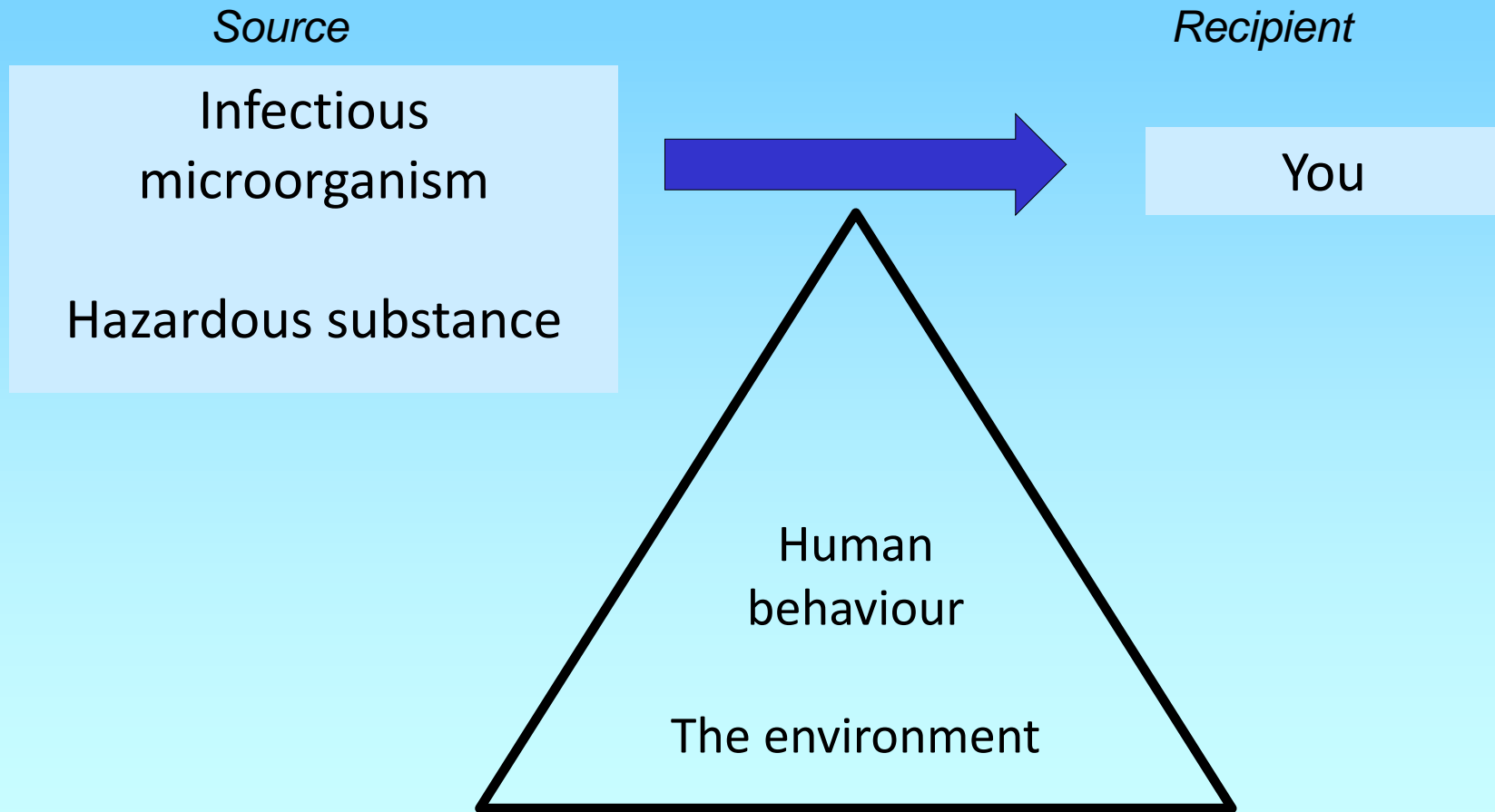


# Practical: Airborne Infection Risk

## Session objectives

1. Introduce disease dynamics and transmission modelling
2. Introduce the parameters that affect airborne transmission and Wells-Riley model
3. Demonstrate how it can be coupled with SEIR models
4. Use simple spreadsheet models to explore the effect of parameters and interventions

