

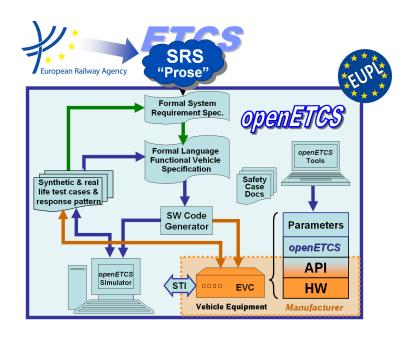
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Work Package 4: "Validation & Verification Strategy"

Final Report on Validation and Verification Report of Implementation/Code

Jens Gerlach and Izaskun de la Torre

December 2015



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OETCS/WP4/D4.3.2 December 2015

Final Report on Validation and Verification Report of Implementation/Code

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Intermediate report

Prepared for openETCS@ITEA2 Project

Abstract: This work package will comprise the activities concerned with verification and validation within openETCS. This includes verification & validation of development artifacts, that is, showing that models and code produced correctly express or implement what they are supposed to. And also, methods and tools to perform such tasks will be evaluated with the goal of assembling a suitable method and tool chain to support a full development.

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1 Introduction

In this intermediate report we describe the activities to formally verify the correctness of parts of the software developed in the OpenETCS project.

While major parts of the functionality of Subset 026 are modelled in higher-level languages, there is also a substantial part of *supporting* software that is developed in the C programming language.

In this document we report about results on the verification of that C code. In particular, we report on the use of static analysis methods (including formal methods) on C code that has been developed by the project partner Siemens.



Figure 1.1. Scope of formal methods with in OpenETCS

Figure 1.1 outlines the roles of formal methods within the OpenETCS project. What this figure shall convey is that even a subsystem such as described by *Subset 026* of the ETCS specification is usually too complex to be completely formally specified. Therefore, *semi-formal modelling techniques* and *tests* and *simulations* play a crucial role to verify that the implementation satisfies its specification. However, for clearly defined modules and select system properties, formal methods can well be applied to establish the correctness of an implementation.

Figure 1.2 shows slightly more detailed the OpenETCS software. The report at hand is limited to the parts encapsulated by C software encapsulated in a dashed box.





Figure 1.2. Scope of code verification

1.1 Software layers

Figure 1.3 shows the layer structure of the OpenETCS C code. The OpenETCS decoder/encoder is a collection of data structures and associated functions for reading and writing ETCS packets from/to a bit stream.



Figure 1.3. Software layers of the OpenETCS C code

In order to fulfill their task the decoder and encoder function rely on an implementation of bit streams in C. The Bitstream package in turn is built on top of the so-called *bitwalker* layer. In order to accomplish the task of formal verification of these layers we also provided several functions that read and write individual bits for basic C types.

The main achievement that we present in this report are the results on the formal specification and formal specification of the various software layers in Figure 1.3.

This report is result of the joint work of many OpenETCS partners, notably:

- CEA LIST
- DLR
- Fraunhofer FOKUS
- Siemens
- SQS

The formal analyses contribute to the ultimate verification goals, which are the following:

1. provide evidence that both the generated and a handwritten C code satisfies accepted quality standards

- 2. develop a formal specification for Subset 026 functionality
- 3. verify with Frama-C/WP that the software satisfies its formal specification
- 4. show that the software does not raise runtime errors

The European standard for railway software [1, § 7.3.4.19] mandates that the specification of software interfaces shall address various properties. Table 1.1 list these properties and also indicates to what extend Frama-C can be used to formally express them.

Property	Specification through Frama-C
pre and post conditions	yes
definition and description of all boundary values for all specified data	yes
behaviour when the boundary value is exceeded	yes
behaviour when the value is at the boundary	yes
time-critical input and output data	no
allocated memory for the interface buffers and the mechanisms to detect that the memory cannot be allocated or all buffers are full, where applicable	yes
existence of synchronization mechanisms between functions	partially

Table 1.1. Properties to be addressed by interface specification according to EN 50128

We see from this table that Frama-C¹ is a well-justified choice for the specification of railway software.

1.2 Structure of this document

We represent the C code and related specifications in a top-down approach. Thus, we start on the level of OpenETCS data packets and explain from there the lower software levels.

- Chapter 2 gives a short overview on the Frama-C/WP tool that plays a central role in the verification of OpenETCS C code. Here we also try to rectify some misunderstandings about formal verification that we have encountered in our work.
- Chapter 3 presents the formal specification of OpenETCS packets in ACSL (the specification language of Frama-C). For the sake of an easier understanding we start with the specification of a concrete packet (AdhesionFactor in Section 3.1) and explain from there how the other specifications look like.
- The OpenETCS packets are written to and read from bit streams which is represented by the type Bitstream and its associated functions. Chapter 4 provides the definition and formal specification of Bitstream operations.

¹Or to be more precise "ACSL" (ANSI/ISO-C Specification Language) which is the specification language of Frama-C.

The implementation of Bitstream itself relies on lower level bit operations. The formal specification of these operations are presented in Chapter 5.

- Chapter 6 lists results of the formal verification with Frama-C/WP.
- In Chapter 7, we draw conclusions from this work and outline the next steps in our verification efforts.



2 An introduction to formal verification with Frama-C/WP

Frama-C is a platform dedicated to source-code analysis of C software. It has a plug-in architecture and can thus be easily extended to different kinds of analyses. The WP plugin of Frama-C allows one to formally verify that a piece of C satisfies its specification. This implies, of course, that the user provides a *formal specification* of what the implementation is supposed to do. Frama-C comes with its own specification language ACSL which stands for *ANSI/ISO C Specification Language*. In order to help potential users to master ACSL we discuss in this chapter a very simple C abs_int that implements the computation of the absolute value for objects of type int.

- In Section 2.1 we will present a straightforward specification of abs_int. We discuss the reasons why Frama-C/WP is not able to verify that our implementation satisfies this specification in Section 2.2.
- In Section 2.3 we provide a more precise specification that can be verified by Frama-C/WP. In Section 2.4 we explain how Frama-C supports—by allowing the separation of the specification from the implementation—good software engineering practices.
- Sections 2.5 and 2.6 discuss, respectively, how Frama-C/WP supports *modular verification* and the formal treatment of *side effects*.

2.1 First steps

We will consider the function that computes the absolute value |x| of an integer x. In order to avoid name clashes with the function abs in C library we use the name abs_int.

The mathematical definition of absolute value is very simple

$$|x| = \begin{cases} x & \text{if } x \ge 0 \\ -x & \text{if } x < 0 \end{cases}$$
 (1)

A straightforward implementation of abs_int is shown in Listing 2.1.

```
int abs_int(int x)
{
   return (x >= 0) ? x : -x;
}
```

Listing 2.1. An implementation of the absolute value function

In order to demonstrate that this implementation is correct we have to provide a formal specification. Listing 2.2 shows our first attempt for an ACSL specification of abs_int that is based on the mathematical definition of the function $x \mapsto |x|$ in Equation 1.

```
/*@
    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;
*/
int abs_int(int x)
{
    return (x >= 0) ? x : -x;
}
```

Listing 2.2. A first attempt to formally specify abs_int

The first thing to note is that ACSL specifications—or *contracts*—are placed in special C (they start with /*@). Thus, they do not interfere with the executable code. The ensures clause in the specification expresses *postconditions*, that is, properties that should be guaranteed *after* the execution of abs_int. The ACSL reserved word \result is used to refer to the return value of a C. Note that we use the usual C ==and <=to express equalities and inequalities in the specification. There is also an additional operator ==> which expresses logical implication.

2.2 Why can Frama-C/WP not verify such a simple function?

Although the specification and implementation in Listing 2.2 look perfectly right, Frama-C/WP cannot verify that the implementation actually satisfies its specification.

The reason becomes clear if we look at some actual return values of abs_int. Listing 2.3 shows our test code whose output is listed in Table 2.1.

```
#include <stdio.h>
#include <limits.h>
extern int abs_int(int);
void print_abs(int x)
 printf("%12d\t\t%12d\n", x, abs_int(x));
int main()
 printf("\n");
 print_abs(0);
  printf("\n");
  print_abs(1);
  print_abs(10);
  print_abs(INT_MAX);
  printf("\n");
  print_abs(-1);
  print_abs(-10);
  print_abs(INT_MIN);
```

Listing 2.3. Some simple test cases for abs_int

X	abs_int(x)	Remark
0	0	✓
1	1	✓
10	10	✓
2147483647	2147483647	✓
-1	1	✓
-10	10	✓
-2147483648	-2147483648	4

Table 2.1. Test results for abs_int

The offending value is in the last line of Table 2.1 which basically states that abs_int (INT_MIN) equals INT_MIN whereas it should equal -INT_MIN. The problem is that the type **int** only present a finite subset of the (mathematical) integers. Many computers use a two's-complement representation of integers which covers the range $[-2^{31} \dots 2^{31} - 1]$ on a 32-bit machine. On such a machine -INT_MIN cannot be represented by a value of the type **int**.

