

# Privacy Preserving Group Ranking

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Semester Project

June 2016

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## 0.1 Motivation

Group ranking is a process used to find a the best candidate from a group. The process involves a party called the *initiator* and others parties called *participants*. The initiator usually has a vector of preferences on some attributes and participants have vectors of values, each corresponding to the attributes sought after by the initiator. At the end of the process, one or more candidates with attributes best matching the initiator preferences will be selected. This has many applications such as online marketing, personal interest matching, job recruitment and selecting candidates for medical experiment.

However, this process is more and more used in virtual environment in today's society and as a consequence privacy concerns emerge. A trivial approach to Group ranking would leak private informations about all the candidates even if some of the will not be picked at the end of the process. As an example-online forms are used to carry such ranking. A naive implementation of the ranking would require that the candidates provide private information of the by answering questions on the form). Since some group ranking imply ranking candidates on based on sensitive information, such implementation of group ranking poses a problem to privacy.

Given the necessity of group ranking in a wide range of real world's application and the need to preserve candidates privacy, is there a way to perform group ranking while preserving privacy of all the parties? How do we prevent candidates to learn informations about other candidates? How do we prevent candidates to learn information about the initiator and thus cheating in the process? This is the subject of this paper.

In this report we present and explain a protocol

that performs privacy preserving group ranking and we give a Java implementation of the protocol.



## 0.2 The protocol

In this section we give a detailed explanation of the protocol.

### 0.2.1 Framework

The protocol is executed cooperatively by n+1 parties. An initiator plus n Participant P0, P1... Pn. The protocol assumes that the participants are willing to accept the initiator invitation and to submit their private information if selected eventually. The questionnaire given by the initiator is represented as a m-dimensional vector. The initiator holds a m-dimensional vector  $\mathbf{v}0$  indicating the preferred values of each of the question of the questionnaire, another m-dimensional vector represents the weight associated to each questions. Furthermore, the questionnaire comprises: "Equal" questions meaning that the initiator is looking for a specific attribute. "Greater than" question means that the initiator is looking for values exceeding some threshold. We assume without loss of generality that the first t questions are "greater than" questions. Finally the answer of each candidates is also represented by a m-dimensional Vector. A complete description of the protocol framework is given below:

generates a group  $\mathbb{G}_q \leftarrow \mathcal{G}(1^K)$ , picks a generator g and publishes them.  $P_0$ also publishes a vector of attribute names and an integer k, where  $1 \le k \le n$ . Private Input:  $\mathbf{v}_0$  and  $\mathbf{w}$  from  $P_0$ ;  $\mathbf{v}_j$  from participant  $P_j$ ,  $1 \le j \le n$ . Secure gain computation:

- 1)  $P_0$  chooses a random h-bit integer  $\rho$ .
- 2) Every participant  $P_j$  generates  $\mathbf{w}_j' = [\mathbf{v}\mathbf{g}_j^\mathsf{T}, (\mathbf{v}\mathbf{e}_j * \mathbf{v}\mathbf{e}_j)^\mathsf{T}, \mathbf{v}\mathbf{e}_j^\mathsf{T}, 1]^\mathsf{T}$ . As in the dot product protocol of Sec. IV-A,  $P_j$  computes QX,  $\mathbf{c}'$ ,  $\mathbf{g}$  and sends
- 3) Upon receiving  $(Q_j X_j, \mathbf{c}'_j, \mathbf{g}_j)$  from a participant  $P_j$ ,  $P_0$  chooses  $\rho_j \leftarrow_R \{0, 1, \cdots, \rho\}$  and constructs  $\mathbf{v}'_j = [\rho \mathbf{w} \mathbf{g}^\mathsf{T}, -\rho \mathbf{w} \mathbf{e}^\mathsf{T}, 2\rho (\mathbf{w} \mathbf{e} * \mathbf{v} \mathbf{e}_0)^\mathsf{T}, \rho_j]^\mathsf{T}$ .  $P_0$  computes  $a_j = z_j \mathbf{c}'_j \cdot \mathbf{v}'_j$ ,  $h_j = \mathbf{g}^\mathsf{T}_j \cdot \mathbf{v}'_j$  and sends them back to  $P_j$ .
- 4) Upon receiving  $(a_j, h_j)$  from  $P_0$ ,  $P_j$  calculates  $\beta_j = (a_j + h_j)$  $R_2/R_3)/b$  and converts it to an unsigned integer (see Sec. III-A).

#### Unlinkable gain comparison:

- ∀1 ≤ j ≤ n, P<sub>j</sub> picks private key x<sub>j</sub> ←<sub>R</sub> Z<sub>q</sub> and publishes y<sub>j</sub> = g<sup>x<sub>j</sub></sup>.  $P_j$  proves the knowledge of  $x_j$  to the rest of parties (Sec. IV-E).
- 6) Each participant  $P_j$  represents her  $\beta_j$  in binary bits  $[\beta_j]_B$   $[\beta_j^l, \beta_j^{l-1}, \cdots, \beta_j^1]$ , encrypts and publishes them as  $E(\beta_j)_B$  $[E(\beta_i^l), \cdots, E(\beta_i^1)]$ . Here, the encryption is done using joint key y = $\prod_{j=1}^{n} y_{j}.$
- 7) Each participant  $P_j$  gets encrypted data  $\{E(\beta_i)_B\}_{i=1,i\neq j}^n$  from others. For each encrypted data  $E(\beta_i)_B$ ,  $P_j$  does following calculation for  $1 \le t \le l$ :
  - $E(\gamma_i^t) = E(\beta_j^t + \beta_i^t 2\beta_j^t \beta_i^t)$ , where  $\gamma_i^t = \beta_j^t \oplus \beta_i^t$ ;  $E(\omega_i^t) = E((l-t+1) \sum_{v=t+1}^l (\gamma_i^t \gamma_i^v) \gamma_i^t)$ ;

  - E(τ<sub>i</sub><sup>t</sup>) = E(ω<sub>i</sub><sup>t</sup> + β<sub>i</sub><sup>t</sup>).
  - $P_j$  sends all the ciphertexts  $\mathcal{E}_j = \{e : e \in E(\tau_i) \land 1 \leq i \leq n \land i \neq j\}$ to  $P_1$ , where  $E(\tau_i) = \{E(\tau_i^t)\}_{t=1}^l$ .
- After receiving the ciphertext sets from all the rest parties, P<sub>1</sub> constructs a vector  $V = [\mathcal{E}_1, \mathcal{E}_2, \cdots, \mathcal{E}_n]$ . Starting at  $P_1$ , each participant  $P_i$  applies following steps to each element  $\mathcal{E}_i$   $(i \neq j)$  in V:
  - For each ciphertext  $(c_t, c'_t) \in \mathcal{E}_i$ , replaces  $c_t$  by  $\tilde{c}_t = c_t/(c'_t)^{x_j}$ . Picks  $r \leftarrow_R \mathbb{Z}_q$  and updates the ciphertext with  $((\tilde{c}_t)^r, (c'_t)^r)$ .
  - Permutes the ciphertexts in each set E<sub>i</sub>.
  - $P_j$  then sends the permuted vector V to  $P_{j+1}$ . If  $P_j$  is the last one,  $P_n$ , she sends the element of the vector back to the corresponding participant.

#### Ranking Submission:

Upon receiving the final result  $\tilde{E}_j$  from  $P_n$ , participant  $P_j$   $(1 \le j \le n)$  decrypts each element ciphertext (c,c') by using  $g^m = c/c'^{x_j}$  and checks  $g^m = 1$ . Let d be the number of zeroes and then the ranking of  $P_j$  is  $d_j = d + 1$ . If  $d_j \leq k$ ,  $P_j$  submits  $\mathbf{v}_j$  to  $P_0$  as well as the ranking.

