## Tarea 10 - Descomposición LU

```
%load_ext autoreload
import numpy as np
from src import multiplicar_matrices, descomposicion_LU, resolver_LU
from src import eliminacion_gaussiana_L,eliminacion_gaussiana_U, determinante, inversa
```

## Conjunto de Ejercicios

1. Realice las siguientes multiplicaciones matriz-matriz:

a.

$$\begin{bmatrix} 2 & -3 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} 1 & 5 \\ 2 & 0 \end{bmatrix}$$

```
%autoreload 2
A = np.array([[2,-3],[3,-1]])
B = np.array([[1,5],[2,0]])
C = multiplicar_matrices(A,B)
print("El resultado de la multiplicación es: \n",C)
El resultado de la multiplicación es:
 [-4 10]
 [ 1 15]]
b.
                                                 \begin{bmatrix} 2 & -3 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} 1 & 5 & -4 \\ -3 & 2 & 0 \end{bmatrix}
```

```
%autoreload 2
A = np.array([[2,-3],[3,-1]])
B = np.array([[1,5,-4],[-3,2,0]])
C = multiplicar_matrices(A,B)
print("El resultado de la multiplicación es: \n",C)
```

El resultado de la multiplicación es: [[ 11 4 -8] [ 6 13 -12]]

c.

$$\begin{bmatrix} 2 & -3 & 1 \\ 4 & 3 & 0 \\ 5 & 2 & -4 \end{bmatrix} \begin{bmatrix} 0 & 1 & -2 \\ 1 & 0 & -1 \\ 2 & 3 & -2 \end{bmatrix}$$

```
%autoreload 2
A = np.array([[2,-3,1],[4,3,0],[5,2,-4]])
B = np.array([[0,1,-2],[1,0,-1],[2,3,-2]])
C = multiplicar_matrices(A,B)
print("El resultado de la multiplicación es: \n",C)
El resultado de la multiplicación es:
```

```
[[-1 5 -3]
[ 3 4 -11]
[-6 -7 -4]]
```

d.

$$\begin{bmatrix} 2 & 1 & 2 \\ -2 & 3 & 0 \\ 2 & -1 & 3 \end{bmatrix} \begin{bmatrix} 1 & -2 \\ -4 & 1 \\ 0 & 2 \end{bmatrix}$$

```
%autoreload 2
A = np.array([[2,1,2],[-2,3,0],[2,-1,3]])
B = np.array([[1,-2],[-4,1],[0,2]])
C = multiplicar_matrices(A,B)
print("El resultado de la multiplicación es: \n",C)
```

El resultado de la multiplicación es:

```
[[ -2 1]
[-14 7]
[ 6 1]]
```

2. Determine cuáles de las siguientes matrices son no singulares y calcule la inversa de esas matrices:

a.

$$\begin{bmatrix} 4 & 2 & 6 \\ 3 & 0 & 7 \\ -2 & -1 & -3 \end{bmatrix}$$

```
%autoreload 2
A = np.array([[4,2,6],[3,0,7],[-2,-1,-3]])
det = determinante(A)
if(det==0):
    print("El determinante es:",det, "\nPor tanto, la matriz es singular y no posee inversa")
else:
    inv = inversa(A)
    print("El determinante es:",det, "\nSu matriz inversa es la siguiente:", inv)
```

El determinante es: 0

[ 0.125 -0.625 0.375]]

Por tanto, la matriz es singular y no posee inversa

b.

$$\begin{bmatrix} 1 & 2 & 0 \\ 2 & 1 & -1 \\ 3 & 1 & 1 \end{bmatrix}$$

c.

