Merge and Select: Visualization of a likelihood based k-sample adaptive fusing

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Abstract

In this article we introduce Merge and Select — a methodology — and factorMerger — an R package — for exploration and visualization of k-group comparisons. Comparison of k-groups is one of the most important issues in exploratory analyses and is has zillions of applications. The classical solution is to test a null hypothesis, that observations from all groups come from the same distribution. If the global null hypothesis is rejected a more detailed analysis of differences among pairs of groups is performed. The traditional approach is to use pairwise post hoc tests in order to verify which groups differ significantly. But this approach fails with large number of groups in both interpretation and visualization layer. The Merge and Select methodology solves this problem by using easy to understand description of LRT based similarity among groups.

Keywords: Post-hoc testing, hierarchical clustering, likelihood ratio test

1 Introduction and Motivation

One of the most frequent tasks in exploratory analyses is the comparison of k-groups. There are zillions of applications, like comparisons of different medical treatments, comparisons of different countries, or comparisons of segments of clients. The classical solution is to test the global hypothesis, that all groups are equal. If the global null hypothesis is rejected a more detailed analysis of differences among pairs of groups is needed. The traditional approach is to perform *post hoc tests* in order to verify which groups differ significantly.

As we show later, this approach fails if the number of groups is large as the number of pairs quickly grow beyond easy interpretation. This is why in this article we introduce Merge and Select - a methodology and an R software package **factorMerger** for exploration and visualization of k-group comparisons.

The larger the number of groups, the more pronounced is the problem with classical post-hoc testing. For example, in the PISA study (*Program for International Students Assessment* 2012) data about academic performance of 15 year old kids from 65 countries is collected. One can use tests like ANOVA or other k-sample tests to verify whatever there are any differences between countries but then the question arises how counties are different. The total number of pairwise comparison is $\frac{65(65-1)}{2} = 2080$ and obviously it is not easy to present such a number of results in an easy to understand way. Figure 1, where results for only 11 European countries are presented, shows how hard it is to read anything when the number of groups is not small.

The problem with post-hoc testing is also related to the inconsistency of results. For a fixed significance level, it is possible that the mean in group A does not differ significantly from the one in group B, similarly with groups B and C. At the same time the difference between group A and C is detected. Then data partition is unequivocal and, as a consequence, impossible to put through.

To deal with this problem, we introduce the *Merge and Select* methodology along with a tool - **factorMerger** - a library for R software (R Core Team 2017). The aim of this methodology is to enrich results from *k-sample* tests together with providing the variety of plots designed for deeper understanding analyzed models. An example of Merge and Select visual presentation is presented in Figure 2.

95% family-wise confidence level

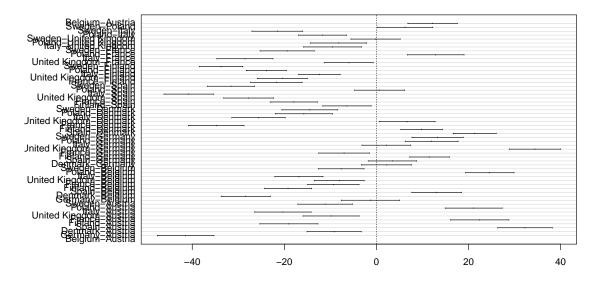


Figure 1: Classical approach to graphical presentation of post-hoc testing of 11 groups with the use of the plot.tukeyHSD function. For each pair of countries the plot presents average difference and a 95% confidence interval. Based on data from PISA 2012 study for 11 counties (55 pairs).

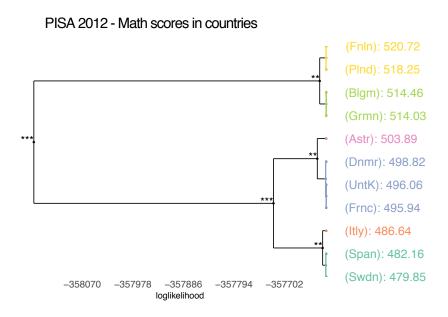


Figure 2: Merging Paths Plot for academic performance among 11 countries. The same data as in the Figure 1 is used. Such plot is much easier to read and interpret.