Figure 1: Framework

Explanation of the protocol In our implementation, the same group will be used for every iteration of the protocol. The implementation uses a prime-order group of at least 1024 bits, thus the computation of discrete log is made difficult.

```
package lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto;
3 import java.math.BigInteger;
4 import java.security.SecureRandom;
6 public class GroupGenerator {
      private static int minBitLength;
10
      private static int certainty;
11
      private static BigInteger ONE = BigInteger.ONE;
12
      private static BigInteger generator, prime, group;
13
      private static SecureRandom secureRandom;
14
15
      public GroupGenerator(int minBitLength, int certainty,
      Secure Random\ ,\ boolean\ length Check)\,\{
           if (minBitLength < 1024 && lengthCheck )
17
                   throw new IllegalArgumentException ("Prime
18
      should have at least 512 bits");
           this.minBitLength = minBitLength;
           this.certainty = certainty;
20
           this.secureRandom = secureRandom;
21
           getSafePrime();
22
23
      }
24
25
26
27
      private static void getSafePrime(){
28
29
           BigInteger a;
30
           do {
31
               a = new BigInteger (minBitLength, secureRandom);
32
33
               a = a.add(ONE);
34
35
               group = new BigInteger(minBitLength, certainty,
36
      secureRandom);
37
               prime = a.multiply(group).add(ONE);
38
           while(!prime.isProbablePrime(certainty));
40
41
42
43
```

```
boolean isGen;
44
45
           do{
                isGen = true;
46
                generator = new BigInteger(prime.bitLength(),
47
      secureRandom);
               generator = generator.mod(prime.subtract(BigInteger.
48
      ONE)).add(BigInteger.ONE);
               generator = generator.modPow(a, prime);
49
                if (generator.equals (ONE)) {
50
                    isGen = false;
51
           while (!(isGen && !generator.equals(BigInteger.ZERO)));
       }
54
55
56
       public static BigInteger getPrime(){
57
           if (prime == null)
58
59
                getSafePrime();
60
61
62
           return prime;
       public static BigInteger getGenerator(){
           return generator;
65
66
67
       public static BigInteger getGroup(){
68
           return group;
69
70
71
72
73
74 }
```

# $\bigcirc$

Secure gain computation First we define what is the gain in the context of this protocol.

Given a criterion vector  $\mathbf{v0} = [\mathbf{v01}, \mathbf{v02}, ..., \mathbf{v0m}]$  and the weight vector  $\mathbf{w} = [\mathbf{w1}, \mathbf{w2}, ..., \mathbf{wm}]$ . The partial gain value of Pj is  $\mathbf{pj} = \sum_{k=t+1}^{m} wkv_k^j - \sum_{k=1}^{t} (w_k(v_k^j)^2 - 2w_kv_k^jv_k^0)$ . In terms of dot products, the partial gain is given by  $wg \cdot vg_j - we \cdot (ve_j * ve_j + 2(we * ve_0) \cdot ve_j ve_j ve_j ve_j$  and vector is an element-wise multiplication of two vectors. veo is equal to part of the criterion vector and vector v

Steps 1 through 4 are implemented by the classes: Owner.java for the initiator.

```
package lasecbachelorprject.epfl.ch.privacypreservinghousing.user;
```

```
3 import java.math.BigInteger;
4 import java.security.SecureRandom;
6 import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto.SecureDotProductParty;
7 import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      helpers. Poll;
9 import static java.lang.Math.ceil;
10 import static java.lang.Math.log;
import static java.lang.System.arraycopy;
12
13
  public class Owner {
14
      //TODO: Normal users with inheritance
      public SecureDotProductParty me;
      private BigInteger rho;
17
      private int h;
18
      private BigInteger[] criterionVector;
19
      public Poll myPoll;
20
21
22
23
      private BigInteger[] myAttVector; // 10 for test
24
      private BigInteger[] myWeightVector;
25
      private BigInteger[] wPrimeVector;
26
      public int 1;
27
      private int k = 2; //for now
28
29
      private int t = 5; // for now
30
      private SecureRandom random;
31
      private final int greaterLength;
      private final int equalLength;
32
33
      public Owner(BigInteger criterionEqualVector [], BigInteger[]
34
       criterionGreaterVector, BigInteger[] weightEqualVector,
      BigInteger[] weightGreaterVector){
           greaterLength = criterionGreaterVector.length;
35
           equalLength = criterionEqualVector.length;
36
37
38
           1 = (int) ceil(log(equalLength + criterionGreaterVector.
      length)) +
                   criterionEqualVector[0].bitLength() +
39
                   2*weightEqualVector[0].bitLength() + 2;
          random = new SecureRandom();
41
42
          do{
43
               h = random.nextInt() \% 20;
44
          \} while (h \le 0);
45
          //TODO: Decomment following line
46
47
          rho = (new BigInteger(h, random)).abs();
48
49
          generateOwnerVprime(criterionEqualVector,
      weightGreaterVector , weightEqualVector ) ;
```

```
51
          me = new SecureDotProductParty(rho);
          me.setMyvector(wPrimeVector);
54
      }
56
57
      private void generateOwnerVprime(BigInteger[]
58
      criterionEqVector, BigInteger[] weightEqualVector, BigInteger
      [] weightGreaterVector) {
           /*Vector of size gr + 2 *eq*/
59
           wPrimeVector = new BigInteger[greaterLength + 2*
60
      equalLength];
61
62
           /*[vgT,..]*/
           arraycopy (weightGreaterVector, 0, wPrimeVector, 0,
63
      greaterLength);
64
           BigInteger v[] = new BigInteger[equalLength];
65
66
           /* [vgT, (ve*ve)T, ...]*/
           for (int i = 0; i < equalLength; i++) {
               v[i] = weightEqualVector[i].negate();
69
           arraycopy(v,0,wPrimeVector,greaterLength,equalLength);
70
           for (int i = 0; i < equalLength; i++) {
72
               v[i] = weightEqualVector[i].multiply(
      criterionEqVector[i]);
               v[i] = v[i].add(v[i]);
75
76
           arraycopy (v, 0, wPrimeVector, greaterLength+equalLength,
      equalLength);
           for (int i = 0; i < wPrimeVector.length; i++) {
77
               wPrimeVector[i] = wPrimeVector[i].multiply(rho);
78
           }
79
80
           myAttVector = new BigInteger[wPrimeVector.length];
81
           for (int i = 0; i < myAttVector.length; i++) {
82
               myAttVector[i] = wPrimeVector[i];
83
84
       }
       public void initiatePoll(int Participants){
89
           myPoll = new Poll(Participants);
90
91
      }
92
93
94
       public BigInteger[] getMyAttVector() {
95
96
           return myAttVector.clone();
```

```
98
99
100
101
102 }
```

