Bending of a beam fixed on two sides

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Abstract

Aim of this project is to explore OpenFOAM capabilities in stress analysis. Results from OpenFOAM was checked with comercial program and analytics results to verified.

1 Introduction

OpenFOAM - open source Field Operation And Manipulation - is a C++ toolbox for the development of customized numerical solvers. It is utilize to pre-/post-processing for the solution of continuum mechanics problems, most often for computational fluid dynamics (CFD).

2 Bending analysis

2.1 Problem definition

Subject of analysis is beam fixed from both sides. Beam is bending by a constant pressure along the length. Please see Figure 1.

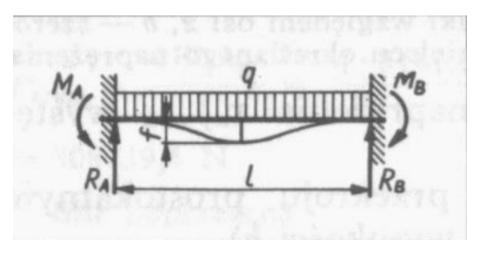


Figure 1: Problem definition.

Dimensions:

l = 10 [m]; a = 1 [m], when a is a side of a beam cross section Loads:

q = 0.1 [MN/m] or in 3D case p = 1 [MPa];

2.2 OpenFOAM results

2.2.1 Mesh generation

Prismatic beam is really simple shape, so only one block was used. To generate mesh paste code bellow in file BlockMeshDict and then use comand *blockMesh*.

```
----*\
8 FoamFile
9
   {
               2.0;
10
      version
              ascii;
11
     format
12
     class
               dictionary;
              blockMeshDict;
13
     object
14 || }
15
  16
17
  convertToMeters 1;
18
  vertices
19
20
21
        (0 0 0)
         (10 0 0)
22
23
        (0 1 0)
         (10 1 0)
24
25
         (0 0 1)
         (10 0 1)
26
         (0 1 1)
27
28
         (10 1 1)
29 || );
30
31
  blocks
  || (
32
33 hex (0 1 3 2 4 5 7 6) (50 5 5) simpleGrading (1 1 1)
34
  );
35
36
  boundary
37
   (
38
      left
39
      {
40
         type patch;
41
         faces
42
         (
            (0 2 6 4)
43
44
45
      }
46
      right
47
48
         type patch;
49
        faces
50
            (1 3 7 5)
51
52
53
      }
54
      down
55
56
         type patch;
57
         faces
58
         (
59
               (0 1 5 4)
60
      }
61
62
      up
63
64
         type patch;
65
         faces
66
         (
  (2 3 7 6)
67
68
         );
69
      }
70
      {\tt frontAndBack}
71
      {
72
         type empty;
73 |
         faces
```

```
75
   (0 1 3 2)
76
   (4 5 7 6)
   );
77
78
79
    );
80
    mergePatchPairs
81
82
   1);
83
84
```

In *vertices* section we have specified corners positions. In *blocks* section beam and division to finite elements were defined. In *boundary* faces were defined. Mesh an be viewed in ParaView, using command $paraFoam \ \mathcal{E}$

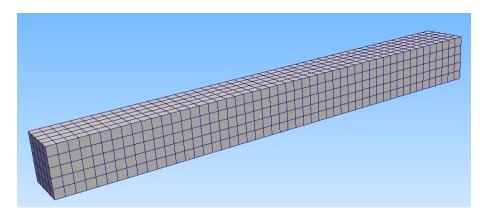


Figure 2: Mesh viewed in ParaView.

