Supplementary Information: Population-scale negative density dependence in per capita population growth rates: understanding the controls on abundance of a common tropical palm.

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S1 TABLES

| Vital rate / stage | 2008 | 2010 | 2012 |
|---------------------|------|------|------|
| Seeds | 2197 | | |
| Recruits | | 389 | 214 |
| Seedling growth | | 353 | 374 |
| Seedling survival | | 517 | 502 |
| Seedling to rosette | | 6 | 3 |
| Rosette growth | | 292 | 295 |
| Rosette survival | | 324 | 321 |
| Rosette to stem | | 0 | 7 |
| Stem growth | | | 364 |
| Stem survival | | | 407 |
| Reproduction | 407 | | 403 |

Table S1. table caption in main text

| Model | Formulation | Priors | Description |
|-------------------------------------|---|--|--|
| 1: Logistic model | $logit(Y(x)) = \beta_0 + \beta_1 x$ | $\begin{cases} \beta_0 \sim Unif(-1000, 1000) \\ \beta_1 \sim Unif(-1000, 1000) \end{cases}$ | Parameters β_0 indicates the point on x when $Y(x) = 0.5$, and β_1 is the rate of increase with size (x) . |
| 2: density dependant Logistic model | $logit(Y(x)) = \beta_0 + \beta_1 x + \beta_2 d$ | $\begin{cases} \beta_0 \sim Unif(-1000, 1000) \\ \beta_1 \sim Unif(-1000, 1000) \\ \beta_2 \sim Unif(-1000, 1000) \end{cases}$ | Parameters β_0 indicates the point on x when $Y(x) = 0.5$, and β_1 is the rate of increase with size (x) while β_2 is the rate of change over adult density d . |

Table S2. Equations for all logistic models, including prior distributions, used for dichotomous variables. Details are given in the text.

| Model | Formulation | Priors | Description |
|----------------|---|--|---|
| 1: Exponential | $f(x) = \beta_0 e^{-\beta_0 x}$ | $\begin{cases} \beta_0 \sim Unif(0, 100) \end{cases}$ | Parameters β_0 is the rate parameter, which indicates the frequency of x at zero and central tendency as mean= $1/\beta_0$ (x). |
| 2: Weibull | $f(x) = \begin{cases} \frac{\beta_0}{\beta_1} \left(\frac{x}{\beta_1} \right) e^{-(x/\beta_1)^{\beta_0}}; x \ge 0 \\ 0; x < 0 \end{cases}$ | $\begin{cases} \beta_0 \sim Unif(0, 1000) \\ \beta_1 \sim Unif(0, 1000) \end{cases}$ | Here β_0 is the scale parameter, while β_1 is shape parameter of the distribution. |
| 3: Log-normal | $f(x) = \frac{1}{x/\sqrt{2\pi\beta_1^2}} e^{-\frac{(\ln x - \beta_0)^2}{2\beta_1^2}}$ | $\begin{cases} \beta_0 \sim Unif(-1000, 1000) \\ \beta_1 \sim Unif(0, 1000) \end{cases}$ | β_0 indicates the natural log of the mean and β_1 is standard deviation. |

Table S3. Equations for all probability density functions, used to estimate univariate distributions. Details are given in the text.