Participant.java for participants.

```
package lasecbachelorprject.epfl.ch.privacypreservinghousing.
      user;
2
3
4 import java.math.BigInteger;
5 import java.security.SecureRandom;
6 import java.util.ArrayList;
7 import java.util.HashMap;
8 import java.util.List;
9 import java.util.Map;
10
  import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      Activities . Application;
{\tt 12} \ import \ lase cbackelor prject. epfl. ch. privacy preserving housing.
      crypto. ElGamal;
import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto.EncryptedBinaryComparator;
14 import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto.SecureDotProductParty;
  import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto.ZeroKnowledgeProver;
  import\ lase cbachelor prject. epfl. ch. privacy preserving housing.
      crypto. ZeroKnowledgeVerifier;
 import lasecbachelorprject.epfl.ch.privacypreservinghousing.
      helpers.DataBase;
18
19 import static lasecbachelorprject.epfl.ch.
      privacy preserving housing \ . \ crypto \ . \ El Gamal \ . \ homomorphic Encryption
20 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.ElGamal.
      multHomomorphicEncryption;
21 import static lasecbachelorprject.epfl.ch.
      privacy preserving housing.\ crypto.\ Encrypted Binary Comparator.
      createBinaryArray;
22 import static lasecbachelorprject.epfl.ch.
      privacy preserving housing\ .\ crypto\ .\ Encrypted Binary Comparator\ .
      finalDecryption;
23 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.SecureDotProductParty.
      copyBigIntArrayToIntArray;
24
  public class Participant extends Person implements User {
26
27
      private final BigInteger prime;
28
      private final BigInteger generator;
```

```
private final int k;
31
       public SecureDotProductParty secureDotProduct;
       public BigInteger[] wPrimeVector;
       private BigInteger privateKey;
33
       private BigInteger publicKey;
34
       public ZeroKnowledgeProver prover;
35
       public ZeroKnowledgeVerifier verifier;
36
       private SecureRandom random;
37
       private BigInteger group;
38
       int replyEqSize;
39
40
       int replyGrSize;
41
       private BigInteger gain;
       private BigInteger[][] cypher;
42
43
       private int myCandidateNumber;
44
       private static Map<Integer , BigInteger[][] > othersGain;
       \begin{array}{lll} \textbf{private} & \textbf{static} & \textbf{List} < \textbf{BigInteger} \ [] \ [] > & \textbf{encryptedComparisonList} \ ; \end{array}
45
       private List<List<BigInteger[][]>> list;
46
       private int 1;
47
       private EncryptedBinaryComparator comparisonTool =
48
      EncryptedBinaryComparator.getGainComparisonTool();
49
       private BigInteger commonKey;
       private List < BigInteger[][] > finalComp;
       private int ranking;
53
       public Participant(BigInteger replyGr[], BigInteger[]
      replyEq,int l, int k) {
           replyEqSize = replyEq.length;
           replyGrSize = replyGr.length;
56
           wPrimeVector = new BigInteger[replyGrSize + 2 *
      replyEqSize];
           generateWPrimeVector(replyGr, replyEq);
           secureDotProduct = new SecureDotProductParty();
           secureDotProduct.setMyvector(wPrimeVector);
60
           group = Application.group;
61
           prime = Application.prime;
62
           generator = Application.generator;
63
           random = new SecureRandom();
64
65
           prover = new ZeroKnowledgeProver(prime, group, generator
66
      );
           verifier = new ZeroKnowledgeVerifier(prime, group,
67
      generator);
           othersGain = new HashMap<>();
           encryptedComparisonList = new ArrayList <>();
           this.l = l;
70
           this.k = k;
       }
72
73
       private void generateWPrimeVector(BigInteger replyGr[],
74
      BigInteger[] replyEq) {
           copyBigIntArrayToIntArray(replyGr, 0, wPrimeVector, 0,
75
      replyGrSize);
```

```
BigInteger [] v = new BigInteger [replyEqSize];
78
           for (int i = 0; i < replyEqSize; i++) {
79
                v[i] = replyEq[i].pow(2);
80
81
           copyBigIntArrayToIntArray(v, 0, wPrimeVector,
82
       replyGrSize, replyEqSize);
           copyBigIntArrayToIntArray(replyEq, 0, wPrimeVector,
83
       replyEqSize + replyEqSize, replyEqSize);
84
85
       public BigInteger[] getReplyVector() {
86
           return wPrimeVector;
87
88
89
90
       public void convertGain(int l) {
91
           BigInteger two = BigInteger.ONE.add(BigInteger.ONE);
92
           gain = secureDotProduct.getBeta().add(two.pow(1));
93
           wPrimeVector = createBinaryArray(gain, l);
94
       public void generatePrivateKey() {
           privateKey = (new BigInteger(prime.bitLength(), random))
       .mod(prime);
           publicKey = generator.modPow(privateKey, prime);
99
           DataBase.getDataBase().publishElGamalPublicKey(this,
100
       publicKey);
           prover.setX(privateKey);
101
       }
102
103
104
       public void setKeyToVerify(BigInteger key) {
105
           verifier.setY(key);
106
107
108
109
       public void encryptWithCommonkey() {
110
           ElGamal.setCommonKey(DataBase.getEncryptionKey());
111
           cypher = ElGamal.encryptMany(wPrimeVector);
112
113
       }
114
115
       public void setMyCandidateNumber(int number) {
117
           myCandidateNumber = number;
118
119
120
       public void sendEncryptedComparisonToDB() {
121
           DataBase.pushComparisonVector(this, comparisonTool.
       getEncryptedComparisons());
123
       public void getEpsilonVector(List<List<BigInteger[][]>> list
```

```
126
           this.list = comparisonTool.chainedDecryption(list,
       myCandidateNumber, privateKey, prime, group);
127
128
129
       public void sendBackDecryptedListToDB() {
130
           DataBase.pushPartialListDecryption(list);
132
133
134
       public void participantGain(Integer participantIndex,
       BigInteger [][] gain) {
           othersGain.put(participantIndex, gain);
136
137
138
       public void compareWithParticipants() {
139
           //List of encrypted bit by bit comparisons
140
           encryptedComparisonList = new ArrayList <>();
141
           //Procedure for candidate I
142
143
           for (Integer index : othersGain.keySet()) {
                //Computation of the gama's factors
                List < BigInteger[] > gamas = new ArrayList <>(l);
146
                //table of beta's
147
                BigInteger[][] betaI = othersGain.get(index);
148
                BigInteger[] tmp;
149
                BigInteger[] tmp2;
150
                for (int t = 0; t < 1; t++) {
                    tmp = homomorphicEncryption(betaI[t], cypher[t])
153
                    tmp2 = multHomomorphicEncryption(betaI[t],
       wPrimeVector[t].multiply(BigInteger.valueOf(-2)));
                    gamas.add(t, homomorphicEncryption(tmp, tmp2));
154
                /*
156
                * Optimisation begin with t = 1 so singe loop
                * Pull the creation outside the loops
158
159
                BigInteger[] val; //(l -t +1)
161
                BigInteger[][] sum = new BigInteger[1][2];
                BigInteger [][] \ negGamaT = new \ BigInteger [1][2];
162
                BigInteger[][] omegas = new BigInteger[1][2];
163
                BigInteger[][] taus = new BigInteger[1][2];
164
165
                for (int t = 0; t < 1; t++) {
                    val = ElGamal.encrypt(BigInteger.valueOf(l - t))
166
                    tmp = ElGamal.getNegativeciphers(gamas.get(t));
167
                    negGamaT[t] = multHomomorphicEncryption(tmp,
168
       BigInteger.valueOf(l - t));
                    sum[t] = homomorphicEncryption(gamas.subList(t +
169
        1, 1));
170
                    omegas[t] = homomorphicEncryption(val, sum[t],
      negGamaT[t]);// E(l-t+1 + sum of (gamav - gmai))
```

```
taus[t] = homomorphicEncryption(omegas[t], betaI
       [t]);
172
                 encryptedComparisonList.add(taus);
173
174
            DataBase.pushComparisonVector(this,
175
       encryptedComparisonList);
176
177
178
179
        public void receiveFinalComp(List<BigInteger[][] > comp) {
181
182
            this.finalComp = comp;
183
184
        }
185
        private void computeSelfRanking(){
186
            ranking = finalDecryption(finalComp);
187
188
        private void rankingSubmission(){
            if (ranking \ll k)
                 DataBase.\,submitsResults\,(\,this\,\,,ranking\,\,,\,\,wPrimeVector\,)\,;
193
        }
194
195
196
```

