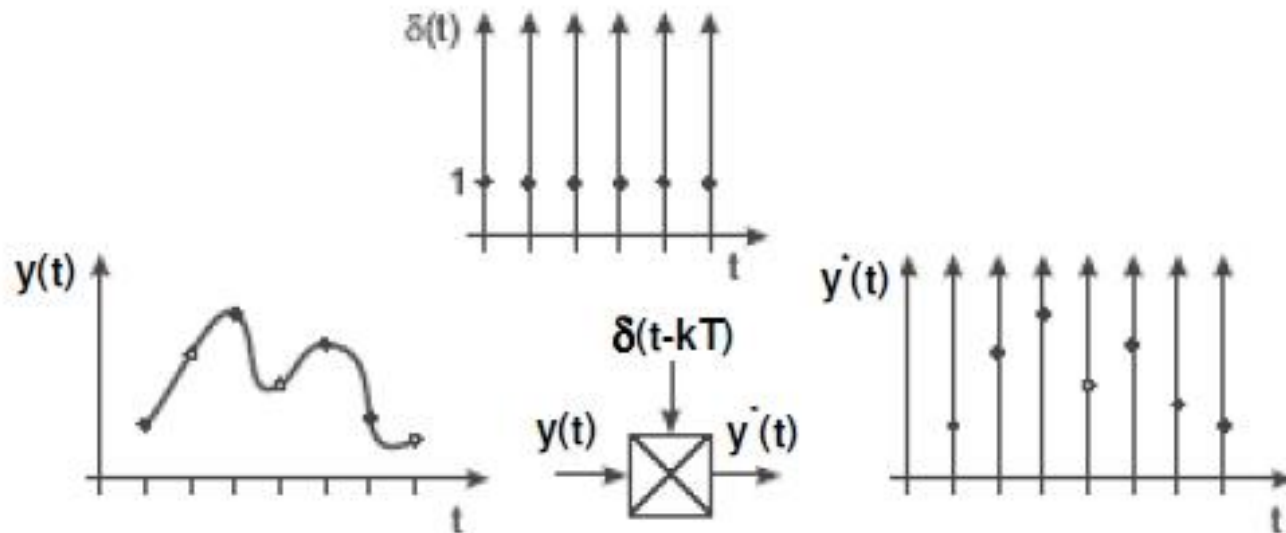




# TECNICAS DIGITALES III

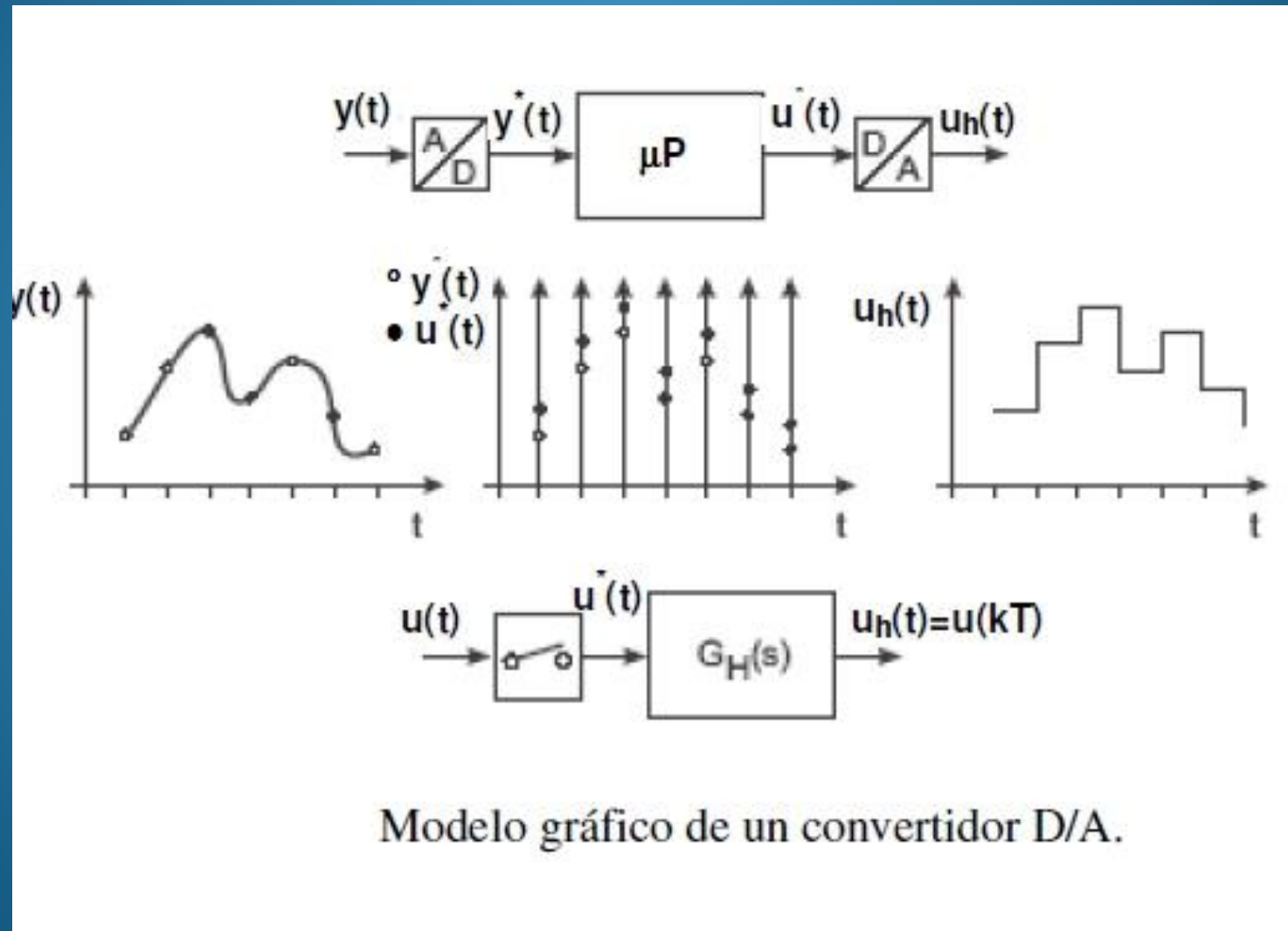
# Conversor AD

$$y(t) \cdot \sum_{k=-\infty}^{\infty} \delta(t-kT) = y^*(t)$$