The aim of **factorMerger** package is to provide informative and easy to understand visualizations of post-hoc comparisons. It works for wide spectrum of probability distribution families of dependent variable as it is based on linear model with Gaussian outcome, generalized linear model with binomial outcome and Cox proportional hazard model with censored outcome. The *Merging Path Plots* (MPP) show consistent and non-overlapping adaptive fusing of groups based on the likelihood ratio test (LRT) statistics. In addition, the Generalized Information Criterion (GIC) is presented for fused models. This criterion may be used to choose the optimal fusion of groups.

2 Background and Related Work

One may find implementations of the traditional post hoc tests in many R packages (R Core Team 2017). For example, package agricolae (de Mendiburu 2016) offers a wide range of them. It gives one of the most popular post hoc test, Tukey HSD test (function HSD.test), its less conservative version — Student-Newman-Keuls test (function SNK.test) or Scheffe test (function scheffe.test) which is robust to group imbalance. These parametric tests are based on Student's t-distribution, thus, are reduced to Gaussian models only. In contrasts, multcomp package (Hothorn et al. 2008) can be used with generalized linear models (function glht) as it uses general linear hypothesis. Similarly to the multcomp, some implementations that accept glm objects are also given in car (linearHypothesis, Fox & Weisberg 2011) and lsmeans (Lenth 2016).

But what about the problem of clustering categorical variable into non-overlapping groups? It has already been present in the literature. First, J. Tukey proposed an iterative procedure of merging factor levels based on the studentized range distribution (Tukey 1949). However, again, statistical test used in this approach made it limited to Gaussian models.

Collapse And Shrinkage in ANOVA (CAS-ANOVA, Bondell & Reich 2008) is an algorithm that extends categorical variable partitioning for generalized linear models. It is based on the Tibshirani's Fused LASSO (Tibshirani et al. 2005) with constraints taken on pairwise differences within a factor, which yields to their smoothing. Yet another approach that is also adjusted to generalized linear models is presented by Delete or Merge Regressors algorithm (DMR4glm, Prochenka 2016). It directly uses the agglomerative hierarchical

clustering (Peter Rousseeuw & Leonard Kaufman 1990) to build a hierarchical structure of groups that are being compared. Experimental studies (Prochenka 2016) show that *Delete or Merge Regressors*'s performance is better than *CAS-ANOVA*'s when it comes to the accuracy of the resulting model. The *Delete or Merge Regressors* method was first implemented in the **DMR** R package (Maj et al. 2013) and is reimplemented for broader number of model families in the **factorMerger** package.

The approach presented in this article extends approaches presented above in following ways:

- in comparison to pairwise tests Merge and Select is easier to interpret.
- the **factorMerger** tree is created based on **ggplot2** (Wickham 2009) graphics and is easy to customize.
- in comparison to Fused LASSO, the **factorMerger** is based on the likelihood ratio test statistic, which has known asymptotic properties. This allows to calculate p-values for selected pairs of groups.
- in comparison to Fused LASSO the obtained group effects (like averages) are not biased and are easier to interpret.
- in comparison to **DMR** the modeling can be applied to wider variety of regression models, like generalized linear models and survival regression models.
- as we will show later, in comparison to **DMR** the resulting structure of groups is more stable.

In the next section we will present the methodology beyond **factorMerger** package.

3 Merging Path Plots

Let k stands for the number of groups, while n_i stands for the number of observations in group $i \in \{1, ..., k\}$. Let y_{ij} denote an observed value of variable of interest for observation $j \in \{1, ..., n_i\}$ in group i. We assume that $y_{ij} \sim F(\theta_i)$, where F is a distribution from exponential family parametrized by $\theta \in \Theta$.

The global null hypothesis is

$$H_0: \forall_{i \in \{1,\dots,k\}} \theta_i = \theta_1$$

and can be tested with the Likelihood Ratio Test for k samples. If the global null hypothesis is rejected, then in the post-hoc analysis we are looking for groups with equal distributions, that is sets of indexes J such as $\forall_{i,j\in J}\theta_i=\theta_j$

In **factorMerger** these sets are obtained in an iterative fashion. In every step two groups are merged into a single one. This step is repeated as long as there is more than one group. The general sketch of the algorithm is described below.

The merging procedure begins with a full model — with all original groups — and iteratively merges a pair of groups until all of them are combined. For considered families of distributions we use generalized linear models or Cox proportional hazard model. Each merging of two groups reduces by one the number of degrees of freedom of a model. In a single iteration pairs worth fusing are considered and the one which optimizes an objective function is merged. In general any model statistic may be used as an objective function, but here we are using the likelihood statistic. We will specify it in details in the next section. A general formulation of the merging procedure is described in Algorithm 1.