SecureDotProductParty.java is used to implement the secure dot product protocol proposed by Ioanids and used in this protocol

```
{\tt 1} \ package \ lase cbackelor prject.epfl.ch.privacy preserving housing. \\
      crypto;
4 import java.math.BigInteger;
5 import java.security.SecureRandom;
6
7
   * Class that a represent parties in secure dot product protocol
8
   */
9
10
public class SecureDotProductParty
12
      private BigInteger [][] Q;
13
      private BigInteger
14
                             [][] X;
      private BigInteger
                            factors [];
15
      private BigInteger
                            qTimesX [][];
16
      private BigInteger
                            [] cPrime;
      private BigInteger
18
19
      private int dDimension;
20
      private SecureRandom secureRandom;
```

```
private int sDimension;
22
23
24
       private BigInteger b;
       private BigInteger [] c;
25
       private int rThRow;
26
       private BigInteger R1;
27
       private BigInteger
                           R2;
28
       private BigInteger
                          R3;
29
30
       private BigInteger [] y;
31
32
       private BigInteger
33
       private BigInteger
34
       private BigInteger
                            h;
35
       private BigInteger
                            rho;
36
       private BigInteger
                            rhoMax;
                            beta;
37
       private BigInteger
38
       public BigInteger [] getPrimeVector() {
39
           return primeVector.clone();
40
41
42
       private BigInteger [] primeVector;
43
45
       public BigInteger dotProduct;
       public BigInteger gain;
46
47
       //TODO: Copy the values so that the vector can't be modified
48
       in the outside
       public SecureDotProductParty(BigInteger rho){
49
50
           secureRandom = new SecureRandom();
51
           this.rhoMax = new BigInteger(String.valueOf(rho));
54
       }
       public SecureDotProductParty(){
56
           secureRandom = new SecureRandom();
57
58
59
60
61
       //initiate The dot product for myVector
       public void initiateDotProduct(){
62
63
65
           //TODO : Constant matrix dimension
66
           sDimension = 100; //1 + secureRandom.nextInt(10);
67
           rThRow = secureRandom.nextInt(sDimension);
68
69
           //Genrate Q and compute b. TODO: Skip rth row in the
70
      for an assigne later
71
          Q = new BigInteger [sDimension][sDimension];
72
           for (int i = 0; i < sDimension; i++) {
               for (int j = 0; j < sDimension; j++) {
```

```
//TODO: Correct BOUnd
74
                         Q[i][j] = BigInteger.ONE;//new BigInteger(
75
       String . valueOf (secureRandom . nextInt(100));
76
            }
78
79
80
            //TODO: b!!!
81
            b = BigInteger.ZERO;
82
83
            for (int i = 0; i < sDimension; i++) {
                b = b.add(Q[i][rThRow]);//safeAdd(b,Q[i][rThRow]);
84
85
86
            //Generate X
           X = new BigInteger [sDimension][dDimension];
87
88
            for (int i = 0; i < sDimension; i++) {
89
                for (int j = 0; j < dDimension; j++) {
90
                     if ( i != rThRow) {
91
                         //TODO: Ccrrect next INT LIMIT
92
93
                         X[i][j] = BigInteger.valueOf(secureRandom.
       nextInt(100)+1);
                     else {
                         X[i][j] = primeVector[j];
96
97
98
99
100
                }
101
102
103
104
            //scalar factor to compute the "c" vector.
105
            // factors[i] = sum(Qji).
106
            factors = new BigInteger [sDimension];
107
108
            factors [rThRow] = BigInteger.ZERO;
109
            for (int i = 0; i < sDimension; i++) {
110
                factors [i] = BigInteger.ZERO;
111
                if ( i != rThRow) {
112
                     for (int j = 0; j < sDimension; j++) {
113
114
                         factors[i] = factors[i].add(Q[j][i]);
115
116
                }
117
            }
118
119
            //Generate c
120
            c = new BigInteger [dDimension];
121
122
123
            for (int i = 0; i < dDimension; i++) {
124
                c[i] = BigInteger.ZERO;
                for (int j = 0; j < sDimension; j++) {
```

```
c[i] = c[i] \cdot add(X[j][i] \cdot multiply(factors[j]));
126
                }
127
            }
128
129
            //Generate f
130
            BigInteger [] f = new BigInteger [dDimension];
            for (int i = 0; i < dDimension; i++) {
132
                f[i] = BigInteger.valueOf(secureRandom.nextInt(100)
      + 1);
134
135
            //TODO: Change the 1
136
           R1 = BigInteger.valueOf(secureRandom.nextInt(100) +1);
137
           R2 = BigInteger.valueOf(secureRandom.nextInt(100) +1);
138
139
           R3 = BigInteger.valueOf(secureRandom.nextInt(100) +1);
140
            //Compute Q*X
141
            qTimesX = new BigInteger [sDimension][dDimension];
142
            for (int i = 0; i < sDimension; i++) {
143
                for (int j = 0; j < dDimension; j++) {
144
                    qTimesX[i][j] = BigInteger.ZERO;
145
                    for (int k = 0; k < sDimension; k++) {
146
                         qTimesX[i][j] = qTimesX[i][j].add(Q[i][k].
       multiply(X[k][j]));
148
149
            }
151
            //c '
            cPrime = new BigInteger [dDimension];
153
            BigInteger R1TimesR2 = R1.multiply(R2);
154
155
            for (int i = 0; i < dDimension; i++) {
                cPrime[i] = c[i].add(R1TimesR2.multiply(f[i]));
156
157
158
            BigInteger
                        R1TimesR3 = R1. multiply (R3);
159
160
            //Generate g
161
            g = new BigInteger [dDimension];
162
            for (int i = 0; i < dDimension; i++) {
163
                g[i] = R1TimesR3.multiply(f[i]);
164
165
166
       }
167
168
169
       public void sendInitialDataToOtherParty(
       SecureDotProductParty party){
            party.receiveQTimesX(qTimesX,cPrime,g);
173
174
175
       public void sendAH(SecureDotProductParty party){
           party.receiveAH(a, h);
```

```
178
       private void receiveAH(BigInteger a, BigInteger h) {
179
180
           this.a = a;
           this.h = h;
181
           beta = (a.add((h.multiply(R2)).divide(R3))).divide(b);
182
       }
183
184
       public void sendBeta(SecureDotProductParty party){
185
           party.receiveBeta(beta);
186
187
       public void sendAlpha(SecureDotProductParty party){
189
190
           party.receiveAlpha(rho);
191
       private void receiveBeta(BigInteger beta) {
192
           this.beta = beta;
193
194
195
       public BigInteger getBeta(){
196
                return beta;
       public BigInteger getAlpha(){return rho;}
201
202
       private void receiveQTimesX(BigInteger [][] qTimesX,
203
       BigInteger [] cPrime, BigInteger [] g) {
          /* if (this.cPrime.length != primeVector.length || this.g.
204
       length != primeVector.length){
                throw new IllegalArgumentException ("The dot product
205
      can't be computed because of dimensions mismatch. Expected
       vector size: "+
206
                                                      myvector.length
      + " received cPrime Size: " + (this.cPrime.length - 1) +"
       received g size: "+ (this.g.length -1));
           }*/
207
           this.qTimesX = qTimesX;
208
           this.cPrime = cPrime;
209
           this.g = g;
210
211
           BigInteger [] rhoVector;
212
213
           rho = new BigInteger (rhoMax. bitLength () −1, secureRandom
214
      );
           rhoVector = primeVector.clone();
215
           rhoVector [rhoVector.length - 1] = rho;
216
217
           /*double[][] qTimesX = (double[][]) get("QtimesX");
218
           double [] cPrime = (double[]) get("cPrime");
219
           double [] g = (double []) get("G");*/
220
221
           y = computeY(qTimesX, rhoVector);
           z = vectorElementsSum(y);
           a = z.subtract (normalDotProduct (cPrime, rhoVector));
```

```
h = normalDotProduct(g, rhoVector);
225
            /*this.put("Y", y);
226
            this.put("Z", z);
this.put("A", a);
227
228
            this.put("H",h);*/
229
230
       }
231
232
233
234
235
       private BigInteger [] computeY(BigInteger [][] qTimesX,
236
       BigInteger [] myVectorPrime) {
237
            int dim = qTimesX.length;
            BigInteger y[] = new BigInteger [dim];
238
            for (int i = 0; i < dim; i++) {
239
                y[i] = normalDotProduct(qTimesX[i], myVectorPrime);
240
241
242
            return y;
243
       public static BigInteger normalDotProduct(BigInteger [] v1,
        BigInteger [] v2 ){
            BigInteger res = BigInteger.ZERO;
246
            for (int i = 0; i < v1.length; i++) {
247
                res = res.add(v1[i].multiply(v2[i]));
248
            }
249
250
            return res;
251
       }
252
253
       private static BigInteger [] vectorAddition(BigInteger [] v1
       , BigInteger v2[]) {
254
            int \dim = v1.length;
            BigInteger [] v = new BigInteger [dim];
255
            for (int i = 0; i < \dim; i++) {
256
                v[i] = v1[i].add(v2[i]);
257
258
            return v;
259
       }
260
261
       public static BigInteger[] vectorsElemMult(BigInteger[] v1,
262
       BigInteger [] v2) {
            BigInteger[] res = new BigInteger[v1.length];
            for (int i = 0; i < v1.length; i++) {
264
                res[i] = v1[i].multiply(v2[i]);
265
266
            return res;
267
       }
268
269
270
       public static BigInteger[] vectorsElemMultMod(BigInteger[]
       v1, BigInteger [] v2, BigInteger prime) {
            BigInteger[] res = new BigInteger[v1.length];
            for (int i = 0; i < v1.length; i++) {
```

```
res[i] = (v1[i]. multiply(v2[i])).mod(prime);
            }
274
275
            return res;
       }
276
277
278
279
280
       public static BigInteger vectorElementsSum(BigInteger [] v1
281
       ) {
            int \dim = v1.length;
            BigInteger res = BigInteger.ZERO;
            for (int i = 0; i < dim; i++) {
284
285
                res = res.add(v1[i]);
286
            }
287
            return res;
       }
288
289
       public static BigInteger [] vectorScalarMult(BigInteger []
290
       vector, BigInteger scalar) {
            BigInteger[] res = new BigInteger[vector.length];
            for (int i = 0; i < vector.length; i++) {
                res[i] = vector[i].multiply(scalar);
295
            return res;
       }
296
297
       public static BigInteger[] vectorScalarMultMod(BigInteger[]
298
       vector, BigInteger scalar, BigInteger prime) {
            BigInteger [] res = new BigInteger [vector.length];
299
            for (int i = 0; i < vector.length; i++) {
300
301
                res[i] = (vector[i]. multiply(scalar)).mod(prime);
            }
302
            return res;
303
       }
304
305
       public static BigInteger[] vectorsElemExpo(BigInteger[] v,
306
       int expo) {
            for (int i = 0; i < v.length; i++) {
307
                v[i] = v[i].pow(expo);
308
309
            return v;
310
       }
311
312
       public static BigInteger[] vectorsElemModExpo(BigInteger[] v
313
        BigInteger expo, BigInteger prime){
            BigInteger[] res = new BigInteger[v.length];
314
            for (int i = 0; i < v.length; i++) {
315
                res[i] = v[i].modPow(expo, prime);
316
317
            return res;
318
319
       }
320
```

```
323
       public void setAlphaMax(BigInteger alphaMax) {
324
            this.rhoMax = alphaMax;
325
326
327
328
       private void receiveAlpha(BigInteger alpha) {
329
            this.rho = alpha;
330
331
332
333
       public void getPartialGain(int 1) {
334
            BigInteger two = BigInteger.ONE.add(BigInteger.ONE);
335
336
            gain = (new BigInteger(String.valueOf(dotProduct))).add(
       two.pow(l-1);
337
338
       public void setMyvector(BigInteger [] vector) {
339
            dDimension = vector.length + 1;
340
341
            primeVector = new BigInteger [dDimension];
            System.\,arraycopy\,(\,vector\,\,,0\,\,,primeVector\,\,,0\,\,,vector\,\,.\,length\,)\,\,;
342
            primeVector [vector.length] = BigInteger.ONE;
343
344
       }
345
346
       public static void copyBigIntArrayToIntArray(BigInteger[]
347
       src, int srcPos, BigInteger [] des, int destPos, int number
348
            for (int i = srcPos, j= destPos; i <srcPos+number; i++,
       j++) {
                des[j] = src[i];
            }
350
351
352
       public BigInteger
                            getRhoForParticipant() {
353
            return rho;
354
355
356
357
358
       static final long safeAdd(long left, long right) {
            if (right > 0 ? left > Long.MAX_VALUE - right
                     : left < Long.MIN_VALUE - right) {
360
                throw new ArithmeticException("Longoverflow");
361
362
            return left + right;
363
       }
364
365
       static final long safeSubtract(long left, long right) {
366
            if (right > 0 ? left < Long.MIN_VALUE + right
367
                     : left > Long.MAX_VALUE + right) {
368
                throw new ArithmeticException("Longoverflow");
369
370
            }
            return left - right;
```

```
373
       static final long safeMultiply(long left, long right) {
374
           if (right > 0 ? left > Long.MAX_VALUE/right
375
                    || left < Long.MIN_VALUE/right
376
                    : (right < -1 ? left > Long.MIN_VALUE/right
377
                    | left < Long.MAX_VALUE/right
378
                    : right == -1
379
                    && left = Long.MIN_VALUE) ) {
380
                throw new ArithmeticException("Integer overflow");
381
382
           }
            return left * right;
       }
384
385
386
       static final long safeDivide(long left, long right) {
           if ((left = Long.MIN_VALUE) && (right = -1)) {
387
                throw new ArithmeticException("Integer overflow");
388
389
           return left / right;
390
391
392
       static final long safeNegate(long a) {
            if (a == Long.MIN_VALUE) {
                throw new ArithmeticException("Integer overflow");
395
           }
396
           return -a;
397
398
       static final long safeAbs(long a) {
399
            if (a == Integer.MIN_VALUE) {
400
                throw new ArithmeticException("Integer overflow");
401
402
403
            return Math.abs(a);
404
405
406
407
408
```