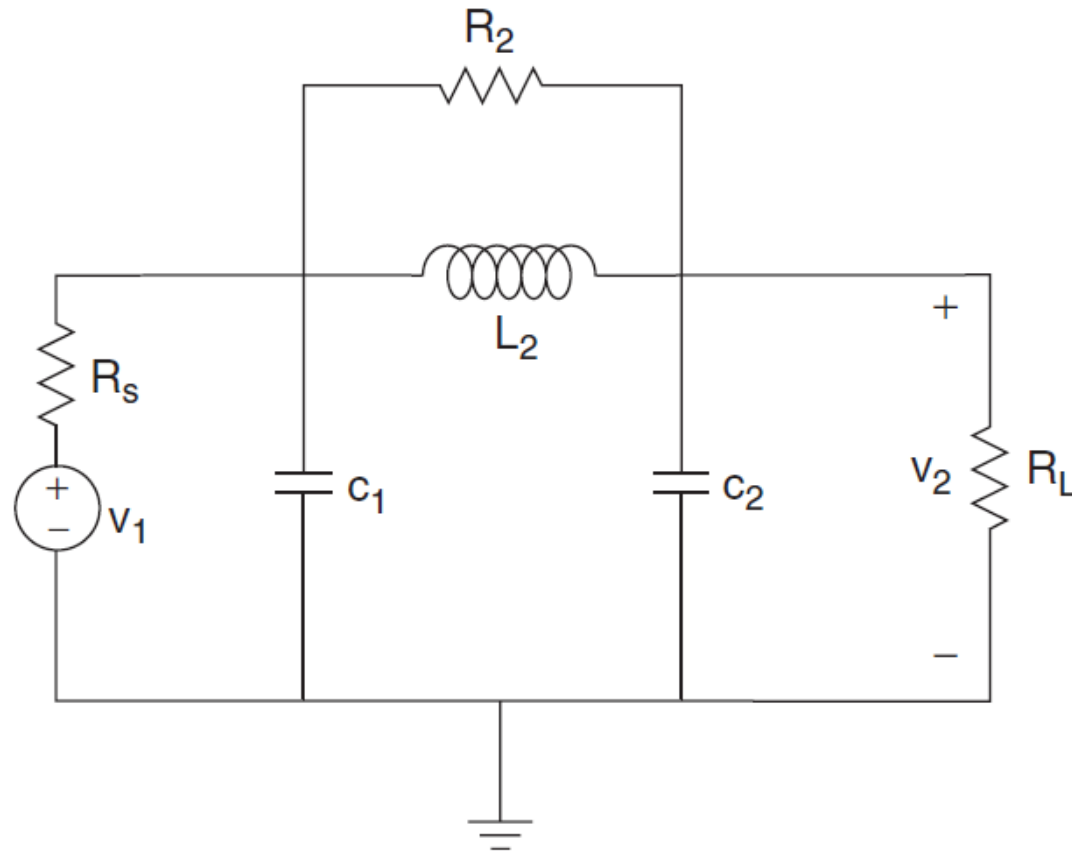
Modelo gráfico de un convertidor A/D.

# Conversor AD



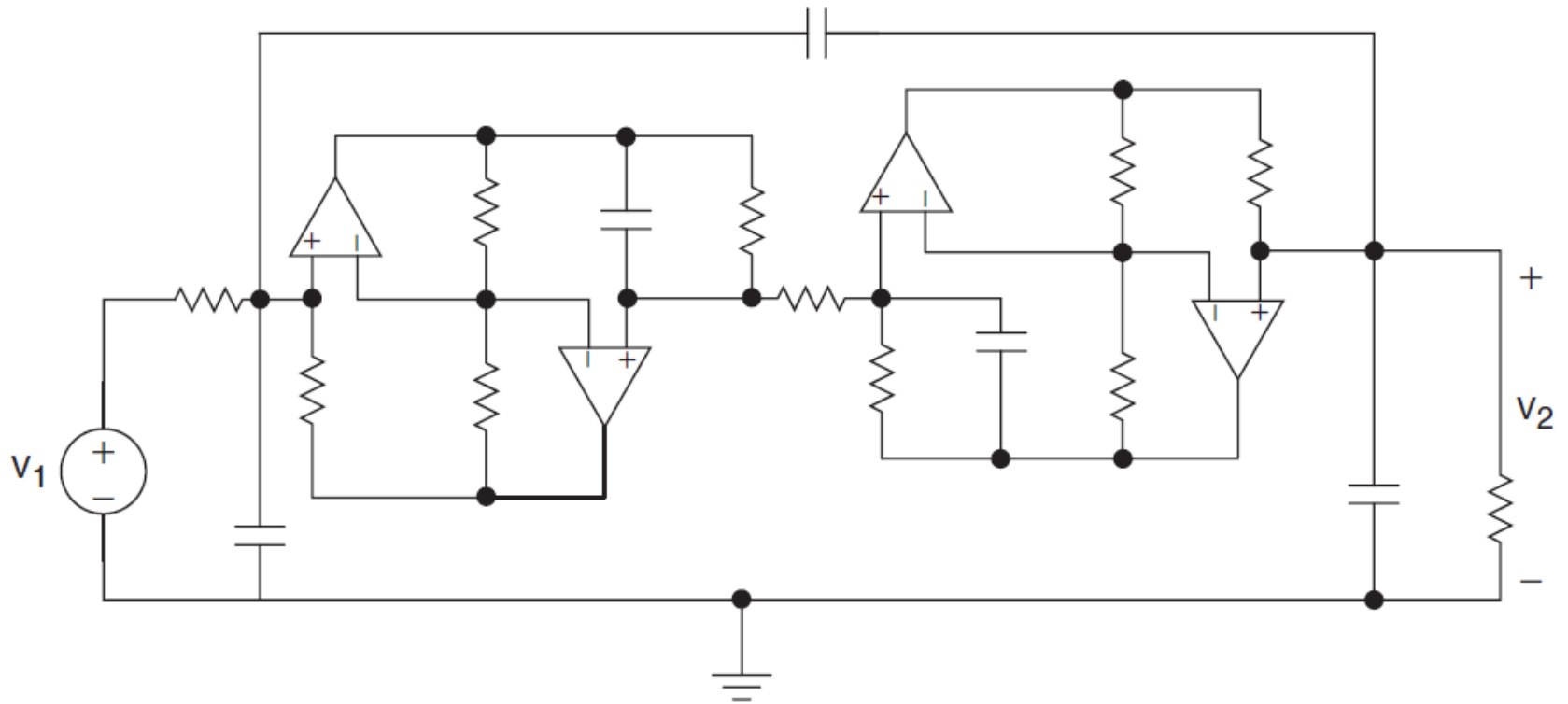
Modelo gráfico de un convertidor D/A.