Algorithm 1 The outline of Merge and Select algorithm implemented in factorMerger

function MERGEFACTORS (responseVariable, groupingVariable, adjacent)

- 4: **while** $|levels(groupingVariable)| \ge 1$ **do** pairsSet := generatePairs(groupingVariable, responseVariable, adjacent)
- 6: $selectedPair := argmax_{pair \in pairsSet} objectiveFunction(pair, responseVariable, groupingVariable)$

groupingVariable := mergeLevels(groupingVariable, selectedPair)

- 8: currentModel := createModel(responseVariable, groupingVariable)mergingPath := add(mergingPath, currentModel)
- 10: **end while** return(mergingPath)

12: end function

The result of the Algorithm 1 is the list of k shrinking models \mathcal{M}_i , where $i \in \{1, ..., k\}$. These models are presented in a graphical way in a *Merging Path Plot* along with diagnostic criteria like Generalized Information Criteria and graphical summaries. The proposed plot contains four panels, that contain all important information in a compact form. An example of these panels is presented in the Figure 3.

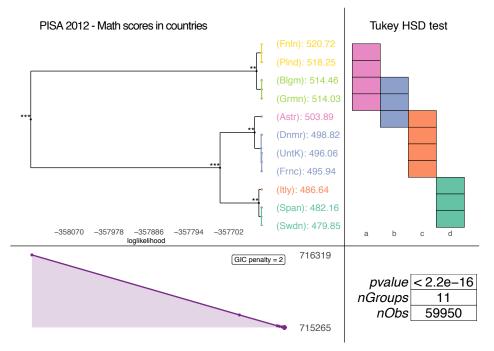
The statistics presented in this plot are described in following subsections.

A. The Merging Paths Plot panel

Shows the hierarchical structure of similarity between groups. Stars presents how significant are differences between two clusters. Height of the join corresponds to the likelihood of the combined model.

B. The response panel

Shows graphical summaries for group separately. Use the responsePanel argument to select the desired summary.



C. The GIC panel

Shows the *Generalized Information Criterion* for all models in MPP panel. Default *penalty*=2 corresponds to the AIC criterion. Colours in the MPP panel corresponds to the optimal model.

D. The summary panel

Shows the no. groups, no. observations, and the p-value for global hypothesis that parameter of interest is equall in all groups.

Figure 3: Four panels of the **factorMerger**'s visualization for the PISA dataset for 11 countries. Panel A summaries the structure of group similarities. It shows the list of models returned in the Algorithm 1. The OX axis presents values of log-likelihood function for each model from the list. Labels on the right margin presents averages of variable of interest for different groups. Stars in different joins of the tree summarize pairwise tests for selected groups of variables. Panel B summarizes the distribution of variable of interest in each group. The summary plotted in this panel may be changed depending of the model family. Panel C shows the Generalized Information Criteria for each model from the list. Panel D presents results from the test for global null hypothesis. Colors in panels A and B are consistent and correspond to optimal segmentation of groups based on GIC score.

3.1 Model families

The Merge and Select algorithm can be performed for any likelihood based model. Current version of the **factorMerger** package supports following parametric models:

• one-dimensional Gaussian (with the argument family = "gaussian"). Here

$$y_{ij} \sim \mathcal{N}\left(\mu_j, \sigma^2\right)$$

and corresponding logarithm of likelihood

$$l(\mu, \sigma | y) = -\frac{n}{2} \log(2\pi) - \frac{n}{2} \log(\sigma^2) - \sum_{j=1}^{k} \sum_{i=1}^{n_j} \frac{1}{2} (y_{ij} - \mu_j)^2 / \sigma^2.$$

Group summaries are averages – maximum likelihood estimates for μ_i .

• n-dimensional Gaussian (with the argument family = "gaussian"). Here Y_{ij} and M_j are vectors and

$$Y_{ij} \sim \mathcal{N}\left(M_j, \Sigma\right)$$
.

The corresponding logarithm of likelihood function

$$l(M, \Sigma|Y) = -\frac{n}{2}\log(2\pi) - \frac{n}{2}\log(|\Sigma|) - \sum_{j=1}^{k} \sum_{i=1}^{n_j} \frac{1}{2} (Y_{ij} - M_j)^T \Sigma^{-1} (Y_{ij} - M_j).$$

Note that, both one-dimensional and n-dimensional Gaussian models use family = "gaussian". However, the visual summary of n-dimensional data requires additional preprocessing – dimensionality reduction – thus, it is considered as a separate category. Group summaries are averages.