| Model | Formulation | Priors | Description |
|--|--|--|--|
| 1: Null + constant variance | $Y(x) \sim N(\beta_0, \sigma = \beta_2)$ | $\begin{cases} \beta_0 \sim Unif(-1000, 1000) \\ \sigma \sim Unif(0, 1000) \end{cases}$ | Null model, growth is independent of size, and normally distributed where variation is described by σ^2 . |
| 2 A: Size dependent linear + constant variance | $Y(x) \sim N(\beta_0 + \beta_1 x, \sigma = \beta_2)$ | $\begin{cases} \beta_{0,1} \sim Unif(-1000, 1000) \\ \sigma \sim Unif(0, 1000) \end{cases}$ | Linear model with constant variance. Individual variation is described by σ^2 . |
| 3 A: Size dependent linear + Heteroscedasticity | $Y(x) \sim N(\beta_0 + \beta_1 x, \sigma = \beta_2 + \beta_3 x)$ | $\begin{cases} \beta_{0,1,2} \sim Unif(-1000, 1000) \\ \beta_3 \sim Unif(0, 1000) \end{cases}$ | Linear model, individual variation may increase with size as defined by $\beta_2 + \beta_3 x$, where β_3 is always positive. |
| 4 A: Size dependent linear + Log-linear Heteroscedasticity | $Y(x) \sim N(\beta_0 + \beta_1 x, \sigma = \beta_2 + \beta_3 log(x))$ | $\begin{cases} \beta_{0,1,2,4} \sim Unif(-1000, 1000) \\ \beta_3 \sim Unif(0, 1000) \end{cases}$ | Linear model, individual variation may increase with size as defined by $\beta_2 + \beta_3 log(x)$, where β_3 is always positive. |
| 2 B: Size & density dependent linear + constant variance | $Y(x) \sim N(\beta_0 + \beta_1 x + \beta_4 d, \sigma = \beta_2)$ | $\begin{cases} \beta_{0,1,2} \sim Unif(-1000, 1000) \\ \sigma \sim Unif(0, 1000) \end{cases}$ | Linear model where Y dependent on size (x) and density (d). Individual variation is described by σ^2 . |
| 3 B: Size & density dependent linear + Heteroscedasticity | $Y(x) \sim N(\beta_0 + \beta_1 x + \beta_4 d, \sigma = \beta_2 + \beta_3 x)$ | $\begin{cases} \beta_{0,1,2,4} \sim Unif(-1000, 1000) \\ \beta_3 \sim Unif(0, 1000) \end{cases}$ | Linear model where Y dependent on size (x) and density (d). Individual variation may increase with size as defined by $\beta_2 + \beta_3 x$, where β_3 is always positive. |
| 4 B: Size & density dependent linear + Log-linear Heteroscedasticity | $Y(x) \sim N(\beta_0 + \beta_1 x + \beta_4 d, \sigma = \beta_2 + \beta_3 \log(x))$ | $\begin{cases} \beta_{0,1,2,4} \sim Unif(-1000, 1000) \\ \beta_3 \sim Unif(0, 1000) \end{cases}$ | Linear model where Y dependent on size (x) and density (d). Individual variation may increase with size as defined by $\beta_2 + \beta_3 log(x)$, where β_3 is always positive. |

Table S4. Equations for all linear models, including prior distributions, used for continuous dependent variables. Details are given in the text.

