# An Entrepreneurship Fiscal Multiplier

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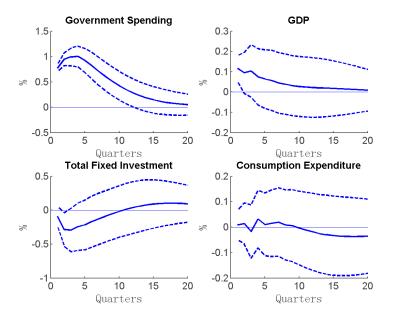
10/9/2015

## Heterogeneity and Macro Policy Facts – Mechanism – Policy Implications

# Heterogeneity and Macro Policy

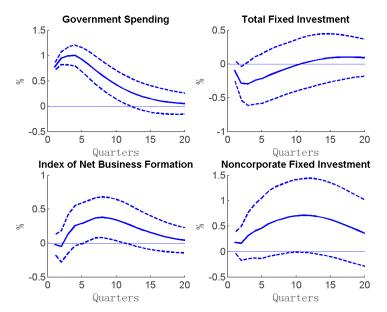
Facts: Entrepreneurs respond differently to Government Spending compared to other households and firms.

# Fiscal multiplier: identified through recursive ordering (log(G), log(Y), MTR, TB3), 1947I-2008IV

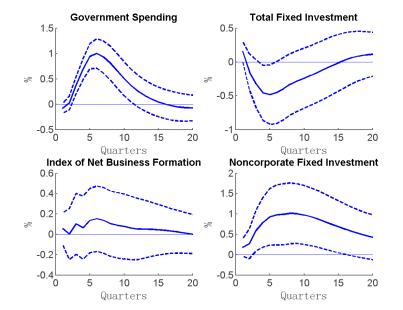


## Entrepreneur fiscal multiplier

(log(G), log(Y), MTR, TB3), 1947I-2008IV



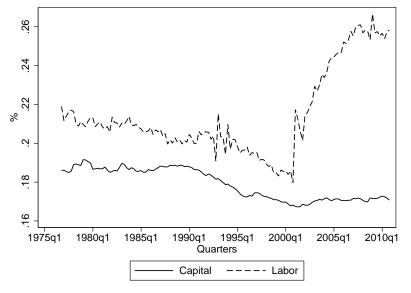
# Entrepreneur fiscal multiplier: Ramey's pdvmily shock (log(G), log(Y), MTR, TB3), 1947I-2008IV



### Mechanism

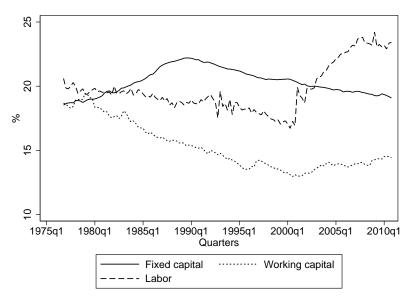
- ▶ Government spending is to be financed by tax.
- ... Tax generates negative income effects, increases labor supply, and decreases saving.
- ▶ ... Wage falls and interest rates rise.
- ▶ ... Entrepreneur sector is more "labor-intensive". Profits increase which encourages entry.

# Mechanism: entrepreneurs use more labor than capital Fractions of factors used in non-corporate sector



### Mechanism

Why does entrepreneur sector use more labor than capital?



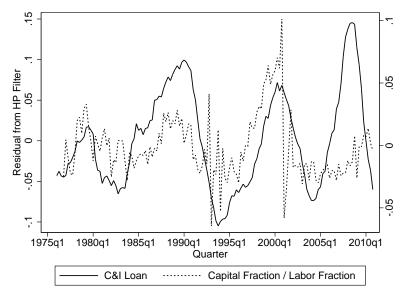
#### Mechanism

Why does entrepreneur sector use more labor than capital?

- ▶ It's not (I'm not assuming) different technology...
- Working capital financing is hampered by financial friction...
- ▶ If this is the case, entrepreneur sector should appear even more "labor-intensive" when credit condition is worse...
- ▶ What's in the data?

