quinta-feira, 8 de dezembro de 2022 15

Exas. for An Introduction to Probability and Statistics by Robots, and Saleh (Thind Edition)

Problems 8.2

1 # Tn is a sequence of entimatours for
$$\theta$$

$E(Tn) \rightarrow \theta$ and $Van(Tn) \rightarrow 0$, $n \rightarrow \infty$

The is consistent for θ

$Tn \rightarrow 0$, so $\lim_{n \rightarrow \infty} E[(Tn - \theta)^2] = 0$
 $n \rightarrow \infty$

III To consistent for 8 and [To-0/ &A<00

$$EL(T_m-\theta)^2] = ... = E[(T_m-E(T_m))^2] + [E(T_m-\theta)]^2$$

Variance

Sign 2

$$\lim_{n\to\infty} t = \left[\left(\tau_n - \theta \right)^2 \right] = \lim_{n\to\infty} \int_{0}^{\infty} \left[\int_{0}^{\infty} \left(\tau_n - \theta \right) \right]^2$$

=0

$$=\lim_{n\to\infty} \left[E(T_n) - E(\theta) \right]^{2}$$

$$: T_n \xrightarrow{2} \theta$$

Resolcias de protessas Raul:

III To consistent for 8 and [To-0/ < A < 00 Se Y for V.A não negativos, $= y = \int_0^\infty y \cdot f_0(y) dy = \int_0^\infty f(y) dx$ $E|T_{M}-9|^{2} \rightarrow 0 , n \rightarrow \infty$ $E|T_n-\theta|^2=\int_0^\infty P(|T_n-\theta|^2>E)dE$ $\begin{cases}
\epsilon = \epsilon^{2} \\
\epsilon = 2\epsilon \cdot \epsilon
\end{cases}$ = 1 = P(|Tm-0| > NE) dE = 2. 500 6. P(|Tn-0| > E) dE $T_n \rightarrow 0$ $\leq Z \cdot A \cdot \int_{0}^{A} P(|T_{m}-\Theta| > E) dE \xrightarrow{T} o, m \rightarrow on$ $,', \quad E \left| T_n - \Theta \right|^2 \rightarrow 0, n \rightarrow \infty \implies T_n \implies \Theta$ $|T_m - \theta| \leq A_m \leq \infty$ Para esse caso, temos: $E|T_n-\theta|^2 \leq 2A_n \int_0^{A_n} P(|T_n-\theta| > \epsilon) d\epsilon$ Una vez que nos salemas o solor, no limite, por causa obo fato de An estor indexado em n, nos ha garantia que $T_n \stackrel{<}{\longrightarrow} 0$.

(2) $\star X_1, ..., X_n A.A. do <math>\overline{U}[0, \Theta], \Theta \in \bigoplus = (0, \infty)$

$$+ X(n) = \max \{ x_1, \dots, x_n \}$$

$$+ X(m) \xrightarrow{P} \theta \} \text{ as a bornentu } M$$

$$P(|X(n) - \theta| > E) \xrightarrow{P} 0, n \xrightarrow{P} 0,$$

$$Von(y_n) = Von(2\overline{x}) = 4 \cdot Von(\overline{x}) = 4 \cdot 4 \cdot 1 \quad \text{in } 0$$

$$= \frac{4 \cdot 0}{72 \cdot m} = \frac{4}{2m}$$

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$$\Rightarrow 0, m \Rightarrow 0.$$
Pulo terrora z, uma vag que $E(y_m) = 0 \times Von(y_m) \Rightarrow 0$

$$m \Rightarrow n, y_m = \frac{1}{2m} \text{ consistante pour } 0.$$

$$\exists \quad x_{x_1}, x_{x_2}, \dots, x_{x_m} \text{ i. i. d. } y_{x_1} \leq 0$$

$$\forall \quad x_{x_2}, x_{x_2}, \dots, x_{x_m} \text{ i. i. d. } y_{x_1} \leq 0$$

$$\forall \quad x_{x_2}, x_{x_2}, \dots, x_{x_m} \text{ i. i. d. } y_{x_1} \leq 0$$

$$\forall \quad x_{x_2}, x_{x_2}, \dots, x_{x_m} = \frac{1}{2m} \cdot \frac{1}{2m$$

$$= \frac{2m+1}{m^{2}+m} \cdot \frac{2}{3} \cdot \frac{2}{x}$$

$$\Rightarrow 0, m \Rightarrow \infty$$

$$\text{Plot Testance 2, storic ring } para \text{ M.}$$

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$$\text{The Testa$$

Fela Lei Forte do Grando Números.

$$y_{m} = \lim_{X \to \infty} (X_{n}) + \lim_{X \to \infty} (X_{m}) \xrightarrow{q \to} E(\ln(x_{n})) = \lim_{X \to \infty} (\ln(x_{n}) + 1) = \lim_{X \to \infty} (\ln(x_{n}) + 1)$$

