PRACTICLE - 1

Bisection method

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B.Voc.(Software Development)

```
In[32]:= Ques - 1
x0 = 0;
x1 = 2.0;
Nmax = 20;
eps = 0.0001;
f[x] := Cos[x];
If[N[f[x0] * f[x1]] > 0,
 Print [
  "Your values do not satisfy the IVP, so change
the values."],
 For [i = 1, i \le Nmax, i++, m = (x0 + x1) / 2;
  if [Abs[(x1 - x0)/2] < eps, Return[m],
  Print[i, "th iteration value is : ", m];
  Print["Estimated error in ", i,
   "th iteration is : ", (x1 - x0)/2];
   If [f(m) * f(x1) > 0, x1 = m, x0 = m]];
 Print["Root is :", m]
  Print["Estimated error in ", i,
   "th iteration is : ", (x1 - x0)/2]]
Plot[f[x], \{x, -1, 3\}, PlotRange \rightarrow \{-1, 1\},
 PlotStyle \rightarrow {Red, Thick}, PlotLabel \rightarrow "f[x]="f[x],
 AxesLabel \rightarrow \{x, f[x]\}
```

1th iteration value is : 1.

Estimated error in 1th iteration is : 1.

2th iteration value is : 1.5

Estimated error in 2th iteration is : 0.5

3th iteration value is : 1.75

Estimated error in 3th iteration is : 0.25

4th iteration value is : 1.625

Estimated error in 4th iteration is : 0.125

5th iteration value is : 1.5625

Estimated error in 5th iteration is : 0.0625

6th iteration value is : 1.59375

Estimated error in 6th iteration is : 0.03125

7th iteration value is : 1.57813

Estimated error in 7th iteration is : 0.015625

8th iteration value is : 1.57031

Estimated error in 8th iteration is: 0.0078125

9th iteration value is : 1.57422

Estimated error in 9th iteration is : 0.00390625

10th iteration value is : 1.57227

Estimated error in 10th iteration is: 0.00195313

11th iteration value is : 1.57129

Estimated error in 11th iteration is : 0.000976563

12th iteration value is: 1.5708

Estimated error in 12th iteration is : 0.000488281

13th iteration value is : 1.57056

Estimated error in 13th iteration is : 0.000244141

14th iteration value is : 1.57068

Estimated error in 14th iteration is : 0.00012207

15th iteration value is : 1.57074

Estimated error in 15th iteration is: 0.0000610352

16th iteration value is : 1.57077

Estimated error in 16th iteration is: 0.0000305176

17th iteration value is : 1.57079

Estimated error in 17th iteration is : 0.0000152588

18th iteration value is : 1.57079

Estimated error in 18th iteration is : 7.62939×10^{-6}

19th iteration value is : 1.5708

Estimated error in 19th iteration is : 3.8147×10^{-6}

20th iteration value is : 1.5708

Estimated error in 20th iteration is : $\text{1.90735} \times \text{10}^{-6}$

Root is :1.5708

Estimated error in 21th iteration is : 9.53674×10^{-7}

Out[38]= Null²