# Conversor AD



**Figure 1.12** A lowpass analog  $LC$  filter.

# Conversor AD



**Figure 1.13** An active- $RC$  lowpass analog filter.

# Conversor AD

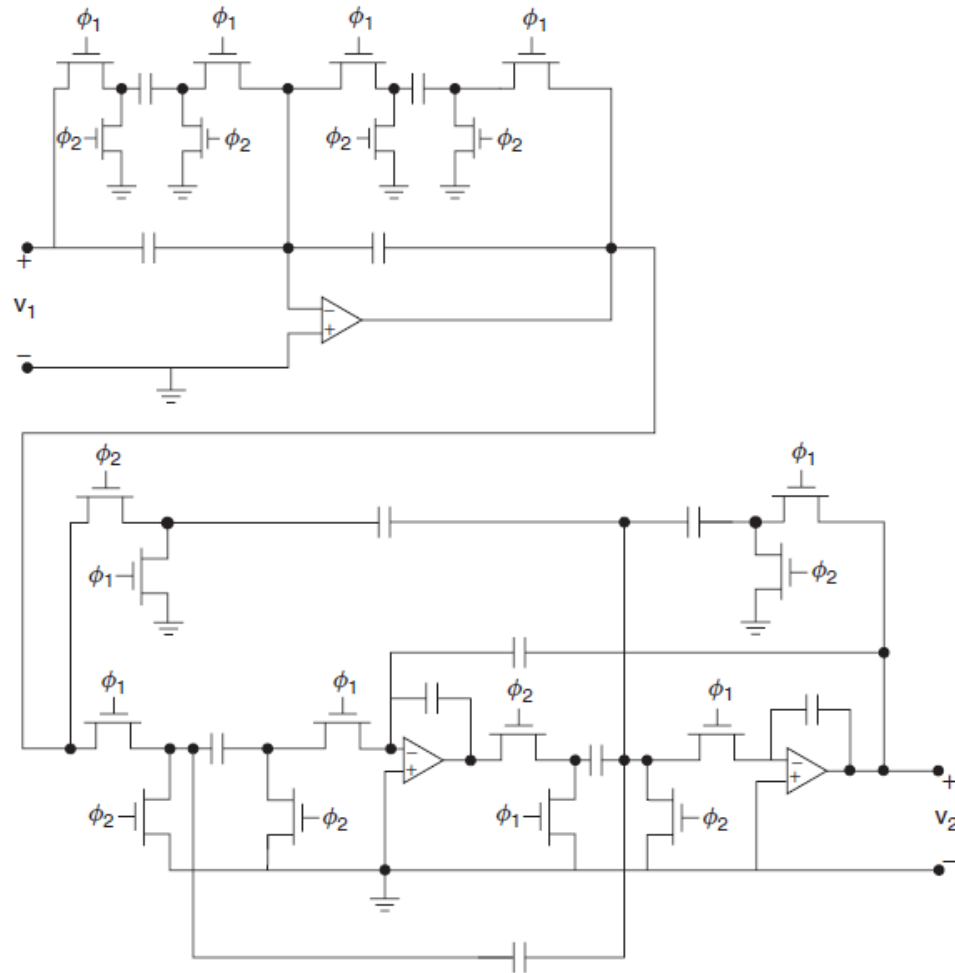


Figure 1.14 A switched-capacitor lowpass (analog) filter.

# Conversor AD

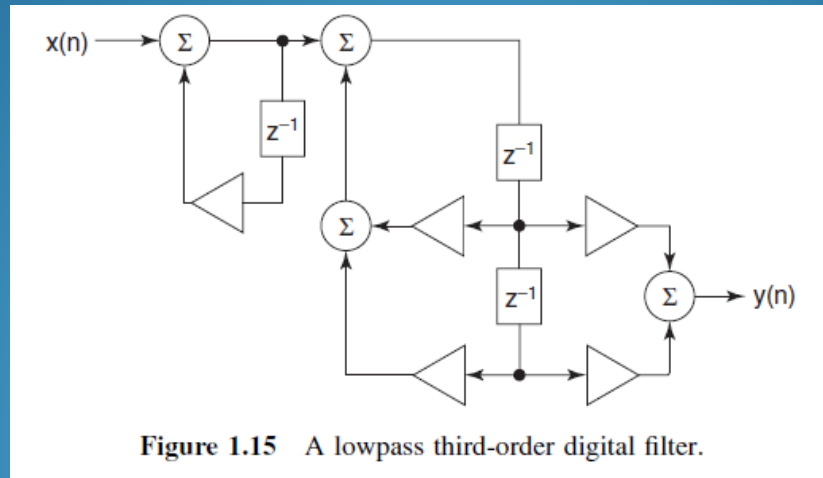


Figure 1.15 A lowpass third-order digital filter.

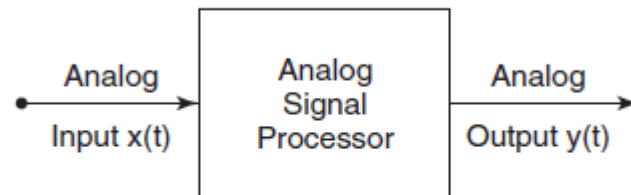


Figure 1.16 Example of an analog signal processing system.

# Conversor AD

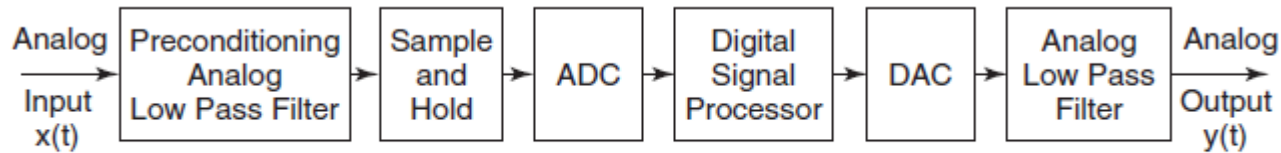


Figure 1.17 Example of a digital signal processing system.

