</i> | n_{10} <i>Known</i> |
| | No | n_{01} <i>Known</i> | n_{00} <i>Unknown</i> |

Estimate n_{22} in order to estimate n

$n_{11} + n_{12} + n_{21} + n_{22} = N = \text{total of victims}$

The count of victims captured into a dataset or combination of datasets is n_{11}, n_{10}, n_{01} , and n_{00} . Each of these cells is a count of victims captured. The subscripts denote which datasets a victim has been captured. The subscripts denotes if the victim has been captured (1), or not been captured by a certain data set. For n_{ij} , i is for dataset #1 and j is dataset #2.

Our estimates are primarily based on Poisson regression.

4.1 Estimating the Total Count of Victims

We are interested in estimating n_{00} , which also allows us to estimate the total number of victims.

The (log of the) expected cell count n_{00} is a function of the other observed cell counts, as shown in the equation below.

$$\log(n_{00}) = \alpha + \beta_1 \cdot \mathbb{1}(x \in n_{10}) + \beta_2 \cdot \mathbb{1}(x \in n_{01})$$

This is the saturated form of the log-linear models introduced in Bishop, Fienberg and Holland (1975). To quote from Agresti, “the saturated GLM has a separate parameter for each observation. It gives a perfect fit. This sounds good, but it is not a helpful model. It does not smooth the data or have the advantages that a simpler model has, such as parsimony. Nonetheless, it serves as a baseline for other models, such as for checking model fit.”

When estimation of the total “population” of missing people in Casanare is the goal (as it typically is with multiple-systems estimation), the key value here is the intercept α . To estimate $\log(n_{00})$, all the other values in the model are zero, as the indicator functions for n_{ij} for zero. Therefore the only term that contributes to the estimate of $\log(n_{00})$ is α . The value of n_{00} is therefore the exponentiated value of α , that is, $\exp(\alpha)$. The total number of cases, N , is the sum of the observed cases plus $\exp(\alpha)$.

$$\log(n_{00}) = \alpha + \underbrace{\beta_1 \cdot \mathbb{1}(x \in n_{10}) + \beta_2 \cdot \mathbb{1}(x \in n_{01})}_{\text{each} = 0}$$

$$\log(n_{00}) = \alpha$$

$$\hat{n}_{00} = \exp\{\hat{\alpha}\}$$

$$\hat{N} = n_{11} + n_{10} + n_{01} + \hat{n}_{00}$$

As with any regression and data mining model, we want to avoid over-fitting. There is a trade off we need to balance between “goodness of fit”, and simple (parsimonious) models.

We need to find the best model in order to get an accurate estimate of α . Thus, we should determine whether the full (saturated) model above, which assumes that all three two-way interactions between datasets are important, is actually necessary. There is one simpler models that assume the two-way interaction.

$$\log(n_{00}) = \alpha + \beta_1 \cdot \mathbb{1}(x \in n_{10}) + \beta_2 \cdot \mathbb{1}(x \in n_{01}) + \beta_{12} \cdot \mathbb{1}(x \in n_{11})$$

In this case, we can clearly write out the possible model. During model selection, we estimate these models and choose the model that minimizes the Bayesian Information Criterion (BIC), a test that weighs goodness of fit against degrees of freedom.

4.2 Challenges with Loglinear models

1. **Interpretation:** The inclusion of so many variables in loglinear models often makes interpretation very difficult.
2. **Independence Assumption:** The frequency in each cell is independent of frequencies in all other cells, which is not necessarily the case here. We attempt to model this.
3. **Sample Size Requirement:** With loglinear models, you need to have at least 5 times the number of cases as cells in your data. If you do not have the required amount of cases, then you need to increase the sample size or eliminate one or more of the variables.

4.3 Choosing our “Systems”

Our dataset encompasses 15 datasets, far too many to model with a loglinear model. We collapse these 15 datasets into 4 systems (i.e. groups) based on the type of organization that produced the dataset.

