

General Sir John Kotelawala Defence University  
**ET3122 Antennas and Propagation**  
**Wideband Antennas**

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# Outline

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- 3 Biconical Arrays
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# Introduction

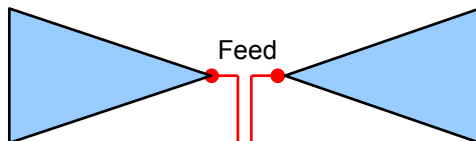
# Motivation

- Modern communication technologies require wide bandwidth
  - ▶ Mobile communication devices with backward compatibility
  - ▶ CDMA
  - ▶ Wideband satellite communication
- Most antennas have a limited bandwidth
  - ▶ Degradation of radiation pattern
  - ▶ Sensitive feed impedance
- How can wideband operation be achieved?

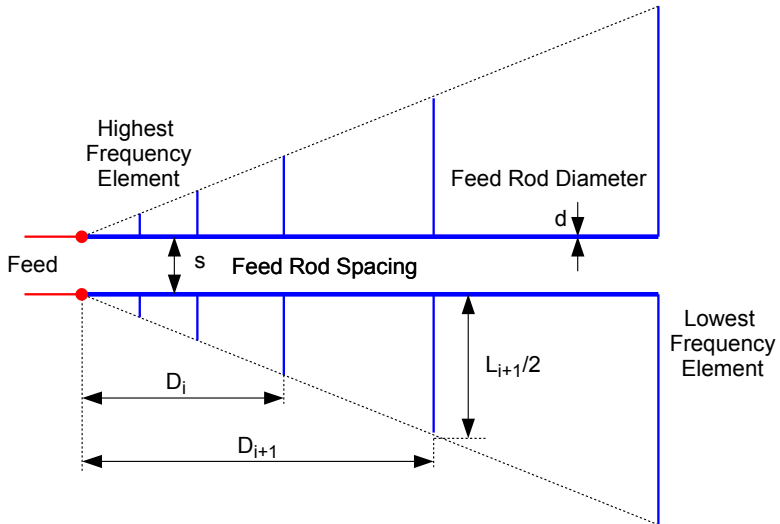
# Log Periodic Arrays

# Rationale

- Use multiple elements of different length
  - ▶ Design so that the current distribution is frequency independent
  - ▶ When this happens, elements do not interfere with each other
- Can also use a continuous structure



# Log Periodic Dipole Antenna



# Design Procedure

## Design Parameters

- Range  $f_{min}$  to  $f_{max}$
- Number of elements  $N$

Take the *geometric ratio*  $\tau$ ,

$$\tau = \sqrt[N-1]{\frac{f_{min}}{f_{max}}}$$

The spacing between two elements is given by  $D_{i+1} - D_i$  where

$$\tau = \frac{D_i}{D_{i+1}}$$

This results in a total antenna length of  $D_N$  with  $D_1$  chosen.



## Design Procedure (Contd..)

The spacing factor ( $\sigma$ ),

$$\sigma = \frac{D_{i+1} - D_i}{2L_{i+1}}$$

The iteration is started with  $L_N = \lambda_{max}/2$  (for  $f_{min}$ ).

The feed spacing  $s$  for a transmission line with characteristic impedance  $z_0$  is given by,

$$s = d \cosh \left( \frac{z_0}{120} \right)$$

# Log Periodic Antenna Design

## Design Specification

A software defined radio unit requires a log periodic antenna to cater a frequency range between 1 - 3.6 GHz. The total length has to be at most 15 cm.

- What makes a good design?
- What is missing?
- Requires antenna theory, mathematics and programming skills to solve

# Design Parameters

- Range  $f_{min}$  to  $f_{max}$  (a requirement)
- Maximum length  $L$  (a constraint)
- Number of elements  $N$ 
  - ▶ Has to be *maximized* for best bandwidth response
- Minimum distance between two elements ( $\delta$ )
  - ▶ If too close, they will appear as a *single element*
  - ▶ This value is missing (found to be 5 mm)

# Design Procedure

Take the *geometric ratio*  $\tau$ ,

$$\tau = \sqrt[N-1]{\frac{f_{min}}{f_{max}}}$$

The geometric ratio also gives the relationship between the distance of two successive elements to the feed end. i.e.,  $D_i$  and  $D_{i+1}$  where

$$\tau = \frac{D_i}{D_{i+1}}$$

## Design Procedure (Contd..)

- Need to relate  $\delta$  and  $L$  into the design
- Minimum distance is between  $D_1$  and  $D_2$

$$D_1 \left( \frac{1}{\tau} - 1 \right) \geq \delta$$

$$D_1 = \tau^{(N-1)} L$$

$$L \left( \tau^{(N-2)} - \tau^{(N-1)} \right) \geq \delta$$

$$L \left( \left( \frac{f_{min}}{f_{max}} \right)^{\frac{(N-2)}{(N-1)}} - \left( \frac{f_{min}}{f_{max}} \right) \right) \geq \delta$$

- How to find  $N$ ?