• binomial (with the argument family = "binomial"). Here

$$y_{ij} \sim \mathcal{B}(p_j, 1)$$
.

After adding the logit link function

$$\log\left(\frac{p_j}{1-p_j}\right) = \beta_j$$

one may write the logarithm of likelihood

$$l(\beta|y) = \sum_{j=1}^{k} \sum_{i=1}^{n_j} y_{ij} \beta_j - y_{ij} \log(1 + \exp \beta_j) + (1 - y_{ij}) \log(1 + \exp \beta_j).$$

Group summaries are proportions of successes as estimates of p.

• survival (with the argument family = "survival"). Here we consider the Cox proportional hazard model (Cox 1992). Let $\lambda_0(t)$ be the baseline hazard function, where t denotes time. Then the hazard function for group j may be expressed as

$$\lambda_i(t) = \lambda_0(t) \cdot \exp(\alpha_i).$$

Corresponding logarithm of partial likelihood is

$$l(\alpha|y) = \sum_{i,j:C_{ij}=1} \left(\alpha_j - \log \left(\sum_{kl:y_{kl} \ge y_{ij}} \exp(\alpha_k) \right) \right).$$

where C_{ij} is the censoring status, $C_{ij} = 1$ means that the observation i from group j is not censored. For this model hazard ratios are the group summaries.

The fusing algorithm that is used in Merge and Select is based on the Likelihood Ratio Test statistic defined as

$$LRT(\mathcal{M}_1; \mathcal{M}_2) = 2 \cdot l(\widehat{\beta_{\mathcal{M}_2}}|y) - 2 \cdot l(\widehat{\beta_{\mathcal{M}_1}}|y), \tag{1}$$

where \mathcal{M}_1 and \mathcal{M}_2 are two nested models. Each model corresponds to a grouping of observations. Groupings for both models are equal except that two groups in \mathcal{M}_2 are merged in one group in \mathcal{M}_1 . The higher the $LRT(\mathcal{M}_1; \mathcal{M}_2)$, the more different are the merged groups. One may interpret the $LRT(\mathcal{M}_1; \mathcal{M}_2)$ as a distance between groups for model \mathcal{M}_1 and \mathcal{M}_2 .

The advantage of the LRT statistic is the known asymptotic behavior (see Wilks 1938). For nested models \mathcal{M}_2 a \mathcal{M}_1 that differs by one degree of freedom it holds

$$LRT(\mathcal{M}_1; \mathcal{M}_2) \stackrel{n \to \infty}{\sim} \chi_1^2$$
.

This asymptotic distribution is used in **factorMerger** to present statistical significance of group joins with the argument panelGrid = TRUE of the plot.factorMerger function.

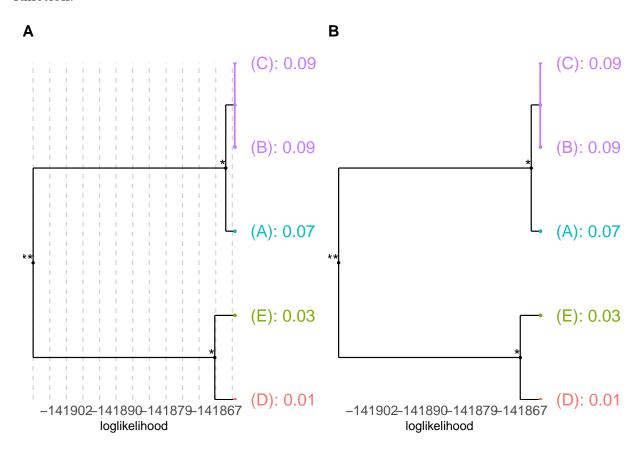


Figure 4: Tree plots with panel grid (Panel A) and without panel grid (Panel B). In Panel A each interval in the OX axis corresponds to the 0.95 quantile of chi-square distribution with one degree of freedom. Models distant more than this interval may be considered as significantly different

3.2 Group summaries

The right panel of the visualization shows graphical summaries of variable of interest in groups. Use the responsePanel argument to choose how groups shall be presented.