Table 2: Example of Information from Systems

| security_ind | forensic_ind | judicial_ind | civil_ind | Freq |
|--------------|--------------|--------------|-----------|------|
| 0 | 0 | 0 | 1 | 5 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 0 | 1 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 1 | 1 |

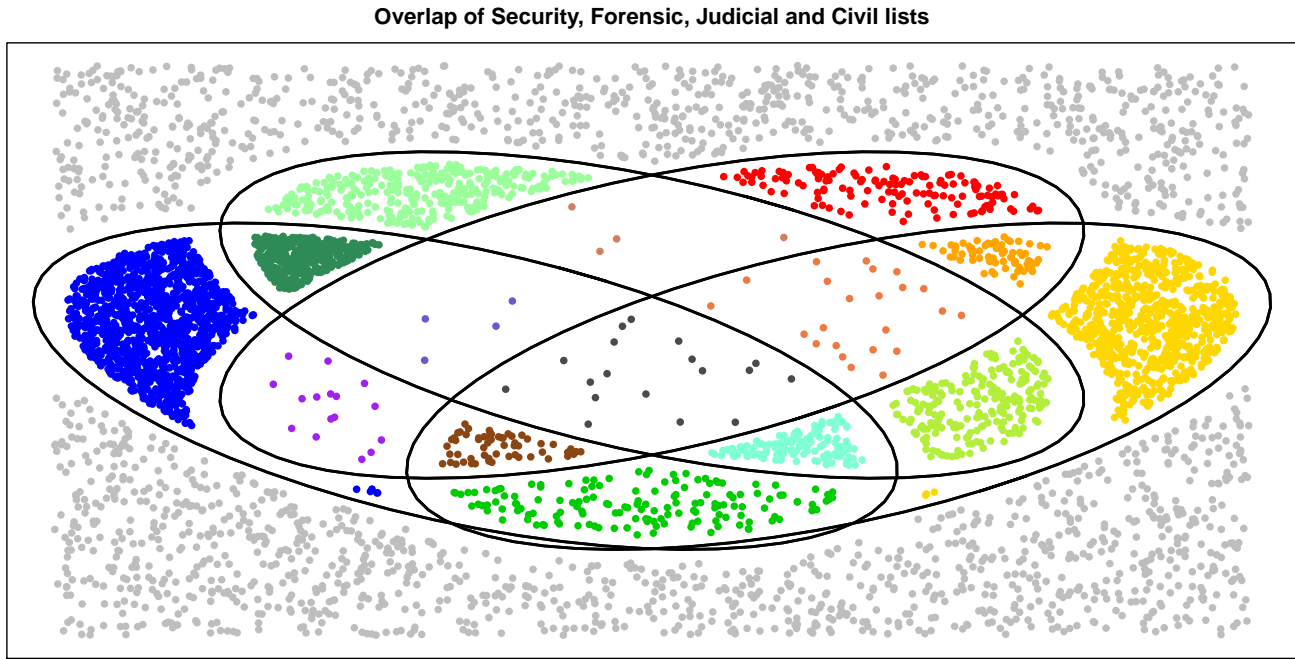


Figure 5: Estimated Venn Diagram of Systems

In the above Venn Diagram, the colored dots represent a specific victim. We are trying to estimate the victims that are not captured in one of the lists (shown by the graph dots). We can see there is not a lot of overlap, which suggests there may be lack of heterogeneity capture probability (i.e. the probability of a victim captured differs from list to list). In addition, this implies that there is likely a much larger population of victims than counted in the 15 datasets.

4.4 Model Definitions

4.4.1 Types of Models

Models will be denoted by M , and the subscripts will denote the type of model.

- M_0 : The M_0 model is the simplest possible multiple source capture recapture model. It assumes that there is no heterogeneity and that all lists (civil, security, judicial, etc) have the same probability of capturing individuals. We know that this is not the case here.
- M_t : This model relaxes the M_0 model to allow for lists to have different capture rates.
- M_h : This model relaxes the M_0 model to allow for individual capture heterogeneity.
- M_{th} : This model allows for both list heterogeneity and capture events having different rates.

4.4.2 Types of Heterogeneity

When heterogeneity in capture probability is present (i.e. the probability of a list capturing a victims differs), there are different forms that this heterogeneity can take.

- Normal: The log odds of capture follows a Normal distribution.
- Darroch: The log odds of capture among those who were not captured follows a Normal distribution.
- Poisson: The log odds of capture among those who were not captured follows a Poisson distribution.
- Gamma: The log odds of capture among those who were not captured follows a Gamma distribution.

