

### 3 BLAST and FASTA

This lecture is based on the following papers, which are all recommended reading:

- D.J. Lipman and W.R. Pearson, Rapid and Sensitive Protein Similarity Searches. Science 227, 1435-1441 (1985).
- Pearson, W.R. and Lipman, D.J. Improved tools for biological sequence comparison. PNAS USA 85, 2444-2448 (1988).
- S.F. Altschul, W. Gish, W. Miller, E.W. Myers and D.J. Lipman. *Basic local alignment search tool*, J. Molecular Biology, 215:403-410 (1990).
- <http://www.ncbi.nlm.nih.gov/BLAST/tutorial/Altschul-1.html>, accessed April 2016.
- D. Gusfield, Algorithms on strings, trees and sequences, pg. 376-381, 1997.

#### 3.1 BLAST

Scenario Queries 散列表

**Pairwise alignment** is used to detect **homologies** between different **protein** or **DNA** sequences, either as global or local alignments.

This can be solved using dynamic programming in time proportional to the product of the lengths of the two sequences being compared.

However, this is **too slow** for **searching current databases** and in practice algorithms are used that run much faster, at the expense of possibly missing some significant hits due to the heuristics employed.

Such algorithms usually **seed and extend** approaches in which first small exact matches are found, which are then extended to obtain long inexact ones.

##### 3.1.1 BLAST terminology

? Hash Tabel NCBI -rv

BLAST, the **Basic Local Alignment Search Tool**, is perhaps the most widely used bioinformatics tool ever written. It is an alignment heuristic that determines local alignments between a *query* and a *database*.

Let  $q$  be the query and  $d$  the database. A *segment* is simply a substring  $s$  of  $q$  or  $d$ .

A **segment-pair**  $(s, t)$  consists of two segments, one in  $q$  and one  $d$ , of the same length.

x x x x x V A L L A R x x x  
... x x x x x x P A M M A R x x x x x x ...

We think of  $s$  and  $t$  as being aligned without gaps and *score* this alignment using a substitution score matrix, such as BLOSUM62.

The **alignment score** for  $(s, t)$  is denoted by  $\sigma(s, t)$ .

**Definition 3.1.1 (HSP)** Let  $C$  be a given minimum score threshold. A segment pair  $(s, t)$  is called a **high-scoring segment pair (HSP)**, if it is locally maximal and  $\sigma(s, t) \geq C$ .

Locally maximal is defined by the X-drop algorithm, described below.

A *word* is simply a short substring.

Seed Extend  
若找到了 seed 就延伸  
... < L L L L G > D I T P ...  
... < L L L L L > D I V R ...

The **goal** of BLAST is to **compute all HSPs between two sequences** (or a query and a database), for a given minimum score threshold  $C$ .

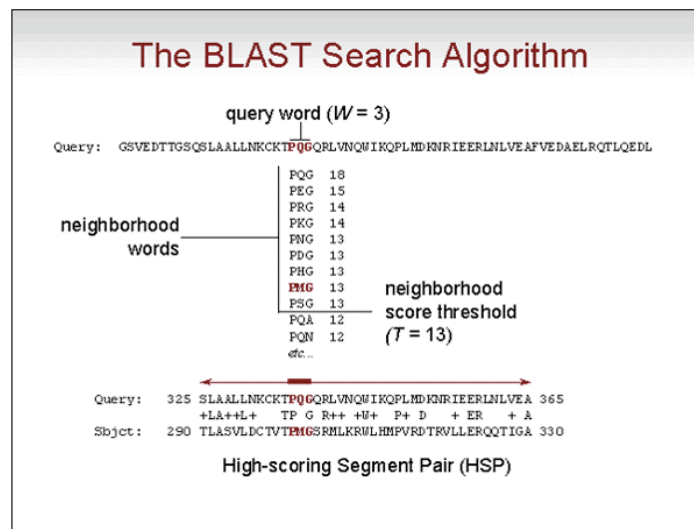
### 3.1.2 The BLAST algorithm

The BLAST algorithm has **three parameters**: The **word size**  $W$ , **word similarity threshold**  $T$  and **minimum match score**  $C$ .