# Disease Transmission

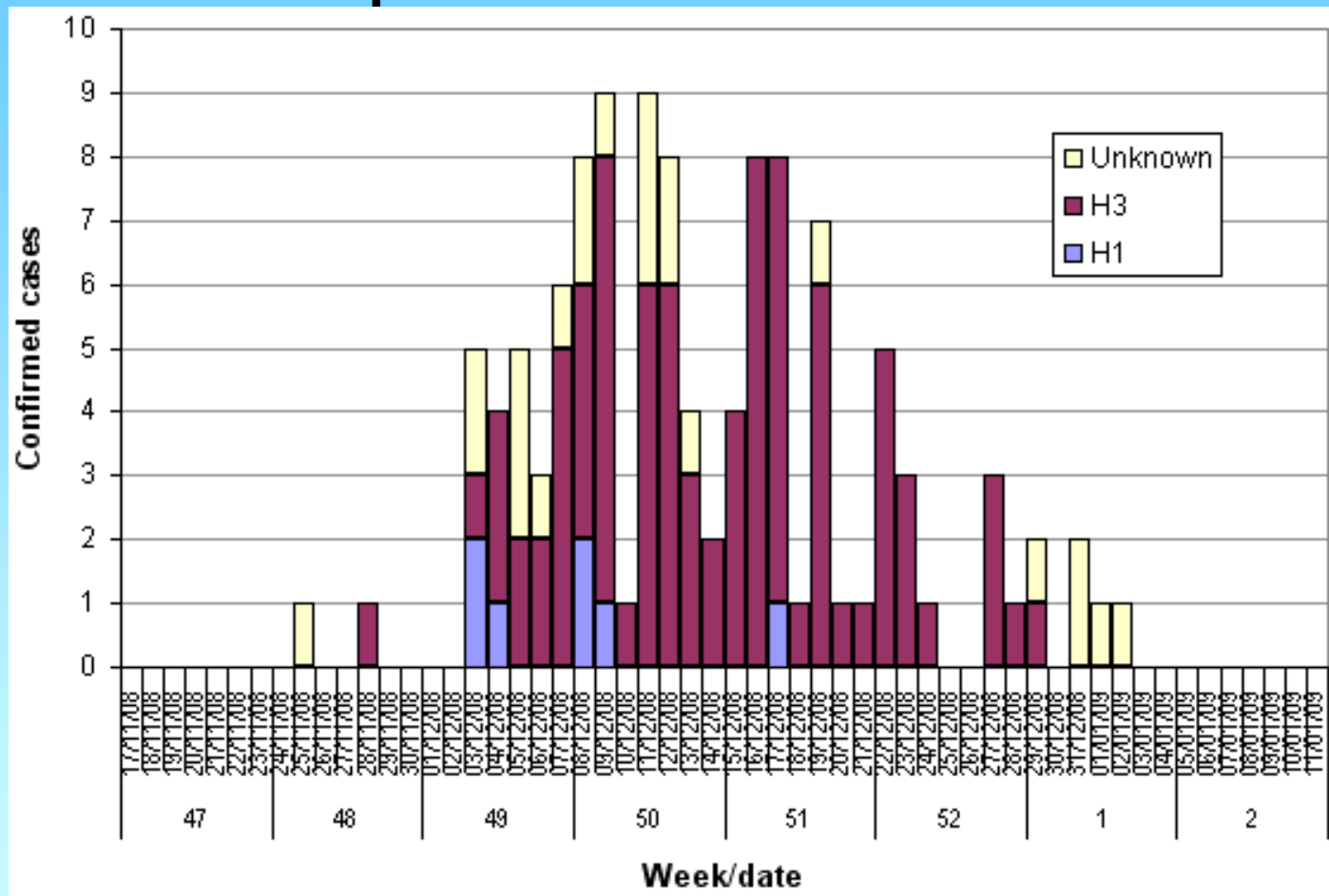


# Disease Dynamics

- Spread of disease depends on many factors:
  - The pathogen concerned - virulence, survival
  - The population of people and their susceptibility to the disease
  - The mode of transmission
  - The time between being exposed to the disease and becoming infectious
  - The symptoms
  - The ability and ease of passing the disease on

.....

