### Modeling structure, learning representations

The two sides of language modeling

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ALPS winter school

january 2023

A ubiquitous problem: comparing sentences

A: I do not like to teach early in the morning

B: I do not like teaching early in the morning

A better than B or B better than A?

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Optimal probabilistic decision rule

A better than  $B \Leftrightarrow P(A) \ge P(B)$ 

P(sentence) is a **language mode**l

A ubiquitous problem: comparing sentences

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Ranking sentences in natural language generation tasks

les enfants ont dansés sur la plage dansé dansée

Useful for speech transcription, OCR correction, spelling / grammar checking, , text generation, machine translation . . .

Optimal probabilistic decision rule

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### Optimal probabilistic decision rule

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### Optimal probabilistic decision rule

B:

A better than 
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P(sentence) is a **language model** 

## A Markov model for natural languages

#### The simplest sequence model: *n*-gram

$$P(w_1 ... w_L) = \prod_{i=1}^{L} P(w_i | w_1 ... w_{i-1})$$

$$= \prod_{i=1}^{L} P(w_i | w_{i-n+1} ... w_{i-1})$$
(2)

- (2): given recent history  $h = w_{i-n+1} \dots w_{i-1}$ , remote words are unimportant.
- linguistically naïve, computationally efficient.
- very old model (Markov, Shannon)

## A Markov model for natural languages

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#### *n*-gram text generation with ancestral sampling

$$w_1 \sim \text{Unif}(W_1); w_2 \sim P(W_2 | w_1); w_3 \sim P(W_3 | w_2 w_1) \dots$$

Length L is not modelled: make sure to know when to stop sampling

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$$= \prod_{i=1}^{L} P(w_i \mid w_{i-n+1} \dots w_{i-1})$$
 (2)

Process more than words: letters, phones, morphs, clauses, speech turns, etc

An effective model of sequences without hierarchical structures

### *n*-gram models are so simple, yet so tricky to estimate

Zipf's curse strickes back

#### Parameter estimation from running texts

Maximum likelihood estimates (with 2-word histories: trigrams)

$$P(w|uv) = \frac{c(uvw)}{\sum_{w'} c(uvw')}$$
(3)

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c() is the count function, h = uv is the history

#### The art of language modeling

- with 100,000 words, 100,000<sup>3</sup> 3-gram counts, most of them 0
- build history classes  $(uv \rightarrow h(uw))$  to keep models small
- building history classes? the science of count smoothing [1992-2012]

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# The art of smoothing

#### Smoothing is some black magic: estimate the probability of unseen events

"+1"-smoothing (Laplace):

$$P_{+1}(w|h) = \frac{c(hw) + 1}{|\mathcal{V}| + c(h)}$$

Variant (add  $+\alpha$ , with  $\alpha$  a parameter). Alternatives

Linear interpolation

Clustering: building word / history classes

Discounting techniques (Katz back-off, Good-Turing back-off, Knesser-Ney smoothing)

Non-parametric Bayesian models

#### A side effect of smoothing

Before smoothing, many word sequences have a null probability:

After smoothing, all word sequences have probability > 0.

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After smoothing, all word sequences have probability > 0.

### **Implementations**

- n-grams, with all bells and whistles: SRILM
- n-grams, scalable & extremely efficient: KenLM
- n-grams, integrate with finite-state tools
- n-grams NLTK basic implementation

- www.speech.sri.com/projects/srilm/
  - https://github.com/kpu/kenlm
    - http://www.opengrm.org/
      - http://nltk.org

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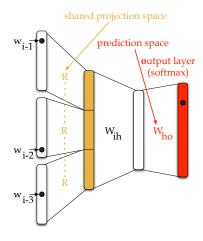
### ngram LMs: a summary

- n-grams LM are computationally efficient models of word sequences
- scales well to very large corpus
- discounting techniques are key to performance
- unknown words a big issue