4.5 Non-Hierarchical Models

After collapsing the 15 lists into four systems, we fit several loglinear models. We see that the best fits clearly take into account both system and individual heterogeneity. We therefore choose the M_{th} model with the log odds of capture among those who were not captured follows a Gamma distribution. We see that the M_0 model demonstrates a clear lack of fit, which we would expect for this data. The models listed below are *not* hierarchical in nature.

We will need the hierarchical structure to perform model selection. It's important to note that a model is not chosen if it bears no resemblance to the observed data. The choice of a preferred model is typically based on a formal comparison of goodness-of-fit statistics associated with models that are related hierarchically (models containing higher order terms also implicitly include all lower order terms). Ultimately, the preferred model should distinguish between the pattern of the variables in the data and sampling variability, thus providing an intuitive interpretation.

The “number of captured units” is the number of observed elements, in this example, the number of people documented as missing/killed, we usually call this N_c (N for overall total, and c denoting captured). The “abundance” column shows the estimate of \hat{N} , the total population including the observed and the estimated unobserved deaths. The AIC and BIC columns show the “information coefficients” which balance the goodness of fit (shown in the “deviance” column) with the information used to estimate the model (degrees of freedom indicate this). Model selection often occurs based on the smallest AIC and BIC values, however this can only be done with hierarchical models which is not the case here.

Table 3: Summary of Models (Non-hierarchical models)

| | abundance | stderr | deviance | df | AIC | BIC |
|---------------|-----------|---------|----------|----|----------|----------|
| M0 | 5604.929 | 100.607 | 2279.471 | 13 | 2376.736 | 2389.057 |
| Mt | 5232.814 | 87.309 | 529.823 | 10 | 633.087 | 663.891 |
| Mh Chao (LB) | 5970.687 | 139.893 | 2253.979 | 12 | 2353.244 | 2371.726 |
| Mh Poisson2 | 6147.489 | 188.431 | 2262.122 | 12 | 2361.387 | 2379.869 |
| Mh Darroch | 6866.486 | 367.890 | 2257.937 | 12 | 2357.202 | 2375.684 |
| Mh Gamma3.5 | 7725.102 | 634.443 | 2256.636 | 12 | 2355.901 | 2374.383 |
| Mth Chao (LB) | 5665.285 | 125.069 | 473.765 | 8 | 581.029 | 624.155 |
| Mth Poisson2 | 6035.010 | 181.678 | 482.267 | 9 | 587.532 | 624.497 |
| Mth Darroch | 7204.688 | 411.304 | 476.057 | 9 | 581.322 | 618.287 |
| Mth Gamma3.5 | 8782.672 | 810.694 | 474.715 | 9 | 579.980 | 616.945 |
| Mb | 4228.193 | 64.664 | 2107.184 | 12 | 2206.448 | 2224.931 |
| Mbh | 3643.007 | 47.707 | 1618.987 | 11 | 1720.252 | 1744.895 |

Each model controls for a subset of all the possible interactions among the models. In the context of MSE, the two- and three-way interactions estimate (and to some extent, control for) associations in the probabilities of capture between (and among) the lists. For example, is a certain person more likely to be seen on one list, and also more likely to be seen on a second list? If associations like this are present (and they usually are), they can bias the estimate.