# Outbreak patterns

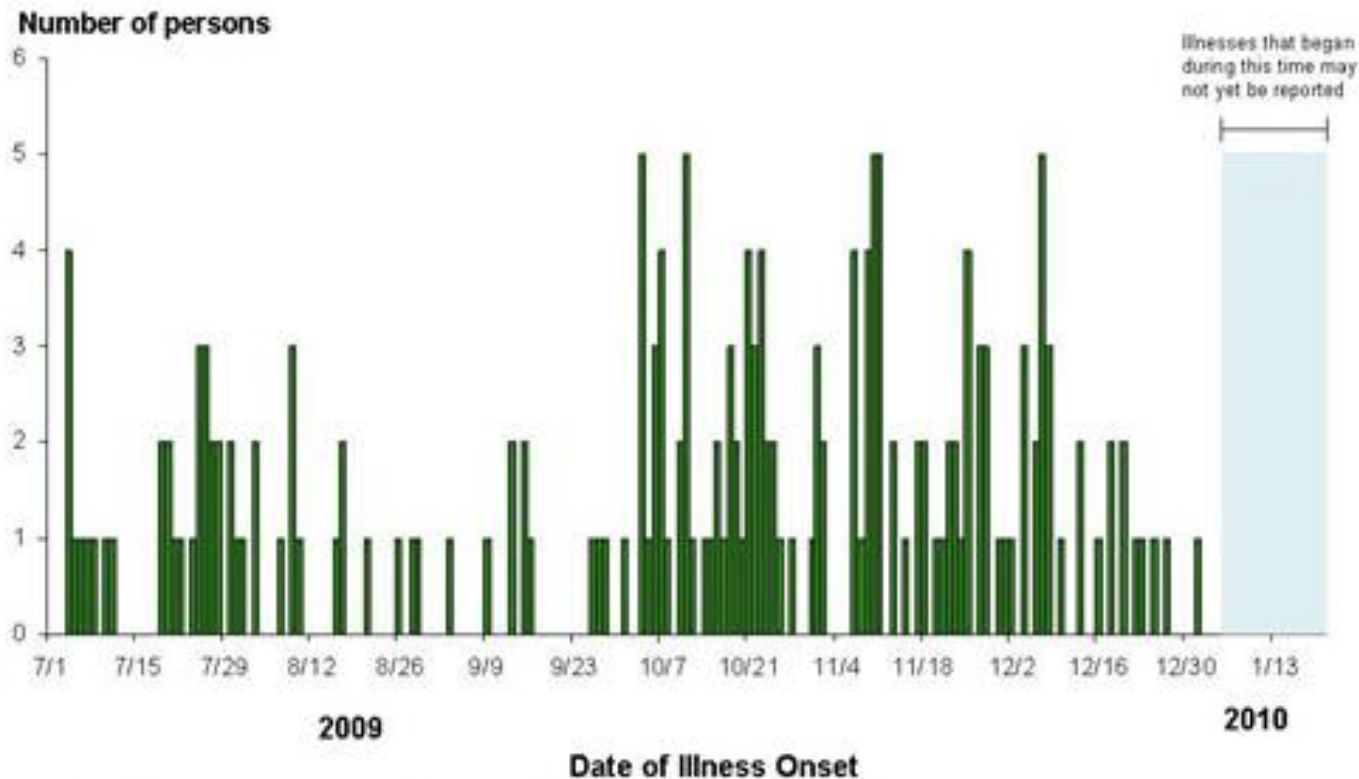


**Royal Liverpool University Hospital, and influenza-like illness rates in Liverpool between week 47/2008 and week 2/2009**

HPA, [www.hpa.org.uk/hpr/archives/2009/news0509.htm](http://www.hpa.org.uk/hpr/archives/2009/news0509.htm)

# Outbreak patterns

## Infections with the outbreak strain of *Salmonella* Typhimurium, by date of illness onset



\* Some illness onset dates have been estimated from other reported information.

# Modelling disease transmission

- Models allow assessment of the relative importance of disease parameters
- Describe the progression of disease over time
- Enable intervention or response to disease
- Earliest model – Daniel Bernolli, vaccination against small pox
- Modern approaches based on models of Reed and Frost (1920's) and McKendrick and Kermack (1927)

# Model requirements

- Will an infection spread?
  - How fast will it spread?
  - How many people will be affected?
  - How long will the outbreak last?
  - What interventions are the most effective?
- 
- In air – how does the building and human breathing ventilation affect risk?

# Wells-Riley Model

- Probability of infection (Pr) linked to disease, occupant and ventilation characteristics

$$Pr = 1 - e^{\left(\frac{Iqpt}{Q}\right)}$$

- Usually used to model new infections ( $N_C$ ) for S susceptibles

$$N_C = S(1 - e^{\left(\frac{Iqpt}{Q}\right)})$$

Q = ventilation rate (m<sup>3</sup>/s)

P = breathing rate (m<sup>3</sup>/s)

I = number of infectors

S = number of susceptibles



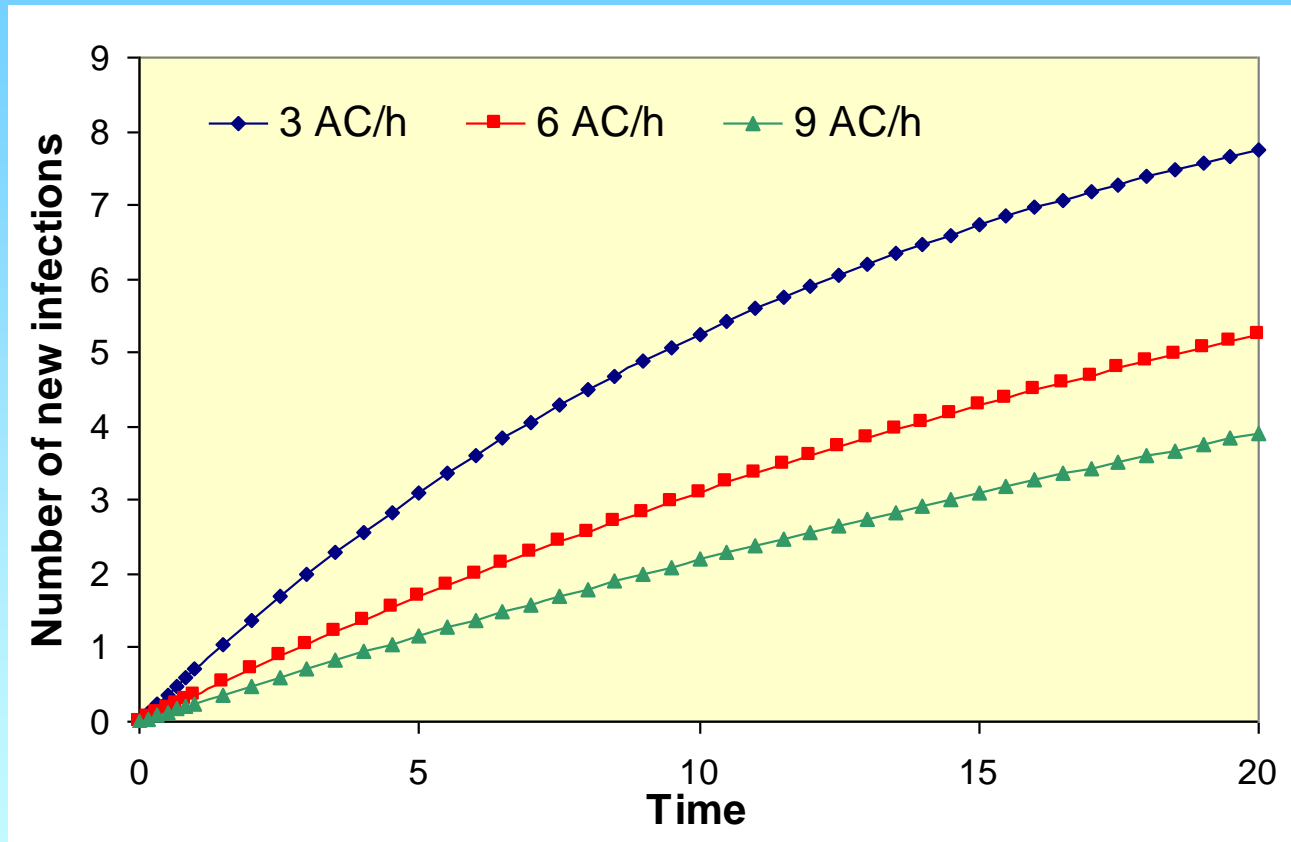
# Quanta (q)

