

# The Search for Harmonic Drums



**PRESENTED BY:**

**TOM EICHLERSMITH (HAMLINE UNIVERSITY)**

**OTHER CONTRIBUTORS:**

**MOHAMED MOHAMED (HAMLINE UNIVERSITY)**

**ASHWIN SRIDHAR (HAMLINE UNIVERSITY)**

**ALEX CAMPBELL (CENTURY COLLEGE)**

# Vocabulary



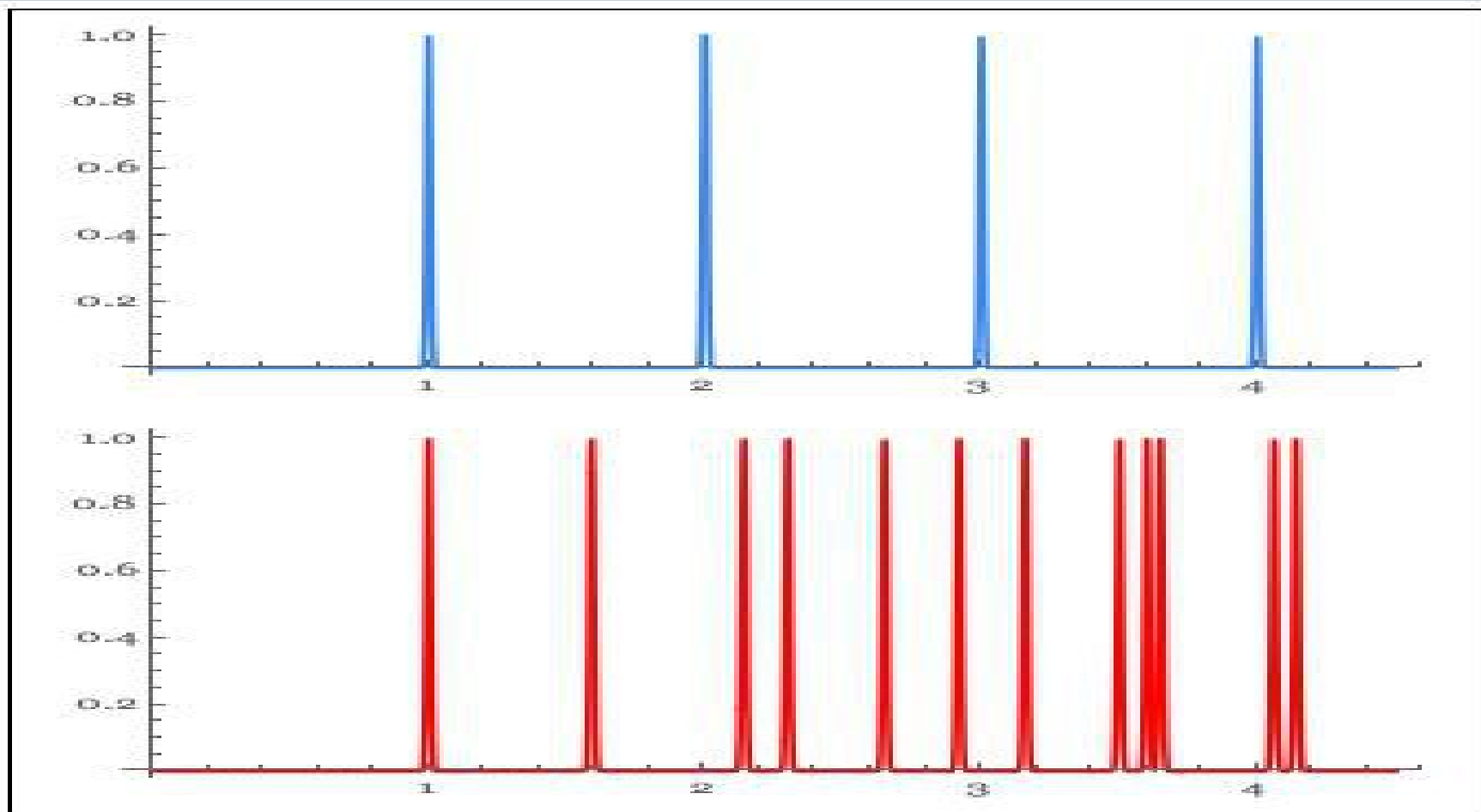
- 🧠 Frequency Spectra
- 🧠 Harmonics
- 🧠 Fundamental Frequency
- 🧠 Frequency Number
- 🧠 Eigenmodes, eigenfrequencies
- 🧠 Intensity

# Mathematics



$$\frac{\partial^2 u}{\partial t^2} = c^2 \nabla^2 u$$

# Circular Drums



# Circular Drums



1.