## Design Procedure (Contd..)

- To find maximum  $N$  evaluate the inequality for  $N > 2$  until the inequality is no longer satisfied (write a simple program)

$$L \left( \left( \frac{f_{min}}{f_{max}} \right)^{\frac{(N-2)}{(N-1)}} - \left( \frac{f_{min}}{f_{max}} \right) \right) \geq \delta$$

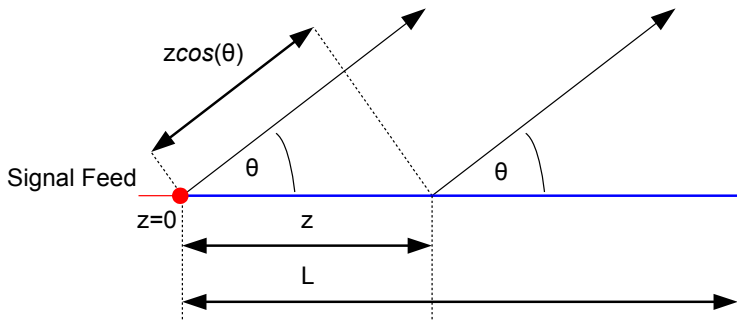
- The result

$N = 3$	0.0373903
$N = 4$	0.0221925
$\vdots$	$\vdots$
$N = 12$	0.0051458
$N = 13$	$0.0046937 < 0.005$ (Answer $N = 12$ )

# Biconical Arrays

# Traveling Wave Antennas

- Traveling wave current distribution like in a transmission line
- A standing wave may be generated depending on the reflection
- Derivations of the longwire antenna ( $L \gg \lambda$ )





# Traveling Wave Antennas

Assuming the end of the line is perfectly matched and lossless,

$$J = I_0 e^{-\gamma z} = I_0 e^{-(\alpha + j\beta)z} = I_0 e^{-j\beta z}$$

Approximate the longwire as a summation of infinitesimal dipoles.  
Therefore, the path difference becomes,

$$R = r - z \cos(\theta)$$

Therefore,

$$dE = \left[ \frac{j\eta k \sin(\theta) I_z e^{-jk(r - z \cos(\theta))}}{4\pi r} dz \right] \underline{\underline{\theta}}$$

# Traveling Wave Antennas (Contd..)

Thus, the integral of the current distribution becomes,

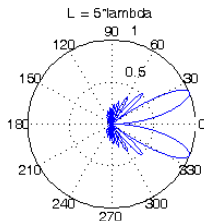
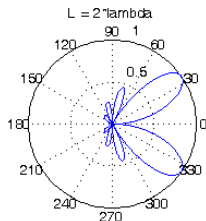
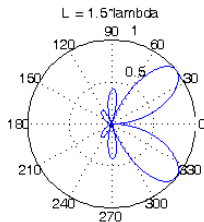
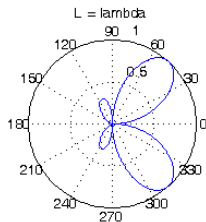
$$E = \left[ \frac{j\eta k e^{-jkr} \sin(\theta)}{4\pi r} \int_0^L I_0 e^{-jkz} e^{jkz \cos(\theta)} dz \right] \underline{\theta}$$

This simplifies to,

$$E = \left[ \frac{j\eta I_0 e^{-jk\left[r + \frac{L}{2}(1 - \cos(\theta))\right]} \sin(\theta) \sin\left[\frac{kL(\cos(\theta) - 1)}{2}\right]}{2\pi r(\cos(\theta) - 1)} \right] \underline{\theta}$$

$$H = \left[ \frac{j I_0 e^{-jk\left[r + \frac{L}{2}(1 - \cos(\theta))\right]} \sin(\theta) \sin\left[\frac{kL(\cos(\theta) - 1)}{2}\right]}{2\pi r(\cos(\theta) - 1)} \right] \underline{\phi}$$