In a specification, Frama-C/WP interprets integers as mathematical entities. Consequently, there is no such thing as an *arithmetic overflow* when adding or multiplying them. In other words, Frama-C/WP is perfectly right not being able to verify that abs_int satisfies the contract in Listing 2.2. Indeed, the implementation does not respect the given specification.

2.3 Sharpening the contract of abs_int

It is of course well known that the operation -x can overflow and it is the fact that Frama-C/WP can detect such overflows that helps to prevent incorrect verification results.

The GNU Standard C clearly states that the absolute value of INT_MIN is undefined.² Under OSX, the manual page of abs mentions under the field of "Bugs":

```
The absolute value of the most negative integer remains negative.
```

Thus, our formal specification should exclude the value INT_MIN from the set of admissible value to which abs_int can be applied. In ACSL, we can use the requires clause to express *preconditions* of a function. Listing 2.4 shows an extended contract of abs_int that takes the limitations of the type int into account.

```
#include <limits.h>

/*@
    requires x > INT_MIN;

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;

*/
int abs_int(int x)
{
    return (x >= 0) ? x : -x;
}
```

Listing 2.4. Taking integer overflows into account

Frama-C/WP is now capable to verify that the implementation of abs_int satisfies the specification of Listing 2.4.

There is an important lesson that can be learned here:

Sometimes developers provide source code and imagine that a tool like Frama-C/WP can verify the correctness of their implementation. In order to fulfill its task, however, Frama-C/WP needs an ACSL specification. Such a specification—which must be based on a reasonably precise description of the admissible inputs and expected behavior—has to come from the *requirements* of the software and is not magically discovered from the source code by Frama-C/WP. The code does what it does. In order to verify that the code does what someone expects, these expectations must be clearly expressed, that is, they must be formally specified.

Of course, it might not always be the goal to verify the complete functionality of a piece of software. Sometimes, it is enough to ensure that individual software components cause no runtime errors, that is, arithmetic overflows or invalid pointer accesses. Frama-C/WP can also be used in this situation. Under the terms of the following minimal specification in Listing 2.5, Frama-C/WP can verify that no runtime error will occur.

²See http://www.gnu.org/software/libc/manual/html_node/Absolute-Value.html

```
#include <limits.h>

/*@
    requires x != INT_MIN;

*/
int abs_int(int x)
{
    return (x >= 0) ? x : -x;
}
```

Listing 2.5. Minimal contract to ensure the absence of runtime errors in abs_int

2.4 Separating specification and implementation

Before we continue exploring more advanced specification and verification capabilities of Frama-C/WP we turn to a simple software engineering question.

It is common practice to put function prototypes into ".h" files and keep the implementation in files ending in ".c". Frama-C/WP supports this separation of specification and implementation. Listing 2.6 shows the file abs2.h which contains a declaration of abs_int together with an attached ACSL specification.

```
#include <limits.h>
/*@
    requires x > INT_MIN;

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;
*/
int abs_int(int x);
```

Listing 2.6. Specifying a function prototype in a header file

Listing 2.7 shows the specification of abs_int in a .c file. Note that the file abs2.h with the specification is included by this file. Frama-C/WP can verify that this implementation satisfies the contract in Listing 2.6.

```
#include "abs2.h"

int abs_int(int x)
{
  return (x >= 0) ? x : -x;
}
```

Listing 2.7. Implementation at a different location than the specification

We remark, that the definition of a very small function like abs_int would normally be placed in a header file so that a compiler can inline the function definition at the call site.

2.5 Modular verification

We now look at a simple example in which our function abs_int is used. More precisely, we include in Listing 2.8 the header file from Listing 2.6 which contains an ACSL specification of abs_int.

```
#include "abs2.h"

void use_1()
{
  int a = abs_int(3);
  int b = abs_int(-1);
  int c = abs_int(INT_MAX);
  int d = abs_int(INT_MIN);

// ...
```

Listing 2.8. A simple example of modular verification

When Frama-C/WP tries to verify the code in Listing 2.8, then it actually tries to establish whether at each program location where it is called the *preconditions* of abs_int are satisfied. Based on the specification of abs_int, Frama-C/WP can indeed verify that for the first three calls the preconditions are fulfilled. For the last call this verification fails because the value INT_MIN is explicitly excluded by the specification in Listing 2.6.

Note that the *implementation* of abs_int does not play any role in determining whether it is safe to call the function in a particular context. This is what we call *modular verification*: a function can be verified in isolation whereas code that calls the function only uses the function contract.

This also means that in a situation as in Listing 2.9, where nothing is known about the argument of abs_int, Frama-C/WP cannot establish that the precondition of abs_int is satisfied or, in other words, that $x > INT_MIN$ holds.

```
#include "abs2.h"

void use_2(int x)
{
  int a = abs_int(x);

  // ...
}
```

Listing 2.9. Another example of modular verification

If, on the other hand, we have precise information on the arguments at call site, then Frama-C/WP can exploit the specification of abs_int in order derive some interesting properties. As an example, we consider the code fragment in Listing 2.10. Here, Frama-C/WP can verify that the assertion after the call of abs_int is correct.

Note that this assertion is a *static* one, that is, it is an ACSL annotation that resides inside a comment and does not affect the execution of the code in Listing 2.10. Also note that unlike

```
#include "abs2.h"

/*@
    requires (10 <= x < 100) || (-200 < x < -50);

*/
void use_3(int x)
{
    int a = abs_int(x);
    //@ assert 10 <= a < 200;

// ...
}</pre>
```

Listing 2.10. A more complex example of modular verification

in C code, *relation chains* with their usual mathematical meaning can be used both in function contracts and assertions.

2.6 Dealing with side effects

Listing 2.11 shows an implementation of abs_int that writes as a side effect the argument x to a global variable a. A natural question is to ask whether this implementation with a side effect also satisfies the specification.

```
#include <limits.h>
extern int a;

/*@
    requires x > INT_MIN;

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;

*/
int abs_int(int x)
{
    a = x; // Is this side effect covered by the specification?
    return (x >= 0) ? x : -x;
}
```

Listing 2.11. An implementation with side effects

Before we answer this question we consider various uses for side effects. There are of course legitimate uses for side effects. The assignment to a memory location outside the scope of the function might be meaningful because an error condition is reported or because some data are logged as in Listing 2.12.

If Frama-C/WP attempts to verify the code in Listing 2.12, then it issues the following warning:

```
Neither code nor specification for function logging, generating default assigns from the prototype
```

Thus, it points out that the called function logging should have a proper specification that clearly indicates its side effects.

```
#include <limits.h>
extern void logging(int);

/*@
    requires x > INT_MIN;

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;

*/
int abs_int(int x)
{
    logging(x);
    return (x >= 0) ? x : -x;
}
```

Listing 2.12. Calling a logging function from abs_int

There are, on the other hand, also good reasons to minimize or even forbid side effects:

- Imagine a malicious password checking function that writes the password to a global variable.
- Another reason is that side effects can make it harder to understand what the real consequences
 of a function call are. In particular, one must be concerned about unintended consequences
 that are caused by side effects The norm IEC 61508 therefore requests in the context of
 software module testing and integration testing:

To show that all software modules, elements and subsystems interact correctly to perform their intended function and do not perform unintended functions (see also. [2, §7.4.7.2,§7.7.2.9])

Of course, it is quite difficult to ensure by testing alone that something does *not* happen.

To come back to our question about Listing 2.11 it is important to understand that Frama-C/WP verifies that the implementation shown there satisfies the specification.