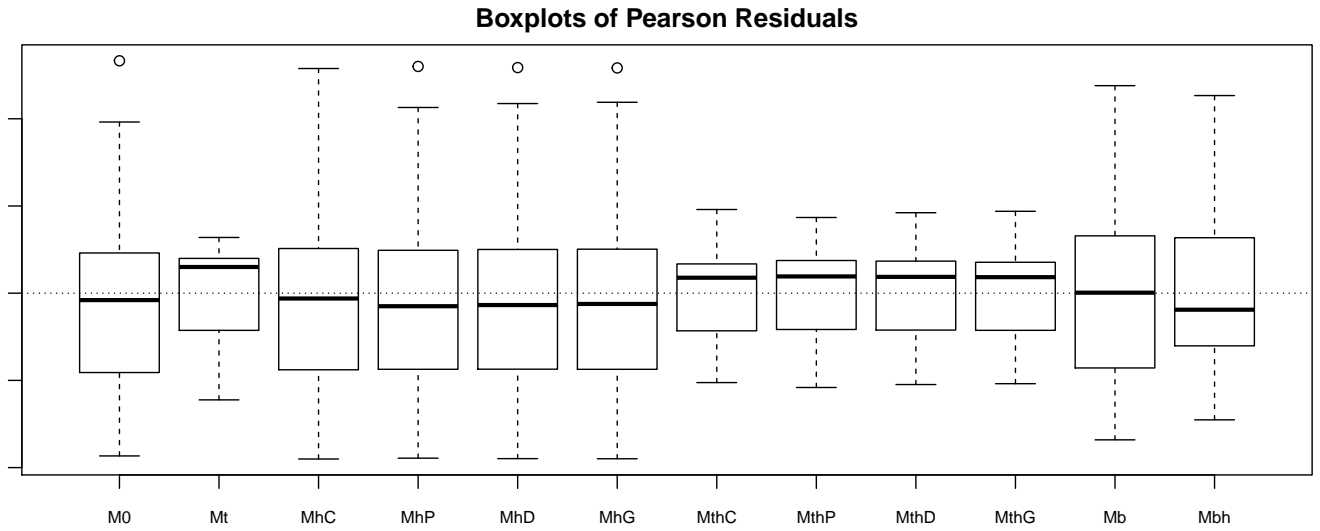


Figure 6: Boxplot of Residuals for Models

These boxplots of residuals offer a general assessment of model fit. These boxplots of residuals offer a general assessment of model fit.

Since the individual cell counts:

$$n_i \sim \text{Pois}(m_i)$$

$$E[n_i] = \text{Var}(n_i) = m_i$$

it follows that the Pearson residuals:

$$r_i = \frac{n_i - \hat{m}_i}{\sqrt{\hat{m}_i}}$$

are approximately mean 0, variance 1. This is why they are sensible residuals to use.

The light dotted line represents zero, and ideally you want the residuals centered around zero. We see that there is significantly less variation in the M_{th} Models. These models account for list heterogeneity (probability of capture for a specific victim varies from list to list) and individual heterogeneity (probability of capture for a specific list varies from victim to victim). Models that account for heterogeneity offer less variation but also do not have residuals centered at zero.