Still useful? Finite-state distillation of neural LMs

## Feed-forward language models [Bengio et al., 2003]

### Continuous space *n*-gram models



$$i = \begin{bmatrix} w_{i-1}^T R, w_{i-2}^T R, w_{i-3}^T R \end{bmatrix}$$
 $h = i^T W_{ih} + b_{ih}$ 
 $o = \tanh(h)^T W_{ho} + b_{ho}$ 

$$P(w_i \mid w_{i-3}, w_{i-2}, w_{i-1}) = \frac{\exp \boldsymbol{o}[w_i]}{\sum_w \exp \boldsymbol{o}[w]}$$

What neural language modeling does:

- encodes history as  $\phi(w_{i-3}, w_{i-2}, w_{i-1})$
- ② compares  $\phi(w_{i-3}, w_{i-2}, w_{i-1})$  and  $R'(w_i)$

### Feed-forward language models [Bengio et al., 2003]

Continuous space *n*-gram models

#### Training FFLMs - maximize log-likelihood / cross-entropy

$$\boldsymbol{\theta}^* = \left[ \mathbf{R}, \mathbf{W}_{ih}, \boldsymbol{b}_i, \mathbf{W}_{ho}, \boldsymbol{b}_o \right] = \underset{\boldsymbol{\theta}}{\operatorname{argmax}} \sum_t \log \frac{\exp \boldsymbol{o}[w_t]}{\sum_w \exp \boldsymbol{o}[w]}$$
$$= \underset{\boldsymbol{\theta}}{\operatorname{argmax}} \sum_t \boldsymbol{o}[w_t] - \log(\sum_w \exp \boldsymbol{o}[w])$$

- softmax(x) =  $\left[\frac{\exp x[i]}{\sum_{k} \exp x[k]}\right]$  computes dense distributions
- embeddings R are learned
- computationally demanding (softmax layer)
- superior to discrete (n-gram) LMs across the board [Schwenk, 2007, Le et al., 2012]

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## Feed-forward language models [Bengio et al., 2003]

### Continuous space *n*-gram models

word (freq.)	model	5 nearest neighbors
is	standard	was are were been remains
900, 350	1 vector init. (*)	was are be were been
conducted	standard	undertaken launched \$270,900 Mufamadi 6.44-km-long
18,388	1 vector init. (*)	pursued conducts commissioned initiated executed
Cambodian	standard	Shyorongi \$3,192,700 Zairian depreciations teachers'
2,381	1 vector init. (*)	Danish Latvian Estonian Belarussian Bangladeshi
automatically	standard	MSSD Sarvodaya \$676,603,059 Kissana 2,652,627
1,528	1 vector init. (*)	routinely occasionally invariably inadvertently seldom
Tosevski	standard	\$12.3 Action,3 Kassouma 3536 Applique
34	1 vector init. (*)	Shafei Garvalov Dostiev Bourloyannis-Vrailas Grandi
October-12	standard	39,572 anti-Hutu \$12,852,200 non-contracting Party's
8	1 vector init. (*)	March-26 April-11 October-1 June-30 August4
3727th	standard	Raqu Tatsei Ayatallah Mesyats Langlois
1	1 vector init. (*)	4160th 3651st 3487th 3378th 3558th

(\*) 1 vector init: share parameters R and  $W_{ho}$  during init.

[Examples from [Le et al., 2010]]

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FFLMs induce similarities between histories and between words

### The infamous < unk >nown word

### "Closed world" assumptions

- The support of LM: a fixed vocab V. Sentences with unknowns have 0 probability.
- The support of LM: a fixed vocab V ∪ { < unk >}.
   Estimation: all words \( \psi \) are unked [makes < unk > very likely].
- Variant: consider classes of < unk > (proper names, numbers, etc).