Unlinkeable Gain comparison NEED TO DESCRIBE PRECISELY UNLINKEABLE!!!! In this phase each participant  $P_i, 1 \leq j \leq n$  blindly compares his gain to others. The gains are converted to binary-array  $\beta$  and each bits is encrypted with a modified version of ElGa cryptosystem beforehand. For the common key y, each participant picks a private key xj, publishes the corresponding public key and proves the knowledge of that key to other participant. The proof of knowledge is done by classes ZeroknowledgeProver.java and ZeroKnowledgeVerifier.java.

```
6 public class ZeroKnowledgeProver {
       private BigInteger x;
       private BigInteger h;
9
       private BigInteger z;
       private BigInteger prime;
11
       private BigInteger group;
       private BigInteger generator;
13
       private SecureRandom secureRandom;
14
15
       public BigInteger r;
16
      //TODO: Group should be the published key
17
18
       public ZeroKnowledgeProver(BigInteger prime, BigInteger
      group, BigInteger generator) {
           this.prime = prime;
19
           this.group = group;
20
           this.generator = generator;
21
           secureRandom = new SecureRandom();
22
23
       public void initiateProof(){
           generateH();
       private void generateH(){
           r = new BigInteger(group.bitLength(), secureRandom);
29
           r = r . mod(group);
30
           h = generator.modPow(r, prime);
31
32
33
34
       public void sendH(ZeroKnowledgeVerifier verifier){
35
           verifier.receiveH(h);
36
37
       private void computeZ(BigInteger c){
38
           z = (r.add(x.multiply(c))).mod(group);
39
40
41
       public BigInteger sendZ(BigInteger c){
42
           computeZ(c);
43
44
           return z;
45
46
       public void receiveC(BigInteger c) {
48
           computeZ(c);
49
50
51
       public void setX(BigInteger x){
           this.x = x;
54
55 }
```

```
crypto;
2
3 import java.math.BigInteger;
4 import java.security.SecureRandom;
6 public class ZeroKnowledgeVerifier {
       private BigInteger y;
       private BigInteger h;
       private BigInteger z;
       private BigInteger prime, group, generator, qMinusOne;
10
11
       private BigInteger c;
       private SecureRandom secureRandom;
12
13
14
       public ZeroKnowledgeVerifier (BigInteger prime, BigInteger
      group, BigInteger generator) {
           this.prime = prime;
           this.generator = generator;
           this.group = group;
17
           this.qMinusOne = group.subtract(BigInteger.ONE);
18
           secureRandom = new SecureRandom();
19
20
21
22
       public BigInteger sendC(){
           c = new BigInteger(group.bitLength(), secureRandom);
23
           return c = c.mod(group);
24
25
      }
26
27
28
29
30
       public void receiveH(BigInteger h) {
31
           this.h = h;
32
33
       public void receiveZ(BigInteger z) {
34
           t\,h\,i\,s\,\,.\,z\,\,=\,\,z\,\,;
35
36
37
       public void setY(BigInteger y) {
38
           t\,h\,i\,s\,\,.\,y\,\,=\,\,y\,;
39
40
41
42
       public boolean verifyWithZ(BigInteger z, BigInteger sharedC)
43
           BigInteger gPowZ = generator.modPow(z,prime);
44
           BigInteger hTimesYPowC = (h.multiply(y.modPow(sharedC,
45
      prime))).mod(prime);
           return gPowZ.equals(hTimesYPowC);
46
47
48 }
```

The actual comparison is executed at step 7. The comparison on Encrypted bits, using additive homomorphism of the modified ElGamal cryptosystem that we shortly describe here.