4.6 Specific Model Results

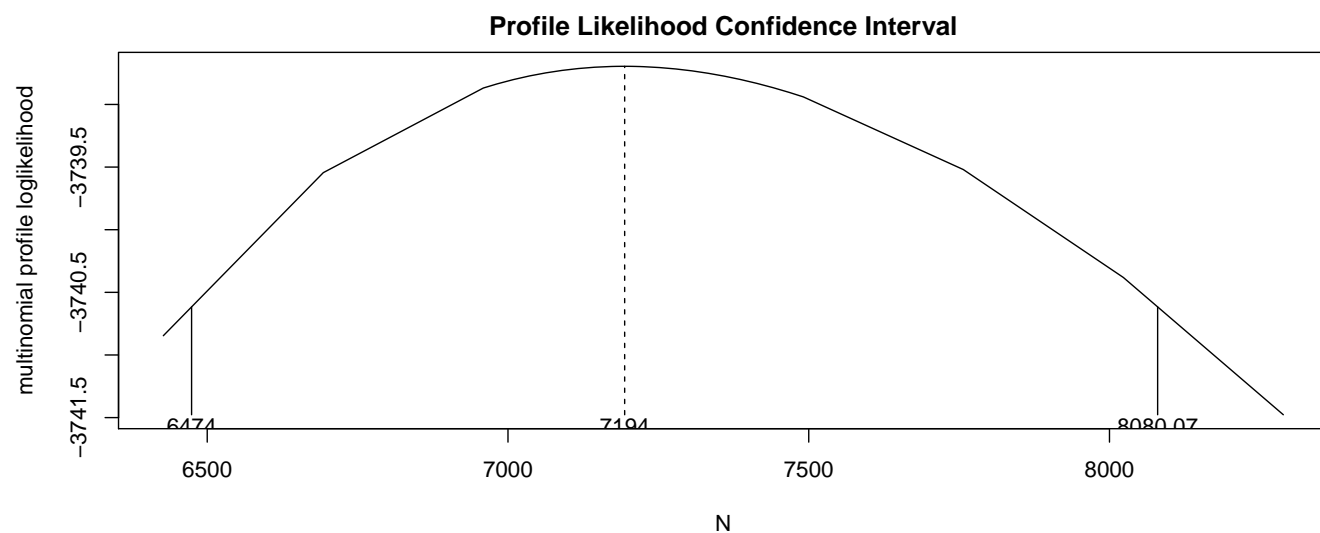


Figure 7: Profile Likelihood of Specific Model

Table 4: Confidence Interval of Specific Model

| | abundance | InfCL | SupCL |
|-------------|-----------|-------|---------|
| Mth Darroch | 7194 | 6474 | 8080.07 |

4.7 Capture Recapture

We display some basic capture-recapture frequency statistics to explore capture patterns. It displays, for $i = 1, \dots, t$, the number of people captured i times (f_i), the number of people captured for the first time on occasion i (u_i), the number of units captured for the last time on occasion i (v_i) and the number of units captured on occasion i (n_i). Here “occasion” should be interpreted as one of the four “systems”– where security is the 1st system, forensic is the 2nd, judicial is the 3rd, and civil is the 4th “occasion”.

If the n_i statistics vary among capture occasions, there is a temporal effect– which we clearly see here. We would expect the top panel of the plot to be linear, while the bottom panel should be concave down or exhibit no pattern for capture patterns that are best fit with M_{th} models.

Table 5: Capture Recapture Statistics

| | i = 1 | i = 2 | i = 3 | i = 4 |
|---|-------|-------|-------|-------|
| fi: number of units captured i times | 2392 | 866 | 225 | 18 |
| ui: number of units captured for the first time on occasion i | 1128 | 1455 | 785 | 133 |
| vi: number of units captured for the last time on occasion i | 317 | 1640 | 1216 | 328 |
| ni: number of units captured on occasion i | 1128 | 2028 | 1387 | 328 |

$$\log\left(\frac{f_i}{\binom{t}{i}}\right) = \log\left(\frac{N \times P(i \text{ captures})}{\binom{t}{i}}\right) = \log(N(1-p)^{t-i}p^i) = \log(N(1-p)^t) + i \log\left(\frac{p}{1-p}\right)$$