#### "Open" world models with subword units: morphemes, char ngrams, bytes, pixels

- morph-based LM: require morphogical analysis, < unk > still possible
- letters: no more unknown words unknown symbols instead?
- a mixture of words and letters

#### Caveats

- Shorter units require longer histories [estimation problems]
- And imply longer sentences [computational problems]

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# Subword units in language models: BPEs, wordpieces, etc

### Byte pair encoding: N deterministic merge operations

- Make symbol map (greedy) Repeat till done: merge most frequent bigram into new compound symbol
- ② Encode (greedy)
  split each word into compound symbols

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#### Example from [Sennrich et al., 2016]

 $L = \{ lower, lowest, newer, wider, wide \}$ 

Segmentations: [low]+ [er#], [low]+ e+ s+ [t#], n+ e+ w+ [er#], [wid]+ [er#], [wid]+ [e#]

https://github.com/rsennrich/subword-nmt

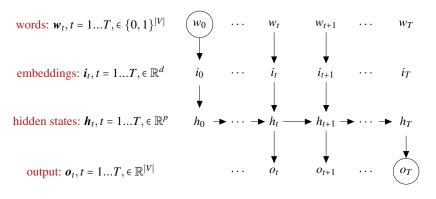
# Subword units in language models: BPEs, wordpieces, etc

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- Encode(greedy)
  split each word into compound symbols
- better solutions: SentencePiece (unigram model), wordPiece
- also regularization through sampling
- handles multilingual vocabularies [use with care]
- segmentation is a latent variable P(w|h) requires summing over segmentations [Cao and Rimell, 2021]

### Recurrent Neural Networks as LMs [Mikolov et al., 2010]

#### From finite to infinite contexts



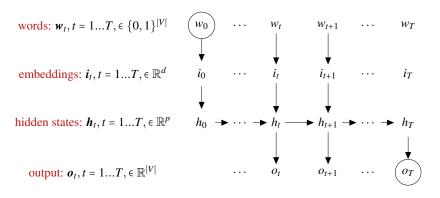
$$i_t = [w_t^T R]$$

$$h_t = \tanh(i_t^T W_{ih} + h_{t-1}^T W_{hh} + b_{ih})$$

$$o = h^T W_{ho} + b_{ho}$$

### Recurrent Neural Networks as LMs [Mikolov et al., 2010]

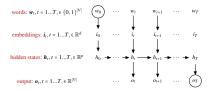
#### From finite to infinite contexts



$$\begin{aligned} \boldsymbol{\theta}^* &= \operatorname*{argmax}_{\boldsymbol{\theta}} \sum_t \log \boldsymbol{o}[w_t] - \log (\sum_w \exp \boldsymbol{o}[w]) \\ \mathrm{P}(w_{t+1} = k \,|\, w_{\leq t}; \theta_{LM}) &= \mathrm{softmax}(\boldsymbol{o}_t = W^{ho} \boldsymbol{h}_t + \boldsymbol{b}^o)[k] \end{aligned}$$

### Recurrent Neural Networks as LMs [Mikolov et al., 2010]

#### From finite to infinite contexts



- train with word prediction objective and cross-entropy loss
- more complex cells  $((w_t, h_t) \rightarrow h_{t+1})$ : GRUs, LSTMs
- same issues as FFLMs with softmax, same solutions apply
- stack several hidden layers  $h_t^k = f(h_{t-1}^k, h_t^{k-1})$ : biRNNs, etc.
- $h_T$ : compact, effective sentence representation for  $w_1 \dots w_T$
- backwards processing computes h

  <sub>-1</sub>
- $[h_T, \bar{h}_{-1}]$  a better representation: text classification, etc.
- $[h_t, \bar{h}_t]$  represents word  $w_t$  and its context

## RNNs as "pure" encoders

#### An approach to sentence classification

 $h_T = \text{RNN}(w_1 \dots w_T)$  encodes a variable-length sentence in a fixed-length vector.

Decision rule for TC tasks, mapping sentences to classes (sentiment / opinion mining, stance detection, entailment, etc):  $w_1 \dots w_T \rightarrow y$ 

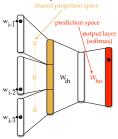
$$P(y = 1 \mid w_1 \dots w_T) = \sigma(\boldsymbol{W}^T \boldsymbol{h}_T + b)$$
  
$$\theta^* = \operatorname{argmax} \sum_{i} \log P(y^{(i)} \mid w_1^{(i)} \dots w_{T^{(i)}}^{(i)})$$

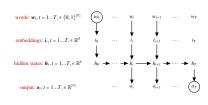
Improved classification results with backward encoding, multiple layers etc.