2.53884



2.53884



4.56119



4.56131



5.2702



# Methods



## Physical

Constructing  
drums

Measuring  
frequency  
spectra

Analyzing  
spectra and  
comparing to  
calculations

## Computational

Define 'good'  
frequency  
spectra

Representing  
border

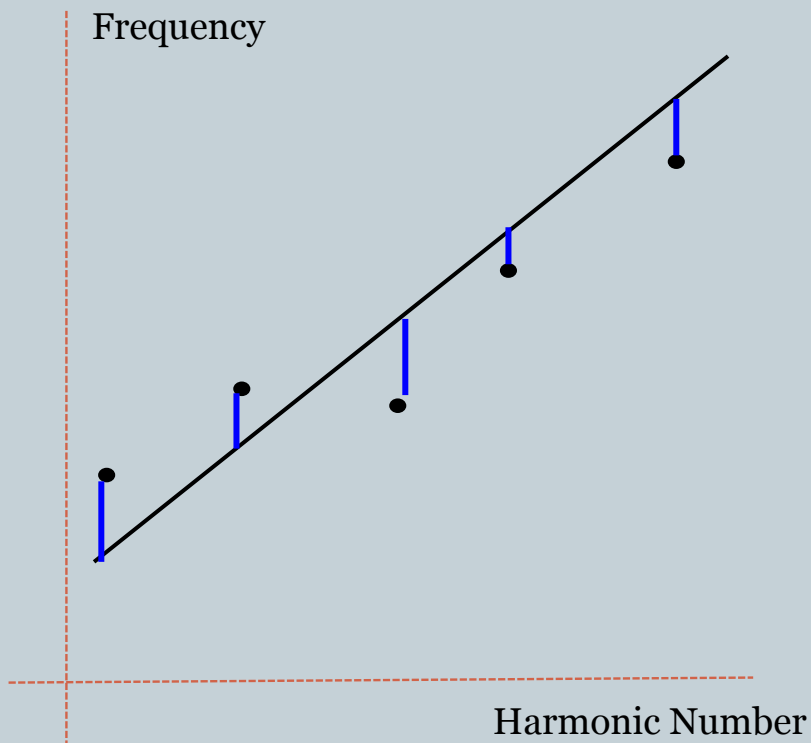
Calculating  
frequency  
spectra

Optimization of  
border shape

# Definition of 'Good'



## 🧠 Linear Fit



## 🧠 Neural Network



# Border Representation





# Frequency Calculation



```
NDEigensystem[  
  {-Laplacian[f[x, y], {x, y}],  
   DirichletCondition[f[x, y] == 0, True]},  
  {f}, {x, y} ∈ region, Num]
```

