

# Discrete- Time Processing of Analog Signals and Rate Conversion

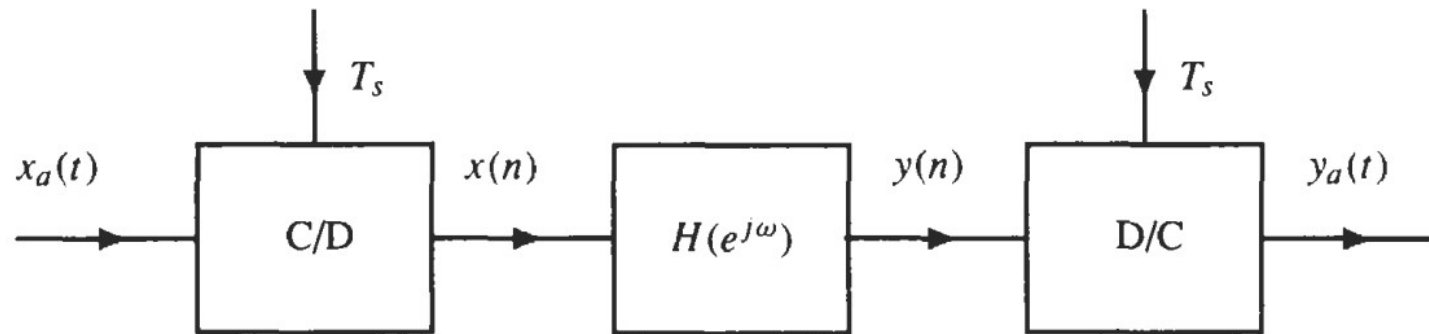
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LECTURE 2



# Processing an analog signal using a discrete-time system.

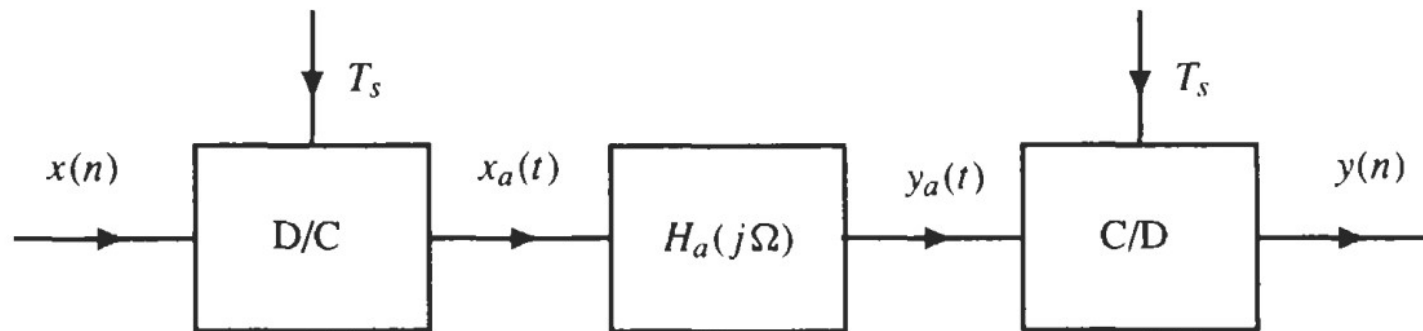
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Processing an analog signal using a discrete-time system.