For *protein* sequences, BLAST operates as follows:

1. The list  $\ell$  of all words of **length**  $W$  that **have similarity**  $\geq T$  to some word **in** the **query sequence**  $q$  is generated.
2. The **database sequence**  $d$  is scanned to **detect** each hit  $t$  of a word  $s$  from the list  $\ell$ .
3. Each such pair  $(s, t)$  (called a *seed*) is extended in either direction until the running score drops  $X$  below the best score seen so far. (This is called the *X-drop algorithm*.)
4. For each seed match, the **best extension** is reported, if it has **score**  $\geq C$ .

In practice:  $W$  is 2 – 4 for proteins.



(<https://www.cs.umd.edu/class/fall2011/cmsc858s/BLAST.pdf>, accessed April 2016)

With care, the list of all words of length  $W$  that have similarity  $\geq T$  to some word in the query sequence  $q$  can be produced in time proportional to the number of words in the list.

All seeds for a query are placed in a **“keyword tree”** and then, for each word in the tree, all exact locations of the word in the database  $d$  are detected in time proportional to the length of  $d$ .

The **original version** of BLAST did **not allow “indels”** (insertions or deletions), making hit extension very fast.

Note that the use of seeds of length  $W$  and the *X-drop* algorithm speed up the algorithm, but imply that BLAST is a heuristic that is not guaranteed to find all optimal local alignments.

For *DNA* sequences, BLAST operates as follows:

- The list  $L$  of all words of length  $W$  in the query sequence  $q$  is generated.
- The database  $d$  is scanned for all hits of words in  $L$ . Blast uses a two-bit encoding for DNA. This saves space and also search time, as four bases are encoded per byte.

In practice,  $W$  is around 12 for DNA.

### 3.1.3 Keyword tree

Assume that we want find occurrences of the words “his”, “hers” and “she” in the text “shishers”.



```

BLASTX 2.2.13 [Nov-27-2005]

Query= 000078_0077_0290 length=107 (107 letters)

Database: nr 3,044,223 sequences; 1,047,289,308 total letters

>gi|16132203|ref|NP_418803.1| lipoate-protein ligase A [Escherichia coli K12]
lipoate-protein ligase A [Escherichia coli K12]
yjjf [Escherichia coli] Lipoate-protein ligase A lipoate-protein ligase A
      Length = 338

Score = 50.4 bits (119), Expect = 2e-05
Identities = 27/36 (75%), Positives = 27/36 (75%), Gaps = 1/36 (2%)
Frame = -1

Query: 107 FSHLLDERFTWARGTA-FRR*KGHITRAQVFTDSL 3
          FSHLLDERFTW      F      KGHITRAQVFTDSL
Sbjct: 252 FSHLLDERFTWGGVELHFDVEKGHITRAQVFTDSL 287

```

### 3.1.5 The BLAST E-value

**Question:** Suppose we have computed an HSP  $(s, t)$  with score  $S$ , how significant is this match? In the following, we assume that the length  $m$  and  $n$  of the query and database are sufficiently large.

**Definition 3.1.2 (E-value)** The number of HSPs with **score  $\geq S$**  that one can expect to see by random chance is known as the E-value, which equals:

$$E = K m n e^{-\lambda S}.$$

The **E-value depend on two parameters,  $K$  and  $\lambda$** . These are based on the **background probabilities of the symbols** and on the **employed scoring matrix**. Essentially, they are scaling-factors for the search space and for the scoring scheme, respectively. (BLAST uses a built-in table of experimentally determined values of  $K$  and  $\lambda$ .)

### 3.1.6 The BLAST bit score

BLAST 有一个 Hard coded Table

In addition to the E-value, BLAST also reports a so-called *bit score*.

For a given HSP  $(s, t)$  we transform the *raw* score  $S = \sigma(s, t)$  into a *bit score* thus:

$$S' = \frac{\lambda S - \ln K}{\ln 2}.$$

Such bit scores make it easier to compare between different BLAST searches, because it hides the two parameters  $K$  and  $\lambda$ . Given the bit score of a match, one can easily compute the E-value that would arise for given query and database lengths. The E-value is obtain from a bit score  $S'$  as follows:

Interpretation of  $E = mn2^{-S'}$ .