Also works with pairs of sentences (textual entailment, discourse modeling):

$$\boldsymbol{h}_{T}^{w} = \text{RNN}(w_{1} \dots w_{T}), \boldsymbol{h}_{S}^{v} = \text{RNN}(v_{1} \dots v_{S})$$
  
 $\boldsymbol{h}^{v,w} = \boldsymbol{h}_{T}^{w} \oplus \boldsymbol{h}_{S}^{v} \text{ or } \boldsymbol{h}^{v,w} = [\boldsymbol{h}_{T}^{w}, \boldsymbol{h}_{S}^{v}] \text{ or } \dots$ 

FFLMs / RNNs predict next word based on a continuous representation of the history with trained similarity





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- FFLMs use a fixed-size history
- RNNs use a pre-defined structure: all words matter, recent words matter more than distant words.

New architecture: SAN-LM (aka Transformers) [Vaswani et al., 2017] trained to learn which history words matter.

### Heads: parameterized computing modules

Query parameters:  $\mathbf{H}_q \in \mathbb{R}^l \times \mathbb{R}^d$ 

Key parameters:  $\mathbf{H}_k \in \mathbb{R}^l \times \mathbb{R}^d$ 

Value parameters:  $\mathbf{H}_{v} \in \mathbb{R}^{o} \times \mathbb{R}^{d}$ 

### Computing attention with heads

Heads linearly transform matrices  $I \in \mathbb{R}^d \times \mathbb{R}^T$  into matrices O in  $\mathbb{R}^o \times \mathbb{R}^T$ .

transform input matrix for words:  $\mathbf{J} = \mathbf{H}_q \times \mathbf{I} \in \mathbb{R}^l \times \mathbb{R}^T$ 

transform input matrix for contexts:  $\mathbf{K} = \mathbf{H}_k \times \mathbf{I} \in \mathbb{R}^l \times \mathbb{R}^T$ 

transform input matrix for outputs:  $\mathbf{L} = \mathbf{H}_{v} \times \mathbf{I} \in \mathbb{R}^{o} \times \mathbb{R}^{T}$ 

compute similarities words/context:  $\mathbf{D} = \mathbf{J} \times \mathbf{K}^T \in \mathbb{R}^T \times \mathbb{R}^T$ 

compute linear weights:  $\tilde{\mathbf{D}} = \operatorname{softmax}(\frac{\mathbf{D}}{\sqrt{d}}) \in [0, 1]^T \times [0, 1]^T$  columnwise

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linear combination of cols:  $\mathbf{O} = \tilde{\mathbf{D}} \times \mathbf{L} \in \mathbb{R}^T \times \mathbb{R}^o$ 

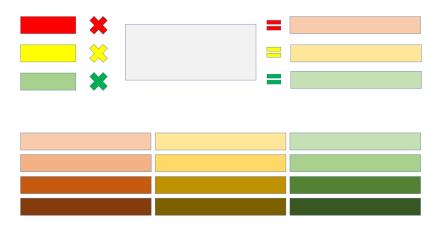
#### Using several Heads [in parallel]: MultiHeads

- one Head :  $\mathbf{I}(d \times T) \to \mathbf{O}(o \times T)$
- k Heads :  $\mathbf{I}(d \times T) \rightarrow [\mathbf{O}_1, \dots, \mathbf{O}_k](ko \times T)$

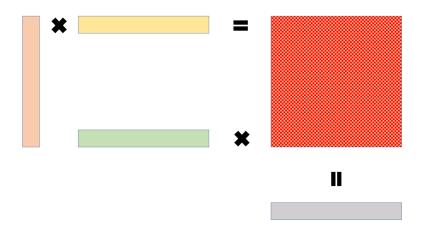
#### Using multiple layers of MultiHeads

- compute with *k* Heads :  $I(d \times T) \rightarrow O = [O_1 ... O_k](ko \times T)$
- enable residual (direct) connections O' = O + I
- pass O' through a "linear" layer O" = O' + W' × RELU(WO), with O"  $\in \mathbb{R}^{(d \times T)}$
- make layers and sublayers comparable through layer normalization (substract mean, divide by stddev)
- stack multiple layers  $I_1 \rightarrow I_2 \rightarrow I_3 \rightarrow I_4...$