# Traveling Wave Antennas - Radiation Patterns



# Standing Wave Antennas

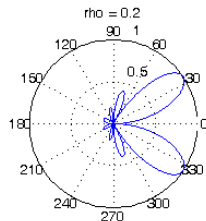
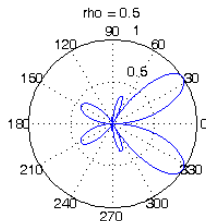
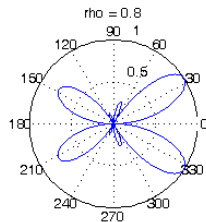
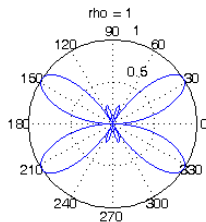
When the longwire has a reflection coefficient of  $\rho$ ,

$$J = I_0 e^{-jkz} + \rho I_0 e^{jkz}$$

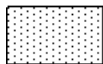
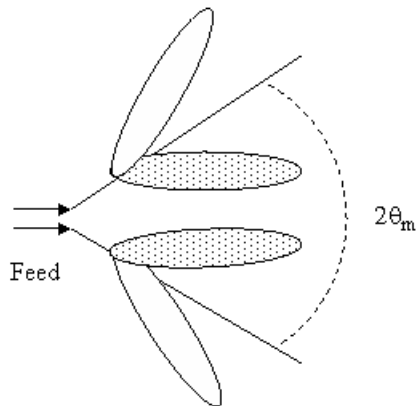
Therefore,

$$E = \left[ \frac{j\eta k e^{-jkr} \sin(\theta)}{4\pi r} \int_0^L \left( I_0 e^{-jkz} + \rho I_0 e^{jkz} \right) e^{jkz \cos(\theta)} dz \right] \underline{\theta}$$

# Standing Wave Antennas - Radiation Patterns

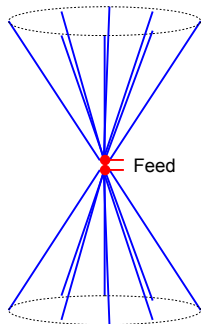


# V Antenna

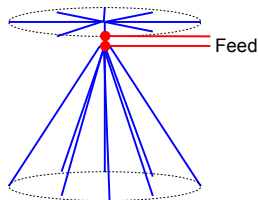


Combining Lobes

# Biconical and Discone Antennas



Wire Biconical Antenna



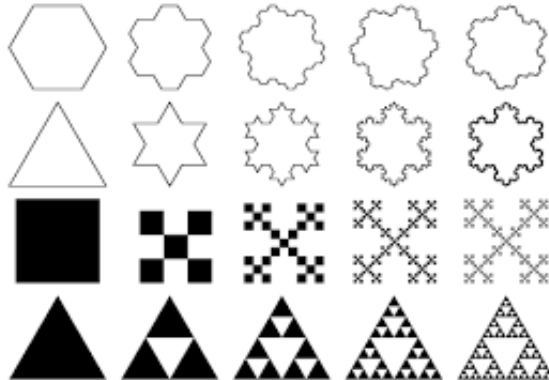
Wire Discone Antenna

- A composite of multiple V antennas
- Can be made solid at microwave frequencies

# Fractal Antennas

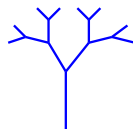


# Self Similarity and Fractals

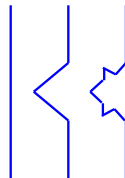


Wolfram Mathworld

# Fractal Antennas



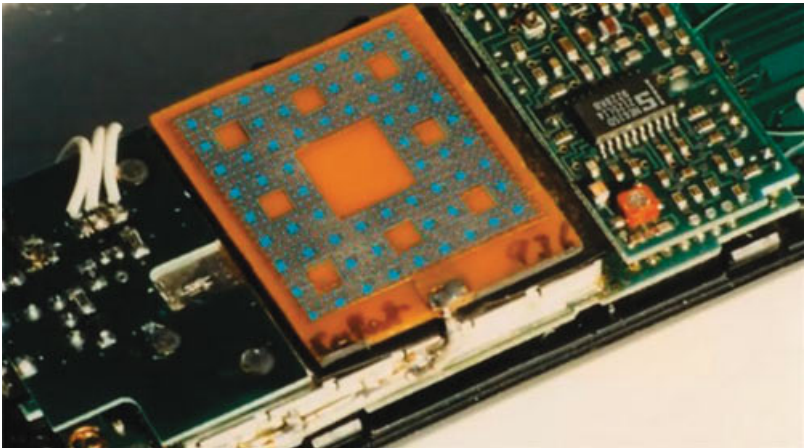
Fractal Tree  
Antenna



Koch Dipole  
Antenna

- Scale invariant
- Can be an iterative feed like the Fractal Tree or compacting like the Koch dipole

# Fractal Antennas (Contd..)



[www.compuart.ru](http://www.compuart.ru)

# Conclusion

# Summary

- Most antennas are reasonably wideband
  - ▶ However, insufficient for modern communication applications
- The main issues of narrowband antennas are
  - ▶ Degradation of radiation pattern
  - ▶ Sensitivity of feed impedance to wavelength
- The main solutions include:
  - ▶ Multiple elements to handle multiple frequencies
  - ▶ Scale invariant structure
  - ▶ Frequency independent current distributions