Delay Element  $X_1(n) \longrightarrow \boxed{z^{-1}} \longrightarrow Y_1(n) = X_1(n-1)$

Multiplier  $X_2(n) \longrightarrow \boxed{K} \longrightarrow Y_2(n) = KX_2(n)$

Adder  $X_3(n) \longrightarrow \bigcirc \Sigma \longrightarrow Y_3(n) = X_3(n) + X_4(n)$   
 $X_4(n) \longrightarrow \bigcirc \Sigma$

Modulator  $X_5(n) \longrightarrow \bigcirc \Sigma \longrightarrow Y_5(n) = X_5(n)m_6(n)$   
 $m_6(n) \longrightarrow \bigcirc \Sigma$

Figure 2.1 The basic components used in a discrete-time system.



# Convensor AD

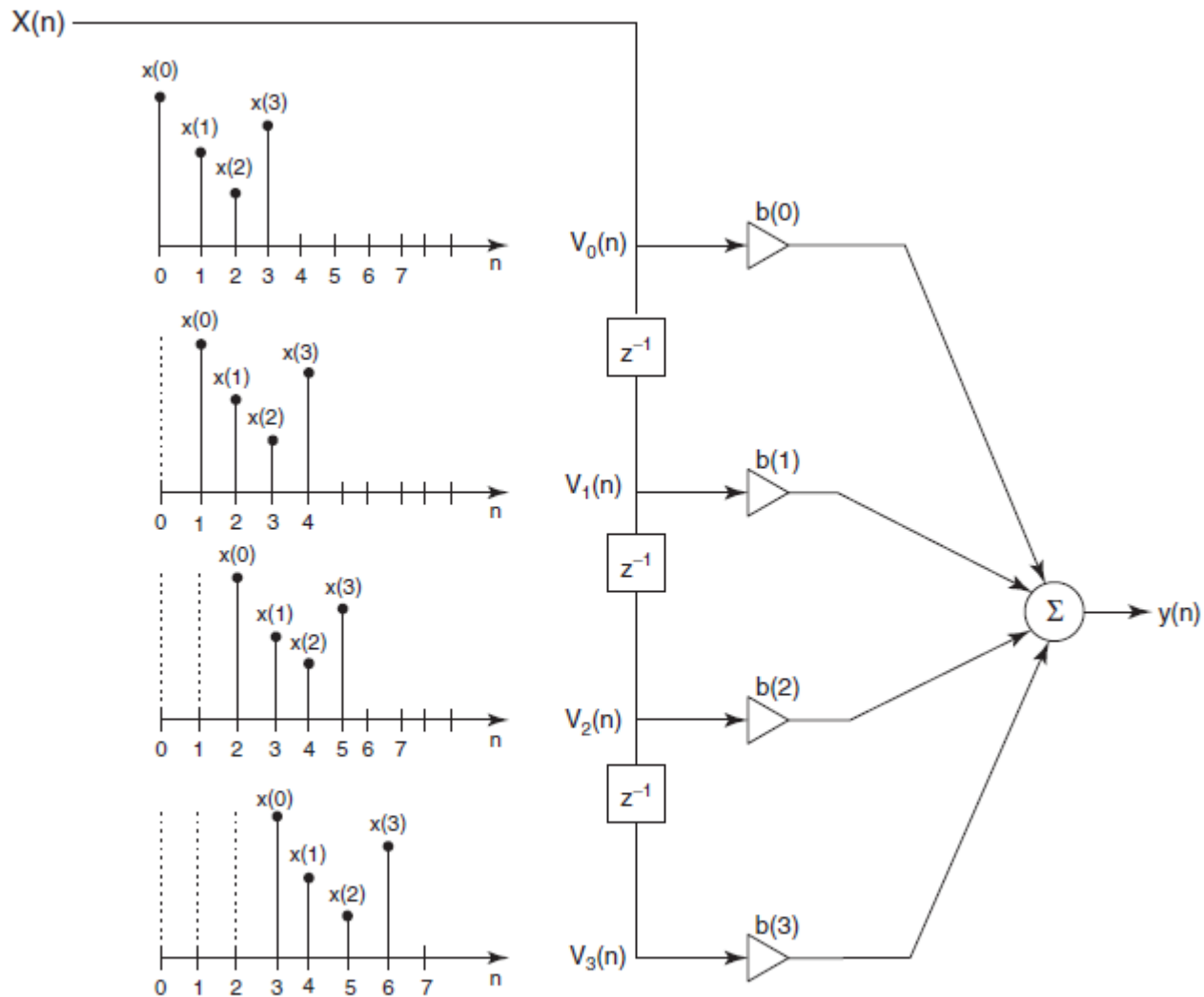
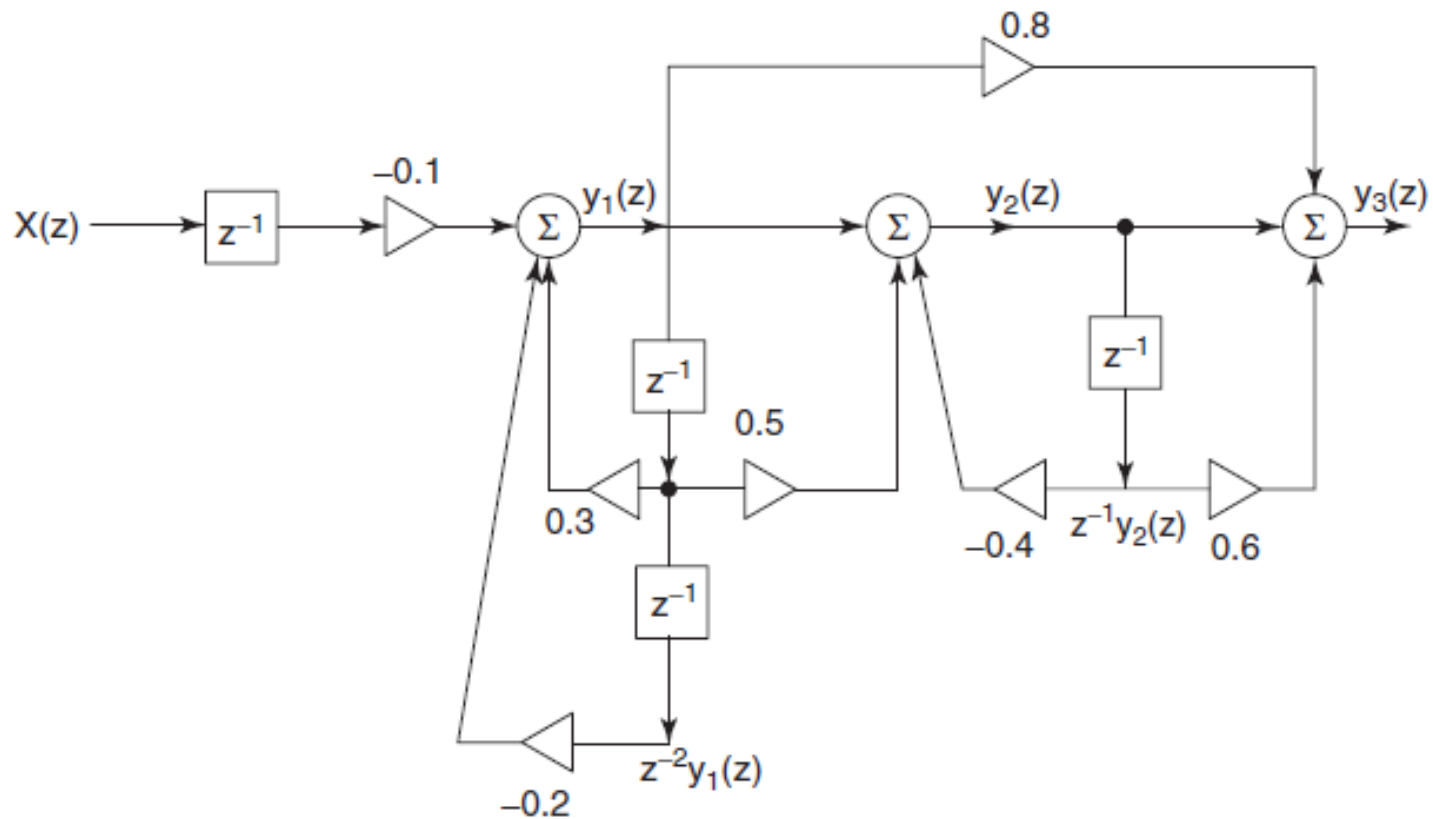