$$\begin{bmatrix} 1 & 1 & -1 & 1 \\ 1 & 2 & -4 & -2 \\ 2 & 1 & 1 & 5 \\ -1 & 0 & -2 & -4 \end{bmatrix}$$

```
%autoreload 2
A = np.array([[1,1,-1,1],[1,2,-4,-2],[2,1,1,5],[-1,0,-2,-4]])
det = determinante(A)
if(det==0):
    print("El determinante es:",det, "\nPor tanto, la matriz es singular y no posee inversa")
else:
    inv = inversa(A)
    print("El determinante es: ",det, "\nSu matriz inversa es la siguiente: ", inv)
El determinante es: 0
Por tanto, la matriz es singular y no posee inversa
d.
                                           \begin{bmatrix} 4 & 0 & 0 & 0 \\ 6 & 7 & 0 & 0 \\ 9 & 11 & 1 & 0 \\ 5 & 4 & 1 & 1 \end{bmatrix}
%autoreload 2
A = np.array([[4,0,0,0],[6,7,0,0],[9,11,1,0],[5,4,1,1]])
det = determinante(A)
if(det==0):
    print("El determinante es:",det, "\nPor tanto, la matriz es singular y no posee inversa")
    inv = inversa(A)
    print("El determinante es: ",det, "\nSu matriz inversa es la siguiente: \n", inv)
El determinante es: 27.9999999999993
Su matriz inversa es la siguiente:
 [[0.25]
                 0.
                                                       ]
 [-0.21428571 0.14285714 0.
                                           0.
                                                      ]
                                                      ]
 [ 0.10714286 -1.57142857 1.
 [-0.5]
                                                      11
                1.
```

3. Resuelva los sistemas lineales 4 x 4 que tienen la misma matriz de coeficientes:

$$\begin{array}{lll} x_1-x_2+2x_3-x_4=6, & x_1-x_2+2x_3-x_4=1, \\ x_1 & -x_3+x_4=4, & x_1 & -x_3+x_4=1, \\ 2x_1+x_2+3x_3-4x_4=-2, & 2x_1+x_2+3x_3-4x_4=2, \\ -x_2+x_3-x_4=5, & -x_2+x_3-x_4=-1, \end{array}$$

Ya que ambos sistemas poseen la misma matriz de coeficientes

$$A = \begin{bmatrix} 1 & -1 & 2 & -1 \\ 1 & 0 & -1 & 1 \\ 2 & 1 & 3 & -4 \\ 0 & -1 & 1 & -1 \end{bmatrix}$$

primero realizaré la descomposición LU para usarla posteriormente para resolver cada sistema.

```
%autoreload 2
A = [[1,-1,2,-1],[1,0,-1,1],[2,1,3,-4],[0,-1,1,-1]]
L,U = descomposicion_LU(A)
print("Matriz L:\n",L)
print("Matriz U:\n",U)
```

```
Matriz L:
 [[ 1. 0.
             0. 0. ]
              0.
 [ 1.
         1.
                     0. ]
                     0. ]
 [ 2.
         3.
               1.
 [ 0.
       -1.
              -0.25 1. ]]
Matriz U:
 [[ 1. -1. 2. -1.]
 [ 0. 1. -3. 2.]
 [ 0. 0. 8. -8.]
 [ 0. 0. 0. -1.]]
%autoreload 2
b_1 = [6,4,-2,5]
sol_1 = resolver_LU(L,U,b_1)
Calculando y
[ 6. -2. -8. 1.]
Verificación Ly=b:
[ 6. 4. -2. 5.]
Calculando x
[ 3. -6. -2. -1.]
Verificación Ux=y:
[ 6. -2. -8. 1.]
%autoreload 2
b_2 = [1,1,2,-1]
sol_2 = resolver_LU(L,U,b_2)
Calculando y
[ 1. 0. 0. -1.]
Verificación Ly=b:
[ 1. 1. 2. -1.]
Calculando x
[1. 1. 1. 1.]
Verificación Ux=y:
[ 1. 0. 0. -1.]
Por tanto, la soluciones obtenidas son: sol_1 = [3, -6, -2, -1] y sol_2 = [1, 1, 1, 1]
```