Exploratory Heterogeneity Graph

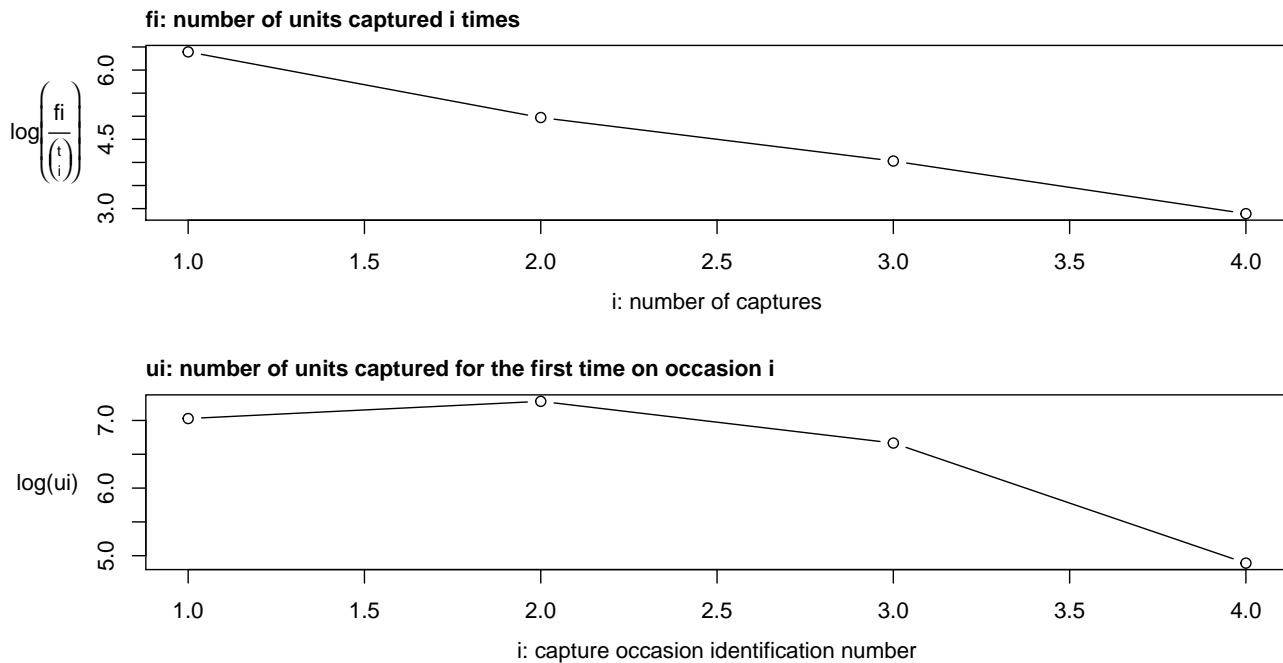


Figure 8: Capture-Recapture Frequency Statistics

4.8 Hierarchical Models

4.8.1 More Interactions: Better Fit

We start by fitting three simple models. The first, and simplest, is the model that assumes independence between the four systems. The second model looks at all possible two-way interactions. The third model looks at all three-way interaction between each of the systems. Recall that 1=Security, 2=Forensic, 3=Judicial, and 4=Civil.

$$\text{Model 1: } \log(\hat{N}) = \alpha + \lambda_1 + \lambda_2 + \lambda_3 + \lambda_4$$

$$\text{Model 2: } \log(\hat{N}) = \alpha + \lambda_1 + \lambda_2 + \lambda_{13} + \lambda_{14} + \lambda_{23} + \lambda_{24} + \lambda_{34}$$

$$\text{Model 3: } \log(\hat{N}) = \alpha + \lambda_1 + \lambda_2 + \lambda_{13} + \lambda_{14} + \lambda_{23} + \lambda_{24} + \lambda_{34} + \lambda_{123} + \lambda_{124} + \lambda_{134} + \lambda_{234}$$

We perform log-likelihood ratio test and see that the higher the order of the interaction, the better the fit (with saturated model signifying a perfect fit). The model deviance (LR statistic for testing against the saturated model) for each is defined as:

$$G^2 = 2 \sum_i n_i \log(n_i / \hat{m}_i) = \sum_i d_i$$

We perform log-likelihood ratio test and see that the higher the order of the interaction, the greater the deviance explained. Each LRT for the nested models demonstrates that- the p-value for the reduction in deviance is significant. Note that these obey the **hierarchy principle**: If the k -way interaction is in the model then every lower order interaction and main effect is also in the model.

Table 6: ANOVA for 3 standard models

| | Deviance | df | Delta(Dev) | Delta(df) | P(> Delta(Dev)) |
|-----------|------------|----|------------|-----------|-----------------|
| Model 1 | 529.822654 | 10 | 0.000000 | 0 | 0 |
| Model 2 | 72.792862 | 4 | 457.029793 | 6 | 0 |
| Model 3 | 9.761127 | 0 | 63.031735 | 4 | 0 |
| Saturated | 0.000000 | 0 | 9.761127 | 0 | 0 |

4.8.2 Iterative Proportional Fitting

We will use iterative proportional fitting to estimate N . The iterative proportional fitting process generates maximum likelihood estimates of the expected cell frequencies for a hierarchical model. In short, preliminary estimates of the expected cell frequencies are successfully adjusted to fit each of the marginal sub-tables specified in the model. The un-adjusted data cells may be referred to as the 'seed' cells, and the selected totals may be referred to as the 'marginal' totals.

Here the marginal subtables would be:

1. Security by Judicial by Forensic systems
2. Security by Forensic by Civil systems
3. Judicial by Forensic by Civil systems
4. Judicial by Civil by Security systems

To do this four-dimensional IPF:

1. Proportionally adjust each (three-dimensional) row of cells to equal the pre-determined totals of Marginal 1.
2. Proportionally adjust each column of cells to equal the pre-determined totals of Marginal 2.
3. Proportionally adjust each slice of cells to equal the pre-determined totals of Marginal 3.
4. Proportionally adjust each stack of cells to equal the pre-determined totals of Marginal 4. This is the end of the first 'Iteration'.
5. Repeat the above steps until the desired level of convergence is reached.

Under mild restrictions, we know that the cell-values at the end of this process that satisfy the fitted marginal totals are the MLEs.