# Mechanism: financial frictions vs labor-intensity

Why does entrepreneur sector use more labor than capital?



### Mechanism

- ▶ Government spending is to be financed by tax.
- ... Tax generates negative income effects, increases labor supply, and decreases saving.
- ▶ ... Wage falls and interest rates rise.
- ... Entrepreneur sector is more "labor-intensive" due to financial frictions.
- ▶ ... Profits increase which encourages entry.
- ➤ ... Anticipating profits increase ⇒ Marginal productivity of capital increases ⇒ Entrepreneurs increase saving (investment) countering the consumption smoothing incentive from negative income effects.

# Quantitative questions

#### Questions:

- ▶ Does this mechanism generate qualitative/quantitative results consistent with data?
- ▶ What are the implications for aggregate response? Does it imply interactions between fiscal policy and other economic conditions?

#### Strategy:

- ▶ A model featuring entrepreneur entry/saving decision which are affected by financial frictions.
- ► Calibrated to match (1) fraction of factor use; (2) entrepreneur size distribution; (3) wealth distribution.
- ▶ Feed in government spending shock and inspect the response.
- ► Feed in fluctuations of credit conditions and inspect the interactions.



# Quantitative questions

#### Questions:

- ▶ Does this mechanism generate qualitative/quantitative results consistent with data?
- ▶ What are the implications for aggregate response? Does it imply interactions between fiscal policy and other economic conditions?

#### Answers:

- ▶ Model generates responses of entrepreneur entry and investment consistent with data.
- Generates a sizable output fiscal multiplier close to data, without any Keynesian features.
- ▶ Both entrepreneur and output multipliers are greater when credit is tighter.

#### Related literature

- ▶ Mechanism of fiscal multiplier. Hall (2009), Dyrda and Ríos-Rull (2012), Woodford (2010), Uhlig (2010).
- ▶ Distributional effects of fiscal policy. Heathcote (2005), Bachmann et al. (2013).
- ▶ State-dependent effects of government spending. Auerbach and Gorodnichenko (2012), Owyang et al. (2013), Fazzari et al. (2015)
- ▶ Entrepreneur entry and saving. Decker et al. (2014), Quadrini (2000), Cagetti and De Nardi (2006), Buera and Shin (2013).
- ▶ Heterogeneous agent model with aggregate fluctuations. Krusell and Smith (1997), Reiter (2009), Winberry (2014).

#### Mechanisms and corresponding model elements

- ▶ Time is discrete. Continuum of Infinitely-lived households with constant measure, a corporate firm, and a government. Single consumption good. Single asset.
- ▶ Households receive shocks on labor productivity and entrepreneur productivity; choose to be entrepreneurs and workers; program consumption/saving, labor/leisure; face tight borrowing constraints across periods.
- ► As a worker, household works and receives wages.
- ▶ As an entrepreneur, household does not work; employs capital and labor to produce at market prices.
- ► Entrepreneur can finance additional capital within period up to a fraction of his own wealth due to financial frictions.
- ▶ A government specifying policies for bond and tax.
- ► Exogenous government spending shocks, financial shocks, and TFP shocks.

Households' problems: as an entrepreneur

$$V^{E}(\varepsilon, \zeta, a; \Omega) = \max_{k_{D}, n_{D}, c, a'} u(c, l) + \beta EV(\varepsilon', \zeta', a'; \Omega')$$

s.t.

$$c + a' \le \pi + a - Tax(\Omega)$$

$$\pi = z\zeta(k_D^{\gamma}n_D^{1-\gamma})^{\theta} - r(\Omega)(k_D - a) - \delta k_D - w(\Omega)n_D$$

$$k_D \le \lambda a$$

$$a' \ge 0$$

$$l = 1$$

s.t.