| Vital.rate | Posterior.model.probabilty | Form |
|--|----------------------------|--|
| Density independent Seedling establishment | 0.0613 | $E(a) = logit^{-1}(\beta_0)$ |
| Density dependent Seedling establishment | 0.9387 | $E(\bar{a}) = logit^{-1}(\beta_0 + \beta_4 a)$ |
| Density independent Initial size | 0.4954 | $L(x_s) \sim \frac{1}{x_s/\sqrt{2\pi\beta_1^2}} e^{-\frac{(\ln x_s - (\beta_0))^2}{2\beta_1^2}}$ |
| Density dependent Initial size | 0.5046 | $L(x_s) \sim \frac{1}{x_s/\sqrt{2\pi\beta_1^2}} e^{-\frac{(\ln x_s - (\beta_0 + \beta_4 a))^2}{2\beta_1^2}}$ |
| Density independent Seedling growth | 0.0847 | $G_s(x_s, a) = \beta_0 + \beta_1 x_s \&$ |
| Density dependent Seedling growth | 0.9153 | $egin{aligned} V_s(x_s) &= eta_2 + eta_3 x_s \ G_s(x_s,a) &= eta_0 + eta_1 x_s + eta_4 a \ \& V_s(x_s) &= eta_2 + eta_3 x_s \end{aligned}$ |
| Density independent Seedling survival | 0.9113 | $S_s(x_s,a) = logit^{-1}(eta_0 + eta_1 x_s)$ |
| Density dependent Seedling survival | 0.0887 | $S_s(x_s, a) = logit^{-1}(\beta_0 + \beta_1 x_s + \beta_4 a)$ |
| Density independent Rosette growth | 0.3416 | $G_r(x_r, a) = \beta_0 + \beta_1 x_r \&$ $V_r(x_r) = \beta_2 + \beta_3 ln(x_r)$ |
| Density dependent Rosette growth | 0.6584 | $G_r(x_r) = \beta_2 + \beta_3 ln(x_r)$ $G_r(x_r, a) = \beta_0 + \beta_1 x_r + \beta_4 a \&$ $V_r(x_r) = \beta_2 + \beta_3 ln(x_r)$ |
| Density independent Rosette survival | 0.8040 | $S_r(x_r, a) = logit^{-1}(\beta_0 + \beta_1 x_r)$ |
| Density dependent Rosette survival | 0.1960 | $S_r(x_r, a) = logit^{-1}(\beta_0 + \beta_1 x_r + \beta_4 a)$ |
| Density independent Adult growth | 0.5788 | $G_h(x_h, a) = \beta_0 + \beta_1 x_h \&$ |
| Density dependent Adult growth | 0.4212 | $\sigma=eta_2 \ G_h(x_h,a)=eta_0+eta_1x_h+eta_4a\ \& \ \sigma=eta_2$ |
| Density independent Adult survival | 0.2351 | $S_h(x_h, a) = logit^{-1}(\beta_0 + \beta_1 x_h)$ |
| Density dependent Adult survival | 0.7649 | $S_h(x_h, a) = logit^{-1}(\beta_0 + \beta_1 x_h + \beta_4 a)$ |
| Density independent Reproduction | 0.2824 | $S_h(x_h, a) = logit^{-1}(\beta_0 + \beta_1 x_h)$ |
| Density dependent Reproduction | 0.7176 | $S_h(x_h, a) = logit^{-1}(\beta_0 + \beta_1 x_h + \beta_4 a)$ |

Table S5. table caption in main text

| | Vital rate | β_0 (intercept/rate) | $\beta_1 \text{ (size/sd)}$ | Formula |
|---|-------------------------|----------------------------|-----------------------------|---|
| 1 | Seedling to rosette | 10.90 | -0.09 | $T_{s\to r}(x_s) = logit^{-1}(\beta_0 + \beta_4 x_s)$ |
| 2 | Rosette to stemmed palm | 9.21 | -0.01 | $T_{r\to h}(x_r) = logit^{-1}(\beta_0 + \beta_4 x_r)$ |
| 3 | Initial size | 7.43 | 0.00 | $B(x_h) = \beta_0 e^{-\beta_0 x_h}$ |

Table S6. table caption in main text

| | Inv. growth (2.5%) | Inv. growth (97.5%) | Stabilization θ (2.5%) | Stabilization θ (97.5%) | Eq. density (2.5%) | Eq. density (97.5%) |
|------------------------------------|--------------------|---------------------|-------------------------------|--------------------------------|--------------------|---------------------|
| Seedling to rosette (mid-point) | 1.0442 | 1.0580 | -0.0289 | -0.0103 | 0.3779 | 0.9424 |
| Rosette to stem (midpoint) | 1.0417 | 1.0598 | -0.0289 | -0.0116 | 0.3567 | 0.8573 |
| Size-dependent seedling to rosette | 1.0473 | 1.0492 | -0.0200 | -0.0198 | 0.4657 | 0.5424 |
| Size-dependent rosette to stem | 1.0481 | 1.0484 | -0.0202 | -0.0197 | 0.4719 | 0.5117 |