4.8.3 Results

Using iterative proportional fitting, we fit all possible second-order interaction models (we restrict to second-order to aid interpretation). These will account for different dependency structures.

We choose the best model according to the BIC criteria, is below: estimates a total for missing/disappeared people as 8817, which is similar to the 8782 than that of the non-hierch., interactionless, model (M_{th}).

Table 7: ‘Top’ Five, ‘Middle’ Five, and ‘Bottom’ Five Models (Hierarchical models)

| | abundance | stderr | bias | deviance | df | AIC |
|-------------------|-----------|-----------|-------------|-----------|----|----------|
| 12,13,14,23,24,34 | 8817.112 | 1515.7607 | 237.8220039 | 72.33182 | 3 | 189.5966 |
| 12,13,14,23,24 | 5076.249 | 168.5601 | 9.6710160 | 93.42304 | 4 | 208.6879 |
| 12,13,14,23,34 | 7308.085 | 455.7503 | 36.3107669 | 73.99807 | 4 | 189.2629 |
| 12,13,14,24,34 | 8695.570 | 493.7868 | 32.6905220 | 72.33923 | 4 | 187.6040 |
| 12,13,23,24,34 | 9267.442 | 876.2745 | 91.6873828 | 72.44539 | 4 | 187.7102 |
| 12,24,34 | 6990.394 | 275.9882 | 8.1501334 | 251.01919 | 6 | 362.2840 |
| 13,14,23 | 5388.545 | 160.4725 | 6.9759022 | 180.47969 | 6 | 291.7445 |
| 13,14,24 | 6408.681 | 225.7425 | 8.3355958 | 397.52853 | 6 | 508.7934 |
| 13,23,24 | 5052.802 | 130.3749 | 3.2161351 | 209.76658 | 6 | 321.0314 |
| 13,23,34 | 5178.863 | 140.5477 | 3.1073571 | 223.51518 | 6 | 334.7800 |
| 14,2,3 | 6349.780 | 217.6530 | 6.4628534 | 444.04882 | 8 | 551.3136 |
| 23,1,4 | 5076.432 | 127.2073 | 1.1770391 | 278.46874 | 8 | 385.7336 |
| 24,1,3 | 6089.940 | 188.3562 | 2.6692553 | 450.63028 | 8 | 557.8951 |
| 34,1,2 | 5903.270 | 172.5871 | 1.4531676 | 404.10047 | 8 | 511.3653 |
| 1,2,3,4 | 6035.010 | 181.6780 | 0.7620688 | 482.26705 | 9 | 587.5319 |

We can see that the independence model listed as “1,2,3,4” has the worst fit— this is to be expected, as we have demonstrated in previous sections the list dependencies

The shorthand “14,2,3” means that lists 1 and 4 are independent of 2, and also independent of list 3, i.e. $(1, 4) \perp\!\!\!\perp 2$ and $(1, 4) \perp\!\!\!\perp 3$. It is represented by:

$$\log(\hat{N}) = \alpha + \lambda_1 + \lambda_2 + \lambda_3 + \lambda_4 + \lambda_{14}$$

The shorthand identifies both the model and the margins that must be fitted to obtain MLEs using IPF. Not all shorthands have a conditional independence interpretation. The top models, all with 5-6 two-way interactions cannot be interpreted in this way.

These the hierarchical models have different estimates, ranging from 5053 to 9268.

We also plot the BIC values for different models and their accompanying estimates of \hat{N} . When we only look at estimates with a corresponding BIC value less 300, the estimates range from 5077 and 9268 (almost the exact same range of estimates when considering all the models).

