SAPIENZA Università di Roma – MSc. in Engineering in Computer Science Artificial Intelligence & Machine Learning – June 10, 2024

Part 1 - Artificial Intelligence

(Time to complete the test: 2:30 hours)

Consider the following scenario. An agent (\odot) moves in a map with four cells, A, B, C, D. Initially, cell A contains the agent and cells B and C contain, respectively, a circle (\bigcirc) and a triangle (\triangle). Cell D is the exit (\diamondsuit). The initial situation is depicted below:

A	B	C	D
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Assume the environment is modelled as follows.

Non-Fluents:

- Item(x), denoting that x is an item.
- $Right(x_1, x_2)$, denoting that cell x_2 is next to the right of cell x_1 ;
- Exit(x), denoting that x is an exit.

Fluents:

- AgentAt(x) denoting that the agent is at cell x.
- AgentHas(x) denoting that the agent has item x with itself (the agent can carry many items);
- ItemAt(x, y) denoting that item x is at cell y.

Actions:

- move(x), which allows the agent to move to cell x. The action can be done if cell x is next to the right of the cell where the agent currently is. The effect is that the agent is in cell x (and no longer in the cell it moved from) and has with itself all the items present in x (in addition to those it already had). Further, the collected items are no longer in the cell.
- drop(), which allows the agent to drop in current location all the items it has with itself. The action can always be done. The effect is that all the items the agent had with itself will now be in the current location.
- exit(), which allows the agent to exit the map. The action can be done if the agent is currently in an exit cell and has all the items with itself. The effect is that the agent is no longer in the cell it was before and keeps all items it had with itself.

Initial situation:

Cell B is next to the right of A, C is next to the right of B, and D is next to the right of C. Cell D is the exit cell. The agent is at cell A. There are two items: circle and triangle. Item circle is in cell B and item triangle is in cell C.

Exercise 1. First, formalize the above scenario as a Basic Action Theory in Reiter's Situation Calculus. Then, given the sequence of actions $\varrho = move(B)$; move(C); move(D), check by regression whether:

- 1. ϱ is executable in S_0 ;
- 2. ρ results in a situation where cell C contains some item;
- 3. ϱ results in a situation where the agent has all the items with itself.

Exercise 2. Consider the following goal: $ItemAt(circle, D) \wedge ItemAt(triangle, D)$. First formalize the above scenario as a PDDL domain file and a PDDL problem file. Then:

- 1. Draw the corresponding transition system;
- 2. Solve planning for achieving the above goal by using forward depth-first search (uninformed), reporting the steps of the forward search computation, and return the resulting plan.

Exercise 3.

- 1. Formalize the following statements in FOL (by introducing suitable predicates, functions and constants):
 - (ϕ_1) Every sphere is a solid.
 - (ϕ_2) Every cube is a solid.
 - (ϕ_3) Every solid is a geometric shape.
 - (ϕ_4) Every square is a geometric shape.
- 2. Considering the KB $\mathcal{K} = \{\phi_1, \dots, \phi_4\}$ defined above, use the tableaux method to check whether it is possible that a square is also a sphere (you must define a suitable FOL formula to express this). If so, show a model I of \mathcal{K} where this holds.

Solution

Precondition Axioms:

- $Poss(move(x), s) \equiv \exists y. (AgentAt(y, s) \land Right(y, x))$
- $Poss(drop(), s) \equiv true$
- $Poss(exit(), s) \equiv \exists x. (AgentAt(x, s) \land Exit(x)) \land \forall y. (Item(y) \supset AgentHas(y, s))$

Successor State Axioms:

- 1. Start with Effect Axioms:
 - $a = move(x) \supset (AgentAt(x, do(a, s)) \land \forall y. (AgentAt(y, s) \supset \neg AgentAt(y, do(a, s))) \land \forall z. (ItemAt(z, x, s) \supset (AgentHas(z, do(a, s)) \land \neg ItemAt(z, x, do(a, s)))))$
 - $a = drop() \supset ((\forall x.(AgentHas(x,s) \supset \neg agentHas(x,do(a,s)))) \land (\forall x \forall y.(AgentHas(x,s) \land AgentAt(y,s)) \supset ItemAt(x,y,do(a,s))))$
 - $a = exit() \supset \forall x. (AgentAt(x, s) \supset \neg AgentAt(x, do(a, s)))$
- 2. Normalize:
 - $a = move(x) \supset AgentAt(x, do(a, s))$
 - $(\exists x.a = move(x) \land AgentAt(y, s)) \supset \neg AgentAt(y, do(a, s))$
 - $\bullet \ (\exists x.a = move(x) \land ItemAt(z,x,s)) \supset AgentHas(z,do(a,s)) \\$
 - $\bullet \ (a = move(x) \land ItemAt(z, x, s)) \supset \neg ItemAt(z, x, do(a, s)) \\$
 - $\bullet \ (a = drop() \land AgentHas(x,s) \land AgentAt(y,s)) \supset ItemAt(x,y,do(a,s)) \\$
 - $(a = drop() \land AgentHas(x, s)) \supset \neg agentHas(x, do(a, s))$
 - $(a = exit() \land AgentAt(x, s)) \supset \neg AgentAt(x, do(a, s))$
- 3. Obtain Successor-State Axioms (SSAs) (by applying Explanation Closure):
 - $AgentAt(x, do(a, s)) \equiv a = move(x) \lor (AgentAt(x, s) \land \neg ((\exists y. a = move(y) \land AgentAt(x, s)) \lor (a = exit() \land AgentAt(x, s)))),$

simplified as:

$$AgentAt(x, do(a, s)) \equiv a = move(x) \lor (AgentAt(x, s) \land \neg((\exists y.a = move(y)) \lor a = exit()))$$

- $AgentHas(x, do(a, s)) \equiv (\exists y.a = move(y) \land ItemAt(x, y, s)) \lor (AgentHas(x, s) \land \neg (a = drop() \land AgentHas(x, s)))$ simplified as:
 - $AgentHas(x, do(a, s)) \equiv (\exists y. a = move(y) \land ItemAt(x, y, s)) \lor (AgentHas(x, s) \land a \neq drop())$
- $ItemAt(x, y, do(a, s)) \equiv (a = drop() \land AgentHas(x, s) \land AgentAt(y, s)) \lor (ItemAt(x, y, s) \land \neg(a = move(y) \land ItemAt(x, y, s))),$

simplified as:

$$ItemAt(x, y, do(a, s)) \equiv (a = drop() \land AgentHas(x, s) \land AgentAt(y, s)) \lor (ItemAt(x, y, s) \land a \neq move(y))$$

Initial Situation:

- $Item(x) \equiv (x = circle) (x = triangle)$
- $Right(x,y) \equiv (x = A \land y = B) \lor (x = B \land y = C) \lor (x = C \land y = D)$
- $Exit(x) \equiv x = D$
- $AgentAt(x, S_0) \equiv x = A$
- $ItemAt(x, y, S_0) \equiv (x = circle \land y = B) \lor (x = triangle \land y = C)$

Regression:

For $\varrho = move(B)$; move(C); move(D), let: $S_1 = do(move(B), S_0)$; $S_2 = do(move(C), S_1)$; $S_3 = do(move(D), S_2)$.

To check whether ϱ is executable in S_0 , we need to check whether: move(B) is executable in S_0 ; move(C) is executable in S_1 ; move(D) is executable in S_2 .

These are equivalent to checking whether:

- $\mathcal{D}_0 \cup \mathcal{D}_{una} \models \mathcal{R}[Poss(move(B), S_0)];$
- $\mathcal{D}_0 \cup \mathcal{D}_{una} \models \mathcal{R}[Poss(move(C), S_1)];$
- $\mathcal{D}_0 \cup \mathcal{D}_{una} \models \mathcal{R}[Poss(move(D), S_2)].$

Let's regress the formulas.