Available options are presented in the Figure 5. Depending on the family of the variable of interest different summaries are appropriate. Possible combinations are presented in the Table 1.

		family	
${\bf response Panel}$	gaussian	binomial	survival
frequency	+	+	+
means	+		
boxplot	+		
tukey	+		
heatmap	+		
profile	+		
proportion		+	
survival			+

Table 1: Different types of graphical summary are appropriate for different model families. Pluses denote which responsePanel may be used for which model family. Examples for each type of panel are presented in the Figure 5.

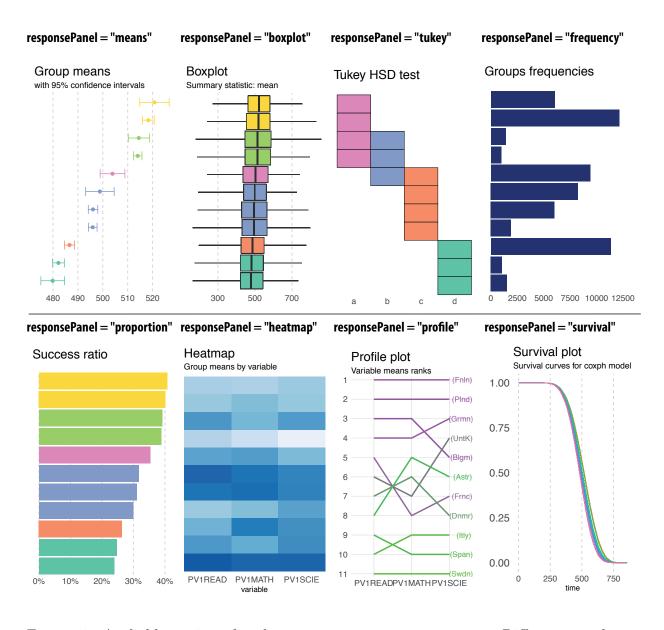


Figure 5: Avaliable options for the responsePanel argument. Different panels are designed to highlight different aspects of groups.

3.3 Optimal grouping selection

The fusing algorithm returns a collection of models of different sizes / different optimal numbers of groups. In order to select the best model first the optimization criterion must be specified. There are three metrics available in **factorMerger**:

- Generalized Information Criterion parameterized by the penalty. If this option is chosen, the model with the lowest GIC is returned.
- p-value for the Likelihood Ratio Test against the full model. If we go with this metric we choose the latest model in the merging path whose p-value for the LRT test against the full model is greater than a given threshold.
- log-likelihood of a model. Similar search is performed as in the previous point, but with models log-likelihood as a model score.

The most natural approach is to pick a model that minimizes the Generalized Information Criteria

$$GIC(\mathcal{M}) = -2l(\mathcal{M}) + p|\mathcal{M}|.$$

Here $|\mathcal{M}|$ denotes the number of groups in model, \mathcal{M} while p is a penalty for model complexity. GIC corresponds to Akaike Information Criterion (AIC) for p = 2 or Bayesian Information Criterion (BIC) for $p = \log(n)$.

To make it easier to select the best model the bottom-left panel presents GIC scores for models in the merging path in the GIC plot. An example of such plot is presented in the Figure 6.

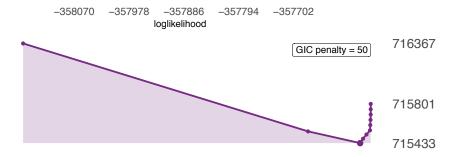


Figure 6: The GIC plot. OX axis corresponds to the log-likelihood for a model. OY axis corresponds to the GIC score for a model. Each dot denotes a single model from the merging path. GIC scores for the best, smallest and largest models are presented in the right axis.

3.4 The Fusing Strategy

The Algorithm 1 presents a general strategy for merging groups. The fully adaptive strategy is time consuming and may be slow for the large number of groups. Thus in the **factorMerger** package we have implemented four versions of the merging algorithms. These versions are summarized below.

Depending on the specific goal some steps of the Algorithm 1 may be performed differently. Possible options are:

- method = "adaptive". The objective function is the logarithm of likelihood. The set pairsSet contains all possible pairs of groups available in a given step. Pairwise LRT distances are recalculated every step. This option is the slowest one since it requires the largest number of comparisons. It requires $O(k^3)$ model evaluations.
- method = "fast-adaptive". Note that computing an objective function can be expensive and, especially for big datasets, it may be beneficial to limit the set of pairs that shall be compared. Also note that it is more likely that a pair of levels i and j will be chosen to merge if corresponding group averages are close. In this option, the objective function is the logarithm of likelihood, but the pairsSet is generated differently, in a following way. For Gaussian family of response, at the very

beginning, the groups are ordered according to increasing averages and then pairsSet contains only pairs of closest groups. For other families the order corresponds to beta coefficients in a regression model. The detailed rules of ordering levels are given in the Table 2. This option is much faster than method = "adaptive" and requires $O(k^2)$ model evaluations.