- Rate of generation of “infectious doses”
- Encompasses concentration, virulence, host susceptibility
- Used in wide range of risk analysis studies and assessment of disease outbreaks
- Usually estimated from past outbreak data – but not always reliable

# Infectious Dose

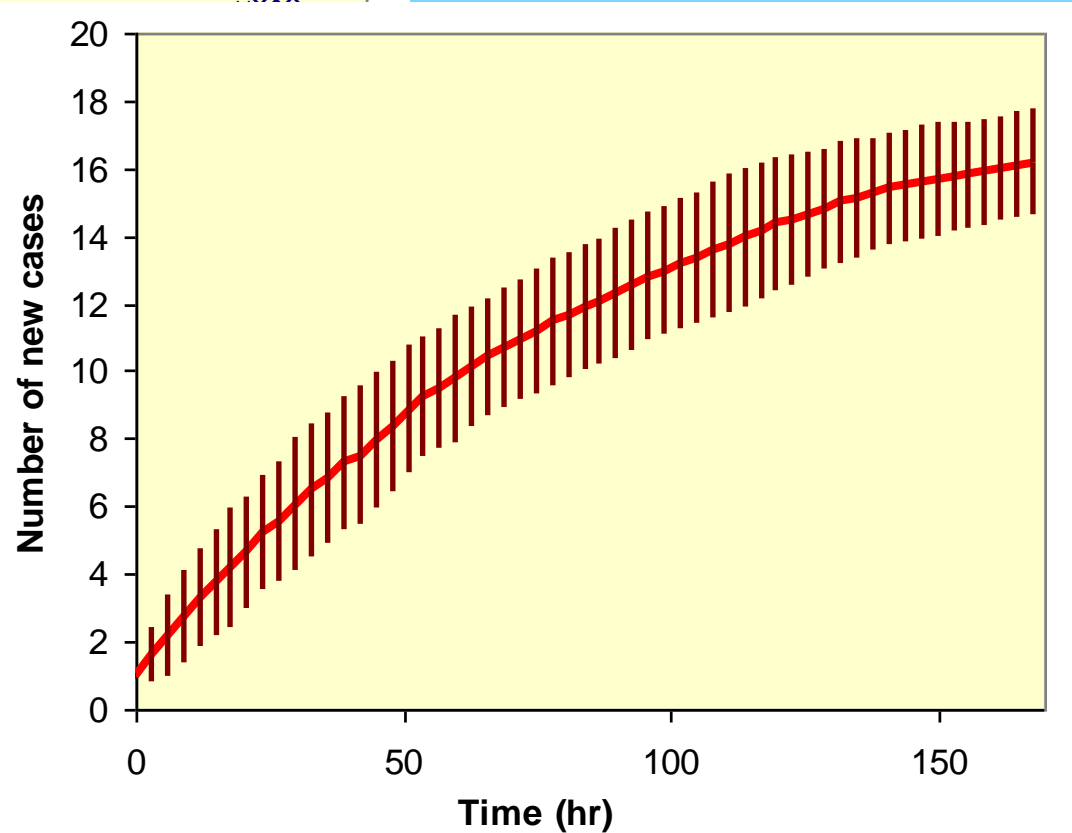
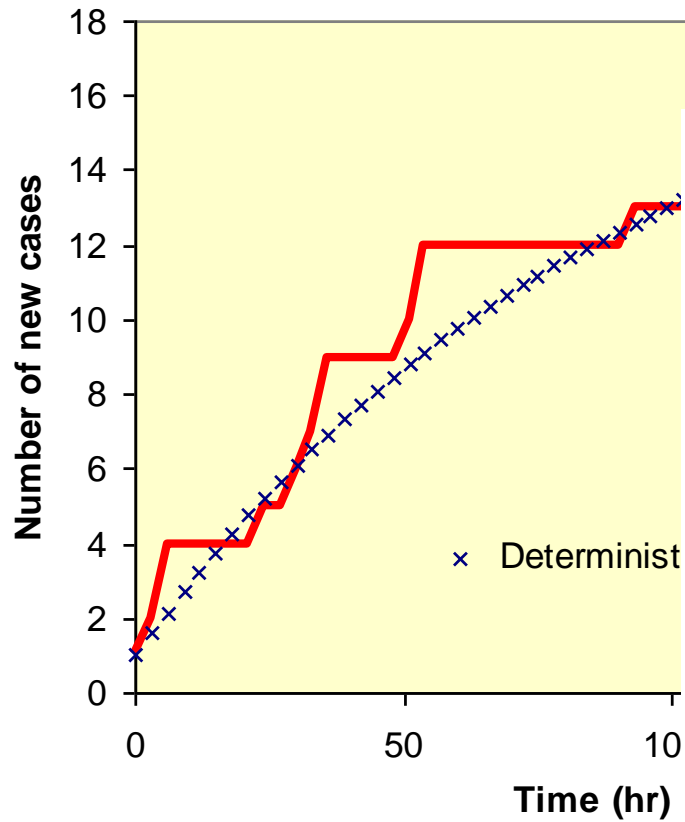
Disease	Case	Quanta/h	Reported by
TB	Average TB patient	1.25	Nardell <i>et al</i> (1991)
TB	Outbreak in office building	12.7	Nardell <i>et al</i> (1991)
TB	Human to guinea pig transmission	0.3-44	Escombe et al (2007)
MDR TB	Human to guinea pig transmission (highest infectors)	40,52,226	Escombe et al (2008)
Measles	Outbreak in a school	570	Rudnick &Milton(2003)
Influenza	School cases in Taiwan	66.91 (LN*)	Liao et al (2005)
Influenza	Aircraft outbreak	79-128	Rudnick &Milton(2003)
SARs	Taipei Hospital outbreak	28.77 (LN*)	Liao et al (2005)
Rhinovirus 16	Experimental data of Dick et al 1987	1-10	Rudnick &Milton(2003)