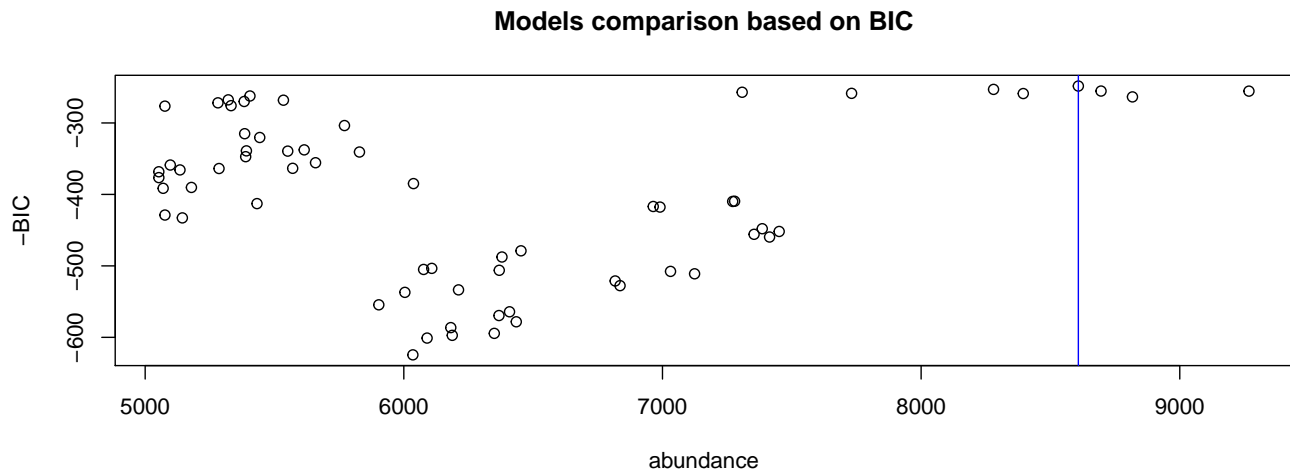


Figure 9: Hierarchical Models BIC Plot

This is the fundamental problem of the frequentist approach. We could just pick the “best” model, i.e., the one with the lowest BIC (note the y-axis is inverted).

Unfortunately, just picking one model ignores the error that we introduce by the selection itself. It also forces us to decide which dependencies among the systems we will control for, forcing us to decide which dependencies will not be included in the model. In the future, we would look into model averaging procedures and Bayesian approaches.

5 Conclusions

Our findings show that the total number of deaths and disappearances in Casanare is far greater than previously assessed. The initial analysis made by Guzman et al. for the Human Rights Data Analysis Group (HRDAG), which used thirteen datasets from 1986-2007, estimated a total of 2,533 deaths and disappearances in Casanare (95% CI: 2239-2867) from 1986-2007, although only about 1,500 were reported as such (Guzman et al., 2007). We only used datasets for a subset of those years, namely 1998-2007 (fifteen datasets in total). Looking at just the raw total from the fifteen datasets, there were 3,501 incidents of deaths or disappearances in Casanare from 1998-2007. Had our analysis also included data that went back to 1986, the raw total would be even higher.

Importantly, given estimation techniques used in our analysis, there is strong evidence that the true total of victims is actually much higher than 3,501. We used multiple systems estimation (MSE) and loglinear modeling to show that the best hierarchical models of the data produce estimates ranging from 5,077 to 9,268. While our estimation of the total number of deaths and disappearances indicates a far greater number of victims, there are some concerns estimating the true total of victims. First, the models themselves indicate a large range of possible numbers. Second, the data may not meet all the MSE and loglinear assumptions (especially the independence assumption), which makes point estimation less valid.

As can be seen, there is a lot of uncertainty about the true total of deaths and disappearances. Nevertheless, the number of deaths and disappearances within any given country is one important human rights measure that serves six inter-related functions: (1) contextual description and documentation, (2) classification, (3) monitoring, (4) mapping and pattern recognition, (5) analysis and policy recommendation, and (6) advocacy and political dialogue (Landman and Carvalho, 2009). While MSE and loglinear modeling can only go so far in terms of the first four functions, these statistical tools for better estimating the total of deaths and disappearances is nevertheless key for, on the one hand, analysis and policy recommendation, and on the other, advocacy and political dialogue. International NGOs like Amnesty International and Human Rights Watch respond based on the severity of human rights violations in a country, opting to use higher estimates of deaths and disappearances for their analysis of the situation in Colombia

and thus their recommendations and advocacy, while the Colombian think tank, CERAC, have lower estimates (Ballesteros et al., 2007). Unfortunately, different estimates can be used as fact by different groups to proffer differing messages about the extent of human rights violations in Colombia. Nevertheless, utilizing statistical tools to show that the true total of victims is markedly higher than previously reported is particularly important for uncovering the extant nature and degree of violence in Colombia.

6 References

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