Puslems 8.3 (a) * XNB(x,B) (i) a desconhecido,/3 conhecido $f(z_1,...,z_n) = \frac{1}{(z_1 - 1)^n} \frac{1}{(z_1 - 1)^n} \frac{1}{(z_1 - 1)^n} \frac{1}{(z_1 - 1)^n} \frac{1}{(z_1 - 1)^n}$ $= \frac{1}{\left[\lceil (\beta) \right]^{n}} \frac{1}{\prod \alpha_{i} (1-\alpha_{i})} \cdot \left[\lceil (\alpha+\beta) \right]^{n} \left[\prod \alpha_{i} (1-\alpha_{i}) \right] \cdot \left[\lceil (\alpha+\beta) \right]^{n} \left[\prod \alpha_{i} (1-\alpha_{i}) \right] \cdot \left[\lceil (\alpha+\beta) \right]^{n}$ M(25, 12, ..., 2m) 8x (TZ:) i. Il 7: i estatuotica suficiente pona a. [ii] \angle conheido, β desunheido $\begin{cases}
(z_1, ..., z_n) = \frac{1}{\left[\int_{-\infty}^{\infty} (1 - z_i) \right]} \cdot \frac{\int_{-\infty}^{\infty} (z_i + z_i)}{\int_{-\infty}^{\infty} (1 - z_i)}
\end{cases}$ $h(z_1, \dots, z_n)$ $g(\pi(z_{-z_i}))$... Il (1-21:) e estatistica suficiente para B. (iii) $\angle 1, 3$ desconhecidos. $\Theta = (\angle 1, \beta)$ $\int [x_1, ..., x_n] = \prod_{\alpha \in \{1-\alpha_i\}} \frac{1}{\prod_{\alpha \in \{1-\alpha_i\}} \prod_{\alpha \in \{1-\alpha_i\}} \frac{1}{\prod_{\alpha$ h(24, ..., 2n) g (Tai, T (1-2i))

.. Tri e TI (1-21) sau estatisticos suficientes para (2) * $X = (X_1, ..., X_n)$ amostra de $N(x + x^2)$, $x \in \mathbb{R}$ conhecido $*T(X) = (\sum Xi, \sum Xi^{z})$ $|\overline{I}| \sum_{n=1}^{\infty} |x_n|^{2n} |x_n|^{2n} = \frac{1}{(\sqrt{2\pi})^n} \cdot \frac{1}{\sqrt{n}} \cdot |x_n|^{2n} = \frac{1}{2\sigma^2}$ $=\frac{1}{\left(\sqrt{z\pi}\right)^{m}}\cdot \ln\left(\frac{1}{zz^{2}}\right) + \ln\left(\frac{z}{z^{2}}\right) + \ln\left(\frac{z}{z}\right)$ $= \frac{1}{(\sqrt{2\pi})^n} \cdot \frac{1}{\sigma^n} \cdot lzp \left(-\frac{2}{2\pi i} + \sqrt{2\pi i} - n\alpha \right)$ h(n1,...,n) 8 (Z=i, Z=i²) $T(x) = (\sum xi, \sum xi^2)$ i estatistica suficienta para TIII Demonstrar que a família de distribuições T(X) é não completa. $E_{\sigma} \left\{ z \left(\sum x_i \right)^z - \left(x_{i+1} \right) \sum x_i^z \right\} = 0, \forall \sigma$ Vorms super que $P(2T_1^2 - (n+1)T_2) = 0) = 1$ $2T_1^2 - (n+1)T_2 = 0 = T_2 = \frac{2}{(n+1)}T_1^2$

3 $* \times_1, ..., \times_n \sim N(\mu, \sigma^2)$ $* \times = (\times_1, ..., \times_n)$ clearly sufficient for $N(\mu, \sigma^2), \mu \in \mathbb{R}, \tau > 0$.

(a) * X_1, X_2 convertor de $P(\lambda)$ * $T(X_1, X_2) = X_1 + \angle X_2$, $\angle > 1$ intervo

Sobre se que T=T(X) et suficiente para 0 se, e somertre se, a distribuições condicional de X, dondo T=t mais depende de O.

$$P(X_1 = 0, X_2 = 1 \mid X_1 + \alpha X_2 = \alpha) = \underbrace{P(X_1 = 0, X_2 = 1)}_{P(X_1 + \alpha X_2 = \alpha)}$$

II Calcular numerador.

$$P(X_1=0, X_2=1) = e^{-\lambda} \cdot e^{-\lambda} \lambda$$
$$= \lambda \cdot e^{-2\lambda}$$

TE Calcular obnominator $P(X_{1} + \alpha X_{2} = \alpha) = P(X_{1} + \alpha X_{2} = \alpha, X_{2} = 1) + P(X_{1} + \alpha X_{2} = \alpha, X_{2} = 0)$ $= P(Y_{1} + \alpha X_{2} = \alpha) | Y_{1} = \alpha | Y_{2} = \alpha) + P(X_{2} = \alpha) + P(X_{2} = \alpha)$ $= P(X_{1} = \alpha) | P(X_{2} = \alpha) | P(X_{2} = \alpha) | P(X_{2} = \alpha)$ $= \lambda \cdot e^{-2\lambda} + \frac{e^{-\lambda} \lambda^{\alpha}}{\alpha!} \cdot e^{-\lambda}$ $= \lambda e^{-2\lambda} \left(1 + \frac{\lambda^{\alpha-1}}{\alpha!}\right)$ $= \lambda e^{-2\lambda} \left(1 + \frac{\lambda^{\alpha-1}}{\alpha!}\right)$ $P(X_{1} = \alpha) | X_{2} = 1 | X_{1} + \alpha X_{2} = \alpha | = \frac{1}{\alpha!} + \frac{\lambda^{\alpha-1}}{\alpha!}$

.. XI + XXZ mao e estatistica suficiente para ?