2.2.2 Boundary and initial conditions

For a stress analysis case without thermal stresses, only displacement D needs to be set. The 0/D is as follows:

```
----*- C++ -*-----
2
3
                                  OpenFOAM: The Open Source CFD Toolbox
                                / Version: 4.1
4
                0 peration
      11
5
                A \quad nd
                                / Web:
                                           www.OpenFOAM.org
        11/
                M anipulation
7
   \*----
8
   FoamFile
9
   {
10
       version
                   2.0;
11
       format
                   ascii;
12
                   volVectorField;
       class
13
14
   }
15
16
17
                   [0 1 0 0 0 0 0];
   dimensions
18
19
   internalField
                   uniform (0 0 0);
20
21
   boundaryField
22
23
       left
24
                           fixedValue;
25
           type
                           uniform (0 0 0);
26
           value
27
       }
28
       up
29
30
                           tractionDisplacement;
           type
                           uniform (0 -1000000 0);
31
           traction
```

```
32 ||
          pressure
                       uniform 0;
33
                       uniform (0 0 0);
          value
34
      }
35
      down
36
37
                        tractionDisplacement;
          type
                       uniform (0 0 0);
38
          traction
39
                       uniform 0:
          pressure
40
          value
                        uniform (0 0 0);
41
      }
42
      right
43
                       fixedValue;
44
          type
45
                       uniform (0 0 0);
46
      }
47
      frontAndBack
48
49
                       empty;
          type
      }
50
51
   }
52
     53
```

In this case on left and right side (patches) we have fixed support handled by fixed Value condition. Patch frontAndBack is declared as empty, because don't participate in 2D bounding. Patches up and down are using tractionDisplacement condition and to face up 1 MPa pressure is applied.

2.2.3 Mechanical properties

The physical properties for the case are set in the mechanical Properties dictionary in the constant directory. Code:

```
-----*- C++ -*------
2
  / =======
3
                        / OpenFOAM: The Open Source CFD Toolbox
                        / Version: 4.1
            0 peration
4
     11
5
             A \quad n d
                        / Web:
                                  www.OpenFOAM.org
      11/
            {\tt M} anipulation
7
8
  FoamFile
9
               2.0;
10
      version
11
      format
               ascii;
               dictionary;
12
      class
13
      location
               "constant";
14
      object
               mechanicalProperties;
  }
15
16
      17
  rho
18
19
  {
20
      type
               uniform;
21
      value
               7850;
22
  }
23
24
25
  {
26
               uniform:
      type
27
               0.3;
      value
28
  }
29
30
  Ē
31
  {
32
      type
               uniform;
33
               2e+11;
      value
  }
34
35
  planeStress
36
               ves:
37
38
     39 || //
```

2.2.4 Thermal properties

In this case we do not want to solve for the thermal equation. Therefore we must set the *thermal-Stress* keyword entry to no in the *thermalProperties* dictionary.

```
3
  1
    11
            F ield
                       / OpenFOAM: The Open Source CFD Toolbox
         / O peration
                       / Version: 4.1
    1.1
4
    \\ / A nd \\/ M aninulata
5
                               www.OpenFOAM.org
  1
           Manipulation /
7
8
  FoamFile
9
  {
10
     version
              2.0;
11
             ascii;
     format
              dictionary;
12
     class
13
     location
              "constant";
             thermalProperties;
14
     object
  }
15
       16
17
18
  C
19
  {
20
              uniform;
     type
21
     value
              434;
22
  }
23
24
25
  {
26
     type
              uniform;
27
              60.5;
     value
28
  }
29
30
  alpha
31
  {
32
     type
              uniform;
33
     value
              1.1e - 05;
  }
34
35
36
  thermalStress
37
38
```

2.2.5 Control

I take this part from OpenFoam user guide. Code:

```
1 || /*-----*
2
  / =======
  / 11 /
3
           F ield
                      / OpenFOAM: The Open Source CFD Toolbox
        / O peration
/ A nd
                      / Version: 4.1
     11 /
                      / Web: www.OpenFOAM.org
5
           Manipulation /
6
     11/
7
  FoamFile
8
9
10
     version
             2.0;
11
     format
             ascii;
12
              dictionary;
             "system";
13
     location
14
     object
             controlDict;
  }
15
  16
17
18
  application
             solidDisplacementFoam;
19
20
  startFrom
              startTime;
21
22
  startTime
24 || stopAt
              endTime;
```

```
26
  endTime
              100;
27
28
  deltaT
               1;
29
30
  writeControl
              timeStep;
31
32
  writeInterval 20;
33
34
  purgeWrite
               0;
35
36
  writeFormat
              ascii;
37
38
  writePrecision 6;
39
  writeCompression off;
40
41
42
              general;
  timeFormat
43
44
  timePrecision
45
46
  graphFormat
47
48
  runTimeModifiable true;
49
50
```