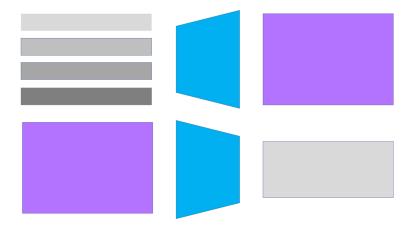
Typical values: 8 Heads of output dimension o = 64, 6 - 12 layers of heads of dimension 512.



Computes J, K, L for 4 Heads



Computes  $\tilde{\mathbf{D}}$  and  $\mathbf{K}$ 

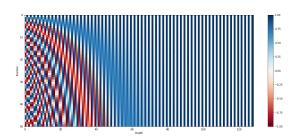


Computes output

#### The initial encoding layer

Input =  $w_1 \dots w_T$ , columns in  $\mathbf{I_1}$  combine word embeddings and positional encodings.

$$\begin{cases} \mathbf{P}[2i,t] = \sin(t/10000^{2i/d}) \\ \mathbf{P}[2i+1,t] = \cos(t/10000^{2i/d}) \end{cases} \in \mathbf{P} \in \mathbb{R}^d \times \mathbb{R}^T$$

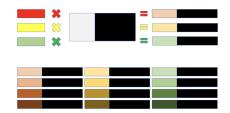


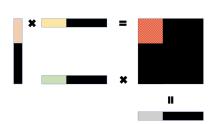
Also trainable PEs, relative PEs [Raffel et al., 2020], Alibi PEs [Press et al., 2022] etc.

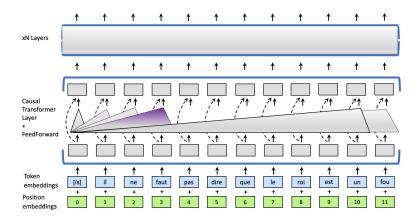
#### Masking & Causality in Language Modeling

The past should not depend on the future. Causal / Masked LMs mask ([\_]) future time steps

```
context predicts
 \langle s > w_1 \dots w_t[\_][\_] \dots \qquad w_{t+1} 
 \langle s > w_1 \dots w_{t+1}[\_][\_] \dots \qquad w_{t+2}
```







Incremental computation: fully causal transformer

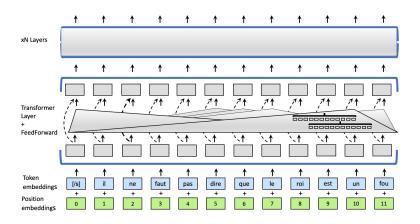
graphics, explanations https://jalammar.github.io/illustrated-gpt2/

#### Self-attention: cooking complex histories

#### Output layer and prediction (MLM)

- pack hidden states  $[\mathbf{I}_K[t], \mathbf{I}_{K-1}[t], \mathbf{I}_{K-2}[t], ...]$  into  $\sum_u \theta_u \mathbf{I}_u[t]$
- project into  $\mathbb{R}^{|\mathcal{V}|}$  to get logits:  $g(\mathbf{W}_o(\sum_u \theta_u \mathbf{I}_u[t]) + \mathbf{b}_o)$
- use softmax to predict next word w<sub>t+1</sub>
- compute loss  $\ell_{ce} = -log P(w^* | w_{< t}) = KL(\mathbb{I}(w^*) \parallel P(W | w_{< t}))$
- back-prop gradient

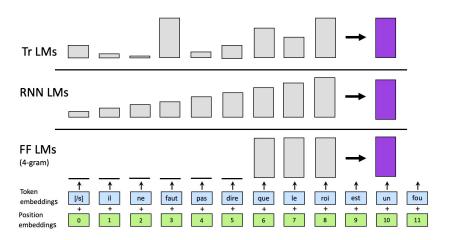
#### Self-attention: cooking complex histories