4. Encuentre los valores de A que hacen que la siguiente matriz sea singular

$$A = \begin{bmatrix} 1 & -1 & \alpha \\ 2 & 2 & 1 \\ 0 & \alpha & -\frac{3}{2} \end{bmatrix}$$

$$\det(A) = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{2} \left( \frac{2(-\frac{3}{2})}{2} - \frac{1}{2} (\alpha) \right) - \frac{1}{2} \left( \frac{-1}{2} (-\frac{3}{2}) - (\alpha) (\alpha) \right)$$

$$= (-3 - \alpha) - \frac{1}{2} (\frac{3}{2} - \alpha^2)$$

$$= -3 - \alpha - 3 + 2\alpha^2$$

$$= 2\alpha^2 - \alpha - 6 = (\alpha - 2)(2\alpha + 3) = 0$$
Para que sea singular.

Para que sea singular.

Entonces, con  $\alpha = 2$  y  $\alpha = -\frac{3}{2}$  la matriz A es singular y no posee inversa.

5. Resuelva los siguientes sistemas lineales:

a.

$$\begin{bmatrix} 1 & 0 & 0 \\ 2 & 1 & 0 \\ -1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 2 & 3 & -1 \\ 0 & -2 & 1 \\ 0 & 0 & 3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 2 \\ -1 \\ 1 \end{bmatrix}$$

```
%autoreload 2
L = np.array([[1,0,0],[2,1,0],[-1,0,1]])
U = np.array([[2,3,-1],[0,-2,1],[0,0,3]])
b = [2,-1,1]
resolver_LU(L,U,b)
```

Calculando y

[ 2. -5. 3.]

Verificación Ly=b:

[ 2. -1. 1.]

Calculando x

[-3. 3. 1.]

Verificación Ux=y:

[ 2. -5. 3.]

Por tanto, la solución es:

$$\begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -3 \\ 3 \\ 1 \end{bmatrix}$$

b.