# Optimization



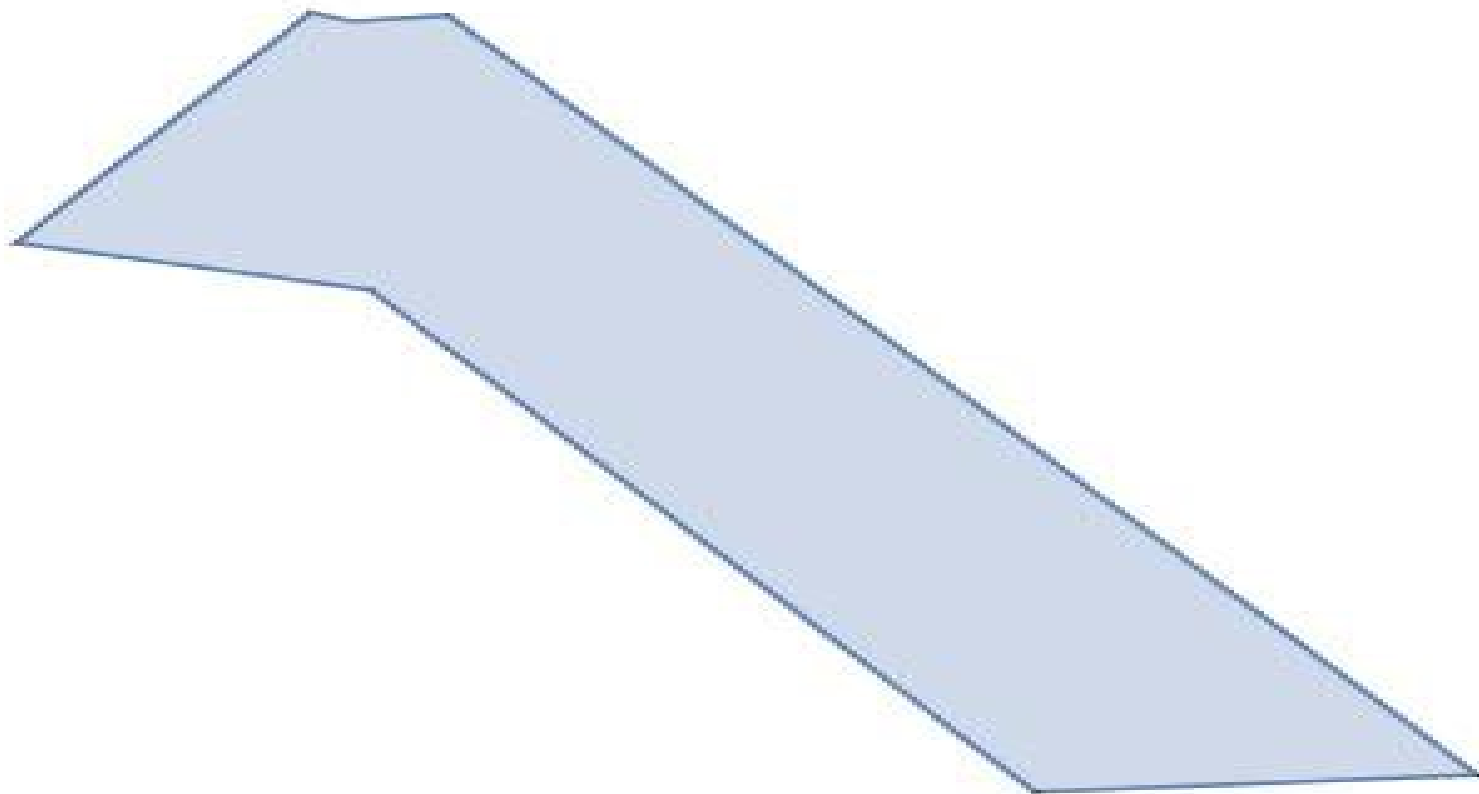
- Random Search

- Differential Evolution

- Nelder Mead

- Simulated Annealing

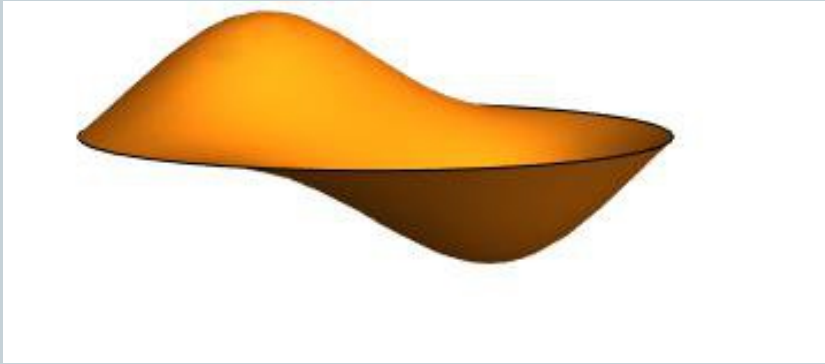
# Results



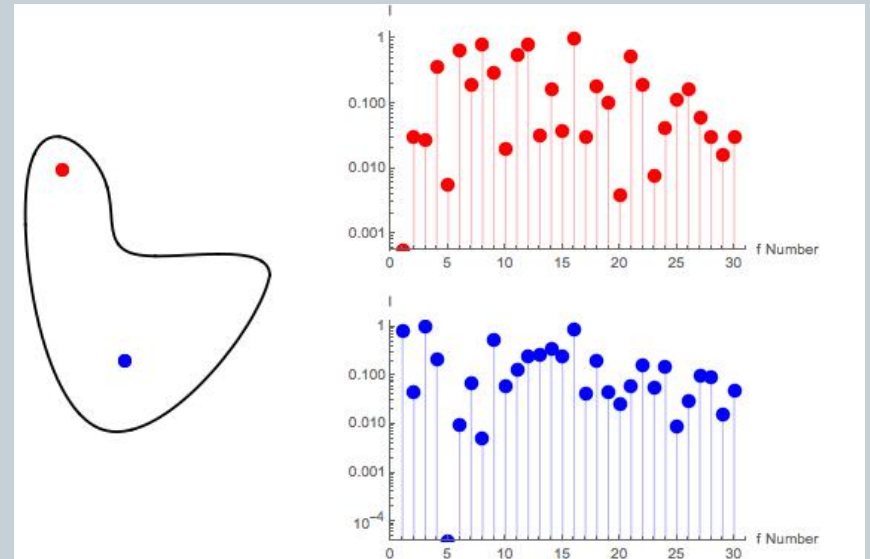
# Unforeseen Complications



## Self-Cancellation



## Varying Intensities



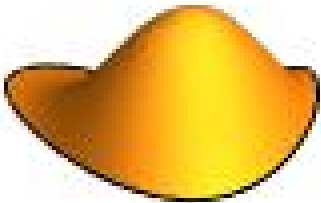


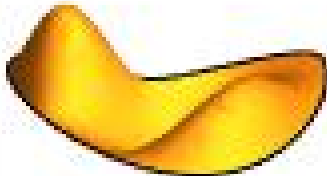

# Future Directions



- 🧠 Run better and longer optimization routines
- 🧠 Better physical testing procedures
- 🧠 Define lowest audible intensity
- 🧠 Include self-cancellation and varying intensities in analysis

# Thank you



1. 	2.05786 	2.44103 
3.12978 	3.99451 	4.33661 