# Processing a discrete-time signal using a continuous-time system.

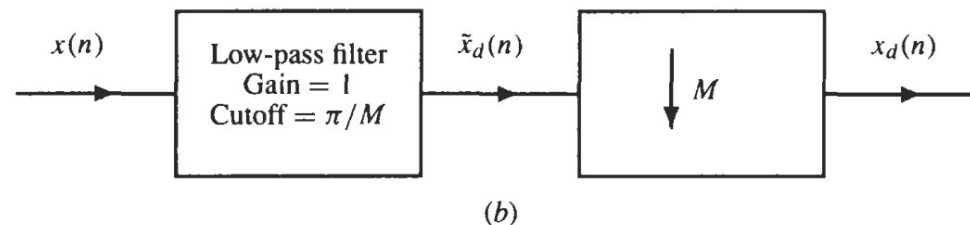
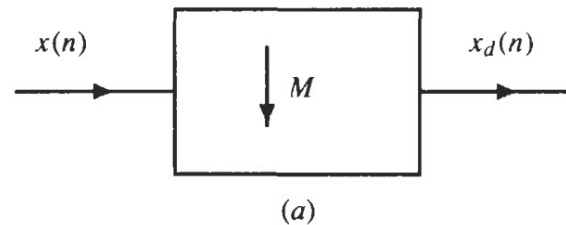
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Processing a discrete-time signal using a continuous-time system.

# Sample Rate Reduction by an Integer Factor

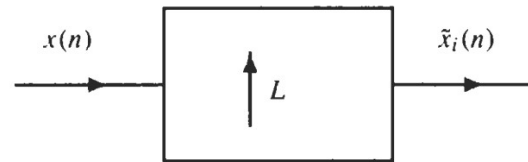
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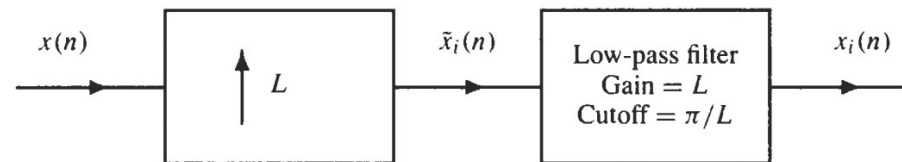
(a) Down-sampling by an integer factor  $M$ . (b) Decimation by a factor of  $M$ , where  $H(e^{j\omega})$  is a low-pass filter with a cutoff frequency  $\omega_c = \pi/M$ .

# Sample Rate Increase by an Integer Factor

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(a)

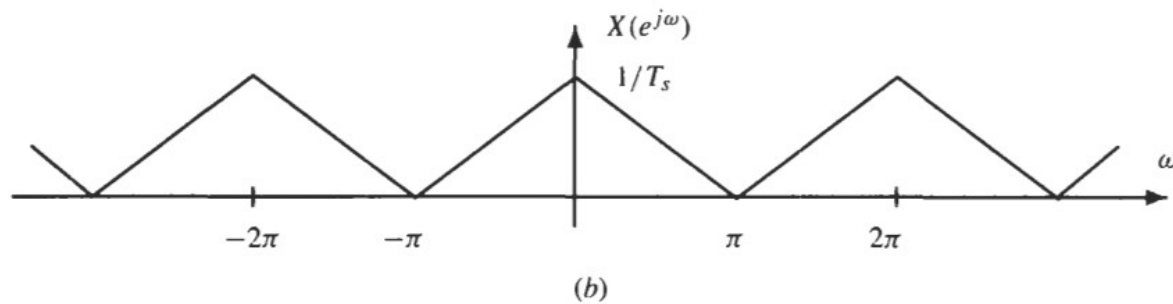
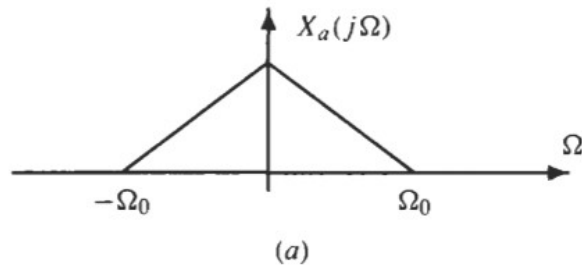


(b)

(a) Up-sampling by an integer factor  $L$ . (b) Interpolation by a factor of  $L$ .