Modified Elgamal Group Gq is a prime order multiplicative group for which the DDH problem is hard and g is a generator in Gq. Then, the ModfielGamal cryptosystem is described as: Key generation: a private key is a random element x in Zq and the corresponding public key is  $y = g^x$ . Encryption: a ciphertext of a message M is of form  $E(M)=(g^my^r,g^r)$ , where r R Zq. ¿¿¿DESCRIPTION OF DECRYPTION ¿¿¿SHOW HOMOMORPHIC ADDITIVITY AND MULTIPLICATIVE IF ONE PLAIN TEXT IS KNOW. ¿¿¿SHOW THAT SINCE WE ARE ONLY WORKING WITH 0 and 1 FOR THE GAIN THERE IS NO PROBLEM WITH DECRYPTION

```
1 package lasecbachelorprject.epfl.ch.privacypreservinghousing.
      crypto;
3 import java.math.BigInteger;
4 import java.security.SecureRandom;
5 import java.util.ArrayList;
6 import java.util.Collection;
  import java.util.HashMap;
  import java.util.List;
9 import java.util.Map;
10
  import lasecbachelorprject.epfl.ch.privacypreservinghousing.user
      . Participant;
12
13 public class ElGamal {
14
      private static BigInteger prime, group, generator, privateKey,
16
       myPublicKey;
      private static final BigInteger ONE = BigInteger.ONE;
      private static ElGamal cryptoSystem;
18
      private static SecureRandom secureRandom;
      private static BigInteger commonKey;
20
      //TODO: Remove after test
21
      private static Map<Participant , BigInteger > mySecretKey;
22
      private static Map<Participant , BigInteger > myPukey;
23
24
      //TODO: fix group, generator. Add method for secret key
25
26
      private ElGamal(BigInteger prime, BigInteger group,
27
      BigInteger generator) {
          mySecretKey = new HashMap<>();
28
          myPukey = new HashMap <> ();
           this.prime = prime;
30
           this.group = group;
31
           this.generator = generator;
          secureRandom = new SecureRandom();
```

```
34
35
       public static ElGamal getElGamal (BigInteger prime,
36
      BigInteger group, BigInteger generator) {
           if (cryptoSystem == null){
37
               cryptoSystem = new ElGamal(prime, group, generator);
38
           }
39
           return cryptoSystem;
40
      }
41
42
43
44
       public static BigInteger[] encrypt(BigInteger bit){
45
46
           if(bit == null) {
               throw new IllegalArgumentException ("Message to
47
      encrypt is null");
48
           BigInteger r = new BigInteger (group.bitLength(),
49
      secureRandom);
           r = r . mod(group);
50
51
           BigInteger gPowMessage = generator.modPow(bit, prime);
52
           BigInteger\ yPowR = commonKey.modPow(r, prime);
           BigInteger[] cipher = new BigInteger[2];
53
           cipher [0] = gPowMessage.multiply(yPowR).mod(prime);
           cipher[1] = generator.modPow(r, prime);
55
           return cipher;
56
57
58
       public static BigInteger[][] encryptMany(BigInteger[] bits){
59
60
           BigInteger[][] res = new BigInteger[bits.length][2];
61
           for (int i = 0; i < bits.length; i++) {
62
               res[i] = encrypt(bits[i]);
           }
63
64
           return res;
65
66
      public static void setPrivateKey(BigInteger privateKey){
67
           if (privateKey == null){
68
               throw new IllegalArgumentException ("Null Argument
69
      to Set
             private key");
70
71
           ElGamal.privateKey = privateKey;
72
           myPublicKey = generator.modPow(privateKey, prime);
75
      public static void setMySKey(Participant p, BigInteger key){
76
           mySecretKey.put(p,key);
77
          myPukey.put(p,generator.modPow(key,prime));
78
79
80
      }
81
82
      public static BigInteger getMyPuKey(Participant p){
          return myPukey.get(p);
```

```
84
85
       public static void setCommonKey(BigInteger commonKey) {
86
           ElGamal.commonKey = commonKey;
87
88
89
90
       public static BigInteger decrypt(BigInteger[] cypher){
91
            if(cypher = null || cypher.length |= 2|| cypher[0] ==
92
       null \mid \mid cypher[1] = null \}
                throw new IllegalArgumentException("null or bad
93
       length cypher");
94
           }
95
            BigInteger msg = (cypher [0]. multiply(cypher [1].modPow(
96
       privateKey.negate(),prime))).mod(prime);
97
            return msg.equals(BigInteger.ONE) ? BigInteger.ZERO :
98
       BigInteger.ONE;
       public static BigInteger decryptMe(Participant p, BigInteger
       [] cypher){
            if(cypher == null || cypher.length != 2|| cypher[0] ==
       null \mid \mid cypher[1] = null \}
                throw new IllegalArgumentException("null or bad
103
       length cypher");
           }
104
            setPrivateKey(mySecretKey.get(p));
            BigInteger msg = (cypher [0]. multiply (cypher [1]. modPow(
106
       privateKey.negate(),prime))).mod(prime);
107
            return msg.equals(BigInteger.ONE) ? BigInteger.ZERO :
108
       BigInteger.ONE;
109
110
112
       public static List<BigInteger> decryptMany(List<BigInteger</pre>
       [] > table) {
114
            ArrayList < BigInteger > res = new ArrayList < > (table.size()
       );
            for (BigInteger[] t: table) {
                res.add(decrypt(t));
117
            return res;
118
       }
119
120
       public static Collection < BigInteger > decryptManyME(
       Participant p, Collection < BigInteger[] > table) {
            ArrayList < BigInteger > res = new ArrayList < > (table.size()
122
       );
            for (BigInteger[] t: table) {
                res.add(decryptMe(p,t));
```

```
126
            return res;
127
128
        public static BigInteger getmyPublicKey(){
129
            return myPublicKey;
130
131
133
        public static BigInteger [] homomorphicEncryption (Collection <
134
       BigInteger[] > ciphers) {
            BigInteger [] res = new BigInteger [] { BigInteger .ONE,
       BigInteger.ONE};
136
            for (BigInteger[] c: ciphers) {
137
                 res = SecureDotProductParty.vectorsElemMultMod(res, c
       , prime);
138
            }
            return res;
139
140
        public static BigInteger[] getNegativeciphers(BigInteger[]
       cypher) {
            return SecureDotProductParty.vectorsElemModExpo(cypher,
       BigInteger.valueOf(Long.parseLong("-1")),prime);
144
145
        public static BigInteger [] homomorphicEncryption (BigInteger
146
       [] c1, BigInteger[] c2){
            return SecureDotProductParty.vectorsElemMultMod(c1,c2,
147
       prime);
148
149
        public static BigInteger [] homomorphicEncryption (BigInteger
150
       []... ciphers){
            BigInteger[] res = new BigInteger []{BigInteger.ONE,
151
       BigInteger.ONE);
            for (BigInteger[] c : ciphers){
152
                 res = homomorphicEncryption(res,c);
153
            return res;
156
        }
        public static BigInteger[] multHomomorphicEncryption(
       BigInteger [] cipher, BigInteger otherWord) {
           {\color{red} \textbf{return}} \hspace{0.2cm} \textbf{SecureDotProductParty.vectorsElemModExpo} \big( \hspace{0.2cm} \textbf{cipher} \hspace{0.2cm},
159
       otherWord, prime);
160
161
        public static BigInteger getPrime(){
162
            return prime;
163
164
165
166
        public static BigInteger getGenerator(){
           return getGenerator();
```

```
168 }
169 public static BigInteger getGroup() {
171 return group;
172 }
173 }
```

The comparison with an other participant's (WLOG  $P_j$ ) gain is done as follow: First stage the participant of concern let say  $P_i$  executes a bit-wise xor with his gain vector  $\beta_i$  gain yielding a new vector  $\gamma$ .

Next stage, the participant generates a new vector  $\omega$  where each elements is computed by the formula  $\omega^t = (l-t+1) - (l-t+1) \cdot \gamma^t + \sum_{v=t+1}^l (\gamma^v)$  Last stage: The last generated vector is  $\tau$  where  $\tau^t = \omega^t + \beta_i^t$  At the end of the process the  $\tau$  vector will have at most one 0 and if it contains on then  $P_i$  has smaller gain than  $P_i$ 

Now we show that this comparison is correct.

**Proof** Let  $a = a_{n-1}...a_1a_0$  and  $b = b_{n-1}...b_1b_0$  be two n bits unsigned numbers in binary form and we want to compare a to b. Let suppose W.L.O.G that the first k-1 most significant bits of a and b are the same,  $0 \le k-1 \le n$ . The  $\gamma$  vector of stage one will have k-1 zeros in the last k-1 elements. This implies that the corresponding values of the  $\omega$  vector will have values of at least 1 so will be the values of the corresponding  $\tau$  vector. The value of the kth element in each vectors depends on the two following cases

Case 1: a is greater than b. In this case  $a^k = 1$  and  $b^k = 0$ . This implies that  $\gamma^k = 1$ . This also means that  $\omega^k = 0$  and  $\tau^t = 0 + a^k k = 1$ .

Case 2: a is smaller than b. We have  $a^k = 0$  and  $b^k = 1$ . This implies that  $\gamma^k = 1$ . This also means that  $\omega^k = 0$  and  $\tau^k = 0 + a^k = 0$ .

