

YOUR TITLE GOES HERE

A Dissertation

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in Partial Fulfillment of the Requirements for the Degree of
Doctor of Philosophy

by

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Cornell University 2012

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BIOGRAPHICAL SKETCH

Scott Clark grew up in Tigard, Oregon and graduated from Central Catholic High School in Portland, Oregon in 2004. He recieved Bachelor of Science degrees in Mathematics, Computational Physics and Physics (Magna Cum Laude) from Oregon State University in 2008.

In 2008 Scott was awarded a Department of Energy Computational Science Graduate Fellowship (CSGF) supporting his doctoral work at Cornell University Center for Applied Mathematics (CAM). He plans to move to San Francisco after graduation and has accepted a position at Yelp Inc.

This document is dedicated to my family.
Your constant, unconditional love and support at every stage of my education
made this possible.

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Part I

ALE: Assembly Likelihood Evaluation

CHAPTER 1
ALE INTRODUCTION

CHAPTER 2

ALE METHODS

2.1 The ALE Score and the likelihood of an assembly

The ALE framework is founded upon a statistical model that describes how reads are generated from an assembly. Given a proposed assembly (a set of scaffolds or contigs), S , and a set of reads R , this probabilistic model gives the likelihood of observing this set of reads if the proposed assembly were correct. We write this likelihood, $P(R|S)$, and its calculation includes information about read quality, agreement between the mapped reads and the proposed assembly, mate pair orientation, insert length (for paired end reads), and sequencing depth. This statistical model also provides a Bayesian prior probability distribution $P(S)$ describing how likely an assembly S would be, if we were unable to observe any read information. This prior probability is computed using the k-mer distribution of the assembly.

The ALE score is computed from these two values, and it is proportional to the probability that the assembly S is correct. We write this probability as $P(S|R)$. Bayes rule tells us that this probability is

$$P(S|R) = \frac{P(R|S) P(S)}{Z} \quad (2.1)$$

where Z is a proportionality constant that ensures that $P(S|R)$ is a probability distribution. We see $P(S|R)$ as a statistical measure of the overall quality of an assembly S . As is typical in large-scale applications of Bayesian statistics, it is computationally intractable to compute the constant Z exactly. The ALE score is computed by replacing the constant Z with an approximation described in the

Methods section.

Although the ALE score can be reported as a standalone value, and understood as an approximation to $P(R \rightarrow S)$, it is most useful for comparing two different assemblies of the same genome, using the same set of reads to evaluate them. As shown in the Methods section, the assembly with the higher ALE score is then also the one with the larger probability of being correct. Moreover, we show that the difference between two assemblies ALE scores describes their relative probabilities of correctness. If one assembly's ALE score is larger than the others, with a difference of x between their ALE scores, then the assembly with the larger ALE score is more likely to be correct by a multiplicative factor of e^x . Below, we refer to the ALE score more precisely as the total ALE score, to differentiate it from the sub-scores (described below) used to construct it.

Figure 1 shows the pipeline used to compute the total ALE score. Given a set of reads and a proposed assembly, ALE first takes as input the alignments of the reads onto the assembly in the form of a SAM or BAM file (Li and Durbin 2009), which can be produced by a third-party alignment algorithm such as bowtie (Langmead et al. 2009) or bwa (Li et al. 2009). ALE then determines the probabilistic placement of each read and a corresponding placement sub-score for each mapped base, which describes how well the read agrees with the assembly. In the case of paired end reads, ALE also calculates an insert sub-score for all mapped bases of the assembly from the read pair, which describes how well the distance between the mapped reads matches the distribution of lengths that we would expect from the library. ALE also calculates a depth sub-score, which describes the quality of the sequencing depth accounting for the GC bias prevalent in some NGS techniques. The placement, insert and depth scores together

determine $P(R|S)$. Independently, with only the assembly and not the reads, ALE calculates the k-mer sub-score and $P(S)$. Each sub-score is calculated for each scaffold or contig within an assembly independently, allowing for variations commonly found in metagenomes. The four sub-scores are then combined to form the total ALE score. The constituent calculations in this pipeline are described in the Methods section.

