

IDO- Tarea 3

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Problema de la ONU

Enunciado

ALGORITMO: Ramificación y Acotamiento 1. Inicializar la lista de nodos pendientes con el nodo raíz. 2. Mientras la lista de nodos pendientes no esté vacía, hacer: a. Seleccionar y eliminar un nodo de la lista de nodos pendientes. b. Si el nodo seleccionado es prometedor, entonces: i. Si el nodo seleccionado es una solución completa, comparar con la mejor solución actual. ii. De lo contrario, ramificar el nodo para generar nuevos nodos y agregarlos a la lista. 3. Devolver la mejor solución encontrada.

$$\begin{aligned} \max \quad & z = 120x_1 + 80x_2 \\ & 2x_1 + x_2 + x_3 = 6 \\ & 7x_1 + 8x_2 + x_4 \leq 28 \\ & x_3 - .5x_4 = 2.5 \\ & x_i \in Z_+ \quad \text{para todo } i \end{aligned}$$

Modelo en julia

Por método de ramificación y acotamiento se tiene el siguiente modelo en julia

Primero realizamos un simplex normal:

```
using JuMP, HiGHS
model = Model(HiGHS.Optimizer)
@variable(model, x[1:4] >= 0)

@objective(model, Max, 120x[1] + 80x[2])

@constraint(model, 2*x[1] + x[2] + x[3] == 6)
@constraint(model, 7*x[1] + 8*x[2] + x[4] <= 28)
@constraint(model, x[3] - 0.5*x[4] == 2.5)

optimization_result = optimize!(model)
```

```
Running HiGHS 1.6.0: Copyright (c) 2023 HiGHS under MIT licence terms
Presolving model
2 rows, 3 cols, 6 nonzeros
2 rows, 3 cols, 6 nonzeros
```

```

Presolve : Reductions: rows 2(-1); columns 3(-1); elements 6(-2)
Solving the presolved LP
Using EKK dual simplex solver - serial
  Iteration      Objective      Infeasibilities num(sum)
      0      -4.9998787442e+01 Ph1: 2(3.375); Du: 2(49.9988) 0s
      2      -2.8000000000e+02 Pr: 0(0) 0s
Solving the original LP from the solution after postsolve
Model  status      : Optimal
Simplex  iterations: 2
Objective value      :  2.8000000000e+02
HiGHS run time       :              0.00

```

El resultado es:

```
value.(x)
```

```

4-element Vector{Float64}:
-0.0
 3.5
 2.5
 0.0

```

Ramificación 1

Con lo cual decidimos ramificar en la variable x_3 , dado que tuvimos soluciones fraccionadas:

Nodo 1

```

model = Model(HiGHS.Optimizer)
@variable(model, x[1:4] >= 0)

@objective(model, Max, 120x[1] + 80x[2])

@constraint(model, 2*x[1] + x[2] + x[3] == 6)
@constraint(model, 7*x[1] + 8*x[2] + x[4] <= 28)
@constraint(model, x[3] - 0.5*x[4] == 2.5)
@constraint(model, x[3] >= 3)

optimization_result = optimize!(model)

```

```

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Presolving model
2 rows, 3 cols, 6 nonzeros
2 rows, 3 cols, 6 nonzeros
Presolve : Reductions: rows 2(-2); columns 3(-1); elements 6(-3)
Solving the presolved LP
Using EKK dual simplex solver - serial
  Iteration      Objective      Infeasibilities num(sum)
          0    -4.9998787442e+01 Ph1: 2(3.375); Du: 2(49.9988) 0s
          3    -2.4000000000e+02 Pr: 0(0) 0s
Solving the original LP from the solution after postsolve
Model   status      : Optimal
Simplex iterations: 3
Objective value      :  2.4000000000e+02
HiGHS run time       :           0.00

```

```
value.(x)
```

```

4-element Vector{Float64}:
 0.0
 3.0
 3.0
 1.0

```

Nodo 2

```

model = Model(HiGHS.Optimizer)
@variable(model, x[1:4] >= 0)

@objective(model, Max, 120x[1] + 80x[2])

@constraint(model, 2*x[1] + x[2] + x[3] == 6)
@constraint(model, 7*x[1] + 8*x[2] + x[4] <= 28)
@constraint(model, x[3] - 0.5*x[4] == 2.5)
@constraint(model, x[3] <= 2)

optimization_result = optimize!(model)

```

```

Running HiGHS 1.6.0: Copyright (c) 2023 HiGHS under MIT licence terms
Presolving model

```

```
Problem status detected on presolve: Infeasible
Model      status      : Infeasible
Objective value      : 0.0000000000e+00
HiGHS run time       : 0.00
ERROR: No LP invertible representation for getDualRay
```

Solución

Por lo tanto la solución es la del nodo 1

Verdadera solución

De hecho la solución final del problema es:

```
using JuMP, HiGHS
model = Model(HiGHS.Optimizer)
@variable(model, x[1:4] >= 0, Int)

@objective(model, Max, 120x[1] + 80x[2])

@constraint(model, 2*x[1] + x[2] + x[3] == 6)
@constraint(model, 7*x[1] + 8*x[2] + x[4] <= 28)
@constraint(model, x[3] - 0.5*x[4] == 2.5)

optimization_result = optimize!(model)
value.(x)
```

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Presolving model

2 rows, 3 cols, 6 nonzeros

0 rows, 1 cols, 0 nonzeros

0 rows, 0 cols, 0 nonzeros

Presolve: Optimal

Solving report

Status	Optimal
Primal bound	240
Dual bound	240
Gap	0% (tolerance: 0.01%)
Solution status	feasible

	240 (objective)
	0 (bound viol.)
	0 (int. viol.)
	0 (row viol.)
Timing	0.00 (total)
	0.00 (presolve)
	0.00 (postsolve)
Nodes	0
LP iterations	0 (total)
	0 (strong br.)
	0 (separation)
	0 (heuristics)

4-element Vector{Float64}:

0.0
3.0
3.0
1.0