$$\begin{bmatrix} 2 & 0 & 0 \\ -1 & 1 & 0 \\ 3 & 2 & -1 \end{bmatrix} \begin{bmatrix} 1 & 1 & 1 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -1 \\ 3 \\ 0 \end{bmatrix}$$

```
%autoreload 2
L = np.array([[2,0,0],[-1,1,0],[3,2,-1]])
U = np.array([[1,1,1],[0,1,2],[0,0,1]])
```

```
b = [-1,3,0]
resolver_LU(L,U,b)
Calculando y
[-0.5 2.5 3.5]
Verificación Ly=b:
[-1. 3. 0.]
Calculando x
[0.5 - 4.5 3.5]
Verificación Ux=y:
[-0.5 2.5 3.5]
Por tanto, la solución es:
                                            \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} 0.5 \\ -4.5 \\ 3.5 \end{bmatrix}
  6. Factorice las siguientes matrices en la descomposición LU mediante el algoritmo de factorización LU
     con l_{ii} = 1 para todas las i.
a.
                                                 3
                                                     9
%autoreload 2
A = [[2,-1,1],[3,3,9],[3,3,5]]
L,U = descomposicion_LU(A)
print("Matriz L:\n",L)
print("Matriz U:\n",U)
Matriz L:
 [[1. 0. 0.]
 [1.5 1. 0.]
 [1.5 1. 1.]]
Matriz U:
 [[ 2. -1. 1. ]
        4.5 7.5]
 [ 0.
 [0. 0. -4.]
b.
                                      \lceil 1.012 -2.132
                                                         3.104
                                       -2.132 	 4.096
                                                        -7.013
                                      3.104
                                                -7.013
                                                         0.014
%autoreload 2
B = [[1.012, -2.132, 3.104], [-2.132, 4.096, -7.013], [3.104, -7.013, 0.014]]
L,U = descomposicion_LU(B)
print("Matriz L:\n",L)
print("Matriz U:\n",U)
Matriz L:
                                0.
                                          ]
 [[ 1.
                  0.
 [-2.10671937 1.
                                          ]
                              0.
 [ 3.06719368 1.19775553 1.
                                          ]]
Matriz U:
 [[ 1.012
                -2.132
                                           ]
                                3.104
 [ 0.
                -0.39552569 -0.47374308]
```

```
[ 0.
               0.
                           -8.93914077]]
c.
                                            1.5 \quad 0 \quad 0
                                           -3 \quad 0.5 \quad 0
%autoreload 2
C = [[2,0,0,0],[1,1.5,0,0],[0,-3,0.5,0],[2,-2,1,1]]
L,U = descomposicion_LU(C)
print("Matriz L:\n",L)
print("Matriz U:\n",U)
Matriz L:
                             0.
                                          0.
                                                     ]
 [[ 1.
                 0.
                                                    ]
 [ 0.5
                1.
                             0.
                                         0.
                                                    ]
 [ 0.
               -2.
                             1.
                                         0.
                                                    ]]
 Г1.
               -1.33333333 2.
                                         1.
Matriz U:
 [[2. 0. 0. 0.]
 [0. 1.5 0. 0.]
 [0. 0. 0.5 0.]
 [0. 0. 0. 1.]]
d.
                                        4.0231
                                                 -2.1732
                                                           5.1967
                               2.1756
                              -4.0231
                                        6.0000
                                                   0
                                                           1.1973
                              -1.0000
                                       -5.2107
                                                 1.1111
                                                             0
                                                          -4.1561_{-}
                               6.0235
                                        7.0000
                                                   0
%autoreload 2
D = [[2.1756, 4.0231, -2.1732, 5.1967], [-4.0231, 6.0000, 0, 1.1973],
     [-1.0000, -5.2107, 1.1111, 0], [6.0235, 7.0000, 0, -4.1561]]
L,U = descomposicion_LU(D)
print("Matriz L:\n",L)
print("Matriz U:\n",U)
Matriz L:
                                                     ]
 [[ 1.
                 0.
                             0.
                                          0.
                                         0.
 [-1.84919103 1.
                                                    ]
                             0.
 [-0.45964332 -0.25012194
                            1.
                                         0.
                                                    ]
 [ 2.76866152 -0.30794361 -5.35228302
                                                    ]]
                                         1.
Matriz U:
 [[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 5.19670000e+00]
 [ 0.00000000e+00 1.34394804e+01 -4.01866194e+00 1.08069910e+01]
 [ 0.00000000e+00 4.44089210e-16 -8.92952394e-01 5.09169403e+00]
 [ 0.00000000e+00 0.00000000e+00 0.0000000e+00 1.20361280e+01]]
```

7. Modifique el algoritmo de eliminación gaussiana de tal forma que se pueda utilizar para resolver un sistema lineal usando la descomposición LU y, a continuación, resuelva los siguientes sistemas lineales.

a.

