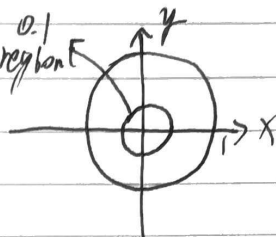


2. (a) The unit circle is



Consider  $P(\text{having an accurate estimator } x) = 1 - P(\text{all } \|x_i\| > 0.1)$

If we have a  $x_i$  that's  $\|x_i\| \leq 1$ , then

$$P(\|x_i\| \leq 0.1) = \frac{P(0, 0.1)}{P(0, 1)} = \frac{(0.1)^d}{1} \text{ with } d = \text{dimension.}$$

$$\text{So } P(x \text{ is accurate}) = 1 - P(\text{all } \|x_i\| > 0.1) \\ = 1 - (1 - (0.1)^d)^n$$

(b) If dimension increases,  $(1 - (0.1)^d)^n \rightarrow 1$ , then  $P(x \text{ is accurate}) \rightarrow 0$

To bound the  $P$  of accurate  $x$ , we need

$$1 - (1 - (0.1)^d)^n > c \text{ with } c \text{ being some constant.}$$

$$(1 - (0.1)^d)^n < 1 - c$$

$$\log_{1 - (0.1)^d} (1 - c) \\ n > \log_{1 - (0.1)^d} (1 - c)$$