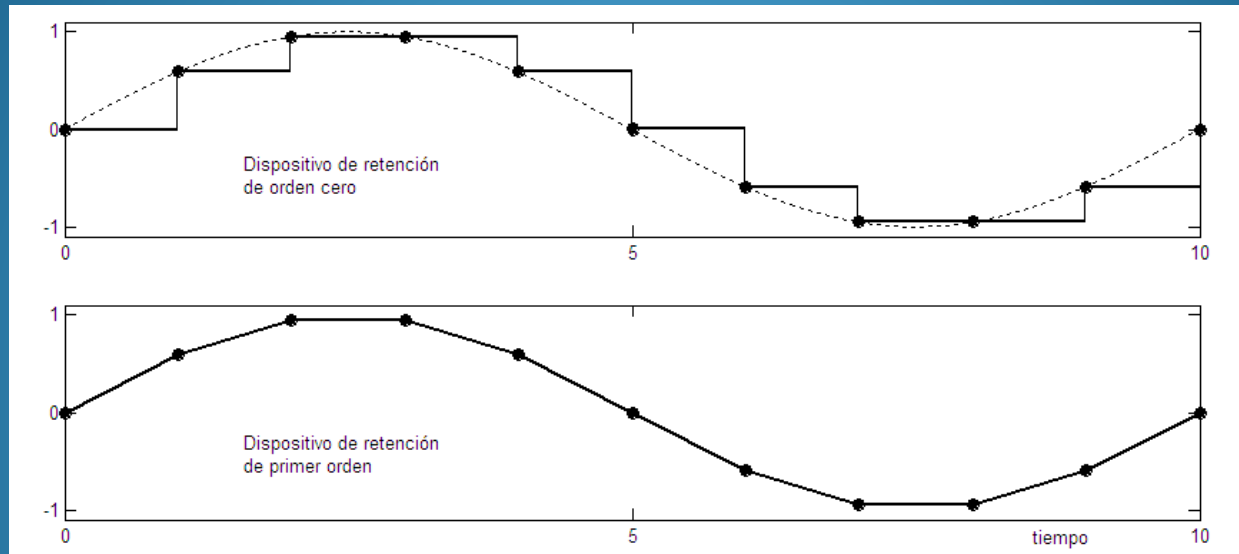
Figure 2.2 Operations in a typical discrete-time system.

# Conversor AD



**Figure 2.3** Schematic circuit for a discrete-time system.

# Retenedor de orden '0' 'zoh'



$$kT \leq \tau < (k+1)T$$

$$h(kT - \tau) = a_n \tau^n + a_{n-1} \tau^{n-1} + \dots + a_1 \tau + a_0 \quad h(kT) = x(kT) \quad a_0 = x(kT)$$

$$h(kT - \tau) = x(kT)$$

$$\sigma = 0 \quad t < 0 \quad \sigma = 1 \quad t \geq 0$$

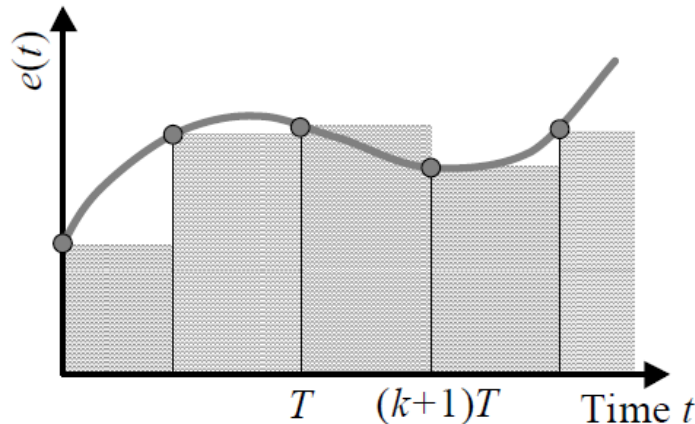
$$h(t) = x(0)[\sigma(t) - \sigma(t-T)] + x(T)[\sigma(t-T) - \sigma(t-2T)] + x(2T)[\sigma(t-2T) - \sigma(t-3T)] \dots x(nT)[\sigma(t-(n-1)T) - \sigma(t-nT)]$$

