

SOLUCIÓN A:

$$\hat{x} = \underset{x}{\operatorname{argmin}} \|Ax - b\|$$

$$A : M \times N \quad \text{con } M, N^*$$

$$x : N \times 1$$

$$b : M \times 1$$

$$J(x) = \frac{1}{2} (Ax - b)^T (Ax - b)$$

$$= \frac{1}{2} (x^T A^T - b^T) (Ax - b)$$

$$= \frac{1}{2} (x^T A^T A x - x^T A^T b - b^T A x + b^T b)$$

REPASO:

$$\frac{\partial}{\partial x} (x^T S x) = 2Sx$$

$$\frac{\partial}{\partial x} (x^T a) = a \quad \frac{\partial}{\partial x} (a^T x) = a^T$$

$$\frac{\partial J}{\partial x} = \frac{1}{2} (2A^T A x - A^T b - (b^T A)^T) = A^T A x - A^T b \stackrel{!}{=} 0$$

$$\Rightarrow \boxed{\hat{x} = [A^T A]^{-1} A^T b}$$

$$\rightarrow \text{Matlab: } x = A \setminus b;$$

* si $M=N \Rightarrow \hat{x} = A^{-1} b$; si $M < N$ no hay soluc.