In addition, these four sub-scores are reported by ALE as a function of position within the assembly, and can be visualized with the included plotting package or imported in table form to another package such as the Integrative Genomics Viewer (IGV) (Nicol et al. 2009), or the UCSC genome browser (Kent et al. 2002). When used in this way, these sub-scores can be used to locate specific errors in an assembly.

2.2 Probabilistic ingredients of the total ALE score

We can combine the two probabilities, $P(R|S)$ and $P(S)$, to provide an expression for the probability of the assembly given the reads, $P(S|R)$. While this combined expression is too computationally expensive to compute exactly, ALE provides a summary measure of quality called the total ALE score that is proportional to $P(S|R)$ and can be used compare assemblies.

Below, we first describe how $P(R|S)$ and $P(S)$ are computed from a set of reads R and a given assembly S . We then describe how they are combined to compute the ALE score, and how the ALE score can be used to compare the qualities of different assemblies. We first provide an overview of how $P(R|S)$ and $P(S)$ are defined and computed, beginning with $P(R|S)$ and then discussing

$P(S)$.

The statistical model from which $P(R|S)$ is calculated supposes that each paired read is generated at random from the genome or collection of genomes according to the following process. First, the distance between the two paired read ends, and their orientation, is chosen at random from a distribution that is specific to the library used to generate them. Second, the locations of the mate pairs on that genome are chosen at random, potentially with a consistent GC bias. Third and finally, the content of each of the two paired ends are generated by taking the genomes true base pairs at the chosen locations and then copying these base pairs into the reported read, with a given probability of error, insertion, or deletion for each base pair given by the sequencers quality score.

The likelihood $P(R|S)$ that results from this process can be factored into three components

$$P(R|S) = P_{placement}(R|S)P_{insert}(R|S)P_{depth}(R|S) \quad (2.2)$$

The first component, $P_{placement}(R|S)$ describes how well the reads contents match the assembly at the locations to which they are mapped. The second component, $P_{insert}(R|S)$, describes how well the distances and orientations between each paired read match the distances and orientations that we would expect from the library. The third component $P_{depth}(R|S)$ describes how well the depth at each location agrees with the depth that we would expect given the GC content at that location. Contributions to these three quantities, as a function of position in the assembly, are used to produce the placement, insert and depth sub-scores.

Together with the likelihood of the reads R given the assembly S , $P(R|S)$, the

ALE framework also depends upon a Bayesian prior probability distribution over assemblies, written $P(S)$. $P(S)$ describes how likely we would believe the assembly S to be, if we did not have any read information. In this prior probability distribution, we encode the belief that within a single genome, each k-mer has a unique k-mer frequency. This is the frequency of any set of k base pairs appearing in order in the genome. This defines a 4^k dimensional vector that is conserved across a genome and can help discover when different genomes have been mistakenly combined in a metagenome setting (Teeling et al. 2004; Woyke et al. 2006). Because $P(S)$ is determined by k-mer frequencies, we use the notation $P_{kmer}(S)$ rather than the more generic $P(S)$ when referring to this probability distribution. Contributions to $P_{kmer}(S)$ as a function of position in the genome is referred to as the k-mer sub-score.

2.2.1 Placement sub-score

$P_{placement}(R|S)$ quantifies the likelihood of observing a read r_i , or set of reads R , given an assembly S . It includes information about how the read maps onto the assembly, the quality score of each base and orientation.

We assume that every paired read is independent of all other pairs of reads, which allows us to write $P_{placement}(R|S)$ as

$$P_{placement}(R|S) = \prod_{r_i \in R} P_{placement}(r_i|S), \quad (2.3)$$

where $P_{placement}(r_i|S)$ describes how well the contents of a single read r_i match the assembly at the locations to which they are mapped, as well as how well the distance and orientation between that reads paired ends match the distance and orientation that we expect from the library. We assume independence of these

distributions, allowing us to write this as

$$P_{placement}(r_i|S) = P_{matches}(r_i|S) P_{orientation}(r_i|S). \quad (2.4)$$