If one wishes to forbid that a function changes global variables one can use an assigns \nothing clause as shown in Listing 2.13. Frama-C/WP will then point out that this implementation prevents the verification of the assigns clause.

```
#include <limits.h>
extern int a;

/*@
    requires x > INT_MIN;

    assigns \nothing; // forbid any side effects

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;

*/
int abs_int(int x)
{
    a = x; // now illegal
    return (x >= 0) ? x : -x;
}
```

Listing 2.13. Specifying the absence of side effects

Of course, an all-or-nothing-approach to side effects is not very helpful for the verification of real-life software. Listing 2.14 shows how the assigns clause of a specification can name the exact memory location that the function is allowed to modify.

```
// Side effects can be controlled on an individual basis.
#include <limits.h>

extern int a;

/*@
    requires x > INT_MIN;

    assigns a; // allow assignment to a (but only to a).

    ensures 0 <= x ==> \result == x;
    ensures 0 > x ==> \result == -x;

*/
int abs_int(int x)
{
    a = x;
    return (x >= 0) ? x : -x;
}
```

Listing 2.14. Finer control of side effects

Note however that assigns a does not imply that a write to a necessarily occurs during the execution of abs. On the other hand, any other memory location must stay unchanged between the initial state and the final state of abs.



3 ETCS data packets

In the following, we give a top-down presentation of the OpenETCS Decoder software. We discuss the highest, i.e. the data packet level, in this chapter; Chapter 4 elaborates on some intermediate, and Chapter 5 on the lowest level.

On the data packet level, a total of 47 different packets are defined as C struct. We exemplify our discussion on the alphabetically first packet, AdhesionFactor (Section 3.1), and give some comments on considerations with respect to other packets (Section 3.2).

In order to cope with the similarity of specification, implementation, and verification tasks for all packets, we have chosen to automatically generate formal specifications and implementations for encoding and decoding data packets from chapter 7 of the ETCS Subset 026 system requirements description.

3.1 Formal specification of AdhesionFactor

3.1.1 AdhesionFactor in ETCS

ETCS Subset 026 defines the package adhesion factor (packet 71) as shown in Table 3.1.

variable name	number of bits
NID_PACKET	8
Q_DIR	2
L_PACKET	13
Q_SCALE	2
D_ADHESION	15
L_ADHESION	15
M_ADHESION	1

Table 3.1. Packet AdhesionFactor as defined by ETCS

3.1.2 The type AdhesionFactor

Listing 3.1 shows the definition of type AdhesionFactor as it is generated from the ETCS specification shown in Section 3.1.1.

```
struct AdhesionFactor
   PacketHeader header:
   // TransmissionMedia=Any
   // This packet is used when the trackside requests a change of
    // the adhesion factor to be used in the brake model.
    // Packet Number = 71
                               // # 2
   uint64_t Q_DIR;
                               // # 13
   uint64_t L_PACKET;
                               // # 2
   uint64_t Q_SCALE;
                               // # 15
   uint64_t D_ADHESION;
                               // # 15
   uint64_t L_ADHESION;
   uint64_t M_ADHESION;
                               // # 1
};
typedef struct AdhesionFactor AdhesionFactor;
```

Listing 3.1. Definition of the type AdhesionFactor

3.1.3 ACSL predicates AdhesionFactor

Listing 3.2 shows the definition of the logic functions BitSize and MaxBitSize for AdhesionFactor. The former function uses a macro that contains the size of AdhesionFactor in bits. The functions are used in Listing 3.8 and Listing 3.9 where the overloading of the logic predicates allows for a more generic ACSL contract for the EncodeBit and DecodeBit functions.

```
/*@
   logic integer BitSize{L} (AdhesionFactor* p) = ADHESIONFACTOR_BITSIZE;
   logic integer MaxBitSize{L} (AdhesionFactor* p) = BitSize(p);
*/
```

Listing 3.2. Definition of the BitSize predicates for AdhesionFactor

Listing 3.3 shows the definition of the Invariant predicate for AdhesionFactor. The predicate is the conjunction of the (trivial) Invariant (uint64_t) predicates of all members of on object of type AdhesionFactor.

Listing 3.3. Definition of the Invariant predicate for AdhesionFactor

Listing 3.4 shows the definition of the <code>UpperBitsNotSet</code> predicate for <code>AdhesionFactor</code>. The predicate <code>UpperBitsNotSet</code> (<code>AdhesionFactor*</code>) evaluates to true if and only if the values of all members of <code>AdhesionFactor</code> fit into their assigned numbers of bits. This functionality is ensured by the conjunction of the <code>UpperBitsNotSet</code> (<code>uint64_t</code>, <code>uint32_t</code>) predicate, which is explained in Section 5.2, for all members of <code>AdhesionFactor</code>.

Listing 3.4. Definition of the UpperBitsNotSet predicate for AdhesionFactor

Listing 3.5 shows the definition of predicate Separated for AdhesionFactor. The predicate Separated (stream, p) is true if and only if the two objects *stream and *p do not overlap in memory. Thus, writing into the stream will not change *p and vice versa.

```
/*@
    predicate Separated(Bitstream* stream, AdhesionFactor* p) =
    \separated(stream, p) &&
    \separated(stream->addr + (0..stream->size-1), p);
*/
```

Listing 3.5. Definition of the Separated predicate for AdhesionFactor

Listing 3.6 shows the definition of the EqualBits predicate for AdhesionFactor. Based on the ETCS specification, this predicate describes a relationship between the bits of the individual members of an object of type AdhesionFactor and those of a bit stream. This predicate will be used to formally describe the transfer of bits from a bit stream to an object of type AdhesionFactor and vice versa. The definition of the predicate EqualBits (AdhesionFactor*) uses the predicate EqualBits (uint64_t), which is explained in Section 4.1.

Listing 3.6. Definition of the EqualBits predicate for AdhesionFactor

3.1.4 Formal specification of AdhesionFactor_UpperBitsNotSet

Listing 3.7 shows the contract of the <code>UpperBitsNotSet</code> function for <code>AdhesionFactor</code>. The function contract includes the <code>requires</code> clauses, labeled <code>valid</code> and <code>invariant</code>. These limit the significance of the <code>ensures</code> and <code>assigns</code> clauses to the <code>AdhesionFactor</code> objects that also satisfy the <code>requires</code> clauses. The <code>valid</code> clause only evaluates to true if the <code>*p</code> is a valid pointer. The <code>invariant</code> clause requires <code>Invariant(p)</code> to evaluate to true. The <code>Invariant(AdhesionFactor*)</code> predicate is explained in Section 3.1.3. The contract also includes a statement on the return value of the function, labeled <code>result</code>. This clause ensures that the function's return value for <code>AdhesionFactor*</code> <code>p</code> matches the evaluation of the predicate <code>UpperBitsNotSet(p)</code> from Section 3.1.3. With the <code>assigns \nothing</code> clause the contract furthermore specifies that this function has no side effects.

Listing 3.7. Contract for UpperBitsNotSet function of AdhesionFactor

3.1.5 Formal specification of AdhesionFactor_DecodeBit

Listing 3.8 shows the contract for the DecodeBit function for AdhesionFactor. The behavior of the function is specified using the two disjoint behaviors normal_case and error_case. The requirements valid_stream, stream_invariant, valid_package and separation apply to both behaviors and limit the set of combinations of input arguments for which the ensures and assigns clauses describe the behavior of the function.

The assigns clauses in the contract's body describe the side effects of the function. If the function contract is split into multiple behaviors, like here, common assigns clauses, which contain the union of the behaviors' assigns clauses, are needed outside of the behaviors. Their meaning will become clear when discussing the individual behaviors.

For both behaviors the unchanged clause states that none of the bits in the bit stream are written by the function.

- The property valid_stream requires that the predicate Readable (stream) is satisfied (see Section 4.1).
- The property stream_invariant is only met if the Invariant predicate is true. The predicate Invariant (Bitstream*, integer) is described in Section 4.1.
- The property valid_package requires that p is a valid pointer for read and write operations.
- The property separation requires that *stream and *p do not overlap in the memory. The Separated predicate was introduced in Section 3.1.3.

The behavior normal_case describes the function's behavior if *stream contains enough unread bits to fill all members of *p. In this case an object of type AdhesionFactor is decoded from the stream and thus *p is written. The latter is stated by the first assigns clause. In this context the ensures clauses equal and upper describe the relationship of the bits in the bit stream and the bits of the members of *p. Furthermore stream->bitpos will be updated. The effects of this operation are described by the second assigns and the increment clauses.

The behavior error_case describes the function's behavior in the opposite case i.e. if \star stream is exhausted before all members of $\star p$ are read. In this case the function has no side effects and in particular does not write $\star p$ or stream->bitpos. The ensures clause

result states that the return value of the function equals 0. In normal_case this value was specified to equal 1.