# Example

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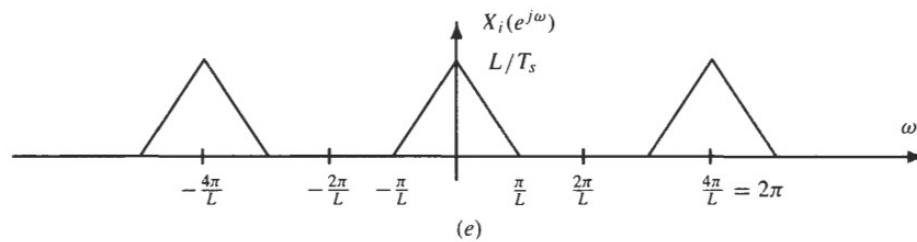
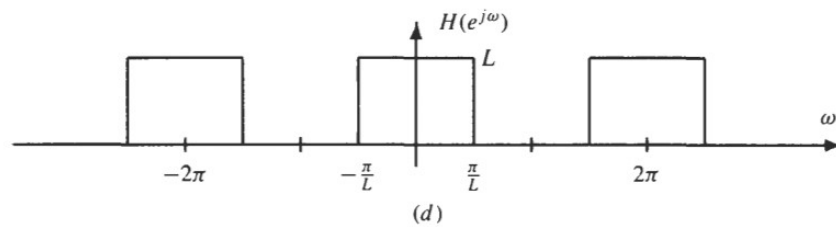
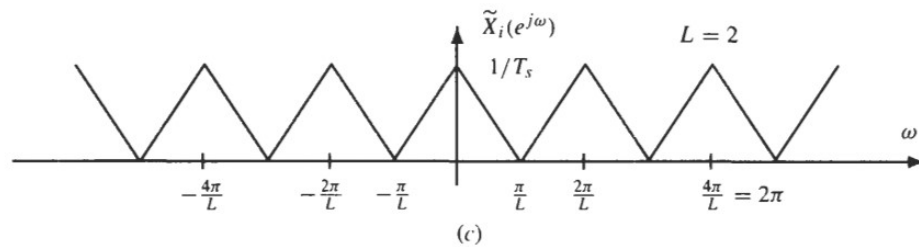


Frequency domain illustration of the process of interpolation.

(a) The continuous-time signal.

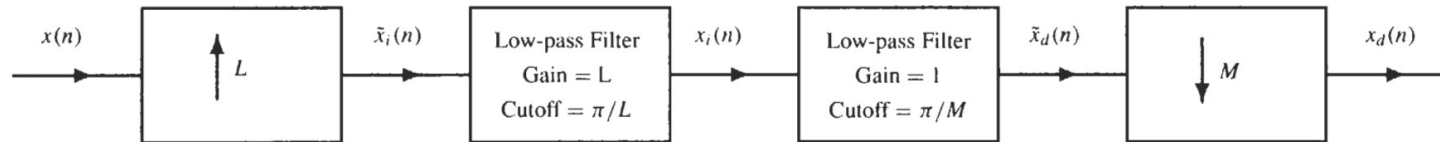
(b) (b) The DTFT of the sampled signal  $x(n) = x_a(nT_s)$ .

# Example

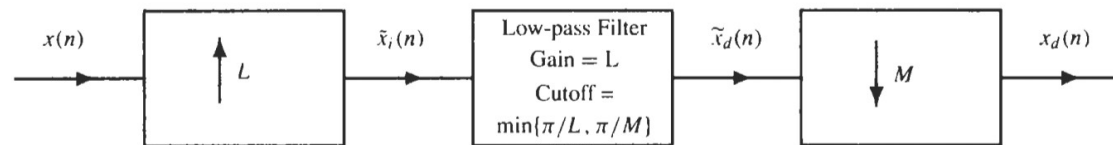


- (c) The DTFT of the up-sampler output.
- (d) The ideal low-pass filter to perform the interpolation.
- (e) The DTFT of the interpolated signal.

# Sample Rate Conversion by a Rational Factor



(a)



(b)

(a) Cascade of an interpolator and a decimator for changing the sampling rate by a rational factor  $L/M$ .

(b) A simplified structure that results when the two low-pass filters are combined.