$$\begin{aligned} 2x_1 - x_2 + x_3 &= -1, \\ 3x_1 + 3x_2 + 9x_3 &= 0, \\ 3x_1 + 3x_2 + 5x_3 &= 4 \end{aligned}$$

```
%autoreload 2
A = [[2,-1,1],[3,3,9],[3,3,5]]
b = [1,0,4]
L,U = descomposicion_LU(A)
print("\nMatriz L:\n",L)
print("\nMatriz U:\n",U)
y = eliminacion_gaussiana_L(L,b)
print("\nValor de y:", y,"\n")
x = eliminacion_gaussiana_U(U,y)
print("\nValor de la solución x:", x)
Matriz L:
 [[1. 0. 0.]
 [1.5 1. 0.]
 [1.5 1. 1.]]
Matriz U:
 [[ 2. -1. 1. ]
 [ 0. 4.5 7.5]
 [ 0. 0. -4. ]]
[[ 1.
       0.
            0.
                1.]
[ 0.
       1.
            0. -1.5
 [ 1.5 1.
                4.]]
            1.
[[ 1.
       0.
            0.
                1.]
[ 0.
       1.
            0. -1.5
 [ 0.
       1.
            1.
                 2.5]]
[[ 1.
       0.
            0.
               1.]
[ 0.
            0. -1.5
       1.
 [ 0.
            1.
                4.]]
Valor de y: [ 1. -1.5 4. ]
[[ 2. -1.
            1.
                 1.]
[0. 4.5 7.5 - 1.5]
[ 0. 0. -4.
                 4.]]
[[ 2. -1.
                 1. ]
            1.
[ 0. 4.5 0.
                 6.]
[ 0. 0. -4.
                 4.]]
[[ 2. -1.
            0.
                 2.]
[ 0. 4.5 0.
                 6.]
[ 0.
       0. -4.
                 4.]]
                         0.
[[ 2.
                                     3.33333333]
              0.
[ 0.
              4.5
                         0.
                                     6.
                                              1
 [ 0.
                                              ]]
              0.
                        -4.
                                     4.
Valor de la solución x: [ 1.6666666 1.3333334 -1.
```

```
\begin{aligned} 1.012x_1 - 2.132x_2 + 3.104x_3 &= 1.984, \\ -2.132x_1 + 4.096x_2 + -7.013x_3 &= -5.049, \\ 3.104x_1 - 7.013x_2 + 0.014x_3 &= -3.895 \end{aligned}
```

```
%autoreload 2
A = [[1.012, -2.132, 3.104], [-2.132, 4.096, -7.013], [3.104, -7.013, 0.014]]
b = [1.984, -5.049, -3.895]
L,U = descomposicion_LU(A)
print("\nMatriz L:\n",L)
print("\nMatriz U:\n",U)
y = eliminacion_gaussiana_L(L,b)
print("\nValor de y:", y,"\n")
x = eliminacion_gaussiana_U(U,y)
print("\nValor de la solución x:", x)
Matriz L:
 [[ 1.
                0.
                             0.
                                       ]
 [-2.10671937 1.
                            0.
                                       ]
 [ 3.06719368  1.19775553
                                       ]]
Matriz U:
 [[ 1.012
               -2.132
                             3.104
                                        ]
 [ 0.
               -0.39552569 -0.47374308]
                           -8.93914077]]
 [ 0.
               0.
[[ 1.
                0.
                            0.
                                         1.984
 Γ0.
                                        -0.869268771
                1.
 [ 3.06719368 1.19775553 1.
                                        -3.895
                                                   ]]
[[ 1.
                0.
                            0.
                                        1.984
                                                   ]
 [ 0.
                1.
                            0.
                                        -0.86926877]
 [ 0.
                1.19775553 1.
                                        -9.98031225]]
[[ 1.
                0.
                            0.
                                         1.984
                                                   ]
 [ 0.
                            0.
                                        -0.86926877]
                1.
 [ 0.
                0.
                            1.
                                        -8.93914077]]
Valor de y: [ 1.984
                         -0.8692688 -8.93914 ]
[[ 1.012
               -2.132
                            3.104
                                         1.98399997]
 [ 0.
               -0.39552569 -0.47374308 -0.86926877]
 [ 0.
               0.
                           -8.93914077 -8.93914032]]
[[ 1.012
              -2.132
                            3.104
                                         1.98399997]
              -0.39552569 0.
 [ 0.
                                        -0.39552572]
 [ 0.
               0.
                           -8.93914077 -8.93914032]]
[[ 1.012
              -2.132
                            0.
                                        -1.11999987]
              -0.39552569 0.
[ 0.
                                        -0.39552572]
 [ 0.
               0.
                           -8.93914077 -8.93914032]]
[[ 1.012
               0.
                            0.
                                         1.01200026]
               -0.39552569 0.
 [ 0.
                                        -0.39552572]
 [ 0.
               0.
                           -8.93914077 -8.93914032]]
```