Table S7. table caption in main text

S2 Figures

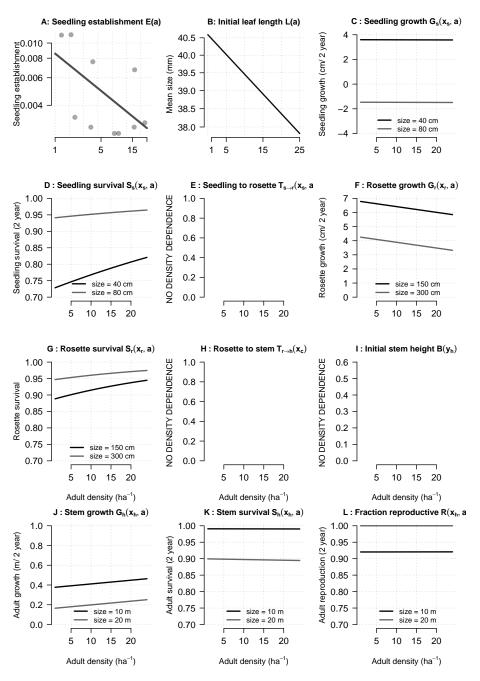


Figure S1. Figure legend in the maintext (allows for easy editing)

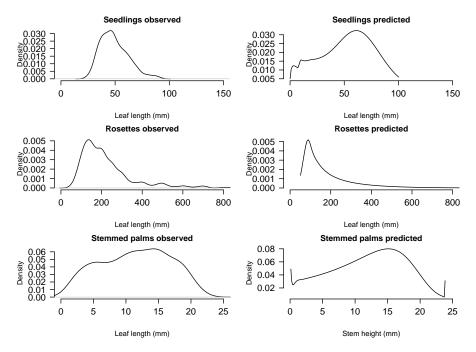


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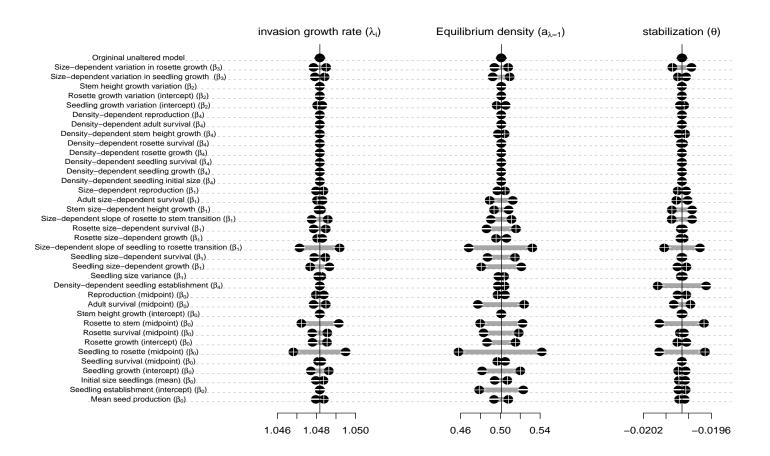


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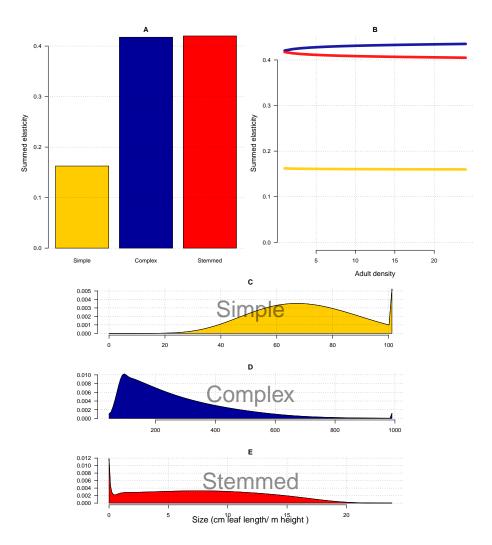


Figure S4. Figure legend in the maintext (allows for easy editing)