# Continuo a discreto

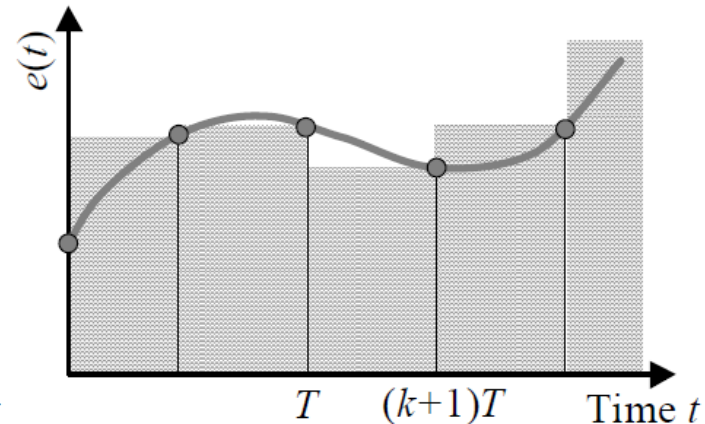
- *Forward Difference:*  $u(k+1) \approx u(k) + e(k) \cdot T$
- *Backward Difference:*  $u(k+1) \approx u(k) + e(k+1) \cdot T$
- *Trapezoidal Approximation:*  $u(k+1) \approx u(k) + \frac{[e(k+1) + e(k)]}{2} \cdot T$   
(Bilinear Transformation)  
(Tustin's Approximation)

- *Forward Difference:*  $C(z) = \frac{U(z)}{E(z)} = \frac{T}{z-1} = \frac{Tz^{-1}}{1-z^{-1}}$
- *Backward Difference:*  $C(z) = \frac{U(z)}{E(z)} = \frac{Tz}{z-1} = \frac{T}{1-z^{-1}}$
- *Trapezoidal Approximation:*  $C(z) = \frac{U(z)}{E(z)} = \frac{T}{2} \frac{z+1}{z-1} = \frac{T}{2} \frac{1+z^{-1}}{1-z^{-1}}$

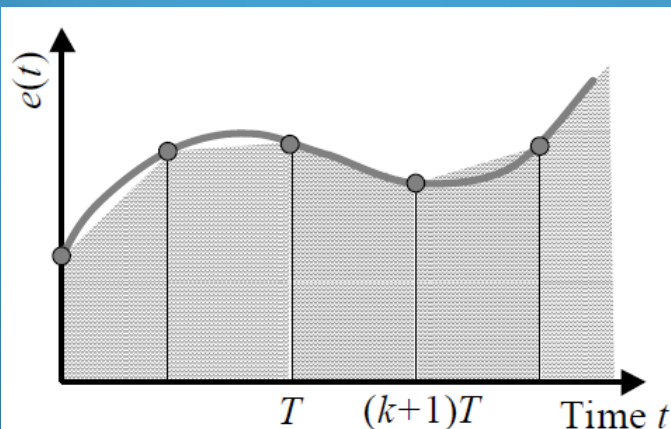
# Continuo a discreto



Forward Difference



Backward Difference



Trapezoidal Approximation

# Continuo a discreto

▪ *Forward Difference:*  $s \rightarrow \frac{z-1}{T}$  i.e.  $C(z) = C(s) \Big|_{s \rightarrow \frac{z-1}{T}}$

▪ *Backward Difference:*  $s \rightarrow \frac{z-1}{Tz}$  i.e.  $C(z) = C(s) \Big|_{s \rightarrow \frac{z-1}{Tz}}$

▪ *Trapezoidal Approximation:*  $s \rightarrow \frac{2}{T} \frac{z-1}{z+1}$  i.e.  $C(z) = C(s) \Big|_{s \rightarrow \frac{2}{T} \frac{z-1}{z+1}}$

$$C(s) = \frac{10s + 1}{s + 1}$$

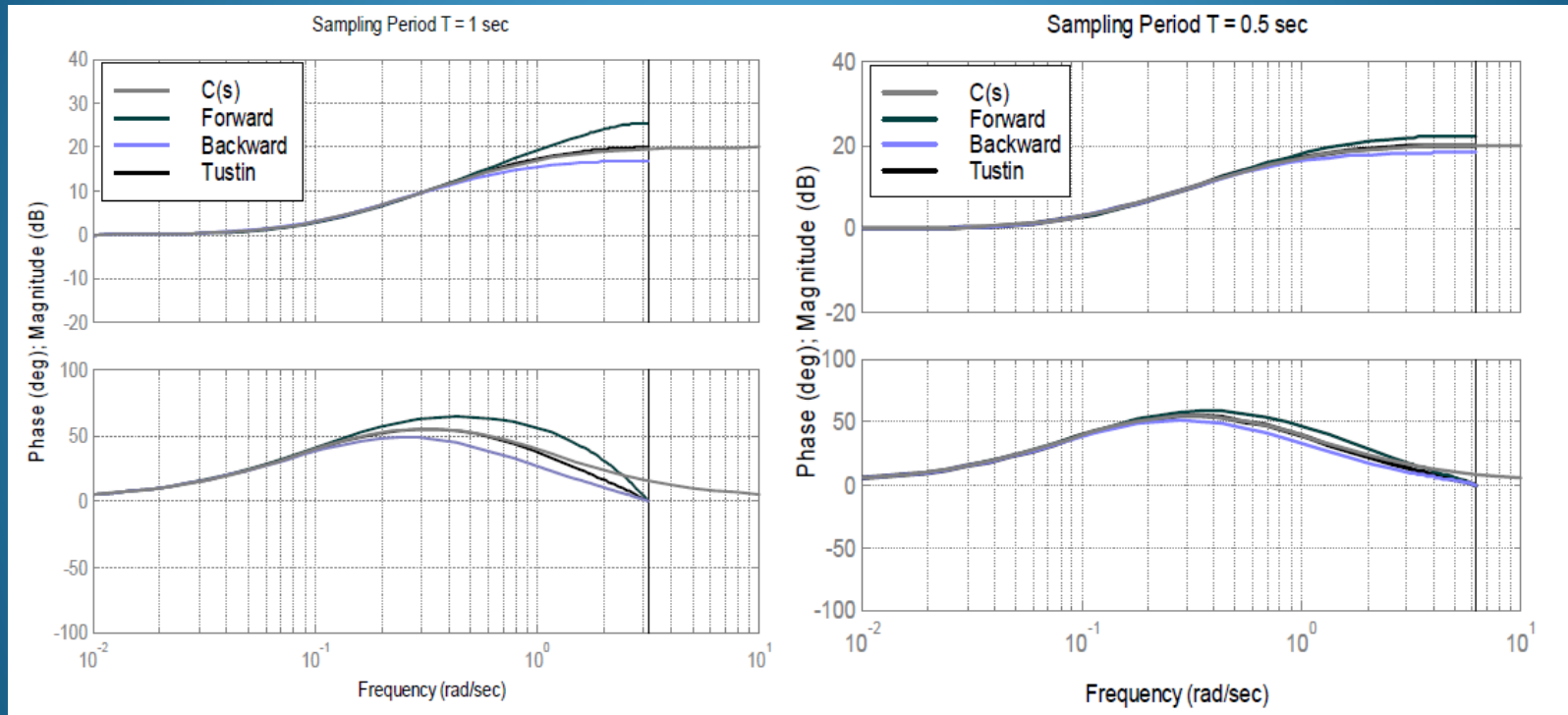
*Forward Difference:*  $C(z) = C(s) \Big|_{s \rightarrow \frac{z-1}{T}} = \frac{10z - (10 - T)}{z - (1 - T)}$