 $-3x_2 + 0.5x_3$ 

=-6.6,

```
2x_1 - 2x_2 + x_3 + x_4 = 0.8
%autoreload 2
A = [[2,0,0,0],[1,1.5,0,0],[0,-3,0.5,0],[2,-2,1,1]]
b = [3,4.5,-6.6,0.8]
L,U = descomposicion_LU(A)
print("\nMatriz L:\n",L)
print("\nMatriz U:\n",U)
y = eliminacion_gaussiana_L(L,b)
print("\nValor de y:", y,"\n")
x = eliminacion_gaussiana_U(U,y)
print("\nValor de la solución x:", x)
Matriz L:
 [[ 1.
                             0.
                                                   ]
                0.
                                        0.
 [ 0.5
                            0.
                                        0.
               1.
                                                  ]
 [ 0.
              -2.
                            1.
                                        0.
                                                  ]
 [ 1.
              -1.33333333 2.
                                        1.
                                                  ]]
Matriz U:
 [[2. 0. 0. 0.]
 [0. 1.5 0. 0.]
 [0. 0. 0.5 0.]
 [0. 0. 0. 1.]]
[[ 1.
               0.
                            0.
                                        0.
                                                    3.
                                                               ]
 [ 0.
               1.
                                        0.
                                                    3.
                                                               1
                            0.
 [ 0.
              -2.
                            1.
                                        0.
                                                   -6.6
                                                               ]
 [ 1.
              -1.33333333 2.
                                        1.
                                                    0.8
                                                               ]]
[[ 1.
               0.
                            0.
                                        0.
                                                    3.
                                                               ]
                                                               ]
 [ 0.
              1.
                            0.
                                        0.
                                                    3.
 [ 0.
              -2.
                                        0.
                                                    -6.6
                                                               ]
                            1.
              -1.33333333 2.
                                                               ]]
 [ 1.
                                                    0.8
                                                               ]
[[ 1.
              0.
                                        0.
                                                    3.
 [ 0.
                                                               ]
               1.
                            0.
                                        0.
                                                    3.
 ΓΟ.
              -2.
                                        0.
                                                    -6.6
                                                               ]
                            1.
 [ 0.
              -1.33333333 2.
                                                   -2.2
                                                               ]]
                                        1.
[[ 1.
               0.
                            0.
                                        0.
                                                    3.
                                                               ]
 [ 0.
               1.
                            0.
                                        0.
                                                    3.
                                                               ]
               0.
                                        0.
                                                   -0.6
                                                               ]
 [ 0.
                            1.
 [ 0.
              -1.33333333 2.
                                        1.
                                                   -2.2
                                                               ]]
[[ 1.
        0.
             0.
                  0.
                       3.]
```

[ 0.

[ 0.

1.

0.

0.

1.

3.]

0.

