## INTRODUCTION to ECONOMETRICS

Home-work I 2020

<u>Deadline</u>. September 13 11h59pm [Paris time] via email in PDF format and first class after the deadline for the printed version of your work again. Delays will be penalized.

<u>Instructions</u>. I am expecting one PDF file for each student named LAST\_NAME.pdf containing the description of the code, the results obtained and their interpretations. This document should be formatted according to the template available on the course web-page. Not respecting the formatting will affect your grade.

## Problem 1 [LLN]

Let X be a random variable representing the roll of a 'fair' dice.

Write the R code to show the Law of Large Numbers in action. Build a Monte Carlo experiment in which you set the sample size n equal to 2, 25, 100 and 1000 and

- 1. show that the range of variation of the sample average  $\bar{X}$  shrinks;
- 2. represent graphically the four cases as in slide 18 in my Class 1 presentation.

## Problem 2 [CLT].

Let X be a Normally distributed random variable with mean  $\mu_{\rm X}$  = -10 and variance  $\sigma_{\rm X}^2$  = 1.

Write the R code to show the Central Limit Theorem in action. Build a Monte Carlo experiment in which you set the sample size n equal to 2, 25, 100 and 1000 and

- 1. show that the distribution of  $\frac{X-\mu_X}{\sqrt{\frac{\sigma_X^2}{n}}}$  converges to a standardized Normal distribution, that is to a Normal distribution with mean and variance equal to 0 and 1 respectively.
- 2. represent graphically the four cases as in slide 23 in my Class 1 presentation.