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• \mathcal{R}[Poss(move(B), S_0)] = \mathcal{R}[\exists y.(AgentAt(y, S_0) \land Right(y, B))] =
          \exists y. \mathcal{R}[AgentAt(y, S_0) \land Right(y, B)] =
          \exists y. \mathcal{R}[AgentAt(y, S_0)] \land Right(y, B) =
          \exists y. AgentAt(y, S_0) \land Right(y, B)
          Since \mathcal{D}_0 \models AgentAt(A, S_0) \land Right(A, B), we have that: \mathcal{D}_0 \cup \mathcal{D}_{una} \models \exists y. (AgentAt(y, S_0) \land Right(y, B)),
          thus move(B) is executable in S_0.
• \mathcal{R}[Poss(move(C), S_1)] = \mathcal{R}[\exists y.(AgentAt(y, S_1) \land Right(y, C))] =
          \exists y. \mathcal{R}[(AgentAt(y, S_1) \land Right(y, C))] =
          \exists y. \mathcal{R}[AgentAt(y, S_1)] \land Right(y, C) =
          \exists y. \mathcal{R}[AgentAt(y, S_1)] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, do(move(B), S_0))] \land Right(y, C) = \exists y. \mathcal{R}[AgentAt(y, C)] = \exists y. \mathcal{
          \exists y. \mathcal{R}[move(B) = move(y) \lor (AgentAt(y, S_0) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(z)) \lor move(B) = exit()))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))] \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B) = move(B)))) \land Right(y, C) = (\exists z.move(B) \land \neg((\exists z.move(B) = move(B) = move(B
          \exists y. \mathcal{R}[move(B) = move(y) \lor (AgentAt(y, S_0) \land \neg(true \lor false))] \land Right(y, C) =
          \exists y. \mathcal{R}[move(B) = move(y) \lor (AgentAt(y, S_0) \land false)] \land Right(y, C) =
          \exists y. \mathcal{R}[move(B) = move(y) \lor false] \land Right(y, C) =
          \exists y. \mathcal{R}[move(B) = move(y)] \land Right(y, C) =
          \exists y.move(B) = move(y) \land Right(y, C)
          Since \mathcal{D}_0 \cup \mathcal{D}_{una} \models move(B) = move(B) \land Right(B,C), we have that: \mathcal{D}_0 \cup \mathcal{D}_{una} \models \exists y.move(B) = move(y) \land B
          Right(y, C) and thus move(C) is executable in S_1.
• \mathcal{R}[Poss(move(D), S_2)] = \mathcal{R}[\exists y.(AgentAt(y, S_2) \land Right(y, D))] = \exists y.\mathcal{R}[AgentAt(y, S_2)] \land Right(y, D)
          we have that:
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thus: $\mathcal{R}[Poss(move(D), S_2)] = \exists y. \mathcal{R}[AgentAt(y, S_2)] \land Right(y, D) = \\ \exists y. move(C) = move(y) \land Right(y, D)$ and again since $\mathcal{P}_0 \sqcup \mathcal{P}_{ord} \models \exists y. move(C) = move(y) \land Right(y, D)$

 $\mathcal{R}[move(C) = move(y) \lor (AgentAt(y, S_1) \land \neg((\exists z.move(C) = move(y)) \lor move(C) = exit()))] = \dots = 0$

and, again, since $\mathcal{D}_0 \cup \mathcal{D}_{una} \models \exists y.move(C) = move(y) \land Right(y, D)$, move(D) is executable in S_2 .

To check whether ρ results in a situation where cell C contains some item, we need to check whether:

 $\mathcal{R}[move(C) = move(y) \lor false] = \mathcal{R}[move(C) = move(y)] = move(C) = move(y)$

$$\mathcal{D}_0 \cup \mathcal{D}_{una} \models \mathcal{R}[\exists x.ItemAt(x, C, S_3)]$$

Let's regress the formula:

 $\mathcal{R}[AgentAt(y, S_2)] =$

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• \mathcal{R}[\exists x.ItemAt(x,C,S_3)] = \exists x.\mathcal{R}[ItemAt(x,C,S_3)] = \exists x.\mathcal{R}[(move(D) = drop() \land AgentHas(x,S_2) \land AgentAt(C,S_2)) \lor (ItemAt(x,C,S_2) \land move(D) \neq move(C))] = \exists x.\mathcal{R}[false \lor (ItemAt(x,C,S_2) \land true)] = \exists x.\mathcal{R}[ItemAt(x,C,S_2)] = \exists x.\mathcal{R}[(move(C) = drop() \land AgentHas(x,S_1) \land AgentAt(C,S_1)) \lor (ItemAt(x,C,S_1) \land move(C) \neq move(C))] = \exists x.\mathcal{R}[false \lor (ItemAt(x,C,S_1) \land false)] = \exists x.\mathcal{R}[false] = false
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Thus, ρ does not result in a situation where cell C contains some item.

