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#### 几何基础

```
int sign(double a)
{
   if(abs(a) < eps) return 0;</pre>
   return a > 0 ? 1 : -1;
}
int cmp(double a, double b)
   if(abs(a - b) < eps) return 0;</pre>
   return a > b ? 1 : -1;
PDD operator + (PDD a, PDD b)
   return { a.x + b.x, a.y + b.y };
}
PDD operator - (PDD a, PDD b)
   return { a.x - b.x, a.y - b.y };
}
PDD operator * (PDD a, double b)
{
   return { a.x * b, a.y * b };
}
double operator * (PDD a, PDD b)
   return a.x * b.y - a.y * b.x;
}
```

```
double operator & (PDD a, PDD b)
{
    return a.x * b.x + a.y * b.y;
}

PDD operator / (PDD a, double b)
{
    return { a.x / b, a.y / b };
}

double get_len(PDD a)
{
    return sqrt(a.x * a.x + a.y * a.y);
}

double get_dist(PDD a, PDD b)
{
    double dx = a.x - b.x, dy = a.y - b.y;
    return sqrt(dx * dx + dy * dy);
}

double area(PDD a, PDD b, PDD c)
{
    return (b - a) * (c - a);
}
```

#### 向量夹角

## 顺时针旋转

```
PDD rotate(PDD a, double b)
{
    return {a.x * cos(b) + a.y * sin(b), -a.x * sin(b) + a.y * cos(b)};
}
```

# 两直线交点(sign(v \* w) != 0)

```
PDD get_line_intersection(PDD p, PDD v, PDD q, PDD w) //两直线交点(点向式)
{
    PDD u = p - q;
    double t = w * u / (v * w);
    return p + v * t;
}
```

#### 点到直线距离

#### 点到线段距离

#### 点在直线上的投影

### 点是否在线段上

### 线段是否相交(不包括端点)

```
bool segment_intersection(PDD a1, PDD a2, PDD b1, PDD b2) //线段与线段是否相交 {
    double c1 = (a2 - a1) * (b1 - a1), c2 = (a2 - a1) * (b2 - a1);
    double c3 = (b2 - b1) * (a1 - b1), c4 = (b2 - b1) * (a2 - b1);
    return sign(c1) * sign(c2) < 0 && sign(c3) * sign(c4) < 0;
}
```

# 射线是否相交

```
bool ray_intersection(PDD a1, PDD a2, PDD b1, PDD b2) //射线与射线是否相交 {
    int s = sign((a2 - a1) * (b2 - b1));
    if(!s) return false;
    return sign(area(b1, b2, a1)) == s && sign(area(a1, a2, b1)) == -s;
}
```

#### 点与多边形的关系

# 点与凸多边形的关系

```
int get_point_convexpolygon(PII* p, int n, PII P) //逆时针存储
{
   p[n] = p[0];
    if(area(p[0], p[1], P) < 0 \mid | area(p[0], p[n - 1], P) > 0)
        puts("OUT");
   else
        int 1 = 0, r = n - 1;
       while(1 < r)
            int mid = 1 + r + 1 >> 1;
            if(area(p[0], p[mid], P) >= 0)   1 = mid;
            else r = mid - 1;
        if(on\_segment(P, p[l - 1], p[l]) \mid\mid on\_segment(P, p[l], p[l + 1]))
            puts("ON");
        else if(area(p[l], p[l + 1], P) > 0)
            puts("IN");
        else
            puts("OUT");
    }
}
```

#### 圆与直线交点

#### 两圆交点

## n个圆的面积交

```
double angle = acos((a.r * a.r + d * d - b.r * b.r) / (2 * d * a.r)),
        delta = atan2(v.y, v.x);
    angle1 = delta - angle, angle2 = delta + angle;
    if(angle1 < -PI)</pre>
        angle1 += 2 * PI;
    if(angle > PI)
        angle1 -= 2 * PI;
    if(angle2 < -PI)</pre>
        angle2 += 2 * PI;
    if(angle2 > PI)
        angle2 -= 2 * PI;
    if(!cmp(d, a.r + b.r) \mid | !cmp(d, abs(a.r - b.r)))
        return 1;
    return 2;
}
double calc(Circle& c, double 1, double r)
                                               //积分
    double res = c.r * c.r * (r - 1) + c.0.x * c.r * (sin(r) - sin(1)) -
        c.0.y * c.r * (cos(r) - cos(1));
    return res / 2;
}
bool compare(Data& a, Data& b)
    if(cmp(a.angle, b.angle)) return cmp(a.angle, b.angle) < 0;</pre>
    return a.state > b.state;
}
void Circle_Union(Circle &c, int n) //area[i]:至少被覆盖i次的面积
{
    for(int i = 1; i <= n; i ++)
        for(int j = 1; j <= n; j ++)
            if(i != j \&\& cmp(c[j].r, c[i].r) >= 0
                && cmp(get_dist(c[i].0, c[j].0), c[j].r - c[i].r) \leftarrow 0)
                c[i].state ++;
    for(int i = 1; i <= n; i ++)
    {
        int cnt = 0, t = 0;
        double angle1, angle2;
        for(int j = 1; j <= n; j ++)
            if(i != j && get_circle_circle_point(c[i], c[j], angle1, angle2) ==
2)
            {
                data_[cnt ++] = \{ angle1, 1 \}, data_[cnt ++] = \{ angle2, -1 \};
                if(cmp(angle1, angle2) > 0)
                    t ++;
        data_[cnt ++] = { -PI, t }, data_[cnt ++] = { PI, -t };
        sort(data_, data_ + cnt, compare);
```

```
int s = c[i].state + data_[0].state;
for(int j = 1; j < cnt; j ++)
{
    ans[s] += calc(c[i], data_[j - 1].angle, data_[j].angle);
    s += data_[j].state;
}
}</pre>
```