2.2.6 Discretisation schemes and linear-solver control

I take this part from OpenFoam user guide. fvSchemes code:

```
2
  / =======
/ OpenFOAM: The Open Source CFD Toolbox
                     / Version: 4.1
                     / Web:
                             www.OpenFOAM.org
7
  \*-----
  FoamFile
8
9
            2.0;
10
     version
11
     format
             ascii;
            dictionary;
12
     class
13
     location
             "system";
14
     object
            fvSchemes;
15
  16
17
  d2dt2Schemes
18
19
  {
20
     default
               steadyState;
  }
21
22
23
  ddtSchemes
24
  {
25
     default
               Euler;
  }
26
27
28
  gradSchemes
29
30
     default
               leastSquares;
               leastSquares;
31
     grad(D)
               leastSquares;
     grad(T)
32
  }
33
34
  divSchemes
35
36
  {
37
     default
               none;
38
     div(sigmaD)
               Gauss linear;
39
  }
40
41 | laplacianSchemes
```

```
42 || {
43
        default
                         none;
        laplacian(DD,D) Gauss linear corrected;
44
45
        laplacian(DT,T) Gauss linear corrected;
46
    }
47
48
    interpolationSchemes
49
    {
50
        default
                         linear;
    }
51
52
53
    snGradSchemes
54
    {
55
        default
                         none;
56
    }
57
fvSolution code:
1
                                   ----*- C++ -*-----
2
3
      11
                  F ield
    1
                                    OpenFOAM: The Open Source CFD Toolbox
 4
                  0 peration
                                    Version: 4.1
5
                  A nd
                                               www.OpenFOAM.org
        11
                                    Web:
6
         11/
                  M anipulation
7
8
    FoamFile
9
10
        version
                     2.0;
11
        format
                     ascii;
12
        class
                     dictionary;
13
                     "system";
        location
14
        object
                     fvSolution;
    }
15
16
17
18
    solvers
19
    {
20
        "(D|T)"
21
        {
22
             solver
                              GAMG;
23
                              1e-08;
            tolerance
24
            relTol
                              0.9;
25
             smoother
                              GaussSeidel;
26
            nCellsInCoarsestLevel 20;
27
        }
28
    }
29
30
    stressAnalysis
31
    {
32
        compactNormalStress yes;
33
        nCorrectors
                         2;
34
                          1e-10;
35
    }
36
37
```

Here is one change in comparison to file from use guide. I have changed nCorrectors value from 1 to 2. It have positive influence on deformation result.

2.2.7 Running the code

To solve the case following lines should be executed in project directory: $solidDisplacementFoam > log \, \mathcal{C}$.

2.2.8 Post-processing

For post-processing individual scalar field components, Sigma(xx), Sigma(xy) etc., can be generated by running the postProcess:

```
postProcess -func "components(sigma)"
```

2.2.9 Results

Results are present by para View. Deformation of beam can by show by using $\mathit{Wrap\ by\ vector}$ command.

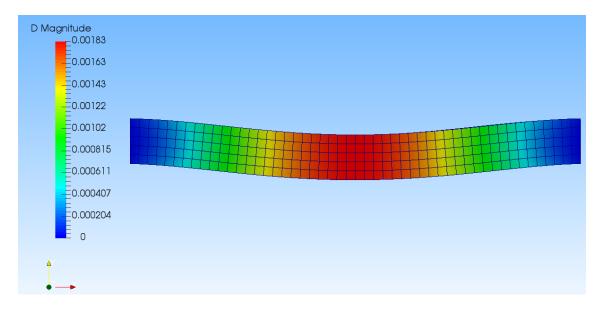


Figure 3: Deformation of a beam.