Households' problems: as a worker

$$V^{W}(\varepsilon, \zeta, a; \Omega) = \max_{c,l,a'} u(c, l) + \beta EV(\varepsilon', \zeta', a'; \Omega')$$
$$c + a' \le w(\Omega)\varepsilon(1 - l) + a(1 + r(\Omega)) - Tax(\Omega)$$

 $c + a \le w(\Omega)\varepsilon(1 - l) + a(1 + r(\Omega)) - lax(\Omega)$  $a' \ge 0$  $0 \le l \le 1$ 

Households' problems: entrepreneur or worker?

$$V(\varepsilon, \zeta, a; \Omega) = E_{\tilde{u_E}, \tilde{u_W}} \max\{V^E(\varepsilon, \zeta, a; \Omega) + \tilde{u_E}, V^W(\varepsilon, \zeta, a; \Omega) + \tilde{u_W}\}$$

$$u_E, u_W \text{ i.i.d. Gumbel distribution.}$$

$$V(\varepsilon, \zeta, a; \Omega) = log(exp(V^{E}(\varepsilon, \zeta, a; \Omega)) + exp(V^{W}(\varepsilon, \zeta, a; \Omega)))$$

$$Pr^{E}(\varepsilon,\zeta,a;\Omega) = \frac{exp(V^{E}(\varepsilon,\zeta,a;\Omega))}{exp(V^{E}(\varepsilon,\zeta,a;\Omega)) + exp(V^{W}(\varepsilon,\zeta,a;\Omega))}$$

#### ► Corporate firm:

$$r = z\gamma(\frac{K}{N})^{\gamma-1}, z(1-\gamma)(\frac{K}{N})^{\gamma}$$

- Government:
  - ▶ Promise to pay interest rates of bond equal to interest rate of capital, state by state, following Heathcote (2005) and Bachmann et al. (2013).
  - ► Tax rule:

$$Tax = \rho_0 + \rho_1 B + \rho_2 G$$

► Budget:

$$B' = B(1+r) + G - Tax$$

Exogenous process:  $log(z') = \rho_z log(z) + \varepsilon^z$ ,  $G' = \rho_G G + (1 - \rho_G) \bar{G} + \varepsilon^G$ ,  $\lambda' = \rho_\lambda \lambda + (1 - \rho_\lambda) \bar{\lambda} + \varepsilon^\lambda$ 

#### Definition of equilibrium

Individual state  $x = (\varepsilon, \zeta, a)$ . Aggregate state  $\Omega = (z, G, \lambda; B, \Phi)$ . A recursive equilibrium is

- 1. Policy and value functions as functions of  $(x, \Omega)$ :  $V(x, \Omega), V^E, V^W, Pr^E, a'^E, a'^W, n, n^D, k^D$
- 2. Aggregates as functions of  $\Omega$ :  $K(\Omega)$ , N, w, r, Tax
- 3. Transition for  $B, J: \Omega \to B'$ . Transition for  $\Phi, H: \Omega \to \Phi'$ .

#### Definition of equilibrium

1. Policy and value functions solve agent's problem.

$$V^{W,E}(x,\Omega) = \max \dots + \beta EV(\varepsilon', \zeta', a'; z', G', \lambda'; J(\Omega), H(\Omega))$$

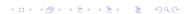
2. Market clear.

$$\begin{split} Labor : & \int n \cdot (1 - Pr^E) d\Phi = \int n^D \cdot Pr^E d\Phi + N \\ Asset : & \int a d\Phi = \int k^D \cdot Pr^E d\Phi + K + B \\ Interest \ rate : & r = z\gamma (\frac{K}{N})^{\gamma - 1} \\ Wage : & w = z(1 - \gamma)(\frac{K}{N})^{\gamma} \end{split}$$

3. Government policy.

$$Tax : Tax = \rho_0 + \rho_1 B + \rho_2 G$$
  
 $Bond : B' = J(B) = B(1+r) + G - Tax$ 

4. Transition of  $\Phi$  is consistent.



#### Model solutions

#### Challenges:

- ▶ Multiple aggregate shocks and continuous aggregate states. Higher moments matter. De Nardi et al. (2015), Bachmann et al. (2013).
- ▶ Pure projection + perturbation (as Reiter (2009)) can't address state-dependent effects.