$P_{matches}(r_i|S)$ measures how well the read matches the section of the assembly to which it maps. Making the assumption that each base j of the read is correctly called by the sequencer independently with a probability equal to the bases quality score Q_j , we can write this as

$$P_{matches}(r_i|S) = \prod_{base_j \in r_i} P(base_j|S) \quad (2.5)$$

where

$$P(base_j|S) = Q_j \quad (2.6)$$

when the base j correctly matches the assembly and

$$P(base_j|S) = (1 - Q_j)/4 \quad (2.7)$$

when it does not. This expression follows from our modeling assumption that all 4 possible errors that the sequencer could have reported at that base (three different substitutions and deletion) are equally likely when the read does not match the sequence. This symmetry requires each of the four possible reported errors (a base not equal to the assembly or a deletion) to have equal probability. An insertion, which does not have a corresponding base in the assembly, is modeled similarly, with the 4 in the denominator representing the uniform likelihood of observing any of the 4 possible bases on the assembly at that position. The product across all bases in a read is then equal to the total probability of observing that particular read at the given location in the assembly.

If the assembly has an unknown base at the location (denoted by an N) then we set

$$P(base_j|S) = 1/4 \quad (2.8)$$

modeling the fact that there is no information about the correct base at that location with a uniform distribution over all 4 possible bases. If an ambiguity code is reported by the sequencer then the above expression is modified to account for a distribution over the possible bases encoded by the corresponding code.

Each read is only allowed to be placed at a single position in the assembly. If the aligner placed a particular read at more than one position we choose a single position at random, weighted by $P_{placement}(r_j|S)$ score for each proposed position of the read on the assembly. This allows for repeat regions to be properly represented with the correct number of reads in expectation.

The orientation likelihood, $P_{orientation}(r_i|S)$, is calculated by first counting the number of times that each orientation occurs in each library from the mapping information. The probability that a particular read from a particular library has a particular orientation is then modeled as that orientations empirical frequency in the library (this can be overridden with user-specified values for the probabilities). The likelihood $P_{orientation}(r_i|S)$ is then the empirical frequency of the observed orientation of the read r_i in the library from which r_i belongs.

After combining these two independent probabilities we are left with the total placement score $P_{placement}(R|S)$ for a given read. Below, we use this when calculating the probability that an assembly is correct given the reads, as well as the overall total ALE score. We also use it to calculate per-base placement scores at particular positions in the assembly. The placement sub-score at a particular position is given as the geometric mean of $P(r_j|S)$ of all r_j covering that specific position,

$$\left[\prod_R P(R|S) \right]^{1/N} \quad (2.9)$$

where the product is over all reads R covering the given position, and N is the

number of such reads.

2.2.2 Insert sub-score

The insert likelihood, $P_{insert}(r_i|S)$, is determined by first observing all insert lengths from all mappings of all reads and calculating the population mean, μ , and standard deviation, σ^2 of these lengths (the mean and standard deviation can also be set by the user, if they are known). This step only needs to be done once. Once completed, we calculate the insert likelihood for each read r_i by assuming that the corresponding observed insert length L_i is distributed normally with this mean and variance, so that

$$P_{insert}(r_i|S) = Normal(L_i; \mu, \sigma^2) \quad (2.10)$$

In this expression, the insert length L_i is computed from the read r_i and its mapping to the assembly S . Similar to the placement score we can calculate the geometric mean of insert scores at a given position to come up with the insert sub-score. This can be useful for determining areas of constriction or expansion within a proposed assembly.

2.2.3 Depth sub-score

$P_{coverage}(R|S)$ describes how well the depth at each location agrees with the depth that we would expect given the GC content at that location (which is ideally Poisson-distributed (Lander and Waterman 1988)).

For each read, the GC content is the proportion of bases that are either G

or C. Modern sequencers and library preparation techniques can bias GC-rich areas of a genome (Aird et al. 2011) This bias affects the observed depth of reads mapping onto specific areas of an assembly. To correct for this bias we first calculate for each of the following 100 ranges of GC content over the average read length, 0% to 1%, 1% to 2%, ..., 99% to 100%, the average observed depth for positions in each contig in the assembly with a GC content in this range. Call $\mu_{depth(X_i)}$ the observed average depth of all reads with a GC content falling in the same range as the GC content percentage X_i . We set the minimum expected depth to be 10, discounting regions of exceptionally low average depth.