The distinguishing predicate for the two behaviors is Normal (Bitstream*, integer), which appears in the assumes clauses within both behaviors and is explained in Section 4.1.

```
/ * @
    requires valid_stream:
                                Readable (stream);
   requires stream_invariant: Invariant(stream, MaxBitSize(p));
   requires valid_package:
                                \valid(p);
   requires separation:
                                Separated(stream, p);
   assigns stream->bitpos;
   assigns *p;
   ensures unchanged:
                                Unchanged{Here,Old} (stream, 0, 8*stream->
       size);
   behavior normal_case:
     assumes Normal {Pre} (stream, MaxBitSize(p));
     assigns stream->bitpos;
     assigns *p;
     ensures invariant: Invariant(p);
     ensures result:
                         \ \ \ == 1;
      ensures increment: stream->bitpos == \old(stream->bitpos) + BitSize(
         p);
     ensures equal:
                         EqualBits(stream, \old(stream->bitpos), p);
      ensures upper:
                         UpperBitsNotSet(p);
   behavior error_case:
     assumes !Normal{Pre}(stream, MaxBitSize(p));
     assigns \nothing;
     ensures result: \result == 0;
    complete behaviors;
   disjoint behaviors;
int AdhesionFactor_DecodeBit(AdhesionFactor* p, Bitstream* stream);
```

Listing 3.8. Contract for DecodeBit function of AdhesionFactor

3.1.6 Formal specification of AdhesionFactor_EncodeBit

Listing 3.9 shows the contract for the <code>EncodeBit</code> function for <code>AdhesionFactor</code>. The behavior of the function is described using the three disjoint behaviors <code>normal_case</code>, <code>values_too_big</code> and <code>invalid_bit_sequence</code>. The requirements <code>valid_stream</code>, <code>stream_invariant</code>, <code>valid_package</code>, <code>invariant</code> and <code>separation</code> are similar to those of the <code>DecodeBit</code> function's contract for <code>AdhesionFactor</code>. The ones not examined in detail here do not differ from the ones in Section 3.1.5.

Like for the DecodeBit function for AdhesionFactor in Section 3.1.5 the assigns clauses in the contract body are the conjunction of the assigns clauses of the individual behaviors.

• Property valid_stream is only met if Writable(stream) applies. The predicate Writable(Bitstream*) requires that the stream is accessible for updates.

- Property valid_package requires *p to be valid pointer.
- Property invariant is only met if the Invariant predicate, which was described in Section 3.1.3, holds for p.

The behaviors of the EncodeBit contract describe one successful case and two error cases.

Behavior normal_case describes a successful encoding of the object *p into the bit stream. The assigns clauses specify that in this case both the bitpos of the stream and the fields of the bit stream are written. The increment clause describes the new value for bitpos. The ensures clauses left, middle and right state that only some bits of the bit stream are written. The updated bits and their relationship to the bits of the members of the object *p are described with the EqualBits predicate, which is described in Section 3.1.3. The Unchanged predicate specifies that the bits in the bit stream before the old stream->bitpos and the after the new stream->bitpos remain unchanged. Unchanged (Bitstream*, integer, integer) is defined in Section 4.1.

Behavior values_too_big describes the scenario in which the value of at least one member of *p is bigger than the specified bit size for that member of AdhesionFactor allows. The numbers of bits for the members of AdhesionFactor are specified in Section 3.1.1. The assigns clause states that this behavior of the function causes no side effects and the result clause ensures that the function will return the value -2. In contrast to normal_case, for this behavior it is assumed that the UpperBitsNotSet (p) predicate evaluates to false. The Normal(stream, MaxBitSize(p)) predicate returns true for both behaviors.

Finally, the behavior invalid_bit_sequence describes the function's behavior if the bit stream is not long enough to write a complete AdhesionFactor object into. This behavior is distinguished from the other behaviors by the evaluation of the predicate Normal (stream, MaxBitSize(p)). Notice that the evaluation of UpperBitsNotSet(p) might be false, too. Like in the value_too_big behavior the function ends without encoding any bits into the stream. Therefore the assigns clause is \nothing. The result clause states that the function's return value equals -1.

```
/ * @
   requires valid_stream:
                             Writable(stream);
   requires stream_invariant: Invariant(stream, MaxBitSize(p));
   requires valid_package:
                               \valid_read(p);
   requires invariant:
                              Invariant(p);
   requires separation:
                              Separated(stream, p);
   assigns stream->bitpos;
   assigns stream->addr[0..(stream->size-1)];
   behavior normal_case:
     assumes Normal{Pre}(stream, MaxBitSize(p)) && UpperBitsNotSet{Pre}(p)
     assigns stream->bitpos;
     assigns stream->addr[0..(stream->size-1)];
     ensures result:
                          \ \ == 1;
      ensures increment: stream->bitpos == \old(stream->bitpos) + BitSize(
         p);
                         Unchanged{Here,Old} (stream, 0, \old(stream->
      ensures left:
         bitpos));
                          EqualBits(stream, \old(stream->bitpos), p);
     ensures middle:
      ensures right:
                          Unchanged{Here,Old}(stream, stream->bitpos, 8 *
         stream->size);
   behavior values too big:
      assumes Normal {Pre} (stream, MaxBitSize(p)) && !UpperBitsNotSet {Pre} (p
     assigns \nothing;
     ensures result:
                             \result == -2;
   behavior invalid_bit_sequence:
     assumes !Normal{Pre}(stream, MaxBitSize(p));
     assigns \nothing;
      ensures result:
                           \result == -1;
    complete behaviors;
   disjoint behaviors;
int AdhesionFactor_EncodeBit(const AdhesionFactor* p, Bitstream* stream);
```

Listing 3.9. Contract for EncodeBit function of AdhesionFactor

3.2 Formal specification of other packets

After examining the definition of the predicates for AdhesionFactor and the formal specifications of the functions AdhesionFactor_EncodeBit and AdhesionFactor_DecodeBit from Section 3.1, the predicates for all other packets and their function's specifications look very familiar. In fact the only difference of the predicates lies in the different sets of sub predicates which are used and depends on the different sets of member variables for the different packets. The overloading feature of ACSL for predicates and logic functions is used to create completely generic formal specifications for the EncodeBit and DecodeBit functions. This means, that for any one of the 47 generated packets the function contracts look just like the ones for AdhesionFactor.



4 The bit stream layer

In this chapter, we describe the intermediate abstractions levels the packet level (Chapter 3) relies on. First, we discuss in Section 4.1 a level where operation arguments typically include a pointer to the C structure Bitstream, which encapsulates bitstream data and all related administration information (see Listing 4.1).

Listing 4.1. Details for the Bitstream data structure

In this chapter, we present a level still working on bit sequences, but with an operation typically having one argument for every bitstream data or administration input. Chapter 5 finally presents lower level implementation details.

4.1 The Bitstream abstraction

The operations on packet data structures were implemented by operations on a **struct** Bitstream* argument. The latter are described in this section.

The operation Bitstream_Read(stream, length) reads the next length bits from the bitstream stream, and returns them as a uint64_t value. Its formal ACSL specification is shown in Listing 4.2. It requires stream

- to point to a valid memory area (requirement property "valid"),
- to adhere to its data type invariant (property "invariant"), and
- not to be exhausted (property "normal").

```
requires valid: Readable(stream);
requires invariant: Invariant(stream, length);
requires normal: Normal(stream, length);

assigns stream->bitpos;

ensures pos: stream->bitpos == \old(stream->bitpos) + length;
ensures changed: EqualBits(stream, \old(stream->bitpos), stream->
    bitpos, \result);
ensures upper: UpperBitsNotSet(\result, length);
ensures size: stream->size == \old(stream->size);
ensures unchanged: Unchanged{Here,Old}(stream, 0, 8 * stream->size);
*/
uint64_t Bitstream_Read(Bitstream* stream, uint32_t length);
```

Listing 4.2. Reading from a bitstream

It is allowed to—and usually in fact will—modify the current bit position within stream, but it has to leave all other memory unchanged (expressed by the "assigns" clause). After completion of the operation,

- the current bit position has been increased accordingly (postcondition property "pos"),
- the return value equals, bit by bit, the stream between the current bit position on entry and that on exit (property "changed"),
- in particular, all but the length least significant bits³ of the return value are zero (property "upper"),
- stream's total size remains unaffected (property "size"), and
- so do all of its content bits (property "unchanged").

The formal definitions of the ACSL predicates used in Bitstream_Read's contract are given in Listing 4.3; they build upon the internal details of the Bitstream data structure shown in Listing 4.1.

