

Problem 1:

$$T(n) = T(n-1) + cn \text{ if } n > 1 \text{ and } T(1) = c$$

n	T(n)
1	$C = 1C$
2	$C + 2C = 3C$
3	$3C + 3C = 6C$
4	$6C + 4C = 10C$
5	$10C + 5C = 15C$
6	$15C + 6C = 21C$

The values 1, 3, 6, 10, 15, 21... are so-called triangular numbers and can be modeled by:

$$T(n) = C\left(\frac{n(n+1)}{2}\right)$$

In order to find the complexity of $T(n)$ we can simplify the right-hand side of the above equation to:

$$T(n) = C\left(\frac{n^2 + n}{2}\right)$$

Dropping constants and lower order terms, we can conclude that the complexity of $T(n)$ is:

$$\theta(n^2)$$