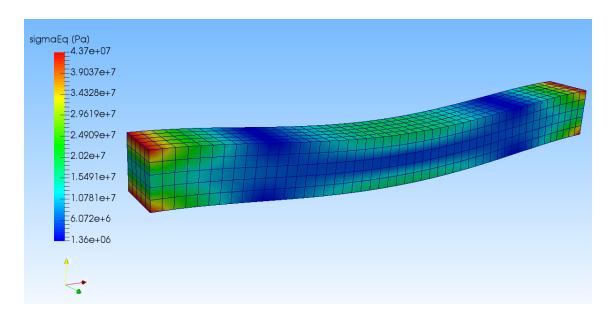


Figure 4: Equivalent stress.

2.3 Results from Ansys

Ansys in version 16.0 was used. See load and supports on Figure 5

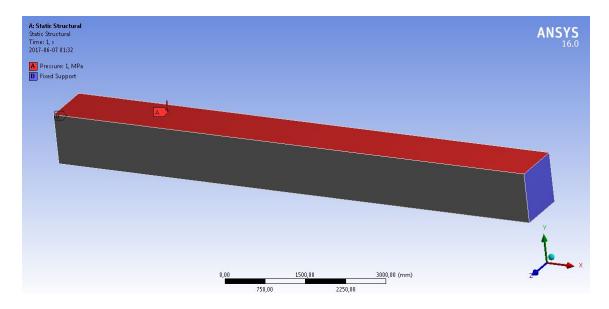


Figure 5: load and supports.

Mesh of beam is shown on Figure 6

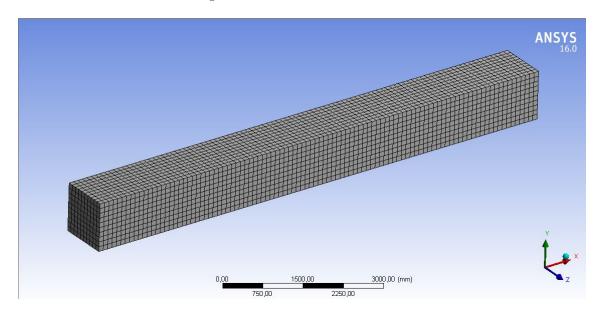


Figure 6: Division into finite elements.

Results:

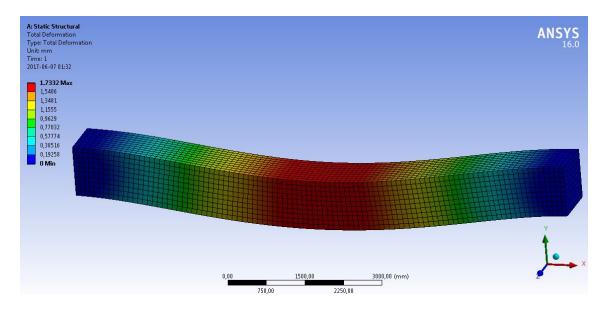


Figure 7: Deformation of a beam.

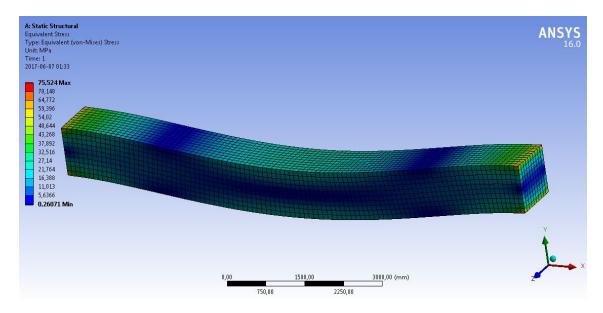


Figure 8: Equivalent stress.

3 Conclusions

Differences between results in OpenFOAM and commercial program are really small. OpenFOAM can be used to stress analysis, but each case have to be checked with lab test or anlitic calculations.