To see this, first solve for  $S$  in the equation for  $S'$  above and then plug the result into the original E-value equation.

### 3.1.7 The BLAST P-value

The number of HSPs  $(s, t)$  with  $\sigma(s, t) \geq S$  that one obtains when comparing against a database of *random sequence* is given by a Poisson distribution. So, the probability of finding exactly  $k$  HSPs with a score  $\geq S$  is given by

$$P(k) = e^{-E} \times \frac{E^k}{k!},$$

泊松分布

where  $E$  is the  $E$ -value for  $S$ .<sup>1</sup>

**Definition 3.1.3 (P-value)** The probability of finding at least one HSP with a score  $\geq S$  “by chance” is

$$P(k \geq 1) = 1 - P(0) = 1 - e^{-E},$$

called the  $P$ -value.

BLAST reports  $E$ -values rather than  $P$ -values because it is easier, for example, to interpret the difference between an  $E$ -value of 5 and 10, than to interpret the difference between a  $P$ -value of 0.993 and 0.99995.

## 3.2 FASTA

FASTA<sup>2</sup> (pronounced fast-ay) is a heuristic for finding significant matches between a query string  $q$  and a database string  $d$ .

FASTA's general strategy is to quickly find the most significant diagonals in the dynamic programming matrix.

The performance of the algorithm is influenced by a *word-size* parameter  $k$ , usually 6 for DNA and 2 for amino acids.

The first step of the algorithm is to determine all exact matches of length  $k$  between the two sequences, called *hot-spots*.

To find these exact matches quickly, a hash table is built that consists of all words of length  $k$  that are contained in the query sequence. Exact matches are then found by look-up of each word of length  $k$  contained in the database.

A *hot-spot* is given by  $(i, j)$ , where  $i$  and  $j$  are the *locations* (i.e., start positions) of an exact match of length  $k$ .

Any such hot-spot  $(i, j)$  lies on the diagonal  $(i - j)$  of the dynamic programming matrix.

Using this scheme, the main diagonal has number 0, whereas diagonals above the main one have positive numbers, the ones below negative.

A *diagonal run* is a set of hot-spots that lie in a consecutive sequence on the same diagonal. It corresponds to a gapless local alignment.

A score is assigned to each diagonal run. This is done by giving a positive score to each match (using e.g. the PAM250 match score matrix in the case of proteins) and a negative score for gaps in the run.

The algorithm then locates the ten best diagonal runs.

Each of the ten diagonal runs is re-scored using the match score matrix and the best-scoring sub-alignment of each is extracted.

The next step is to combine high scoring sub-alignments into a single larger alignment, allowing the introduction of gaps into the alignment.

Finally, a *banded* Smith-Waterman dynamic program is used to produce an optimal local alignment along the best matched regions.

In this way, FASTA determines a highest scoring region, not all high scoring alignments between two sequences. Hence, FASTA may miss instances of repeats or multiple domains shared by two proteins.

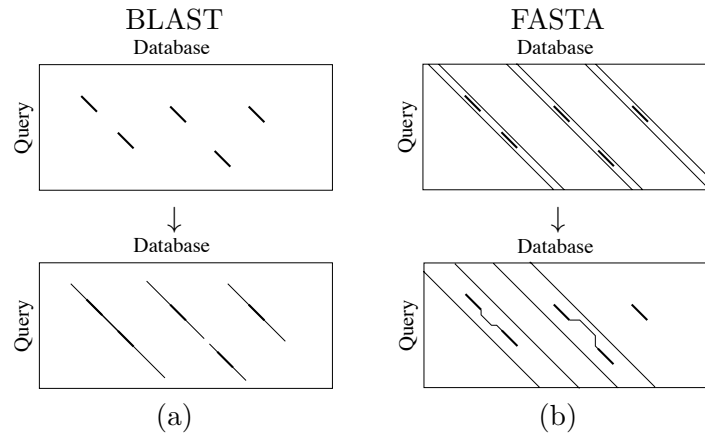
<sup>1</sup> Recall **Poisson distribution**: The probability that exactly  $k$  events occurs in a fixed time period, given that the expected number of events is  $\lambda$  in that time period, is given by:

$$P(k, \lambda) = \frac{\lambda^k e^{-\lambda}}{k!}.$$

Example: Assume that a call center gets 10 calls per hour, on average. The probability that it will get 100 calls in a given hour is  $P(100, 10)$ .