We model the depths to be Poisson distributed about a mean drawn from a Gamma distribution centered at the expected depth for that position given its GC content. This models the dependence of the expected depth on more than just the GC content at that position, such as the presence of hard stops, and the GC content at nearby positions. It results in an infinite mixture of Poissons that is equivalent to a Negative Binomial distribution. For simplicity and computational convenience, we make an independence assumption when computing this component. This causes the expected coverage at a location to depend only upon the GC content at that position, and not the GC content at nearby positions.

Then, at any given position the depth sub-score is

$$\begin{aligned}
& P_{depth}(d_j|S, X_i) \\
&= \text{Poisson}(d_j; Y_i], Y_i \sim \text{Gamma}(\max(10, \mu_{depth(X_i)}), 1) \\
&= \text{NegBinom}(d_j; \max(10, \mu_{depth(X_i)}), 1/2)
\end{aligned} \tag{2.11}$$

where the depth is d_i and where the GC content percentage X_i is averaged across all reads that map (in the placement step) to that position.

2.2.4 k-mer sub-score

$P_{kmer}(S) \propto P(S)$, the k-mer sub-score, describes the likelihood of the assembly S , in the absence of any read information. Within this prior probability distribution, we encode the belief that within a single genome, each k-mer (a permutation of k base pairs, where k is a fixed user defined number initially set to 4) has a unique k-mer frequency. This is the frequency with which the k-mer appears in the genome. The 4^k dimensional vector giving this frequency for each k-mer is conserved across a genome and can help determine if two different genomes have been mistakenly combined (Teeling et al. 2004; Woyke et al. 2006). Let K be the set of all possible unique k-mers, so $|K| = 4^k$, and for each i in K let n_i be the number of times this k-mer appears in a contig in the assembly. Then, the frequency f_i of a particular k-mer i within a contig is

$$f_i = \frac{n_i}{\sum_{j \in K} n_j} \quad (2.12)$$

The k-mer score is the product of this frequency over each k-mer appearing in each contig of the assembly S , which can be written as

$$P_{kmer}(S) = \prod_{i \in K} f_i^{n_i} \quad (2.13)$$

This is equivalent to assuming each k-mer in the assembly is drawn independently with identical distributions from a multinomial distribution with probabilities empirically estimated from the assembly.

The k-mer sub-score of a base at any given position in the assembly is the (geometric) average of $P_{kmer}(S)$ of all k-mers that cover that position. In calculating this average, the very first base in the genome only has one contributing k-mer, the second has two, up to k contributing k-mers after $k - 1$ bases.

2.3 Approximating Z

Bayes rule tells us that the probability that the assembly S is correct is

$$P(S|R) = \frac{P(R|S)P(S)}{Z} \quad (2.14)$$

where Z is a proportionality constant that ensures that $P(S|R)$ is a probability distribution, where Z is found by summing over all possible assemblies S' ,

$$Z = \sum_{S'} P(R|S')P(S') \quad (2.15)$$

Z cannot be explicitly computed because the space of all possible assemblies is far too large (4^L where L is the length of the assembly).

Instead we compute below an approximation \hat{Z} to Z . This provides an approximation to $P(S|R)$,

$$P(S|R) \approx \frac{P(R|S)P(S)}{\hat{Z}} \quad (2.16)$$

We can compare two assemblies generated from the same library of reads without calculating Z , the denominator in our Bayesian likelihood framework, because it cancels when taking the ratio of the likelihoods of the two assemblies. To determine a total ALE score for a single assembly, however, we must calculate or approximate Z . Our goal in approximating Z is to use a quantity that does not depend on the assembly S (or only depends weakly through some empirically estimated quantities included as parameters in the overarching statistical model), and is approximately of the same order of magnitude as the exact value of Z . In this section, we refer to our approximate Z as \hat{Z} , and define it as a product of terms,

$$\hat{Z} = \hat{Z}_{placement} \hat{Z}_{insert} \hat{Z}_{depth} \hat{Z}_{kmer}. \quad (2.17)$$

We define each term in this product separately.