- method = "fixed". This option is based on the DMR algorithm introduced in Prochenka (2016). It was extended to cover survival models. The largest difference between this option and the method = "adaptive" is, that in the first step a pairwise distances are calculated between each groups based on the LRT statistic. Then the agglomerative clustering algorithm is used to merge consecutive pairs. It means that pairwise model differences are not recalculated as LRT statistics in every step but the complete linkage is used instead. This option is very fast and requires $O(k^2)$ comparisons.
- method = "fast-fixed". This option may be considered as a modification of the method = "fixed". Here, similarly as in the "fast-adaptive" version, we assume that if groups A, B and C are sorted according to their increasing beta coefficients, then it is worthwhile to join groups A and B or groups B and C (but not groups A and C). This assumption enables to implement the complete linkage clustering more efficiently in a dynamic manner. The biggest difference is that in the first step we do not calculate the whole matrix of pairwise differences, but instead only the differences between consecutive groups. Then in each step only a single distance is calculated. This reduces the number of model evaluations to O(k). Detailed description of beta coefficient is given in the Table 2.

family	ordering statistic for a given group	
one-dimensional Gaussian	average in a group	
multi-dimensional Gaussian	average in a group after the Kruskal's non-metric	
	multidimensional scaling (Venables & Ripley 2002)	
	to a one-dimensional space	
binomial	proportion of successes in a group	
survival	logarithm of a hazard ratio for a group	

Table 2: Factor ordering by model family for method = "fast-adaptive" and method = "fast-fixed"

Described options differ in two ways. First, they differ in terms of computational time. The fastest option is to preliminarily sort groups and then use the dynamic complete-linkage hierarchical algorithm which enables to join only adjacent groups. The slowest option is to calculate pairwise differences between groups after each fusion. Time performance comparisons are presented in Figure 7.

At the same time, the slowest option is the most accurate one, in terms that it gives models paths with highest log-likelihoods and is stable. Simple example that brings closer those characteristics is visualized in the Figure 8.

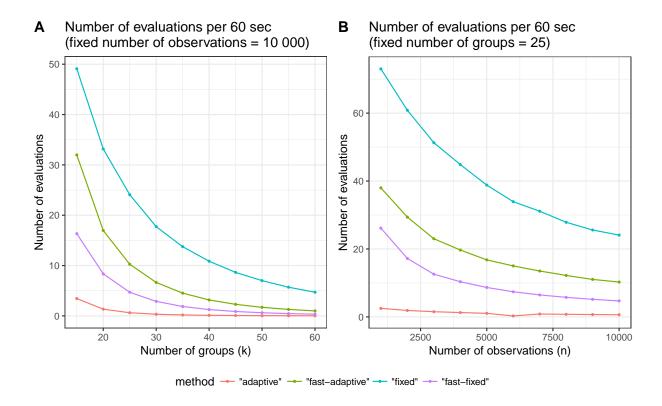


Figure 7: Average number of evaluations per 60 seconds for different number of groups (Panel A) and different sample sizes (Panel B). Fastest algorithms are those which limit comparisons only to consecutive groups ("fast-adaptive" and "fast-fixed"). For 10 observations methods "fast-fixed" and "fast-adaptive" are 5 times faster than method "adaptive". For 60 observations those evaluation time ratios grow up to 200 and 42, respectively for "fast-fixed" and "fast-adaptive" against "adaptive".