³ Bit positions are counted differently in Frama-C and in the openETCS project, cf. Figure 5.1 in Section 5.2. In this report, we preferably used the terms "least" and "most significant bit(s)" to designate a (range of) bit position(s) independent of the coordinate system.

```
/ * @
 predicate
    Readable{L} (Bitstream* stream) = \valid(stream) &&
      \valid_read(stream->addr + (0..stream->size-1));
 predicate
   Writeable{L} (Bitstream* stream) = \valid(stream) &&
      \valid(stream->addr + (0..stream->size-1));
 predicate
    Invariant{L} (Bitstream* stream, integer length) =
      \separated(stream, stream->addr + (0..stream->size-1)) &&
     Invariant(stream->size, stream->bitpos, length);
 predicate
   Normal{L} (Bitstream* stream, integer length) =
     Normal(stream->size, stream->bitpos, length);
 predicate
   Unchanged(A,B)(Bitstream* stream, integer first, integer last) =
      \forall integer i; first <= i < last ==>
        (\at(Bit8Array(stream->addr, i),A) <==>
         \at(Bit8Array(stream->addr, i),B));
 predicate
    EqualBits{A} (Bitstream* stream, integer first, integer last, uint64_t
       value) =
     EqualBits(A)(stream->addr, first, last, value);
```

Listing 4.3. ACSL predicates used in bitstream layer contracts

- Predicate Readable requires that a stream's data area is complete accessible for read.
- Similarly, predicate Writeable requires that it is accessible for update.
- Predicate Invariant requires that a **struct** Bitstream's data area doesn't overlap with the **struct** itself, and that some further, lower-level invariant holds (see Section 4.3 below, in particular Listing 4.7).
 - In a similar way, predicate Normal and EqualBits is reduced to a lower-level predicate of the same name, respectively.⁴
- A clause Normal (size, bitpos, length) requires bitpos to be such that at least length more bits are available beyond it in a stream of byte-size size.⁵
- A clause Unchanged {A, B} (stream, first, last) succeeds if, and only if, all data bits [first...last) of stream agree in memory state A and B. For example, it is used with A and B instantiated to Frama-C's reserved keyword "Here" and "Old", denoting the memory state after and before operation completion and entry, respectively; cf. Listing 4.6.
- A clause EqualBits (addr, first, last, value) requires bits [first...last) in the byte array at addr to coincide with the corresponding least significant bits of value, cf. Figure 4.1.

⁴Frama-C allows for predicate overloading.

⁵ We tacitly assume that each stream has a multiple of 8 bits available.

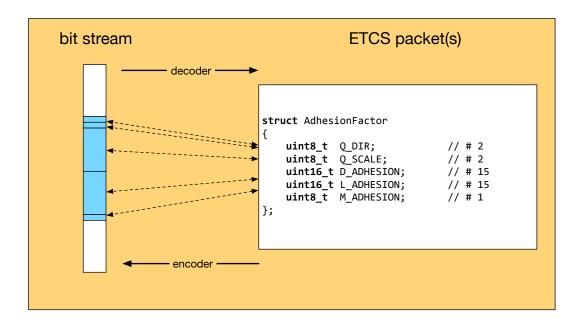


Figure 4.1. Bit coincidences required by EqualBits

4.2 Auxiliary Bitstream functions

As a kind of constructor for type Bitstream, we provide the operation Bitstream_Init, shown with its contract in Listing 4.4.

```
requires valid:
                      Writeable(stream);
  requires bit_size: 8 * size <= UINT32_MAX;</pre>
  requires valid_pos: bitpos <= 8 * size;</pre>
  requires separated: \separated(addr + (0..size-1), stream);
  assigns stream->addr, stream->size, stream->bitpos;
  ensures
          addr:
                      stream->addr == addr;
                      stream->size == size;
  ensures
           size:
                      stream->bitpos == bitpos;
  ensures
          bitpos:
  ensures invariant: Invariant(stream, 0);
void Bitstream_Init(Bitstream* stream, uint8_t* addr, uint32_t size,
   uint32_t bitpos);
```

Listing 4.4. Setting-up a bitstream

Moreover, we provide a test for exhaustion of a Bitstream, shown in Listing 4.5.

```
/*@
  requires valid:    Readable(stream);
  requires invariant: Invariant(stream, length);

  assigns \nothing;

  ensures result: \result <==> Normal(stream, length);
*/
int Bitstream_Normal(const Bitstream* stream, uint32_t length);
```

Listing 4.5. Testing a bitstream for exhaustion

4.3 Writing bit sequences

In this section, we describe the operations that handle plain bit sequences. They are used to implement the Bitstream operations for Section 4.1.

Listing 4.6 shows contract of the Bitstream_Write operation, and moreover exemplifies its implementation.

```
/ * @
  requires valid: Writeable(stream);
 requires invariant: Invariant(stream, length);
 requires normal: Normal(stream, length);
 requires upper:
                     UpperBitsNotSet(value, length);
 assigns stream->addr[0..stream->size - 1];
  assigns stream->bitpos;
 ensures pos:
                      stream->bitpos == \old(stream->bitpos) + length;
  ensures changed:
                      EqualBits(stream, \old(stream->bitpos), stream->
     bitpos, value);
  ensures unchanged: Unchanged{Here,Old}(stream, 0, \old(stream->bitpos))
     ;
  ensures unchanged: Unchanged{Here,Old}(stream, stream->bitpos, 8 *
    stream->size);
                      stream->size == \old(stream->size);
 ensures size:
void Bitstream_Write(Bitstream* stream, uint32_t length, uint64_t value)
    Bitwalker_Write(stream->addr, stream->size, stream->bitpos, length,
       value);
    //@ assert EqualBits(stream, stream->bitpos, stream->bitpos + length,
       value);
    stream->bitpos += length;
    //@ assert EqualBits(stream, \at(stream->bitpos,Pre), stream->bitpos,
       value);
}
```

Listing 4.6. Writing to a bitstream

Most parts of the contract are quite similar to that of <code>Bitstream_Read</code> in Listing 4.2. Differences are the following:

• We require that the value to be written fits into the specified length, i.e. its unused most significant bits are zero (requirement property "upper").

• The operation is allowed to change the contents of the bitstream (first assigns clause) in addition to the streams current bit position (second assigns clause), but no other memory locations.

• Since we couldn't specify in the assigns clauses which bits exactly are allowed to be modified, we give the details in two ensures clauses named "unchanged": All bits before the stream's bitpos on operation entry, and after its bitpos on exit, must remain unchanged.

The implementation just employs the lower-level operation <code>Bitwalker_Write</code> to write the bits, and appropriately updates the <code>stream</code>'s <code>bitpos</code>. Two assertions were needed to help the provers establishing that <code>value</code>'s bits are actually written to <code>stream</code>'s data array by <code>Bitwalker_Write</code>, and that they aren't subsequently destroyed by the increment of <code>bitpos</code>

The formal definitions of the used ACSL predicates are given in Listing 4.7. Again, the tacit assumption that the array contains sensible data up to its very last bit is used in predicate Normal.

Listing 4.7. ACSL predicates used in bit sequence layer contracts

Listing 4.8 shows the contract, and the implementation, of the Bitwalker_Write operation.

```
/ * @
                     Writeable(addr, size);
 requires valid:
 requires invariant: Invariant(size, bitpos, length);
 requires normal: Normal(size, bitpos, length);
                     UpperBitsNotSet(value, length);
 requires upper:
 assigns addr[0..size-1];
 ensures left:
                       Unchanged{Here,Old} (addr, 0, bitpos);
  ensures middle:
                       EqualBits (addr, bitpos, bitpos + length, value);
                       Unchanged{Here,Old} (addr, bitpos + length, 8 * size)
 ensures right:
void Bitwalker_Write(uint8_t* addr, uint32_t size, uint32_t bitpos,
   uint32_t length, uint64_t value);
{
      loop invariant bound:
                              bitpos <= i <= bitpos + length;
      loop invariant left:
                              Unchanged{Here, Pre} (addr, 0, bitpos);
      loop invariant middle: EqualBits(addr, bitpos, i, value, length);
                             Unchanged{Here, Pre} (addr, i, 8 * size);
      loop invariant right:
      loop assigns i, addr[0..size-1];
      loop variant bitpos + length - i;
    */
    for (uint32_t i = bitpos; i < bitpos + length; ++i)</pre>
        int flag = TestBit64(value, (64 - length) + (i - bitpos));
        SetBit8Array(addr, size, i, flag);
}
```

Listing 4.8. Writing a bit sequence

4.4 Reading bit sequences

The following peculiarities are observed when the former is compared to Bitwalker_Read's contract in Listing 4.9.

```
/*@
                       Readable(addr, size);
 requires valid:
 requires invariant: Invariant(size, bitpos, length);
                       Normal(size, bitpos, length);
 requires normal:
 assigns
           \nothing;
 ensures
                        EqualBits(addr, bitpos, bitpos + length, \result);
           equal:
 ensures
           upper:
                        UpperBitsNotSet(\result, length);
uint64_t Bitwalker_Read(uint8_t* addr, uint32_t size, uint32_t bitpos,
   uint32_t length);
```

Listing 4.9. Reading a bit sequence

- We require that the value to be written fits into the specific length, i.e. all but its length least significant bits are zero (requirement property "upper").
- The operation may modify the data array at addr, but nothing else.