Lastly,  $\omega^j \geq 1, j < k$ . This comes form the fact that  $(l-t+1)-(l-t+1)\cdot \gamma^j \geq 0$  and also the sum is at least 1 due to the  $\gamma^k$ . This shows that the comparison method will give at then at most one zero and if a ; b then the comparison will yield one zero and none otherwise.(i.e a  $\geq$  b).

These operation are done with the class EncryptedBinaryComparator.java

```
package lasecbachelorprject.epfl.ch.privacypreservinghousing.
crypto;

import java.math.BigInteger;
import java.security.SecureRandom;
import java.util.ArrayList;
import java.util.Arrays;
import java.util.Collections;
```

```
8 import java.util.HashMap;
9 import java.util.List;
10 import java.util.Map;
11
12 import lasecbachelorprject.epfl.ch.privacypreservinghousing.user
      . Participant;
13
14 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.ElGamal.decrypt;
15 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.ElGamal.decryptMany;
16 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.ElGamal.homomorphicEncryption
17 import static lasecbachelorprject.epfl.ch.
      privacypreservinghousing.crypto.ElGamal.
      multHomomorphicEncryption;
18
19
  public class EncryptedBinaryComparator {
20
21
       private static BigInteger[][] myGain;
22
       private static Map<Integer , BigInteger[][] > othersGain;
23
      private static List < BigInteger [][] > encryptedComparisonList;
      private static BigInteger[] plainGain;
25
      private static BigInteger[] othersPlain;
26
      private static int 1;
27
      private static EncryptedBinaryComparator gainComparisonTool;
28
29
      private static Map<Participant, BigInteger[][] > selfGain;
      private static Map<Participant ,Map<Integer , BigInteger[][]>>
30
       selfOthersGain;
31
      private static Map<Participant, List<BigInteger[][]>>
      selfCryptComp;
      private static Map<Participant, BigInteger[] > selfPlainGain;
32
       public static List<BigInteger[] > gamas;
33
       public static BigInteger[][] betaI;
34
       public static BigInteger[] tmp;
35
       public \ \ \underline{static} \ \ BigInteger[] \ \ tmp2; //(1 \ -t \ +1 \ )
36
       public static BigInteger[] val;
37
       public static BigInteger[][] sum;
38
       public static BigInteger[][] negGamaT;
39
       public static BigInteger[][] omegas;
40
      public static BigInteger[][] taus;
       private EncryptedBinaryComparator(){
43
           selfCryptComp = new HashMap<>();
44
           selfGain = new HashMap <> ();
45
           selfPlainGain = new HashMap<>();
46
           selfOthersGain = new HashMap<>();
47
           othersGain = new HashMap<>();
48
49
      }
50
      public static EncryptedBinaryComparator
      getGainComparisonTool() {
```

```
if(gainComparisonTool = null){
53
               gainComparisonTool = new EncryptedBinaryComparator()
      ;
           }
54
           return gainComparisonTool;
56
57
      public static void setMyGain(BigInteger [][] encryptedGain,
58
      BigInteger [] plainGain) {
           if (encryptedGain == null)
59
               throw new NullPointerException ("Null encryptedGain")
60
           l = encryptedGain.length;
61
62
           myGain = encryptedGain.clone();
           EncryptedBinaryComparator.plainGain = plainGain.clone();
63
64
       public static void setL(int l){
65
           EncryptedBinaryComparator.l = l;
66
67
       public static void setMyGainMe(Participant p, BigInteger
68
       [][] encryptedGain, BigInteger[]plainGain){
           if(encryptedGain == null)
               throw new NullPointerException ("Null encryptedGain")
           selfGain.put(p,encryptedGain);
           selfPlainGain.put(p, plainGain);
72
73
74
75
      }
76
77
       public static void setOthersGain(Integer participantIndex,
79
      BigInteger [][] gain) {
           others Gain.put (participant Index, gain);
80
81
82
       public static void setOthersGainMe(Participant p, Integer
83
      participantIndex, BigInteger[][] gain){
           if(selfOthersGain.get(p) = null){}
84
85
86
           others Gain.put (participant Index, gain);
       }
89
       /**
       * Compares own gain with other's
90
91
       public static void compareWithParticipants(){
92
           //List of encrypted bit by bit comparisons
93
           encryptedComparisonList = new ArrayList <>();
94
95
           //Procedure for candidate I
           for (Integer index: othersGain.keySet()) {
96
97
               //Computation of the gama's factors
```

```
gamas = new ArrayList <>(1);
100
                //table of beta's
                betaI = othersGain.get(index).clone();
                for (int t = 0; t < l ; t++) {
102
                    tmp = homomorphicEncryption(betaI[t], myGain[t]);
                    tmp2 = multHomomorphicEncryption(betaI[t],
       plain Gain [t]. multiply (BigInteger.valueOf(-2));
                    gamas.add(t, homomorphicEncryption(tmp, tmp2));
                    //Un-comment and bring fields back in the method
106
                    BigInteger expe1 = plainGain[t].add(decrypt(
107
       betaI[t])).mod(BigInteger.valueOf(2));
                    BigInteger expe2 = plainGain[t].add(othersPlain[
       t]).mod(BigInteger.valueOf(2));
                    BigInteger res = decrypt(gamas.get(t));
109
110
                    if(!(othersPlain[t].equals(decrypt(betaI[t]))))
111
                        throw new IllegalStateException();
112
                    if (!othersPlain [t]. equals (decrypt (othersGain.get
113
       (index)[t])))
                        throw new IllegalStateException();
114
                    if (!plainGain[t].equals(decrypt(myGain[t])))
                        throw new IllegalStateException();
                    if (!expe1.equals(expe2))
                        throw new IllegalStateException();
118
                    if (!expe2.equals(res))
119
                        throw new IllegalStateException();
120
121
                }
122
                  Optimisation begin with t = 1 so singe loop
124
                * Pull the creation outside the loops
125
126
                 */
               sum = new BigInteger[1][2];
127
               negGamaT = new BigInteger[1][2];
128
                omegas = new BigInteger[1][2];
129
                taus = new BigInteger[1][2];
130
                List < BigInteger > plainGama = decryptMany(gamas);
131
                for (int t = l-1; t >= 0; t--) {
132
                    val = ElGamal.encrypt(BigInteger.valueOf(l-t));
                    tmp = ElGamal.getNegativeciphers(gamas.get(t));
135
                    negGamaT[t] = multHomomorphicEncryption(tmp,
       BigInteger.valueOf(l-t));
                    sum[t] = homomorphicEncryption(gamas.subList(t
136
      +1,1));
                    omegas[t] = homomorphicEncryption(val, sum[t],
137
      negGamaT[t])
                   ;// E(1-t+1 + sum of (gamav - gmai) - gamai)
                    taus[t] = homomorphicEncryption(omegas[t],
138
      myGain[t]);
                    BigInteger expSum = BigInteger.valueOf(l-t);
139
                    BigInteger\ expeNegGama = plainGama.get(t).
140
       multiply (expSum).negate();
141
                    BigInteger\ expGamSum = SecureDotProductParty.
       vectorElementsSum((BigInteger[])plainGama.subList(t+1,1).
       toArray(new BigInteger[1-t-1]));
```

```
BigInteger\ expeOmeg = expSum.add(expeNegGama).
142
       add (expGamSum);
                    BigInteger expTau = expeOmeg.add(plainGain[t]);
143
                    if(!compEncrypted(plainGama.get(t),(decrypt(
144
       gamas.get(t)))))
                        throw new IllegalStateException();
145
                    if (!compEncrypted(expSum, decrypt(val)))
146
                        throw new IllegalStateException();
147
                    if (!compEncrypted(expeNegGama, decrypt(negGamaT[t
148
       ])))
149
                        throw new IllegalStateException();
                    if(!compEncrypted(expGamSum, decrypt(sum[t])))
                        throw new IllegalStateException();
151
                    if(!compEncrypted(expeOmeg,decrypt(omegas[t])))
153
                        throw new IllegalStateException();
                    if(!compEncrypted(expTau,decrypt(taus[t])))
154
                        throw new IllegalStateException();
155
156
157
                encryptedComparisonList.add(taus);
158
159
           }
160
       }
162
163
        * Method that's compare two ElGamal encrypted numbers.
164
        * Computes the XOR bit-by-bit and finally.
165
        * Computation is done so that the first right most bit is
       set to Zero
        * Since the encryption Scheme is Homomorphic we can compute
167
       : M1+M2 also M1*M2
168
        * M1, M1 in F2
        * @param cipher1
169
        * @param cipher2
170
171
       public static List<BigInteger[] > compareNumbers(BigInteger[]
172
       plain1 , BigInteger[][] cipher1 , BigInteger[][] cipher2){
            if (cipher1.length != cipher2.length){
173
                throw new IllegalArgumentException ("Ciphers must
174
       have the same size");
175
           checkInput(cipher1);
            checkInput(cipher2);
            int l = cipher1.length;
            //List of encrypted bit by bit comparisons
179
180
181
182
                //Computation of the gama's factors
183
                List < BigInteger[] > gamas = new ArrayList <>(l);
184
                //table of beta's
185
                BigInteger[] tmp;
186
187
                BigInteger [] tmp2;
                for (int t = 0; t < l; t++) {
```

```
tmp = homomorphicEncryption(cipher1[t], cipher2[t
       ]);
                      tmp2 = multHomomorphicEncryption(cipher2[t],
190
       plain1[t]. multiply(BigInteger.valueOf(-2)));
                      gamas.add(t, homomorphicEncryption(tmp, tmp2));
191
192
                 /*
193
                    Optimisation begin with t = 1 so singe loop
194
                    Pull the creation outside the loops
195
196
197
                 BigInteger [] val; //(1-t+1)
                 \label{eq:list_bound} List \! < \! BigInteger[] \! > \ sum = \ new \ ArrayList \! < \! > \! (1);
                 List < BigInteger[] > negGamaT = new ArrayList <>(1);
199
                 List < BigInteger[] > omegas = new ArrayList <>(l);
200
201
                 List < BigInteger[] > taus = new ArrayList <>(1);
                 for (int t = 1 -1; t >= 0; t--) {
202
                      val = ElGamal.encrypt(BigInteger.valueOf(l-t));
203
                      tmp = ElGamal.getNegativeciphers(gamas.get(t));
204
                      negGamaT.add(t, multHomomorphicEncryption(tmp,
205
       BigInteger.valueOf(l-t));
                     sum.add(t, homomorphicEncryption(gamas.subList(t
       +1,1)));
                      omegas.add(t, homomorphicEncryption(val, sum.get(t
       ), \operatorname{negGamaT.get}(t)); // E( l-t+1 + \operatorname{sum of}(\operatorname{gamav} - \operatorname{gmai}))
                      taus.add(t, homomorphicEncryption(omegas.get(t),
208
       cipher1[t]));
209
                 return
                          taus:
210
211
212
213
       }
214
215
216
        /**
         * Check the encrypted input
217
         * Mostly for size
218
         * @param cipher1
219
220
        private static void checkInput(BigInteger[][] cipher1) {
221
            for (BigInteger[] c: cipher1) {
222
223
                 if(c.length! = 2 \mid | c[0] = null \mid | c[1] = null)
                      throw new IllegalArgumentException ("Bad cipher
224
       as argument either size or one of cipher component is Null");
                 }
        }
227
228
        public static BigInteger[][] getEncryptedCompWithCandidate(
229
       Integer candidateIndex) {
            return encryptedComparisonList.get(candidateIndex);
230
231
232
        public static List<BigInteger[][] > getEncryptedComparisons()
```

```
return new ArrayList <> (encryptedComparisonList);
235
236
237
       /**
238
        * Method for chained decryption(i.e Phase 8)
239
        * @param list V vector in the paoer
240
        * @param myIndex
241
        * @param privateKey
242
        * @param prime
243
244
        * @return
245
        */
       public static List<List<BigInteger[][]>> chainedDecryption(
246
      privateKey , BigInteger prime , BigInteger group) {
247
           BigInteger r;
           for (int i = 0; i < list.size(); i++) {
248
               if(i != myIndex){
249
                    for (int j = 0; j < list.size(); j++) {
250
                        r = new BigInteger (group.bitLength (), new
251
      SecureRandom());
                        r = r.mod(group);
                        for (int k = 0; k < l; k++) {
                            BigInteger ct = list.get(i).get(j)[k]
      ][0];
                            BigInteger ct_prime = list.get(i).get(j)
255
      [k][1];
                            ct = (ct.multiply((ct_prime.modPow(
256
      privateKey , prime)).modInverse(prime))).modPow(r,prime);
257
                            list.get(i).get(j)[k][0] = ct;
                            list.get(i).get(j)[k][1] = ct_prime.
258
      modPow(r,prime);
259
                        Collections.shuffle(Arrays.asList(list.get(i
260
       ).get(j)));
                   }
261
262
263
           return list;
264
265
266
268
        * Returns the binary representation of a number as an array
269
        * i.e if g = abcd with a, b, c, d in \{0,1\}
270
        * then the array is [d,c,b,a] and indexOf(d) = 0;
271
        * @param gain the number to convert
272
        * @return
273
        */
274
275
       public static BigInteger [] createBinaryArray(BigInteger gain
       , int length){
           String t = (gain.toString(2));
           int l = t.length();
```

```
BigInteger[] binaryVector = new BigInteger[length];
279
            for (int i = 0; i < length; i++) {
                if(i < l)
280
                    binaryVector[i] = new BigInteger(String.valueOf(
281
       t.charAt(l-i-1));
282
                else {
283
                    binaryVector[i] = BigInteger.ZERO;
284
285
           }
286
287
            return
                    binary Vector;
288
       }
289
290
       public static int finalDecryption(List<BigInteger[][] > comp)
            ArrayList < BigInteger > res;
291
            int nb = 0;
292
            for (BigInteger[][] b: comp) {
293
                res = (ArrayList)decryptMany(Arrays.asList(b));
294
                for (BigInteger c: res) {
295
                         if (c.equals (BigInteger.ZERO)) {
                             nb++;
299
300
           return nb + 1 ;
301
       }
302
303
304
305
       public static BigInteger[] getOthersPlain() {
306
           return othersPlain;
307
308
       public static void setOthersPlain(BigInteger[] othersPlain)
309
       {
           EncryptedBinaryComparator.othersPlain = othersPlain;
310
311
312
       private static boolean compEncrypted (BigInteger expected,
313
       BigInteger res) {
           return (!expected.equals(BigInteger.ZERO) && res.equals(
314
       BigInteger.ONE) ||
                    expected.equals(BigInteger.ZERO) && res.equals(
       BigInteger.ZERO));
316
317
       public static int findDiffindex (BigInteger n1, BigInteger n2
318
       ) {
            int length = Math.max(n1.bitLength(),n2.bitLength());
319
            BigInteger[] v1 = createBinaryArray(n1, length);
320
321
            BigInteger[] v2 = createBinaryArray(n2,length);
322
            int index = v1.length - 1;
            boolean found = false;
            while (! found) {
```

```
if (!v1[index].equals(v2[index])){
    found = true;
}

left found = true;

left
```