#### Solutions:

- ▶ Discretize value functions and distributions. Solve non-stochastic steady state.
- Solve dynamics by linear perturbation around non-stochastic steady state. State variables include the discretized distributions over individual states. Jump variables include the discretized value functions over individual states.
- Only use linear perturbation as **forecasting rules of future value functions**. In simulations, solve decision
  problems and market clear conditions exactly, and update
  future states exactly.

# Linear forecasting is very accurate

## Forecasting error (%):

Vars	1-step	100-step	1000-step
r	0.4261		
W	0.1626		
Ea	0.0249		
$Ea^2$	0.0181		
$Ea^3$	0.0276		
$Ea^4$	0.0382		

#### Calibration

#### Parameters fixed exogenously

$$\begin{array}{l} u = \frac{(c^{\chi}l^{1-\chi})^{1-\sigma}}{1-\sigma}, \; \sigma = 2 \\ F(K,L) = zK^{\gamma}L^{1-\gamma}, \; \gamma = 0.36 \\ \varepsilon, \; \varepsilon' = \rho_{\varepsilon}\varepsilon + e', \; \rho_{\varepsilon} = 0.94, \sigma_{\varepsilon}^2 = 0.01 \\ z, \; \rho_z = 0.75, \; \sigma_z = 0.012, \; \mathrm{US} \; \mathrm{Data} \\ G, \; \rho_G = 0.8909, \; \sigma_G = 0.0145 \, \bar{G}, \; \mathrm{US} \; \mathrm{Data} \\ \lambda, \; \rho_{\lambda} = 0.9170, \; \sigma_{\lambda} = 0.049, \; \mathrm{matching} \; \mathrm{anecdotal} \; \mathrm{evidence} \; (\mathrm{Khan} \; \mathrm{and} \; \mathrm{Thomas} \; (2013)) ; \end{array}$$

...debts falling more than 26% as a financial crisis...

...13 crises in the last 200 years (800 quarters)...

... Average duration is 2 years...

## Calibration

#### Parameters calibrated to match moments

Parameters	Value	Target	Data	Model
δ	0.021	r	0.0125	0.0125
$\beta$	0.980	K/Y	10.6	10.85
$\chi$	0.31	$ar{n_w}$	0.33	0.33
$p_1$	0.0039	% Entrepreneurs	0.0755	0.072
$p_2$	0.97	Gini	0.81	0.76
$\mu_{\zeta}$	0.76	% Size 1-5	0.7510	0.7768
$\sigma_{\zeta}$	0.23	% Size 6-10	0.1460	0.1124
$\theta$	0.76	Capital fraction	0.1780	0.1854
$\lambda$	1.32	Labor fraction	0.2180	0.2086
$\overline{Tax}$	1.68	G/Y	0.2086	0.2086
$ar{B}$	0.3597	$\mathrm{B/Y}$	1.2	1.2

## Model performance

Size and wealth distribution

Size of entrepreneur firms measured by employment level, KFS

	1-4	5-9	10-19	20-99	100+
Data	75.1	14.6	6.6	3.5	0.3
Model	77.7	12.4	5.0	4.9	0.0

Wealth distribution, SCF, Díaz-Giménez et al. (2011)

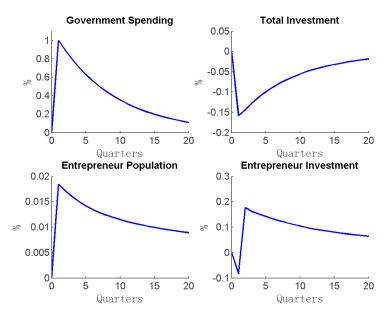
	Top 1%	Top 5%	Top 10%	Top 20%	Gini
Data	30	51	64	79	0.79
Model	23.8	57.6	82.5	91.2	0.76

TODO(wenlan): business cycle property

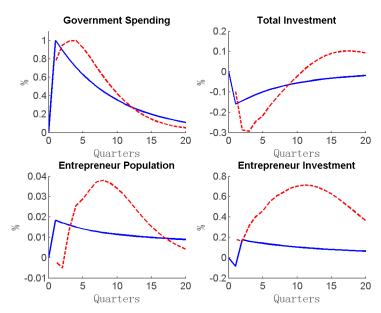
## Roadmap for results

- ► Entrepreneur fiscal multiplier.
- ▶ Implied for output.
- ▶ State-dependent effects.