*Backward Difference:*  $C(z) = C(s) \Big|_{s \rightarrow \frac{z-1}{Tz}} = \frac{(10 + T)z - 10}{(1 + T)z - 1}$

*Trapezoidal Approximation:*  $C(z) = C(s) \Big|_{s \rightarrow \frac{2}{T} \frac{z-1}{z+1}} = \frac{(20 + T)z - (20 - T)}{(2 + T)z - (2 - T)}$



# Continuo a discreto



# Realización de controladores y filtros digitales

Función de transferencia pulso y pasaje de tiempo continuo a tiempo discreto

```
>> num=[3 2 1];  
>> den=[1 1 3 1];  
>> s1=tf(num,den)  
  
Transfer function:  
    3 s^2 + 2 s + 1  
-----  
s^3 + s^2 + 3 s + 1  
  
>> fz=tf(num,den,1e-3)  
  
Transfer function:  
    3 z^2 + 2 z + 1  
-----  
z^3 + z^2 + 3 z + 1  
  
Sampling time: 0.001
```

```
>> fz2=c2d(s1,1e-3,'tustin')  
  
Transfer function:  
0.0015 z^3 - 0.001499 z^2 - 0.0015 z + 0.001499  
-----  
z^3 - 2.999 z^2 + 2.998 z - 0.999  
  
Sampling time: 0.001
```

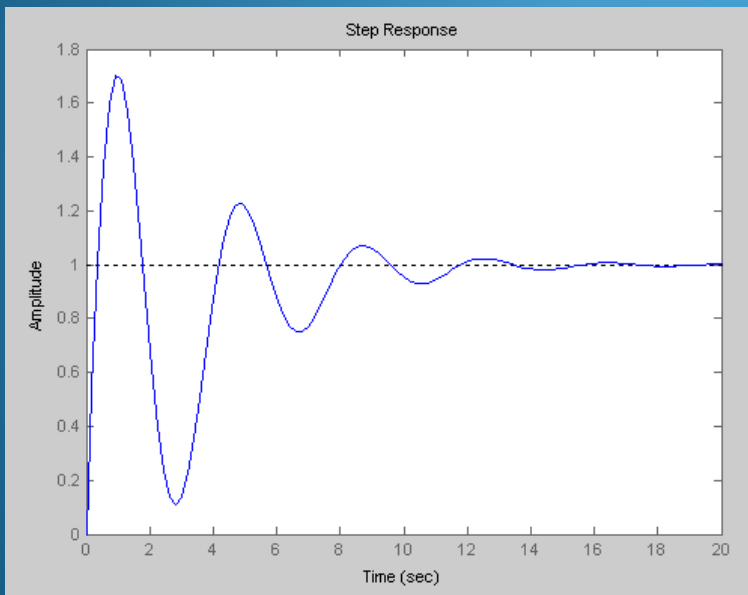
```
>> fz2=c2d(s1,1e-3,'imp')  
  
Transfer function:  
    3 z^3 - 5.998 z^2 + 2.998 z  
-----  
z^3 - 2.999 z^2 + 2.998 z - 0.999  
  
Sampling time: 0.001  
>> fz2=c2d(s1,1e-3,'zoh')  
  
Transfer function:  
0.002999 z^2 - 0.005997 z + 0.002997  
-----  
z^3 - 2.999 z^2 + 2.998 z - 0.999  
  
Sampling time: 0.001
```



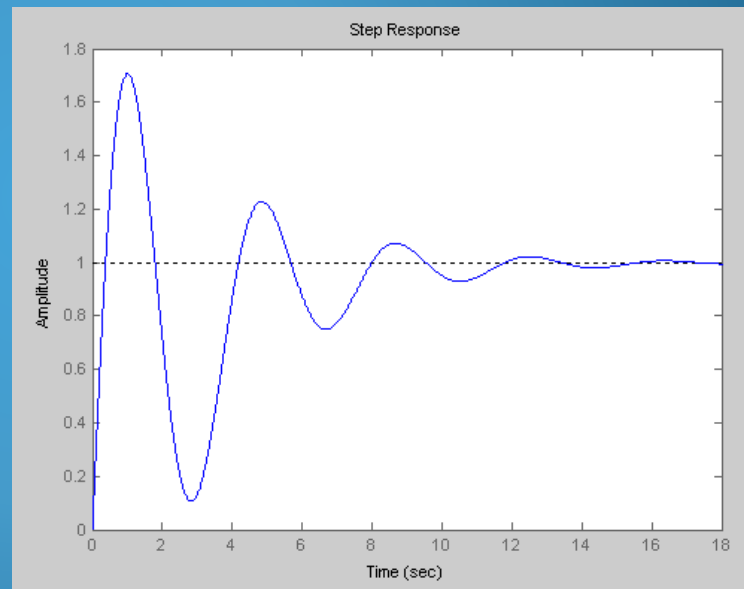
# Realización de controladores y filtros digitales