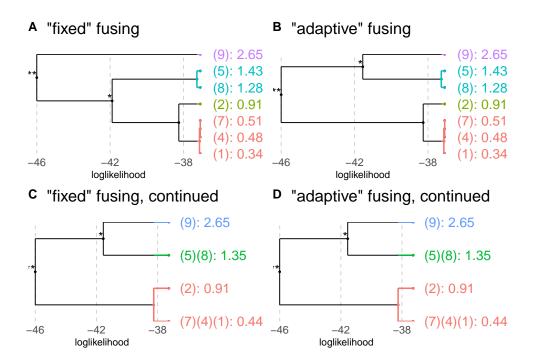


Figure 8: A comparison of methods "fixed" (left panels) and "adaptive" (right panels). We start with a sample consisting of 7 subgroups (top panels). First four steps of both algorithms are the same, but then the "fixed" algorithm chooses to merge groups (8)(5) and (9), while the "adaptive" algorithm goes with groups (1)(4)(7)(2) and (8)(5). The latter results in a model with higher log-likelihood ("fixed": -41.57 vs. "adaptive": -41.89). Note that if we choose different starting point (bottom panels) the "fixed" algorithm changes its path.

4 Examples

The **factorMerger** package is highly customizable. In this section we present three different case studies to illustrate the use of **factorMerger** in real world examples. Each scenario is associated with a particular model family and also presents specific function arguments in action.

4.1 Gaussian models - what can you do with factorMerger?

PISA (Program for International Students Assessment 2012) is a program maintained by OECD to gather information on students' performance on various cognitive tests in countries around the world. Based on multiple survey results so-called plausible values are modeled which resemble individual test scores of students and can be used as a comparable measure. Those values are calculated in three different fields: mathematics, science and reading. Moreover, plausible values are normally distributed in the population have conditionally Gaussian distribution.

The **factorMerger** package provides a student-level dataset (data("pisa2012")) which contains all tree plausible values, together with country affiliations. This data is a weighted version of the original data from the **PISA2012lite** package (Biecek 2015). A total number of rows is 271322 and a total number of groups is 43.

Let us assume that we have only one explanatory variable, country, which we want to use to predict students' plausible values in mathematics.

```
library(factorMerger)

library(dplyr)

data("pisa2012")

# we use "fast-fixed" method to boost evaluation time oneDimPisa <- mergeFactors(response = pisa2012$math, factor = pisa2012$country, method = "fast-fixed")</pre>
```

Note that it is only one command needed to perform the merging procedure.

We can use the obtained object to display the history of merging — each row of the table describes one step of the algorithm.

```
mergingHistory(oneDimPisa, showStats = TRUE) %>%
        head(5)
    groupA groupB
                     model pvalVsFull pvalVsPrevious
 0
                   -1606256
                                1.0000
                                                1.0000
 1 (Swdn) (SlvR) -1606256
                                0.9932
                                                0.9932
   (RssF) (Span) -1606256
                                0.9997
                                                0.9805
 3 (Chil) (Mlys) -1606256
                                                0.9459
                                0.9999
# 4 (Frnc) (UntK) -1606256
                                1.0000
                                                0.9213
```

Here, in the second step Russian Federation (RssF) and Spain (Span) were united. Log-likelihood, whose value is given in the model column, decrease was marginal, p-values for the LRT test against the full model and against the previous model were 0.9999 and 0.9325, respectively. This means that the data partition created after two joins is equally good as the previous one and as the initial one.

Let us create a data partition based on the model with the lowest AIC in the merging path (GIC penalty = 2). Final grouping names are concatenations of original levels names.

We can also see the final data partition. Below original abbreviated group labels are printed (orig) together with their final cluster name (pred). For example, Poland (Plnd) ends up in the (Cand) (Plnd) group, which consists of two members: Poland and Canada (Cand).

```
getOptimalPartitionDf (oneDimPisa,
```

4.2 The binomial model - GIC manipulation

This section uses a dataset included in the **factorMerger** package (data("ess")) on happiness of 21 European countries based on the European Social Survey (*European Social Survey 2014*). A binary variable called *happy* specifies if a given individual considers themselves a happy person (or, more precisely, his/her answer for the question "Taking all things together, how happy would you say you are?" was greater than 5 in a scale of 0 to 10). Again, data is weighted according to original weights given by ESS. A total number of rows in ess is 200075, there are 21 countries included.

By default the plot.factorMerger function uses GIC with the penalty equal to two (Akaike Information Criterion). However, in some cases it may not be restrictive enough. Since the number of observation is large, we may use large GIC penalty, like 500.