# Wells-Riley Results

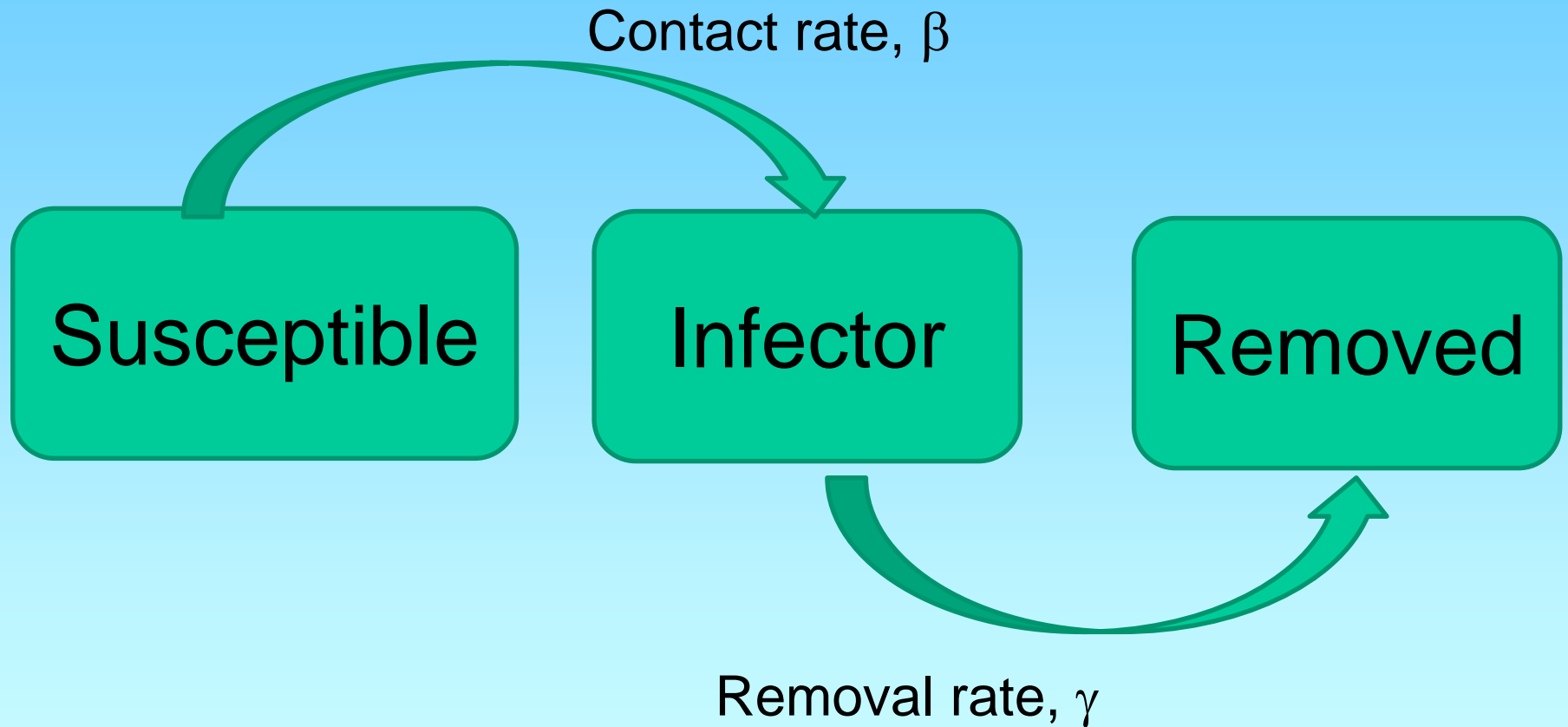


Fully mixed room: 10 susceptibles, 1 infector, 12 quanta/hr,  
10 l/min pulmonary ventilation, 32.25 m<sup>3</sup> room