2.3.1 Approximating $Z_{\text{placement}}$

$\hat{Z}_{\text{placement}}$ is defined as

$$\hat{Z}_{\text{placement}} = \prod_{r \in R} \hat{Z}_{\text{placement}}(r|S). \quad (2.18)$$

In this expression R is the set of reads actually observed, r is one read in this set of reads, and $\hat{Z}_{\text{placement}}(r|S)$ is defined as

$$\begin{aligned} \hat{Z}_{\text{placement}}(r|S) &= \mathbb{E} [P_{\text{placement}}(r')|S] \\ &= \sum_{r' \in R'} [P_{\text{placement}}(r'|S)]^2 \\ &= \sum_{\text{matches}} \sum_{\text{orientations}} (P_{\text{matches}}(r'|S) P_{\text{orientations}}(r'|S))^2 \end{aligned} \quad (2.19)$$

In this expression R' is the set of all possible reads of the length given by r , and we sum over all possible matches and orientations, which is analogous to summing over all possible reads. Although S appears in this expression, its value does not depend on S because of permutation symmetry. This symmetry allows us to calculate this expression analytically, without enumerating over R' . In addition to its lack of dependence of S and its ease of computation, this choice for $P_{\text{placement}}(r)$ is motivated by the belief that this quantity scales roughly like

$$P_{\text{placement}}(r) = \sum_{S'} P_{\text{placement}}(r|S') P(S'), \quad (2.20)$$

which is a quantity identical in form to Z , but restricted to the placement probability of a particular read.

2.3.2 Approximating Z_{insert}

We define

$$\begin{aligned} \hat{Z}_{\text{placement}}(r|S) &= \mathbb{E} [P_{\text{insert}}(r')|S] \\ &= \sum_{r' \in R'} [P_{\text{insert}}(r'|S)]^2 \\ &= \sum_{\text{insert}} (P_{\text{insert}}(r'|S))^2 \end{aligned} \quad (2.21)$$

Where again, in this expression R' is the set of all possible reads of the length given by r , and we sum over all possible insert lengths.

2.3.3 Approximating Z_{depth}

We define \hat{Z}_{depth} as,

$$\hat{Z}_{depth} = \prod_{base_i \in S} \hat{Z}_{depth}(X_i|S) \quad (2.22)$$

where

$$\hat{Z}_{depth}(X_i|S) = \mathbb{E} [P_{depth}(X_i|S)|S] = \sum_{d=0}^{\infty} (P_{depth}(d|X_i, S))^2, \quad (2.23)$$

where P_{depth} is defined as before. Although S appears in this expression, its value does not depend on S . We can calculate this expression analytically using a hyper-geometric function, see implementation.

2.3.4 Approximating Z_{kmer}

We define \hat{Z}_{kmer} as the expected kmer score,

$$\hat{Z}_{kmer} = \mathbb{E} [P_{kmer}(S)] = \left(\sum_{i \in K} f_i^2 \right)^N \quad (2.24)$$

where f_i , K and n_i are defined as before. This method finds the expected k-mer score for a uniform random k-mer and applies that score N times. Although \hat{Z}_{kmer} depends on S through the empirically determined f_i , which may be undesirable, this dependence follows naturally from our statistical model because the f_i are considered parameters, which are estimated from data and then treated as known by the model.

The preceding calculations allow us to approximate Z and find an absolute likelihood score for a given assembly without comparing it to another with the same library and alignment.