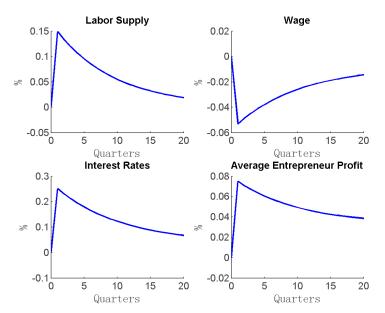
## Entrepreneur fiscal multiplier



## Entrepreneur fiscal multiplier

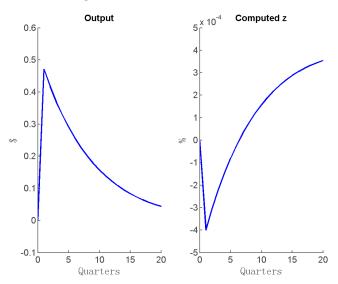


## Entrepreneur fiscal multiplier: Mechanism

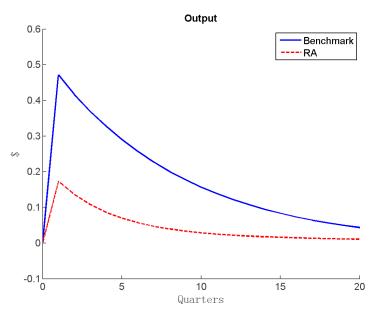


Mechanism: Wealth distribution and occupation choice

## Output multiplier

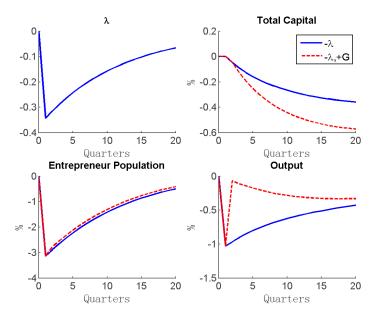


# Output multiplier: heterogeneity matters



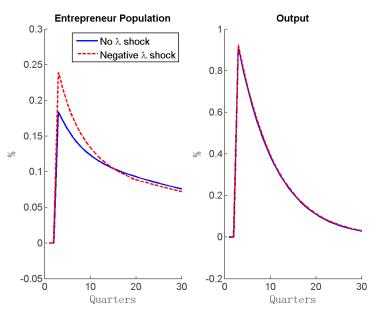
## State-dependent multiplier

Response to  $-\lambda$  shock at period 1, +G shock at period 2



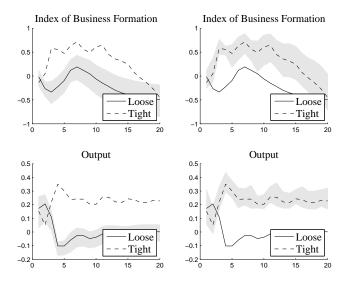
# State-dependent multiplier

Response to +G shock, no  $\lambda$  shock V.S.  $-\lambda$  shock



## STVAR and state-dependent response

Following Auerbach and Gorodnichenko (2012):



#### Conclusions

#### Facts:

- Government spending crowds out overall investment but crowds in entrepreneur activity of both entry and investment.
- ▶ The effect is larger when credit condition is worse.

#### Mechanism:

- ► Entrepreneur sector uses more labor than capital due to financial frictions.
- ▶ Change in factor prices caused by G shock increases profits of entrepreneur activity, encourages entry and investment.

#### Implications:

- ► An output multiplier close to data.
- ▶ State dependence consistent with data.

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