To check whether ϱ results in a situation where the agent has all the items with itself, we need to check whether:

$$\mathcal{D}_0 \cup \mathcal{D}_{una} \models \mathcal{R}[\forall x.Item(x) \supset AgentHas(x, S_3)]$$

(Alternatively, the simpler formula; $\neg AgentHas(circle, S_3) \land \neg AgentHas(triangle, S_3)$ could be checked) Let's regress the formula:

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• \mathcal{R}[\forall x.Item(x) \supset AgentHas(x,S_3)] = \forall x.\mathcal{R}[Item(x) \supset AgentHas(x,S_3)] = \forall x.\mathcal{R}[Item(x)] \supset \mathcal{R}[AgentHas(x,S_3)] = \forall x.\mathcal{R}[Item(x)] \supset \mathcal{R}[AgentHas(x,S_3)] = \forall x.\mathcal{R}[AgentHas(x,S_3)] = \forall 
     \forall x.Item(x) \supset \mathcal{R}[AgentHas(x, S_3)]
     We have:
     \mathcal{R}[AgentHas(x, S_3)] =
     \mathcal{R}[(\exists y.move(D) = move(y) \land ItemAt(x, y, S_2)) \lor (AgentHas(x, S_2) \land move(D) \neq drop())] =
     \mathcal{R}[(\exists y.move(D) = move(y) \land ItemAt(x, y, S_2)) \lor (AgentHas(x, S_2) \land true)] =
     \mathcal{R}[(\exists y.move(D) = move(y) \land ItemAt(x, y, S_2)) \lor (AgentHas(x, S_2))] =
     \mathcal{R}[\exists y.move(D) = move(y) \land ItemAt(x, y, S_2)] \lor \mathcal{R}[AgentHas(x, S_2)] =
     \exists y. \mathcal{R}[move(D) = move(y) \land ItemAt(x, y, S_2)] \lor \mathcal{R}[AgentHas(x, S_2)] =
     (\exists y.move(D) = move(y) \land \mathcal{R}[ItemAt(x, y, S_2)]) \lor \mathcal{R}[AgentHas(x, S_2)]
     Let's regress ItemAt(x, y, S_2):
     \mathcal{R}[ItemAt(x, y, S_2)] =
     \mathcal{R}[(move(C) = drop() \land AgentHas(x, S_1) \land AgentAt(y, S_1)) \lor (ItemAt(x, y, S_1) \land move(C) \neq move(y))] =
     \mathcal{R}[(false \land AgentHas(x, S_1) \land AgentAt(y, S_1)) \lor (ItemAt(x, y, S_1) \land move(C) \neq move(y))] =
     \mathcal{R}[false \lor (ItemAt(x, y, S_1) \land move(C) \neq move(y))] =
     \mathcal{R}[ItemAt(x, y, S_1)] \land move(C) \neq move(y)
     We have:
     \mathcal{R}[ItemAt(x, y, S_1)] =
     \mathcal{R}[(move(B) = drop() \land AgentHas(x, S_0) \land AgentAt(y, S_0)) \lor (ItemAt(x, y, S_0) \land move(B) \neq move(y))] =
     \mathcal{R}[(false \land AgentHas(x, S_0) \land AgentAt(y, S_0)) \lor (ItemAt(x, y, S_0) \land move(B) \neq move(y))] =
     \mathcal{R}[ItemAt(x, y, S_0) \land move(B) \neq move(y)] =
     ItemAt(x, y, S_0) \land move(B) \neq move(y)
     Thus:
     \mathcal{R}[ItemAt(x, y, S_2)] = ItemAt(x, y, S_0) \land move(B) \neq move(y) \land move(C) \neq move(y)
     Let's regress AgentHas(x, S_2):
     \mathcal{R}[AgentHas(x, S_2)] =
     \mathcal{R}[(\exists y.move(C) = move(y) \land ItemAt(x, y, S_1)) \lor (AgentHas(x, S_1) \land move(C) \neq drop())] =
     \mathcal{R}[(\exists y.move(C) = move(y) \land ItemAt(x, y, S_1)) \lor (AgentHas(x, S_1) \land move(C) \neq drop())] =
     \mathcal{R}[(\exists y.move(C) = move(y) \land ItemAt(x, y, S_1)) \lor (AgentHas(x, S_1) \land true)] =
     \mathcal{R}[(\exists y.move(C) = move(y) \land ItemAt(x, y, S_1)) \lor AgentHas(x, S_1)] =
     (\exists y.move(C) = move(y) \land \mathcal{R}[ItemAt(x, y, S_1)]) \lor \mathcal{R}[AgentHas(x, S_1)]
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 $\mathcal{R}[ItemAt(x, y, S_1)]$ was computed above.