# Stochastic Effects



# Epidemic models



# SIR Deterministic Formulation

- For a closed population of  $N$  people – no increase or decrease eg. Birth rate

$$N = S + I + R$$

- Assume homogeneity - every person has the same probability of infection, with contact rate  $\beta$
- People recover at a rate  $\gamma = 1/\text{duration of infection}$
- Consider rate of transition between states
- Expressed as ordinary differential equations

# SIR Deterministic model

$$\frac{dS}{dt} = -\beta SI$$

Rate susceptibles  
become infectious

$$\frac{dI}{dt} = \beta SI - \gamma I$$

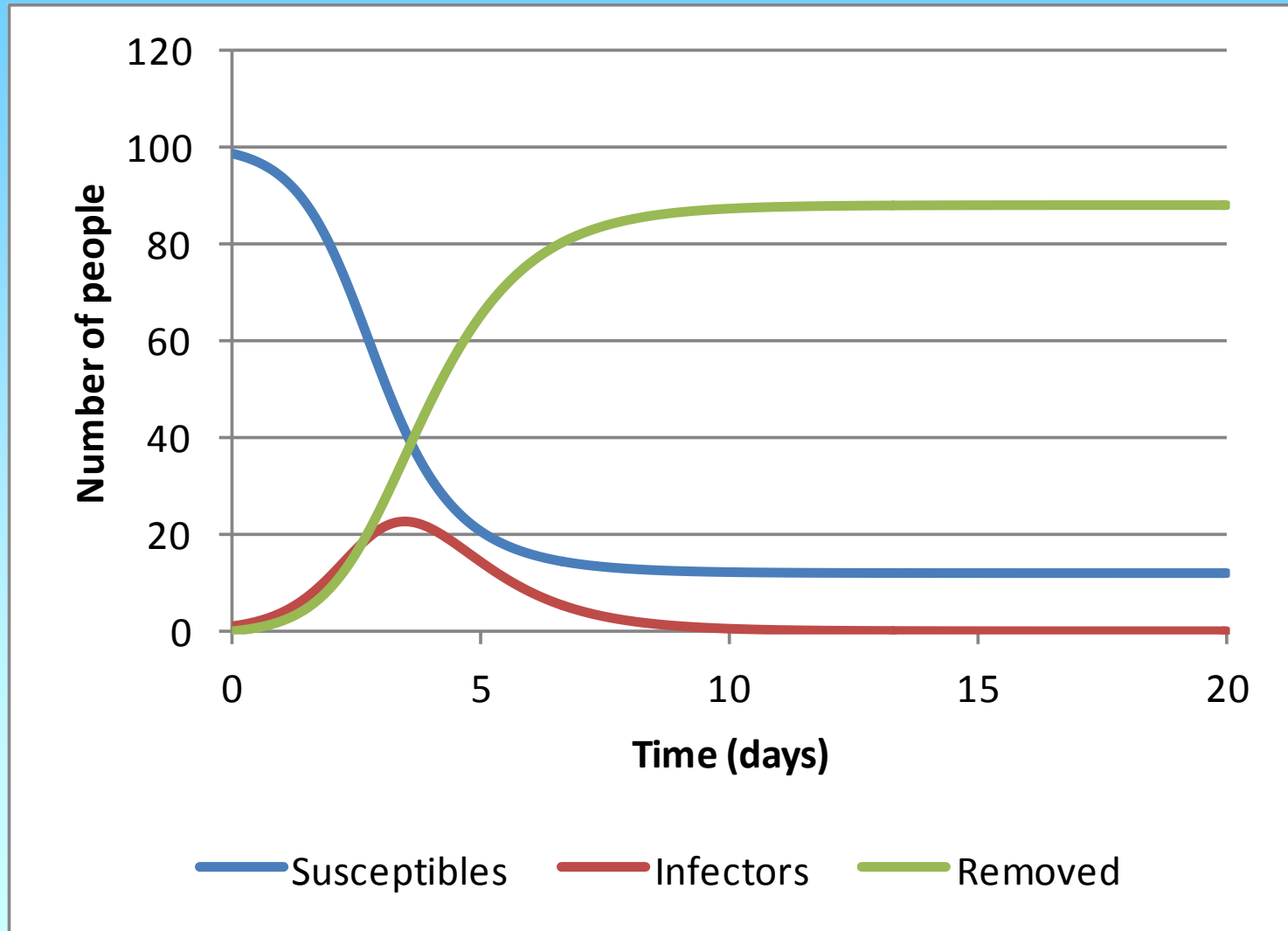
Rate infectors  
change = new  
infectors – those who  
recover/are removed