• Again, we give the details of which data bits exactly are allowed to be changed in two ensures clauses, named "left" and "right", and requiring all bits before bitpos and after bitpos+length to remain unchanged, respectively.

In the implementation, which is shown here as an example, we used the straight-forward algorithm that takes a bit from value and places it into the addr array, bit by bit. In order for the provers to establish that algorithm's correctness, we had to provide a total of six ACSL clauses about the loop:

- The loop variable, i, always ranges in the interval [bitpos...bitpos+length]—loop invariant property "bound". Note that the highest value is actually taken, viz. on exit of the loop body in the last iteration, subsequently causing the loop to terminate.
- The bits before bitpos, and after bitpos+length remain as they were on operation entry—invariant property "left" and "right", respectively.
- In the ith iteration, the bits [bitpos...bitpos+i) agree with the least significant i bits of value—invariant property "middle".
- The loop code is allowed to modify the variable i, and the whole array at addr, but nothing else—loop assigns clause.
- The value of the integer expression bitpos+length-i is non-negative throughout the whole loop execution, but is decreased in every iteration loop variant clause. Therefore, the loop is guaranteed to terminate eventually.

The operations we have discussed here are based on operations to write and to read a single bit. The details of the latter, as well as of the predicates used in their contracts, are given in Chapter 5.

4.5 Verification of the Bitstream abstraction

Critics of the formal software verification approach often argue that verifying an operation against its formal specification results in little or no increase of trustworthiness when

- the specification, including all auxiliary definitions etc., is as complex as the operation's implementation, or/and
- the specification essentially duplicates the implemented algorithm in a different (such as functional rather than imperative) language.

Both criteria may be seen to be met by our Bitwalker case study.

However, since the operations we dealt with essentially implement a communication protocol, there is a very simple "high-level" property that should be satisfied, viz. that a "send" operation is inverse to a "receive" operation. This property can be stated formally in a very brief and understandable way. It ensures, in a mathematical context, that both operations implement bijective mappings, that is, in an engineering sense, that the communication channel neither looses, nor subjoins information. In fact, we have achieved to formally prove this property.

More particularly, in our setting, we could show that the operations <code>Bitstream_Read</code> and <code>Bitstream_Write</code> are inverse to each other. To this end, we set up two fictitious <code>C</code> procedures realizing the composition of both operations in the two possible orders.

Listing 4.10 shows the procedure for the scenario "use Bitstream_Write to write a value to a stream, then immediately read it back using Bitstream_Read".

```
/ * @
   requires valid:
                       Writeable(stream);
   requires invariant: Invariant(stream, length);
   requires normal: Normal(stream, length);
   requires upper:
                       UpperBitsNotSet(value, length);
   assigns stream->addr[0..stream->size-1];
   assigns stream->bitpos;
   ensures equality:
                       \result == value;
uint64_t Bitstream_WriteThenRead(Bitstream* stream, uint32_t length,
   uint64 t v>
{
   //@ ghost uint32_t old_pos = stream->bitpos;
   Bitstream_Write(stream, length, value);
    //@ assert equal: EqualBits(stream, old_pos, old_pos+length, value);
    / * @
       assigns stream->bitpos;
       ensures reset: stream->bitpos == \at(stream->bitpos,Pre);
    stream->bitpos -= length;
   uint64_t result = Bitstream_Read(stream, length);
    //@ ghost uint32_t new_pos = stream->bitpos;
    //@ assert equal_result: EqualBits(stream, old_pos, new_pos, result);
    //@ assert equal_value: EqualBits(stream, old_pos, new_pos, value);
    /*@ assert aux:
                            \forall integer k; old_pos <= k < new_pos ==>
                               \let j = new_pos - 1 - k;
                               (BitTest (value,
                                               j) <==> BitTest(result, j))
    //@ assert left:
                            EqualBits64 (result, value, 64-length, 64);
    //@ assert compare:
                            EqualBits64(result, value, 0, 64);
   return result;
```

Listing 4.10. Verifying the scenario "write, then read"

The procedure's body code is straightforward; after <code>Bitstream_Write</code>, we have to seek back to the original bit position, before calling <code>Bitstream_Read</code>". We could show that the read value always equals the written one, provided

- the stream is accessible for both read and update (requirement property "valid"),
- it satisfies its type invariant (property "invariant"; cf. Listing 4.3 and 4.7),
- the stream's current bit position is sufficiently small such that all value bits still fit into the stream (property"normal"), and

• the most significant value bits that are not written are all zero (property"upper").

This ensures that the bitstream communication channel doesn't loose information—every value we write into it can completely be restored.

Vice versa, we could also show that the channel doesn't transmit more information than is needed to fulfill its task. Listing 4.11 shows the procedure for the scenario "use Bitstream_Read to read a value from a stream, then immediately write it back using Bitstream_Write".

```
/ * @
    requires valid:
                         Writeable(stream);
    requires invariant: Invariant(stream, length);
                        Normal(stream, length);
    requires normal:
    assigns stream->addr[0..stream->size-1];
    assigns stream->bitpos;
    ensures unchanged: Unchanged{Here,Old}(stream, 0, 8 * stream->size);
*/
void Bitstream_ReadThenWrite(Bitstream* stream, uint32_t length)
    //@ ghost uint32_t old_pos = stream->bitpos;
    uint64_t value = Bitstream_Read(stream, length);
    //@ assert equal: EqualBits(stream, old_pos, old_pos+length, value);
    stream->bitpos -= length;
    //@ assert stream->bitpos == old_pos;
    Bitstream_Write(stream, length, value);
    //@ assert unchanged: Unchanged{Here,Pre}(stream, old_pos, stream->
       bitpos);
}
```

Listing 4.11. Verifying the scenario "read, then write"

We were able show that this leaves the whole stream unchanged, provided the first three requirement properties from <code>Bitstream_WriteThenRead</code> are met. As an example for a channel transmitting redundant information, consider a bitstream implementation with <code>Bitstream_Write</code> storing each byte twice in succession and <code>Bitstream_Read</code> ignoring every second byte. Such a stream doesn't meet our property, since, starting from a stream with non-agreeing adjacent bytes, there is no way to reproduce it by a "read, then write" scenario.

5 Low-level bitstream operations

In this chapter, we describe the implementation of the low-level bitstream operations. They were used to implement the bit sequence abstraction level, cf. Chapter 4. Since a write operation moves bits from a uint64_t value into an array of uint8_t values, and a read operations moved them the other way round, we need bit operations on both data types. They are given in Subsection 5.1.1 for an array of uint8_t, in Subsection 5.1.2 for a single uint8_t, and in Subsection 5.1.3 for single uint64_t.

5.1 Reading and writing individual bits

5.1.1 8 bit arrays

In this section, we discuss the operations for read and write of a single bit from/into a byte array.

The operation TestBit8Array (addr, size, pos) returns the posth bit within the array at addr of byte-size size.⁶ Its contract and its implementation is shown in Listing 5.1. See Listing 5.8 for the definition of the predicate Bit8Array. The array bits are counted starting with the most significant one of the first byte, cf. Figure 5.1 below. A call to TestBit8 (bytevalue, bitadr) returns the bitadrth bit within bytevalue, this operation is discussed in Subsection 5.1.2 below.

```
/*@
    requires valid: \valid_read(addr + (0..size-1));
    requires size: 8 * size <= UINT32_MAX;
    requires pos: pos < 8 * size;

    assigns \nothing;

    ensures result: \result != 0 <==> Bit8Array(addr, pos);

*/
static inline int TestBit8Array(uint8_t* addr, uint32_t size, uint32_t pos
)
{
    return TestBit8(addr[pos / 8], pos % 8);
}
```

Listing 5.1. Reading a bit of an uint8_t array

Similarly, the operation SetBit8Array(addr, size, pos, flag) sets the posth bit within the array at addr of byte-size size to flag. Its contract is shown in Listing 5.2. It requires

- the whole array to be accessible for update (requirement property "valid"),
- each possible bit position in the array to fit into a uint32_t (property "size"), and
- the given pos to be a valid bit position in the array (property "pos").