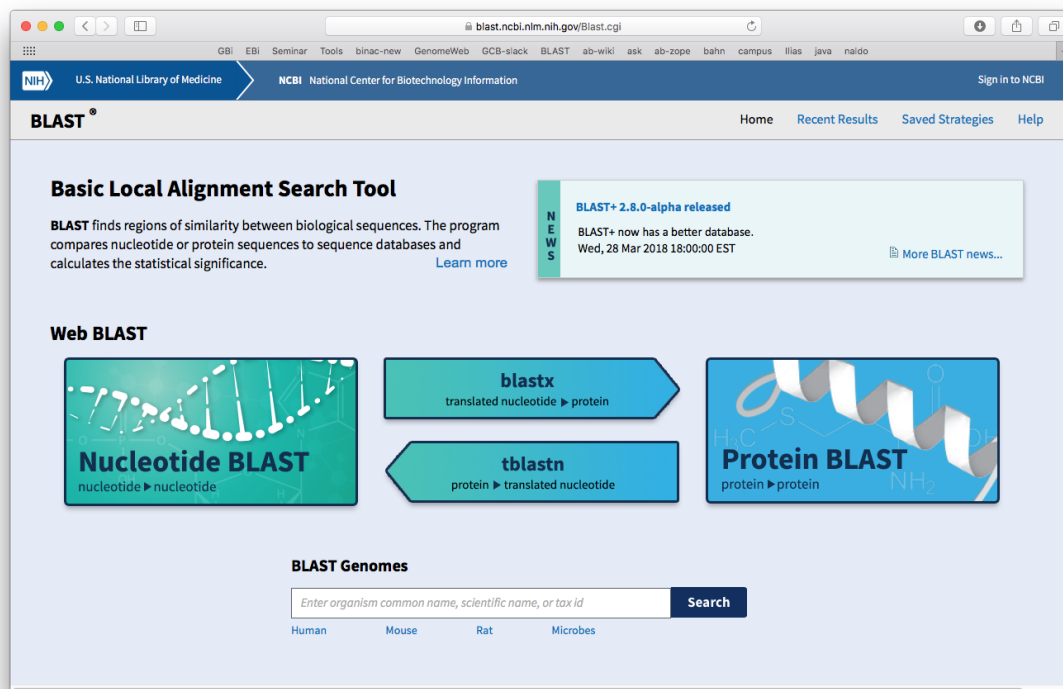
<sup>2</sup>Lipman, DJ; Pearson, WR (1985). Rapid and sensitive protein similarity searches. Science 227 (4693): 1435-41

### 3.3 BLAST and FASTA



(a) In BLAST, individual seeds are found and then extended without indels. (b) In FASTA, individual seeds contained in the same diagonal are merged and the resulting segments are then connected using a banded Smith-Waterman alignment.

### 3.4 BLAST as a web service



<http://www.ncbi.nlm.nih.gov/BLAST/>

### 3.4.1 BLAST run example

blast.ncbi.nlm.nih.gov/Blast.cgi?PROGRAM=blastx&PAGE\_TYPE=BlastSearch&...