Pasaje de una función en tiempo continuo a tiempo discreta con Matlab

Respuesta al escalón  $F(s)$



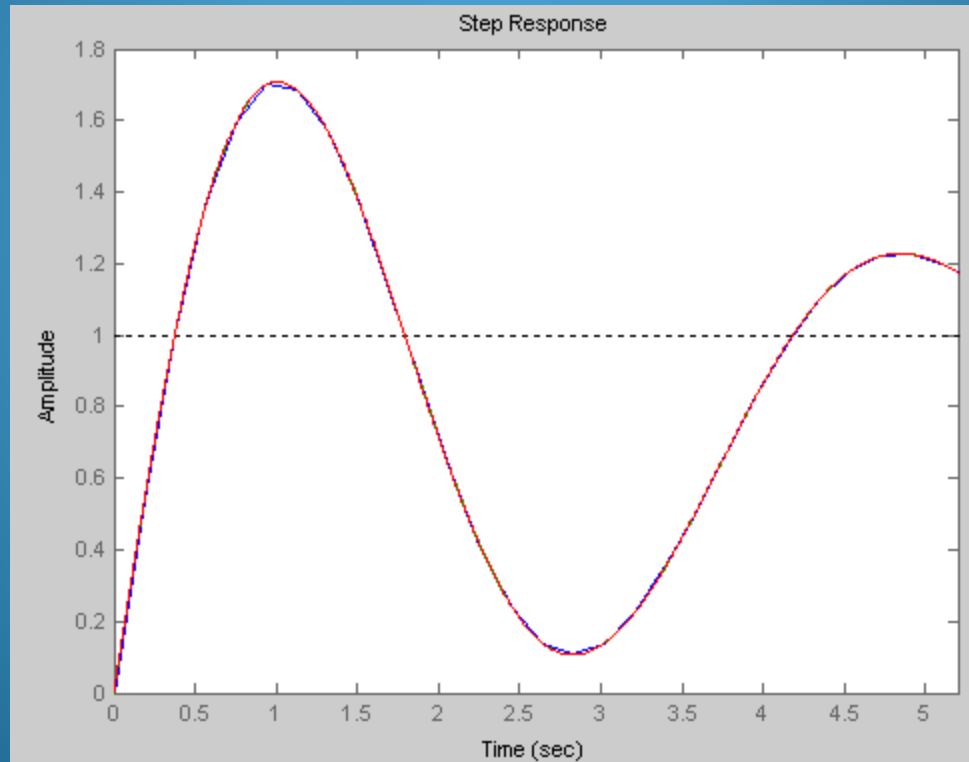
Respuesta al escalón  $F(z)$  'toustin'  $T_s=1e-3$



# Realización de controladores y filtros digitales

Respuesta al escalon  $F(z)$  'zoh'  $T_s=0.1$  (Azul)

$F(z)$  'tustin'  $T_s=0.1$  (rojo) t verde



# Realización de controladores y filtros digitales

**Diagrama en bloques de los filtros que involucren retardos, sumadores y restadores**

**Programación Directa :** Utiliza un elemento de retraso por cada retraso que aparece en el numerador o denominador. Solo útil académicamente.

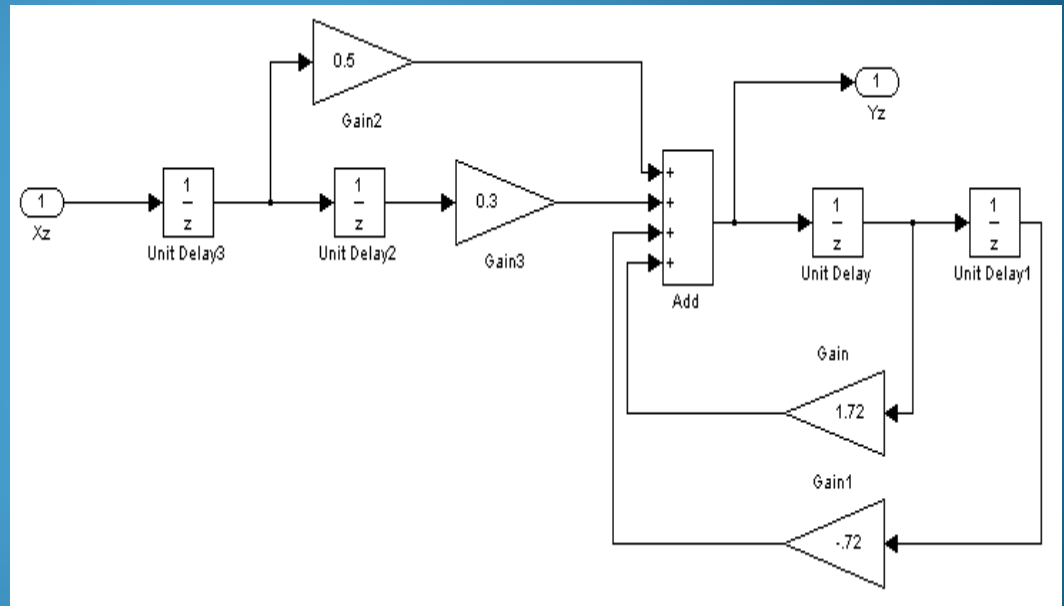
**Programación estándar:** Minimiza el numero de retardos.

**Errores en la realización:**

1. Error de cuantificación de la señal de entrada.
2. Error por la acumulación en el redondeo de las operaciones aritméticas.
3. Error por cuantificación de coeficientes.

# Realización de controladores y filtros digitales

**Programación Directa :** Utiliza un elemento de retraso por cada retraso que aparece en el numerador o denominador. Solo útil académicamente.



$$\frac{Y}{X} = \frac{0.5z + 0.3}{z^2 - 1.7z + 0.72}$$

$$\frac{Y}{X} = \frac{0.5z^{-1} + 0.3z^{-2}}{1 - 1.7z^{-1} + 0.72z^{-2}}$$

$$Y(1 - 1.7z^{-1} + 0.72z^{-2}) = (0.5z^{-1} + 0.3z^{-2})X$$

# Realización de controladores y filtros digitales

**Programación estándar:** Minimiza el numero de retardos.

$$\frac{Y}{X} = \frac{0.5z + 0.3}{z^2 - 1.7z + .72}$$

$$\frac{Y}{X} = 0.5z^{-1} + 0.3z^{-2} \frac{1}{1 - 1.7z^{-1} + .72z^{-2}} \frac{H}{H}$$