$$\frac{dR}{dt} = \gamma I$$

Rate infectors  
recover/are removed

Numerical solution is straightforward

# SIR outputs





# Reproduction rate

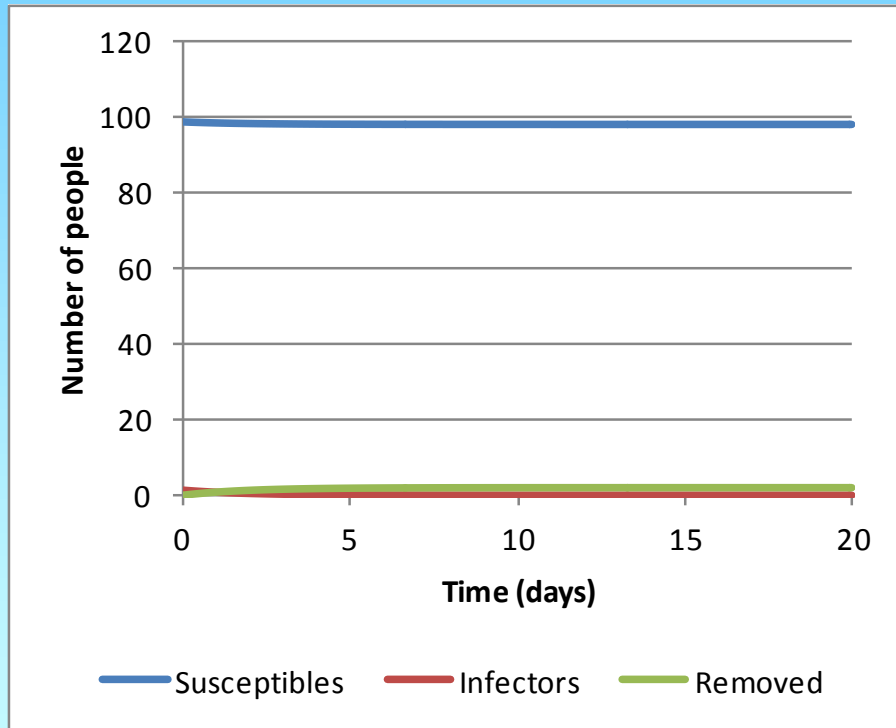
- Measure of rate of spread of an infection

**$R_o$  = number of secondary cases  
produced by an infector**

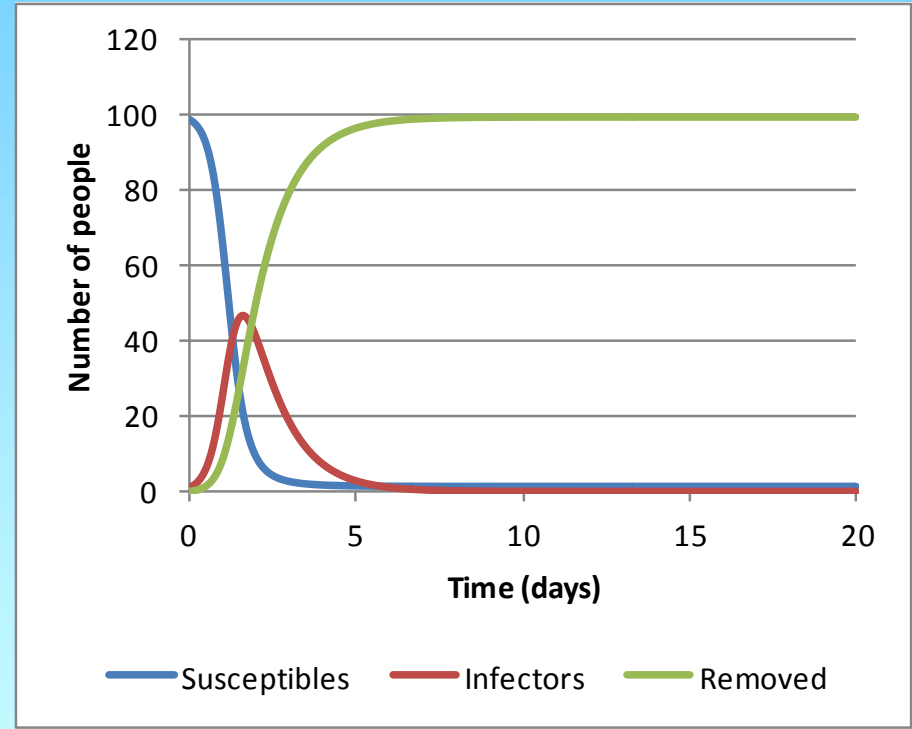
- $R_o < 1$ : infection will die out
- $R_o > 1$ : infection will spread through
- $R_o = 1$ : Epidemic threshold
- Can estimate from