0. -0.6]

```
Valor de y: [ 3.
                  3. -0.6 3.]
[[ 2.
                                                     3.
                                                               ]
               0.
                                         0.
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
                                                                ]
 [ 0.
                                                    -0.60000002]
               0.
                            0.5
                                         0.
 [ 0.
               0.
                                                                ]]
                            0.
                                         1.
                                                     3.
                                                                ]
[[ 2.
                            0.
                                         0.
                                                     3.
               0.
                                                                ]
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
 [ 0.
                                         0.
                                                    -0.60000002]
               0.
                            0.5
 [ 0.
                                                                ]]
               0.
                            0.
                                         1.
                                                     3.
[[ 2.
               0.
                            0.
                                         0.
                                                     3.
                                                                ]
                                                                ]
 [ 0.
                                                     3.
               1.5
                            0.
                                         0.
 [ 0.
               0.
                            0.5
                                         0.
                                                    -0.60000002]
 [ 0.
                                                                ]]
               0.
                            0.
                                         1.
                                                                ]
[[ 2.
               0.
                            0.
                                         0.
                                                     3.
                                                                ]
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
 [ 0.
               0.
                            0.5
                                         0.
                                                    -0.60000002]
 [ 0.
                                                                ]]
               0.
                            0.
                                                     3.
                                         1.
                                                                ]
[[ 2.
               0.
                            0.
                                         0.
                                                     3.
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
                                                                ]
                                                    -0.60000002]
 [ 0.
               0.
                            0.5
                                         0.
 [ 0.
               0.
                            0.
                                                     3.
                                                                ]]
                                         1.
                                                                ]
[[ 2.
               0.
                            0.
                                         0.
                                                     3.
                                                                ]
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
 [ 0.
                            0.5
                                         0.
                                                    -0.60000002]
               0.
 [ 0.
               0.
                            0.
                                         1.
                                                                ]]
                                                                ]
[[ 2.
                                         0.
                                                     3.
               0.
                            0.
                                                                ]
 [ 0.
               1.5
                            0.
                                         0.
                                                     3.
 [ 0.
               0.
                            0.5
                                         0.
                                                    -0.60000002]
 [ 0.
               0.
                            0.
                                                     3.
                                                                ]]
Valor de la solución x: [1.5 2. -1.2 3.]
d.
                     2.1756x_1 + 4.0231x_2 - 2.1732x_3 + 5.1967x_4 = 17.102,\\
                       -4.0231x_1 + 6.0000x_2
                                                +1.1973x_4 = -6.1593,
                        -1.0000x_1 - 5.2107x_2 + 1.1111x_3
                                                            = 3.0004,
                         6.0235x_1 + 7.0000x_2 +
                                                   -4.1561x_4 = 0.0000
$
%autoreload 2
b = [17.102, -6.1593, 3.0004, 0.0000]
```

[ 0.

[[ 1.

[ 0.

[ 0.

[ 0.

0.

0.

1.

0.

2.

0.

0.

1.

0.

1.

0.

0.

0.

1.

1.8]]

3.]

3.]

3.]]