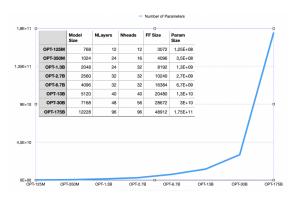
Non causal transformers are contextual representation learners

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# Self-attention: cooking complex histories



#### From language models to "foundational" models



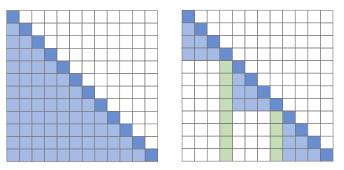
Dimensions of very large language models (OPT from Meta)

The GPT-style family: GPT1-3 (OpenAI), Megatron (Nvidia), Gopher / Chinchilla (DeepMind), HyperClova (NaverLabs), GPT-J (EuletherAI), OPT (Meta), Bloom (BigScience)

#### From language models to "foundational" models

Algorithmic issues [Tay et al., 2022]:

- extends context length T: costs  $O(T^2)$  + positional embeddings + gradients storage
- increase depth costs gradients storage

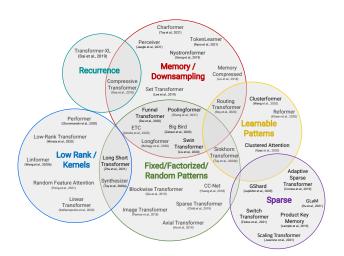


full attention

local attention + sentinels

 also: random or hierarchical sparse attention masks, parameter sharing, approximate dot product computation, etc

#### From language models to "foundational" models



A bestiary of efficient transformers [Tay et al., 2022]

# Large Language Models are \*very\* powerful

Natural language processing tasks, such as question answering, machine translation, reading comprehension and summarization, are typically approached with supervised learning on task-specific datasets. We demonstrate that language models begin to learn these tasks without any explicit supervision (...) [Radford et al., 2019]

- ✓ scoring model for disambiguation tasks (as any language model)
- continuous representations of sentences and paragraphs: towards transfert learning
- ✓ simple and effective generation mechanism  $Gen(w_1...w_T) = argmax_{w_{t+1}...w_T} P(w_{t+1}...w_T | w_1...w_t)$
- use generation as multitask processing with prompts / instructions

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Prompt (ANLI)	The Gold Coast Hotel & Casino is a hotel and casino located in Paradise, Nevada. This locals' casino
	is owned and operated by Boyd Gaming. The Gold Coast is located one mile west of the Las Vegas
	Strip on West Flamingo Road. It is located across the street from the Palms Casino Resort and the
	Rio All Suite Hotel and Casino. Question: The Gold Coast is a budget-friendly casino. True, False,
	or Neither?
Answer (OK)	Neither
Answer (KO)	True
Answer (KO)	False
Prompt (PIQA)	How to apply sealant to wood ?
Answer (OK)	Using a brush, brush on sealant onto wood until it is fully saturated with the sealant.
Answer (KO)	Using a brush, drip on sealant onto wood until it is fully saturated with the sealant.
Prompt (COPA)	My body cast a shadow over the grass because
Answer (OK)	the sun was rising.
Answer (KO)	the grass was cut.

examples from Radford et al. [2019]

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Also: summarization / compression, machine translation (!), arithmetic (!!)

#### Current challenges for language modeling

- find the right modeling units (between char-based and word-based)
- model very long range context-dependency beyond syntax: [Dai et al., 2019] repetitions, style, discourse consistency, etc.
- towards better text generation through better searching
- improve training efficiency / scalability; reduce the carbon emissions of large-scale LMs
- (continuous) online adaptation of LMs
- omitigate the biases of "stochastic parrots" (also: privacy issues, etc) [Bender et al., 2021]

The race for size not finished - from GPT2 (1.5b) to GPT3 (175b) to T5 to GShard (600b), Switch-C (1.6t) to PALM and beyond

#### Implementations and models available online

- https://transformer.huggingface.co/
- https://github.com/facebookresearch/fairseq
- https://www.tensorflow.org/hub?hl=en
- https://github.com/openai/gpt-2

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