⁶ This parameter isn't actually used in the code, but merely in the contract.

The assigns clause allows the operation to change the contents of the array, but no other memory locations. On completion, the operation shall guarantee

- that the value of flag⁷ is actually stored at the designated bit position (postcondition property "middle"; the call Bit8Array () succeeds if, and only if, the posth bit within the byte array at addr is set, cf. Listing 5.8 in Section 5.2), and
- that all other bits remain unchanged (properties "left", "right").

Two fairly sophisticated hints had to be provided as assertions in the body in order for the provers to establish the contract's post-conditions.

```
/ * @
   requires valid: \valid(addr + (0..size-1));
                    8 * size <= UINT32_MAX;
   requires size:
                    pos < 8 * size;
   requires pos:
   assigns addr[0..size-1];
   ensures left: Unchanged{Here,Old}(addr, 0, pos);
   ensures middle: Bit8Array(addr, pos) <==> (flag != 0);
   ensures right: Unchanged{Here,Old} (addr, pos + 1, 8 * size);
static inline void SetBit8Array(uint8_t* addr, uint32_t size, uint32_t pos,
    int flag)
{
   uint32_t i = pos / 8u;
   uint32_t k = pos % 8u;
    addr[i] = SetBit8(addr[i], k, flag);
    // The following assertion claims that in byte with index "pos/8"
    // the bits with indices different from "k" do not change
    / * @
     assert bits_in_byte:
        \forall integer j; (0 <= j < 8 && j != k) ==>
        (Bit8(addr[pos/8], j) <==> \at(Bit8(addr[pos/8], j), Pre));
    */
    // The following assertion claims that in every byte
    // with an index that is different from "pos/8" no bit is changed.
       assert other_bytes:
        \forall integer 1, j; (0 <= 1 < size && 1 != pos/8 && 0 <= j <
           8) ==>
          (Bit8(addr[1], j) <==> \at(Bit8(addr[1], j), Pre));
}
```

Listing 5.2. Writing a bit of an uint8_t array

5.1.2 8 bits

The operation TestBit8 (value, pos) returns the posth bit of value. Its contract is shown in Listing 5.3.

 $^{^{7}}$ Any non-zero flag value is treated like 1. This is ensured by the contract of the called operation SetBit8, cf. Subsection 5.1.2.

```
/*@
    requires pre: pos < 8;

    assigns \nothing;

    ensures pos: \result != 0 <==> Bit8(value, pos);

*/
static inline int TestBit8(uint8_t value, uint32_t pos)
{
    uint8_t mask = ((uint8_t) 1) << (7u - pos);
    uint8_t flag = value & mask;

    return flag != 0;
}</pre>
```

Listing 5.3. Reading a bit of uint8_t

- The value of pos must not exceed 7 (requirement property "pre"),
- no memory may be modified (assigns), and
- the result is non-zero if, and only if, the specified bit is set (postcondition property "pos"; the call Bit8 (value, pos) succeeds if, and only if, the posth of the byte value is set, cf. Listing 5.8 in Section 5.2).

The shown implementation additionally guarantees that the result is zero or one, which is not specified in the contract since this property isn't needed. Returning just flag rather than flag!=0u would satisfy the contract also, and would be slightly faster.

Dual to TestBit8, the operation SetBit8 (value, pos, flag) returns value, with the posth bit set to flag. Its contract is shown in Listing 5.4.

- Again, the value of pos mustn't exceed 7 (requirement property "pre"),
- no memory may be modified (assigns clause),
- the return value coincides with value, except possibly at pos (postcondition properties "left" and "right"; a call EqualBits8 (x, y, first, last) succeeds if, and only if, the uint8_t values x and y agree on all bits in range [first...last), cf. also Listing 5.10 in Section 5.2), and
- flag is written to the appropriate bit of value (property "pos").

The implementation branches on the value of flag, and clears or sets the appropriate bit in the usual way. Note that both our contract and our implementation enable us to set a bit by supplying a flag value of e.g. 2, whereas the code "mask=flag<< (7-pos); return (value&~mask) mask|" does not.

```
requires pre: pos < 8;
assigns \nothing;
ensures left: EqualBits8(\result, value, 0, pos);
ensures pos: Bit8(\result, pos) <==> (flag != 0);
ensures right: EqualBits8(\result, value, pos + 1, 8);
*/
static inline uint8_t SetBit8(uint8_t value, uint32_t pos, int flag)
{
    uint8_t mask = ((uint8_t) 1) << (7u - pos);
    return (flag == 0) ? (value & ~mask) : (value | mask);
}</pre>
```

Listing 5.4. Writing a bit of uint8_t

5.1.3 64 bits

The operations to read and write a bit of a uint64_t are closely similar to those working on a uint8_t. They are shown in Listing 5.5 and 5.6 without repeating the comments given in Subsection 5.1.2 for the 8 bit version. See Listing 5.8 for the employed ACSL predicates.

```
/*@
    requires pre: pos < 64;

    assigns \nothing;

    ensures set_bit: \result != 0 <==> Bit64(value, pos);

*/
int TestBit64(uint64_t value, uint32_t pos)
{
    uint64_t mask = ((uint64_t) 1) << (63u - pos);
    uint64_t flag = value & mask;

    return flag != 0u;
}</pre>
```

Listing 5.5. Reading a bit of uint 64_t

Listing 5.6 shows the operation SetBit64. Note that it has a redundant postcondition, viz. property "upper", which guarantees that the leading zeros in value are kept in the result, up to, but excluding position pos. This property was needed to enable the provers to verify code that uses SetBit64.

Listing 5.6. Writing a bit of uint 64_t

The operation UpperBitsNotSet64 (value, length) succeeds, i.e. returns a non-zero value, if, and only if, all bits of value except the least significant length ones are zero. It is used in the implementation of packet writing functions like AdhesionFactor_EncodeBit (see Section 3.1.6) to check that no non-zero bits from the packet structure (like struct AdhesionFactor) are ignored due to space limitations in the bitstream.

```
/*@
    requires pre: length <= 64;
    assigns \nothing;
    ensures not_set: \result <==> UpperBitsNotSet(value, length);
*/
int UpperBitsNotSet64(uint64_t value, uint32_t length);
```

Listing 5.7. Test that upper bits are not set

5.2 Formalization of bit operations in Frama-C

The definition of predicate Bit8 is shown in Listing 5.8. It relies on the Frama-C library predicate BitTest, performing a coordinate transformation to fit Frama-C's notion of bit positions with the OpenETCS project's notion, cf. Figure 5.1.

```
/*@
   predicate Bit8{A} (uint8_t v, integer n) = BitTest(v, 7 - n);

predicate Bit64{A} (uint64_t v, integer n) = BitTest(v, 63 - n);

predicate Bit8Array{A} (uint8_t* a, integer n) = Bit8(a[n / 8],n % 8);
*/
```

Listing 5.8. Definition of bit test predicates

— Insert drawing —

Figure 5.1. Bit coordinates in Frama-C and in the OpenETCS project

The predicate UpperBitsNotSet (value, length) succeeds if, and only if, all but possibly the least significant length bits of value are zero. Its definition is shown in Listing 5.9.

```
predicate
    UpperBitsNotSet{A}(integer value, integer length) =
    \forall integer i; length <= i ==> !BitTest(value, i);
```

Listing 5.9. Definition of the low-level predicate UpperBitsNotSet

Listing 5.10 shows the predicate EqualBits64 that was used in the 64-bit operations' contracts. The call EqualBits64 (x,y,first,last) succeeds if, and only if, the uint64_t values x and y agree on all bits in the range from first to last). The predicate EqualBits8, used in Subsection 5.1.2, is defined in similar way; its definition need not be shown here.

```
/*@
predicate
    EqualBits64{A}(uint64_t x, uint64_t y, integer first, integer last) =
    \forall integer i; 64 - last <= i < 64 - first
    ==> (BitTest(x, i) <==> BitTest(y, i));
```

Listing 5.10. Definition of the low-level predicate EqualBits 64

In order for the provers to find all low-level validation proofs, we needed to supply three redundant properties about EqualBits64 and UpperBitsNotSet; they are shown in Listing 5.11. Axiom equal_bits64_0 states that two uint64_t values must be equal, if they agree on all 64 bit positions. Axiom upper_bits_less_than states that in a nonnegative number less than 2^n all bits are zero, except for possibly the least significant n ones. The necessity of these extra axioms might indicate an incompleteness in Frama-C's actual bit-operator theory; this is currently investigated. Axiom equal_bits64_1 is just a (relaxed) rephrasing of the definition in Listing 5.10, using a different index scheme. It is necessary due to the provers' weakness in applying index transformations.