-0.6]

```
L,U = descomposicion_LU(A)
print("\nMatriz L:\n",L)
print("\nMatriz U:\n",U)
y = eliminacion_gaussiana_L(L,b)
print("\nValor de y:", y,"\n")
x = eliminacion_gaussiana_U(U,y)
print("\nValor de la solución x:", x)
Matriz L:
 [[ 1.
                0.
                             0.
                                         0.
                                                    ]
 [-1.84919103 1.
                            0.
                                        0.
                                                   ]
                                                   ]
 [-0.45964332 -0.25012194
                                        0.
                           1.
                                                   ]]
 [ 2.76866152 -0.30794361 -5.35228302 1.
Matriz U:
 [[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 5.19670000e+00]
 [ 0.00000000e+00 1.34394804e+01 -4.01866194e+00 1.08069910e+01]
 [ 0.00000000e+00 4.44089210e-16 -8.92952394e-01 5.09169403e+00]
 [ 0.00000000e+00 0.00000000e+00 0.00000000e+00 1.20361280e+01]]
[[ 1.
               0.
                            0.
                                        0.
                                                    17.102
                                                               1
 [ 0.
               1.
                            0.
                                        0.
                                                    25.46556496]
 [-0.45964332 -0.25012194 1.
                                                     3.0004
                                        0.
                                                               ]
 [ 2.76866152 -0.30794361 -5.35228302
                                                     0.
                                                               ]]
[[ 1.
               0.
                                        0.
                                                    17.102
                                                               ]
 [ 0.
                            0.
                                        0.
                                                    25.46556496]
               1.
 [ 0.
              -0.25012194 1.
                                                    10.86122
                                        0.
                                                               ]
                                                               ]]
 [ 2.76866152 -0.30794361 -5.35228302 1.
                                                     0.
[[ 1.
                 0.
                               0.
                                             0.
                                                         17.102
 Γ
    0.
                 1.
                               0.
                                             0.
                                                         25.465564961
 0.
                -0.25012194
                                                         10.86122
                               1.
                                             0.
                                                                    ٦
 Γ
   0.
                -0.30794361 -5.35228302
                                                        -47.34964929]]
                                             1.
ΓΓ 1.
                 0.
                               0.
                                             0.
                                                         17.102
                                                                    1
 0.
                 1.
                               0.
                                             0.
                                                         25.46556496]
 0.
                 0.
                                             0.
                                                         17.23071662]
                               1.
                -0.30794361 -5.35228302
 0.
                                                        -47.34964929]]
[[ 1.
                               0.
                                             0.
                                                         17.102
   0.
 [
                 1.
                               0.
                                             0.
                                                         25.46556496]
 0.
                 0.
                                             0.
                                                         17.23071662]
                               1.
 [
                              -5.35228302
                                                        -39.50769122]]
   0.
                 0.
                                             1.
[[ 1.
               0.
                            0.
                                        0.
                                                    17.102
 [ 0.
               1.
                            0.
                                        0.
                                                    25.46556496]
 [ 0.
               0.
                                        0.
                                                    17.23071662]
                            1.
 [ 0.
               0.
                            0.
                                        1.
                                                    52.71598078]]
Valor de y: [17.102 25.465565 17.230717 52.71598 ]
[[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 5.19670000e+00
   1.71019993e+017
 [ 0.00000000e+00 1.34394804e+01 -4.01866194e+00 1.08069910e+01
```

```
2.54655647e+017
[ 0.00000000e+00     4.44089210e-16     -8.92952394e-01     5.09169403e+00
  1.72307167e+01]
[ 0.00000000e+00 0.00000000e+00 0.00000000e+00 1.20361280e+01
  5.27159805e+01]]
[[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 5.19670000e+00
  1.71019993e+01]
[ 0.00000000e+00 1.34394804e+01 -4.01866194e+00 1.08069910e+01
  2.54655647e+01]
[ 0.00000000e+00 4.44089210e-16 -8.92952394e-01 0.00000000e+00
 -5.06994697e+001
[ 0.0000000e+00 0.0000000e+00 0.0000000e+00 1.20361280e+01
  5.27159805e+01]]
[[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 5.19670000e+00
  1.71019993e+01]
\begin{bmatrix} 0.00000000e+00 & 1.34394804e+01 & -4.01866194e+00 & 0.00000000e+00 \end{bmatrix}
 -2.18670265e+01]
[ 0.0000000e+00 4.44089210e-16 -8.92952394e-01 0.00000000e+00
 -5.06994697e+00]
5.27159805e+01]]
-5.65857084e+00]
[ 0.00000000e+00 1.34394804e+01 -4.01866194e+00 0.00000000e+00
 -2.18670265e+01]
[ 0.00000000e+00 4.44089210e-16 -8.92952394e-01 0.00000000e+00
 -5.06994697e+00]
5.27159805e+01]]
[[ 2.17560000e+00 4.02310000e+00 -2.17320000e+00 0.00000000e+00
 -5.65857084e+001
[ 0.00000000e+00 1.34394804e+01 0.0000000e+00 0.0000000e+00
  9.49870688e-01]
[ 0.00000000e+00 4.44089210e-16 -8.92952394e-01 0.00000000e+00
 -5.06994697e+00]
5.27159805e+01]]
[[ 2.17560000e+00 4.02310000e+00 0.00000000e+00 0.00000000e+00
  6.68028266e+00]
[ 0.00000000e+00 1.34394804e+01 0.0000000e+00 0.0000000e+00
  9.49870688e-017
-5.06994697e+001
5.27159805e+01]]
[[2.17560000e+00 0.0000000e+00 0.0000000e+00 0.0000000e+00
  6.39593946e+00]
[ 0.00000000e+00 1.34394804e+01 0.0000000e+00 0.0000000e+00
  9.49870688e-01]
[ 0.00000000e+00     4.44089210e-16 -8.92952394e-01     0.00000000e+00
```

Valor de la solución x: [2.9398508 0.07067764 5.677735 4.3798122 ]

## Link del repositorio:

 $https://github.com/MarckHA/Tarea\_10-Descomposicion-LU.git$