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For AgentHas(x, S_1), we have:

\mathcal{R}[AgentHas(x, S_1)] =

\mathcal{R}[(\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor (AgentHas(x, S_0) \land move(B) \neq drop())] =

\mathcal{R}[(\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor (AgentHas(x, S_0) \land move(B) \neq drop())] =
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\mathcal{R}[(\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor (AgentHas(x, S_0) \land true)] =
\mathcal{R}[(\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0)] =
(\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0)
Thus, we obtain:
\mathcal{R}[AgentHas(x, S_2)] =
       (\exists y.move(C) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y)) \lor
       (\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0)
Hence: \mathcal{R}[AgentHas(x, S_3)] =
       (\exists y.move(D) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y) \land move(C) \neq move(y)) \lor
       (\exists y.move(C) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y)) \lor
       (\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0))
Putting these results together, we obtain:
\mathcal{R}[\forall x.Item(x) \supset AgentHas(x, S_3)] =
       \forall x.Item(x) \supset
              (\exists y.move(D) = move(y) \land ItemAt(x, y, S_0) \land \neg(move(B) = move(y)) \land move(C) \neq move(y)) \lor
              (\exists y.move(C) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y)) \lor
              (\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0)
Since we have that circle and triangle are the only items and:
\mathcal{D}_0 \cup \mathcal{D}_{una} \models Item(circle) \supset (move(B) = move(B) \land ItemAt(circle, B, S_0)) and
\mathcal{D}_0 \cup \mathcal{D}_{una} \models Item(triangle) \supset (move(C) = move(C) \land ItemAt(triangle, C, S_0) \land move(B) \neq move(C))
then:
\mathcal{D}_0 \cup \mathcal{D}_{una} \models
       \forall x.Item(x) \supset
              (\exists y.move(D) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y) \land move(C) \neq move(y)) \lor
              (\exists y.move(C) = move(y) \land ItemAt(x, y, S_0) \land move(B) \neq move(y)) \lor
              (\exists y.move(B) = move(y) \land ItemAt(x, y, S_0)) \lor AgentHas(x, S_0)
```

Thus, ϱ results in a situation where the agent has all the items with itself.

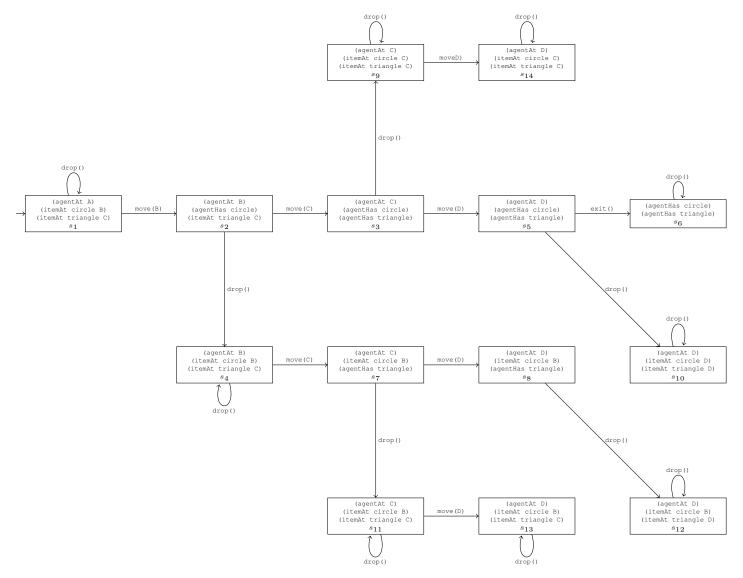
PDDL:

Domain file:

```
(define (domain grid_domain)
 (:requirements :adl)
 (:types location item)
 (:predicates
   (item ?x-item)
   (right ?x1 ?x2-location)
   (exit ?x-location)
   (agentAt ?x-location)
   (agentHas ?x-item)
   (itemAt ?x-item ?y-location)
 )
 (:action move
   :parameters (?x - location)
   :precondition ((exists ?y - location) (and (agentAt ?y) (right ?y ?x)))
   :effect (and
     (agentAt ?x)
     (forall (?y-location) (when (agentAt ?y) (not (agentAt ?y))))
     (forall (?y-item) (when (itemAt ?y ?x) (and (not (itemAt ?y ?x)) (agentHas(?y)))))
   )
```

```
); end of move
 (:action drop
   :parameters ()
   :precondition ()
   :effect
       (forall (?x-location)
        (forall (?y-item)
          (when
            (and (agentAt ?x) (agentHas ?y))
            (and (itemAt ?y ?x) (not (agentHas ?y)))
          )
        )
 ); end of drop
 (:action exit
   :parameters ()
   :precondition (and
     (exists (?x - location) (and (agentAt ?x) (exit ?x)))
     (forall (?x - item) (agentHas ?x))
   :effect (forall (?x-location) (not (agentAt ?x)))
 ); end of exit
); end of define
Problem file:
(define (problem grid_problem) (:domain grid_domain)
 (:objects
   A B C D - location
   circle triangle - item
 )
   (right A B) (right B C) (right C D)
   (exit D)
   (agentAt A)
   (itemAt circle B) (itemAt triangle C)
 )
 (:goal (and (itemAt circle D) (itemAt triangle D)))
```

Transition System:



DFS Algorithm:

```
DFS(domain d, state init, formula goal){
    // d: input domain;
    // init: initial state;
    // goal: goal formula;
    Stack t = [(init, empty)]; // Open set (stack)
    Set m = {init}; // Marked states
    while (!t.empty()) {
        (state,plan) = t.pop(); // plan is action sequence followed to reach s
        if (s \modeling goal) return plan; // if s satifies goal state, return plan
        forall (actions a executable in s)
        s'=d.delta(s,a) // s' is successor of s under a (d.delta is transition function of d)
        if (s' \notin m) {// if s' not marked
            m.add(s'); // mark s'
            t.push((s',plan·a)); // add s' with plan extended by a to open set t}
   }
   return noplan; // no plan found
}
```

```
DFS(grid_domain, s_1, (itemAt circle D) \land (itemAt triangle D)):
```

```
0. t = [(s_1, \text{ empty})]
  m = \{s_1\}
1. (state, plan) = (s_1, \text{ empty})
   t = [(s_2, move(B))]
   m = \{s_1, s_2\}
2. (state, plan) = (s_2, \text{ move (B)})
   t = [(s_3, move(B) move(C)),
          (s_4, \text{ move(B) drop())}]
   m = \{s_1, s_2, s_3, s_4\}
3. (state, plan) = (s_3, move(B) move(C))
   t = [(s_5, move(B) move(C) move(D)),
          (s_9, \text{ move(B) move(C) drop())},
          (s_4, \text{ move (B) drop ())}]
   m = \{s_1, s_2, s_3, s_4, s_5, s_9\}
4. (state, plan) = (s_5, move (B) move (C) move (D))
   t = [(s_{10}, move(B) move(C) move(D) drop()),
          (s_6, \text{ move}(B) \text{ move}(C) \text{ move}(D) \text{ exit}()),
          (s_9, \text{ move (B) move (C) drop ())},
          (s_4, \text{ move (B) drop ())}]
   m = \{s_1, s_2, s_3, s_4, s_5, s_9, s_{10}\}
5. (state, plan) = ((s_{10}, \text{ move}(B) \text{ move}(C) \text{ move}(D) \text{ drop}())
   return (move(B) move(C) move(D) drop())
```

Solution plan is: (move(B) move(C) move(D) drop())

FOL:

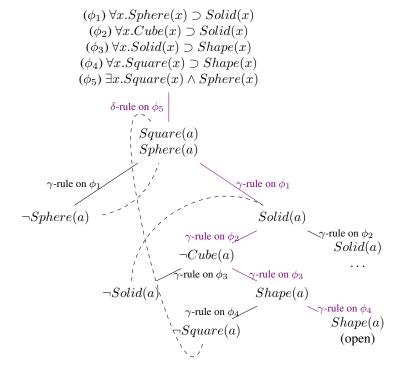
Predicates:

- Sphere(x): x is a sphere
- Cube(x): x is a cube
- Solid(x): x is a solid
- Square(x): x is a square
- Shape(x): x is a geometric shape

Formulas:

- (ϕ_1) Every sphere is a solid: $\forall x.Sphere(x) \supset Solid(x)$
- (ϕ_2) Every cube is a solid: $\forall x.Cube(x) \supset Solid(x)$
- (ϕ_3) Every solid is a geometric shape: $\forall x.Solid(x) \supset Shape(x)$
- (ϕ_4) Every square is a geometric shape: $\forall x. Square(x) \supset Shape(x)$
- (ϕ_5) It is possible that a square is also a sphere: $\exists x. Square(x) \land Sphere(x)$

Let $\mathcal{K} = \{\phi_1, \phi_2, \phi_3, \phi_4\}$. We need to check whether $\mathcal{K} \cup \{\phi_5\}$ is satisfiable. Let's construct the tableau for $\mathcal{K} \cup \{\phi_5\}$:



The coloured path gives us a model I of K:

- $\Delta^I = \{a\}$
- $Sphere^I = \{a\}$
- $Cube^I = \{\}$
- $Solid^I = \{a\}$
- $Square^I = \{a\}$
- $\bullet \ Shape^I=\{a\}$