Listing 5.11. ACSL axioms used in 64-bit contracts

For a nonnegative integer v, the predicate BitTest(v,n) succeeds if, and only if, the n^{th} bit is set in the binary representation of v, i.e. iff the truncating integer division of v by 2^n yields an odd number. This predicate comes with the standard library of the Frama-C system, however, without any detailed documentation. Its declaration is shown in Listing 5.12.

```
/*@
    predicate    BitTest(integer v, integer n);
*/
```

Listing 5.12. The Frama-C library predicate BitTest



6 Formal verification

6.1 Bit stream and lower-level bit operations

component	vcs			individual provers			
component	all	proven	(%)	qed	alt-ergo	cvc4	z3
bit stream	58	58	100	19	0	0	39
bit stream (inverse)	58	58	100	33	2	1	22
lower-level bit ops	126	126	100	55	0	1	70

Table 6.1. verfication result for bit stream and lower-level bit operations

6.2 Verification of packets without N_ITER

PacketID	VCs		Individual Provers				
TacketiD	All	Proven	(%)	Qed	Alt- Ergo	CVC4	Z3
16	436	436	100	318	0	1	117
39	483	483	100	346	0	1	136
42	559	543	97	399	0	1	143
45	389	389	100	290	0	1	98
57	483	483	100	346	0	1	136
65	624	624	100	430	0	1	193
66	389	389	100	290	0	1	98
71	530	530	100	374	0	1	155
72	999	957	95	671	0	1	285
76	958	938	97	644	9	1	284
90	474	465	98	341	0	1	123

Table 6.2. Verfication result for TrackToTrain packets without ${\tt N_ITER}$ part 1

PacketID	VCs		I	ndividu	al Provei	.s	
1 acketiD	All	Proven	(%)	Qed	Alt- Ergo	CVC4	Z3
131	624	624	100	430	0	1	193
132	389	389	100	290	0	1	98
133	718	718	100	486	0	1	231
134	624	624	100	430	0	1	193
136	474	465	98	341	0	1	123
137	389	389	100	290	0	1	98
138	483	483	100	346	0	1	136
139	483	483	100	346	0	1	136
140	389	389	100	290	0	1	98
141	436	436	100	318	0	1	117
254	342	342	100	262	0	1	79

Table 6.3. Verfication result for TrackToTrain packets without N $_$ ITER part 2

PacketID	VCs			Individual Provers			
Tacketib	All	Proven	(%)	Qed	Alt- Ergo	CVC4	Z3
1	973	948	97	649	6	2	291
4	342	342	100	262	0	1	79
9	342	342	100	262	0	1	79
44	389	389	100	290	0	1	98

Table 6.4. Verfication result for TrainToTrack packets without ${\tt N_ITER}$

PacketID	VCs			Individual Provers			rs.
PacketiD	All	Proven	(%)	Qed	Alt- Ergo	CVC4	Z3
255	239	239	100	192	0	1	46

Table 6.5. Verfication result for BothWays packets without N_{\perp} ITER

PacketID	Packetname	N_ITER	Conditionals
3	NationalValues	dynamic	conditional
5	Linking	dynamic	conditional
12	Level1MovementAuthority	dynamic	-
15	Level23MovementAuthority	dynamic	-
16	RepositioningInformation	static	-
21	GradientProfile	dynamic	-
27	InternationalStaticSpeedProfile	dynamic	-
39	TrackConditionChangeOfTractionPower	static	-
41	LevelTransitionOrder	dynamic	conditional
42	SessionManagement	static	conditional
45	RadioNetworkRegistration	static	-
46	ConditionalLevelTransitionOrder	dynamic	conditional
49	ListOfBalisesForSHArea	dynamic	conditional
51	AxleLoadSpeedProfile	dynamic	-
57	MovementAuthorityRequestParameters	static	-
58	PositionReportParameters	dynamic	-
63	ListOfBalisesInSRAuthority	dynamic	conditional
65	TemporarySpeedRestriction	static	-
66	TemporarySpeedRestrictionRevocation	static	-
67	TrackConditionBigMetalMasses	dynamic	-
68	TrackCondition	dynamic	conditional

Table 6.6. TrackToTrain packets part 1

PacketID	Packetname	N_ITER	Conditionals
70	RouteSuitabilityData	dynamic	conditional
71	AdhesionFactor	static	-
72	PacketForSendingPlainTextMessages	static	conditional
76	PacketForSendingFixedTextMessages	static	conditional
79	GeographicalPositionInformation	dynamic	conditional
80	ModeProfile	dynamic	-
90	TrackAheadFreeUpToLevel23TransitionLocation	static	conditional
131	RBCTransitionOrder	static	-
132	DangerForShuntingInformation	static	-
133	RadioInfillAreaInformation	static	-
134	EOLMPacket	static	-
136	InfillLocationReference	static	conditional
137	StopIfInStaffResponsible	static	-
138	ReversingAreaInformation	static	-
139	ReversingSupervisionInformation	static	-
140	TrainRunningNumberFromRBC	static	-
141	DefaultGradientForTemporarySpeedRestriction	static	-
254	DefaultBaliseLoopOrRIUInformation	static	-

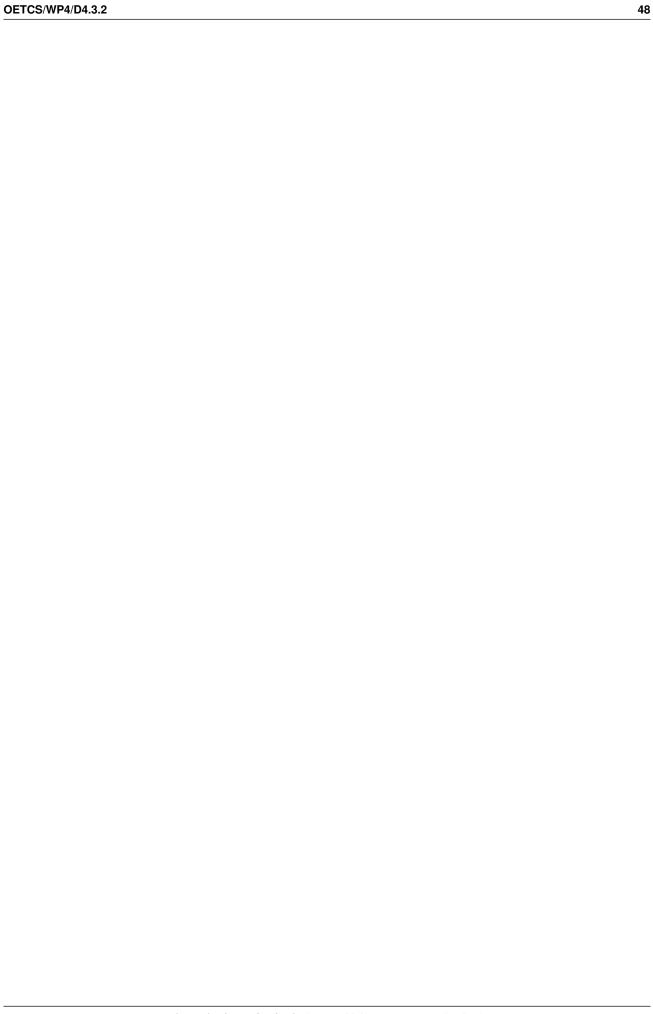
Table 6.7. TrackToTrain packets part 2

PacketID	Packetname	N_ITER	Conditionals
1	PositionReportBasedOnTwoBaliseGroups	static	conditional
3	OnboardTelephoneNumbers	dynamic	-
4	ErrorReporting	static	-
9	Level23TransitionInformation	static	-
11	ValidatedTrainData	dynamic	-
44	DataUsedByApplicationsOutsideTheERTMSETCSSystem	static	-

Table 6.8. TrainToTrack packets

PacketID	Packetname	N_ITER	Conditionals
255	EndOfInformation	static	-

Table 6.9. BothWays packets



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