U.S. National Library of Medicine | NCBI National Center for Biotechnology Information | Sign in to NCBI

**BLAST** » blastx | Home | Recent Results | Saved Strategies | Help

Translated BLAST: blastx

blastn | blastp | **blastx** | tblastn | tblastx

Enter Query Sequence

BLASTX search protein databases using a translated nucleotide query. [more...](#) | [Reset page](#) | [Bookmark](#)

Enter accession number(s), gi(s), or FASTA sequence(s) | Clear

>HISEQ:457:C5366ACXX:2:1101:10864:11946  
 GAAACGGTTTTTCGGGTCGGGTATTTCGATCTCGACCGTGGGGCGGAACCTGATGACCTTG  
 CGCGGAGGGATCCTTACGGGGGCACCGTACGGGGATTA

Query subrange | From | To

Or, upload file | Choose File | no file selected

Genetic code | Standard (1)

Job Title | Enter a descriptive title for your BLAST search

☐ Align two or more sequences

Choose Search Set

Database | Non-redundant protein sequences (nr)

Organism | Enter organism name or id—completions will be suggested | ☐ Exclude | Enter organism common name, binomial, or tax id. Only 20 top taxa will be shown.

Exclude | ☐ Models (XM/XP) | ☐ Uncultured/environmental sample sequences

Entrez Query | Enter an Entrez query to limit search | [You Tube](#) | [Create custom database](#)

**BLAST** | Search database Non-redundant protein sequences (nr) using Blastx (search protein databases using a translated nucleotide query) | ☐ Show results in a new window

[Algorithm parameters](#)

blast.ncbi.nlm.nih.gov/Blast.cgi

U.S. National Library of Medicine | NCBI National Center for Biotechnology Information | Sign in to NCBI

**BLAST** » blastx » RID-EJK3MVZ8014 | Home | Recent Results | Saved Strategies | Help

Format Request Status

[\[Formatting options\]](#)

Job Title: HISEQ:457:C5366ACXX:2:1101:10864:11946

Request ID	EJK3MVZ8014
Status	Searching
Submitted at	Wed May 2 01:28:20 2018
Current time	Wed May 02 01:28:27 2018
Time since submission	00:00:06

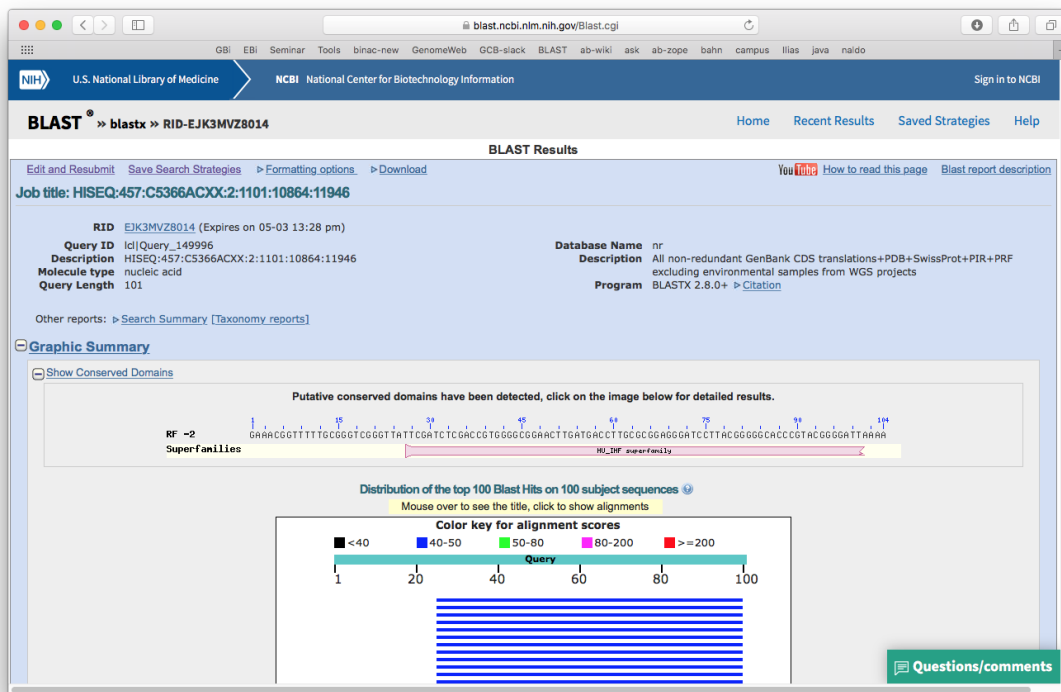
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### 3.4.2 BLAST run output