$$R_o = N \frac{\beta}{\gamma}$$

# Epidemic threshold



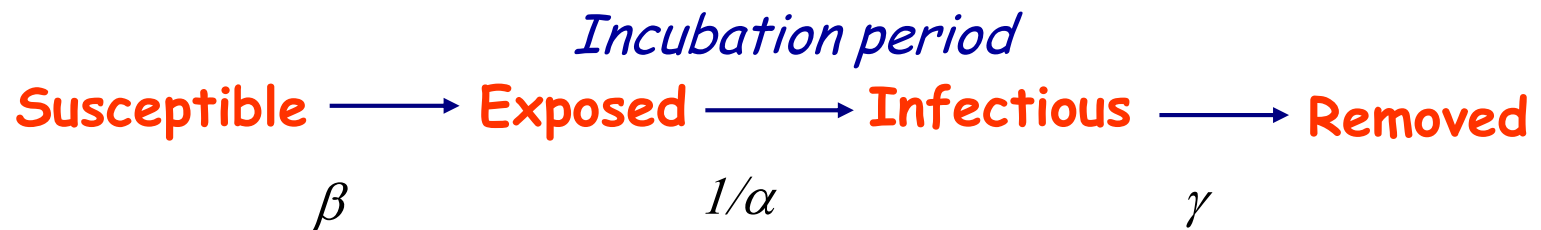
$R_0 < 1$



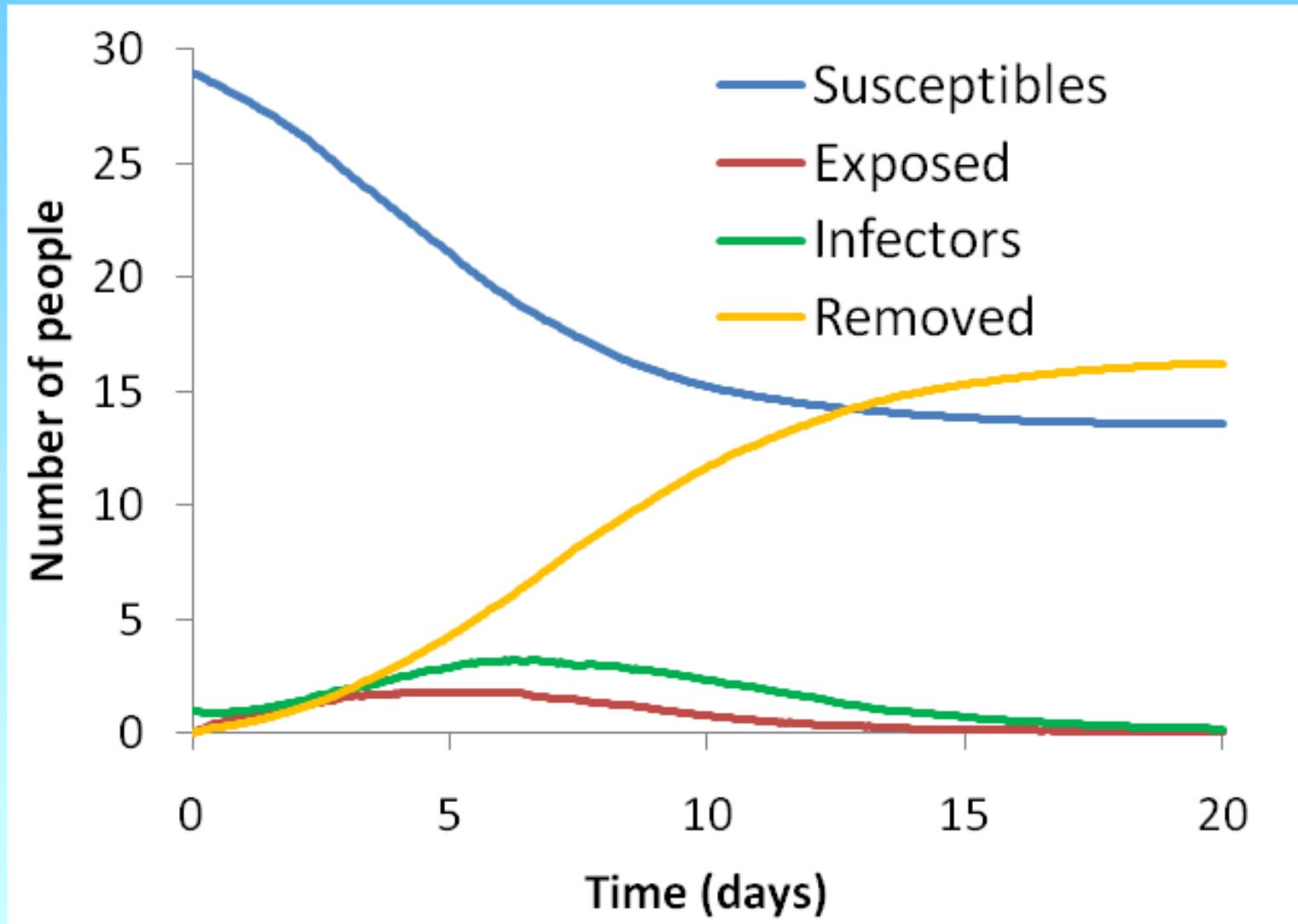
$R_0 > 1$

# SEIR Models

- Most common variant on SIR model
- Acknowledges that most diseases have an incubation period between exposure and becoming infectious



# SEIR Outputs



# Linking air and epidemic models

- Wells-Riley developed for TB – generally long incubation period
- Can be applied to short incubation infections such as influenza, SARs etc.
- Contact rate determined by air flows and breathing rate

$$\beta = \frac{pq}{Q}$$

Can use to estimate effectiveness of environmental controls

# Activity

In groups or individually:

- Use the spreadsheet models provided to explore how changes to disease parameters and the environment affect outbreaks
- Use the models to evaluate the scenarios described