



# Model Structure Determination

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- Unsupervised Approach

Example: Principal Component Analysis

B1 Backward, B1 Forward, B2, B4...

$$\begin{aligned} X^T X &= V D V^T \\ &\downarrow \\ &\lambda_1 \lambda_2 \dots \\ \underline{p} &= \sum \lambda_i \\ \underline{p}_1 &= \sum \lambda_i^{(1)} \quad \underline{p}_2 \end{aligned}$$

- Supervised Approach

Example: Regression models

LASSO, RIDGE regression, etc.

Forward, Backward, Stepwise Regression

Nonlinear Stepwise Regression

## — All Combinations of Factors

Let  $p_{\max}$  – max. number of potential factors

Number of models to be examined:  $n = 2^{p_{\max}} - 1$

Examples:

$$p_{\max} = 3$$

$$n = 2^3 - 1 = 7$$

$$\{x_1\}, \{x_2\}, \{x_3\}, \{x_1, x_2\}, \{x_1, x_3\}, \{x_2, x_3\}, \{x_1, x_2, x_3\}$$

$$p_{\max} = 20$$

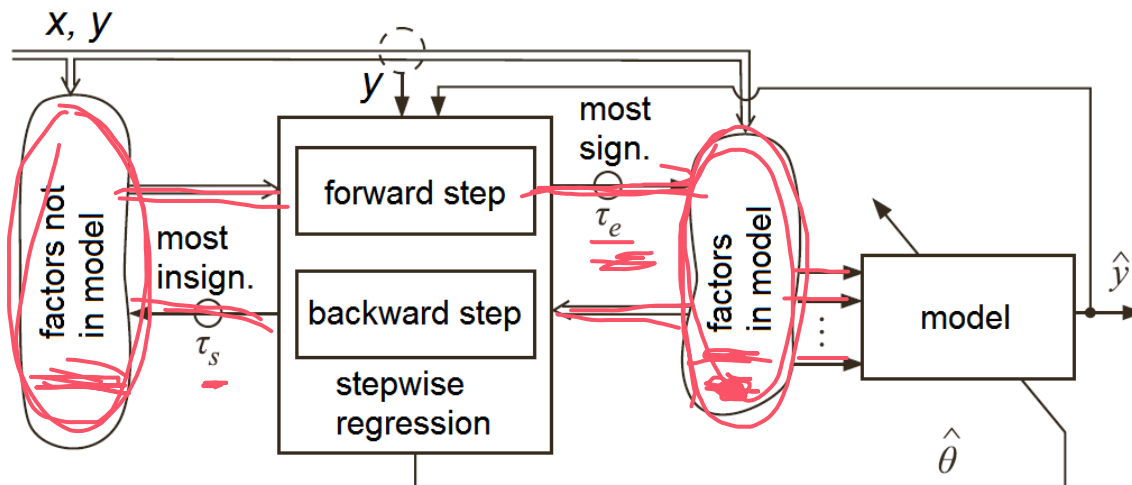
$$n \approx 1.0485 \times 10^6$$

$$p_{\max} = 50$$

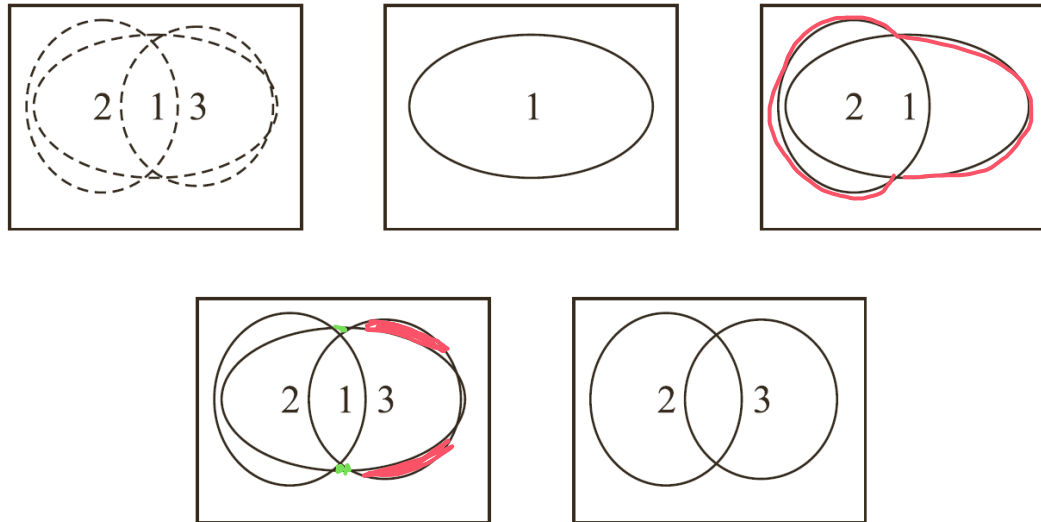
$$n \approx 1.1259 \times 10^{15}$$

## — Iterative Approach

- Forward regression
- Backward regression
- Stepwise regression
- Groupwise approach  
/e.g. for dummies/
- Linear & Non-linear models



## — Factors Selection and Multicollinearity



## Literature

Efremov, A. Multivariable System Identification. Monograph, second edition, ISBN 978-954-9489- 42-2, DAR-RH, VT

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