2.4 Relationship of the difference of total ALE scores to probability of correctness

Here we derive an expression described in the Results section for the difference of two total ALE scores in terms of the probability that an assembly is correct. Suppose we have two assemblies, S_1 and S_2 . Call A_1 the total ALE score of the first assembly, and A_2 the total ALE score of the second assembly both generated from the same set of reads R . The difference of these scores is then

$$\begin{aligned}
A_1 - A_2 &= \log(P(R|S_1)) + \log(P(S_1)) - \log(\hat{Z}) + \log(P(R|S_2)) + \log(P(S_2)) + \log(\hat{Z}) \\
&\approx \log(P(R|S_1)) + \log(P(S_1)) - \log(Z) + \log(P(R|S_2)) + \log(P(S_2)) + \log(Z) \\
&= \log\left(\frac{P(R|S_1)P(S_1)}{P(R|S_2)P(S_2)}\right)
\end{aligned} \tag{2.25}$$

2.5 Thresholding the total ALE score

In the plotting program distributed with ALE we use a thresholding algorithm to highlight potential areas of poor assembly quality using the per-base ALE scores. We do this by averaging scores within windows, allowing for the discovery of large errors in the assembly while smoothing out the noise. By the Central Limit Theorem, when we average many independent and identically

distributed random variables the result is approximately normally distributed. This allows us to create a threshold for which to delineate good scores from bad and pinpoint problematic regions. This is represented by a solid black line in the figures labeled 5σ . This line is calculated by assuming that the individual scores at each position in the assembly are drawn from a mixture of two normal distributions: one for high accuracy and another for low accuracy. We use maximum likelihood to determine the mean and variance of the two underlying distributions. The threshold is set as five standard deviations from the mean of the high accuracy distribution. This allows us to readily find areas of inaccuracy that are unlikely to be drawn from an accurate region. Five standard deviations corresponds to 1 false positive in 2 million positions if the joint normal distribution assumptions hold. The number of standard deviations at which the black line is drawn can be set from the command line by the user.

A black bar is drawn on the plot if the likelihood falls below the threshold at a significant fraction of the positions in any contiguous region with a given length (this fraction and length are user defined, and are initially set to 0.01% and 1000bp respectively) see figure XXX. These red bars correspond to regions of potential inaccuracy in the assembly that should be examined further. The plotter outputs these regions in a tab delineated text file for easy input into genome viewing software programs like IGV.

2.6 Influence of alignment input

ALE takes as input a proposed assembly and a SAM/BAM (Li 2009) file of alignments of reads onto this proposed assembly. This allows ALE to calculate the

probability of observing the assembly given the reads. ALE assumes that this mapping will include, if not all possible mappings, at least the "best" mapping for each read in the library (if such a mapping exists). For assemblies with many repeat regions (≥ 100) or libraries with large insert sizes, this can be difficult to obtain due to the bias introduced using default parameters of standard aligners. While an extensive review of alignment packages and their optimization is beyond the scope of this paper a review can be found in (Li and Homer 2010). If an assembly has many repeats and the aligner bias causes the reporting of reads only mapping to a fraction of possible regions, then ALE will see the unmapped regions as having 0 depth (no supporting reads) which will result in artificially low depth sub-scores. The robustness of ALE will still allow for comparison between assemblies with similar biases, but should be taken into account if the input to ALE is biased for only certain assemblies. To avoid this bias some mappers must be explicitly forced to search for all possible placements (-a in bowtie).

In summary, ALE determines the likelihood of an assembly given the reads and an accurate, unbiased alignment of those reads onto the assembly, without which the model assumptions are violated. These preconditions are usually met except for certain pathological genomes, and even in these cases can be readily corrected for by changing the parameters of the aligner used to make ALEs input.

CHAPTER 3
ALE RESULTS

CHAPTER 4

ALE IMPLEMENTATION

Part II

EPI: Expected Parallel Improvement

CHAPTER 5
EPI INTRODUCTION

CHAPTER 6
EPI METHODS

CHAPTER 7
EPI RESULTS

CHAPTER 8

EPI IMPLEMENTATION

Part III

Velvetrope

CHAPTER 9
VELVETROPE INTRODUCTION

CHAPTER 10

VELVETROPE METHODS

CHAPTER 11
VELVETROPE RESULTS

CHAPTER 12

VELVETROPE IMPLEMENTATION

APPENDIX A
CHAPTER 1 OF APPENDIX

Appendix chapter 1 text goes here