Once the comparison with all of the others gain is done, the participant proceed to decrypt the comparison in a chained fashion. And at last each Participant count the number of zeros yielded by comparing his gain with others and submit his ranking and his gain to the initiator if the number of zero is less than k, meaning that the participants is amongst the kth the best participants.

### 0.3 Simulation and results

¿¿¿SHOW CODE FOR A SMALL APPLICATION
¿¿¿PLOT DIFFERENT RUNNING TIMES AS FUNCTION OF ONE PARAMETER: number Participant, security parameter of ELGAMAL

## 0.4 Conclusion

 $\ensuremath{\ensuremath{\mathcal{L}}\ensuremath{\ensuremath{\ensuremath{\mathcal{L}}\ensuremath{\ensuremath$ 

¿¿¿¿DESCRIPTION OF WHAT CAN BE DONE IF SOME PARTICI-PANTS ARE DISHONEST AND COLLARBORATES ¿¿¿MENTION THE FACT THAT THERE COULD BE A POSSIBLE AT-TACK ON THE DOT PRODUCT PROTOCOL SO THAT AT LEAT ONE

TACK ON THE DOT PRODUCT PROTOCOL SO THAT AT LEAT ONE PRIVATE ATTRIBUTE CAN BE LEARNED. QUOTE PAPER PROOVING IMPOSSIBILITY OF DISTRIBUTED SECURE DOT PRODUCT ¿¿¿¿THANK THE LAB FOR THE PROJECT AND HANDAN FOR A GOOD SUPERVISION.

# 0.5 Bibliography