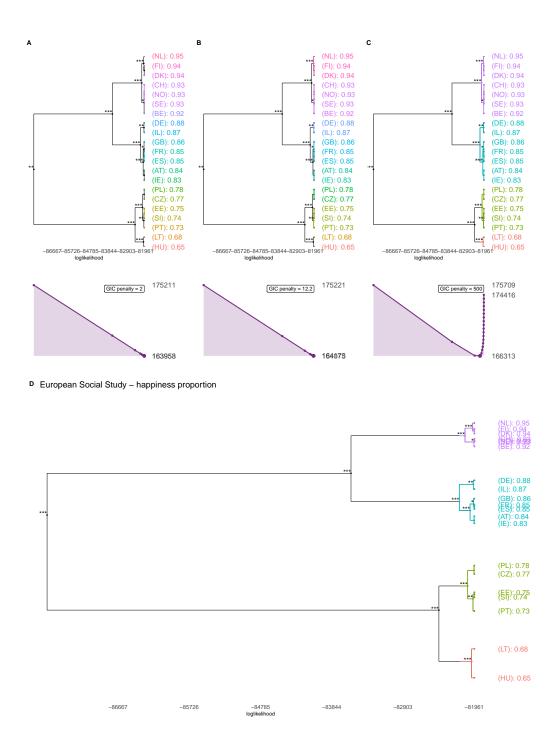


Figure 9: Results for GIC with different penalties: AIC with penalty = 2 (Panel A), BIC with penalty = 12.2 (Panel B) and GIC with penalty = 500. Optimal numbers of groups for those penalties are: 17, 9, 4. The tree panel for GIC with penalty = 500 is presented in Panel D. Nodes positions on OY axis correspond to fractions of happy citizens in given country / groups of countries.

4.3 The survival model - customization of the visualization

In this example we use data from the The Cancer Genome Atlas Project (*The Cancer Genome Atlas Wiki* 2015) from the **RTCGA.clinical** package (Kosinski 2016). TCGA is a public funded project that aims to catalogue and discover major cancer-causing genomic mutations to create a comprehensive *atlas* of cancer profiles. The **RTCGA.clinical** package provides a snapshot of those clinical data created at 2015-11-01. In our example we focus on patients who suffer from breast cancer and are treated with different drugs. We are interested whether drug treatments may be grouped according to their effectiveness.

The sataset used in this example is also included in the **factorMerger** package (data ("BRCA")). First, some data preprocessing is performed.

Now we can plot the result. By default four panels are included in the plot, the tree is colored to denote final clusters, nodes are spaced using equal distance.

Let's add some customization!

```
plot (drugMerge,
    # show groups' effects in the tree
    nodesSpacing = "effects",
    # add custom title
    title = "BRCA: _patient _survival _vs._drug_treatment",
    # display only two panels
    panel = "response",
    # do not color clusters
    colorClusters = FALSE,
    # mark optimal model with a vertical line
    showSplit = TRUE,
    # set your favorite RColorBrewer palette
    palette = "Dark2")
```

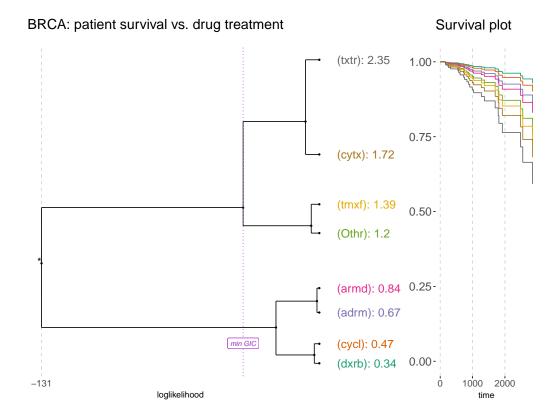


Figure 10: Customized plot.factorMerger output. Colors of OY axis' labels are guides for the right panel. Tree nodes are spaced according to group effects. A vertical line is added to mark the optimal data partition.

5 Summary and Future Directions

Merge and Select is a novel approach to summarize groups similarities based on the LRT statistic. It is a useful tool to explore group similarities in k-sample problems.

In this article we have presented the methodology and that applications of this methodology as it is implemented in the **factorMerger** R package. Currently the implementation is limited to a single grouping variable. The natural extension of this approach is related to including more grouping variables, possibly with interactions. Other possible updates are related to different classes of models. Instead of the Likehood Ratio Test other tests may be used. For example, the Wilcoxon test may be used for semi-parametric modeling.

Even with these limitations **factorMerger** is a useful tool for exploratory analysis as it helps to summarize structure of groups' in a single plot.

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PBI: Wewntrzne recenzje: BMIA? PTSE? APRO?

PBI: Doda uchwyty archivista

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